1. Given five memory partitions of 100Kb, 500Kb, 200Kb, 300Kb, 600Kb (in order), how would the first-fit, best-fit, and worst-fit algorithms place processes of 212 Kb, 417 Kb, 112 Kb, and 426 Kb (in order)? Which algorithm makes the most efficient use of memory?

First-fit:

212K is put in 500K partition

417K is put in 600K partition

112K is put in 288K partition (new partition 288K = 500K - 212K)

426K must wait

Best-fit:

212K is put in 300K partition

417K is put in 500K partition

112K is put in 200K partition

426K is put in 600K partition

Worst-fit:

212K is put in 600K partition

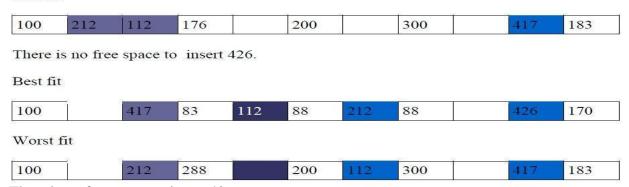
417K is put in 500K partition

112K is put in 388K partition

426K must wait

OR

First fit



There is no free space to insert 426.

In this example, best-fit turns out to be the best.

2. Assuming a 4 KB page size, what are the page numbers and offsets for the following address references (provided as decimal numbers):

- a. 2375
- b. 19366
- c. 30000
- d. 256
- e. 16385

## Assumption:

- (max) Physical/logical Address Space = 32,768 because part c has the highest address 30,000,

which would fit in an addressible space of this size. This would require a 15 bit address size.

- A Physical/logical address of 32,786 would have  $m' = 15 (2^15) = 32,768$ 

Page size: 
$$2^n = 4KB = 4,096$$
 bytes  $n = 12$ 

Page count = 8, bits required: 3, 0 indexed: 0-7

Page Number Page Offset

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| 3 bits | 12 bits | (m-n) n
```

a. 3275 => (binary) 110011001011

000110011001011 (zero padded to 15 bits)

Page: (binary) 000 -> (decimal) 0 [the first page]
Offset: (binary) 110011001011 -> (decimal) 3,275

b. 19366 => (binary) 100101110100110

Page: (binary) 100 -> (decimal) 4
Offset: (binary) 101110100110 -> (decimal) 2,982

000000100000000

c. 30000 => (binary) 111010100110000

Page: (binary) 111 -> (decimal) 7

Offset: (binary) 010100110000 -> (decimal) 1,328

d. 256 => (binary) 000000100000000 (zero padded to 15 bit)

Page: (binary) 000 -> (decimal) 0 Offset: (binary) 000100000000 -> (decimal) 256

e. 16385 => (binary) 100000000000001

Page: (binary) 100 -> (decimal) 4 Offset: (binary) 000000000001 -> (decimal) 1

- 3. Consider a logical address space of 64 pages of 1024 words each, mapped onto a physical memory of 32 frames.
- a. How many bits are there in the logical address?
- b. How many bits are there in the physical address?

Answer:

$$2^n = 2048 = n = 11 \text{ (page size)}$$

a. How many bits are required in the logical address?

How many for page number and how many for page offset?

8 pages \* 2048 bytes = 16,384 bytes total logical memory

$$16.384 = 2^14 = 14$$
 bits

8 pages can be accessed with 3 bits  $(2^3 = 8)$ 

2048 bytes per page can be access with 11 bits.

Page Number Page Offset

b. How many bits are required in the physical address?

How many for frame number and how many for page offset?

16 frames \* 2048 bytes per frame = 32,768 bytes total physical memory

$$32,768 = 2^{15} = 15$$
 bits

16 pages can be accessed with 4 bits  $(2^4 = 4)$ 

2048 bytes per page can be access with 11 bits.

Frame Number Frame Offset

- a. Logical address: 16 bits
- b. Physical address: 15 bits
- 4. Consider a logical address space of 32 pages with 1024 words per page; mapped onto a physical memory of 16 frames.
- a. How many bits are required in the logical address?
- b. How many bits are required in the physical address?

Answer:

a. 
$$2^5 + 2^10 = 15$$
 bits.

b. 
$$2^4 + 2^10 = 14$$
 bits.

- 5. Consider a paging system with the page table stored in memory.
- a. If a memory reference takes 200 nanoseconds, how long does a paged memory reference take?
- b. If we add associative registers, and 75 percent of all page-table references are found in the associative registers, what is the effective memory reference time? (Assume that finding a page-table entry in the associative registers takes zero time if the entry is there.)

## Answer:

- a. 400 nanoseconds: 200 nanoseconds to access the page table and 200nanoseconds to access the word in memory.
- b. Effective access time =  $0.75 \times (200 \text{ nanoseconds}) + 0.25 \times (400 \text{nanoseconds}) = 250 \text{ nanoseconds}$ .
- 6. Consider the following segment table:

Segment	Base	Length	
0	219	600	
1	2300	14	
2	90	100	
3	1327	580	
4	1952	96	

What are the physical addresses for the following logical addresses?

- a. 0,430
- b. 1,10
- c. 2,500
- d. 3,400
- e. 4,112

## Answer:

a. Logical address < Length of the segment

Add base address with Logical address

$$219 + 430 = 649$$

b. Logical address < Length of the segment

Add base address with Logical address

$$2300 + 10 = 2310$$

 $\circ$ . Logical address < Length of the segment

illegal reference, trap to operating system

 ${\tt d}$ . Logical address  ${\tt <}$  Length of the segment

Add base address with Logical address

$$1327 + 400 = 1727$$

 $_{\mbox{\scriptsize e}}$  . Logical address < Length of the segment 112>96

illegal reference, trap to operating system