

1. Given five memory partitions of 100Kb, 500Kb, 200Kb, 300Kb, 600Kb (in order), how would the first-fit, best-fit, and worst-fit algorithms place processes of 212 Kb, 417 Kb, 112 Kb, and 426 Kb (in order)? Which algorithm makes the most efficient use of memory?

First-fit:

212K is put in 500K partition

417K is put in 600K partition

112K is put in 288K partition (new partition 288K = 500K - 212K)

426K must wait

Best-fit:

212K is put in 300K partition

417K is put in 500K partition

112K is put in 200K partition

426K is put in 600K partition

Worst-fit:

212K is put in 600K partition

417K is put in 500K partition

112K is put in 388K partition

426K must wait

**OR**

First fit

100	212	112	176		200		300		417	183
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There is no free space to insert 426.

Best fit

100		417	83	112	88	212	88		426	170
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Worst fit

100		212	288		200	112	300		417	183
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There is no free space to insert 426.

In this example, best-fit turns out to be the best.

2. Assuming a 4 KB page size, what are the page numbers and offsets for the following address references (provided as decimal numbers):

- 2375
- 19366
- 30000
- 256
- 16385

Assumption:

- (max) Physical/logical Address Space = 32,768 because part c has the highest address 30,000,

which would fit in an addressable space of this size. This would require a 15 bit address size.

- A Physical/logical address of 32,786 would have 'm' = 15 ( $2^{15}$ ) => 32,768

Page size:  $2^n = 4\text{KB} = 4,096$  bytes

$n = 12$

Page count = 8, bits required: 3, 0 indexed: 0-7

Page Number    Page Offset

| 3 bits |    12 bits    |

(m-n)            n

a. 3275 => (binary) 110011001011

000110011001011 (zero padded to 15 bits)

Page: (binary) 000 -> (decimal) 0 [the first page]

Offset: (binary) 110011001011 -> (decimal) 3,275

b. 19366 => (binary) 100101110100110

Page: (binary) 100 -> (decimal) 4

Offset: (binary) 101110100110 -> (decimal) 2,982

0000001000000000

c. 30000 => (binary) 111010100110000

Page: (binary) 111 -> (decimal) 7

Offset: (binary) 010100110000 -> (decimal) 1,328

d. 256 => (binary) 000000100000000 (zero padded to 15 bit)

Page: (binary) 000 -> (decimal) 0

Offset: (binary) 000100000000 -> (decimal) 256

e. 16385 => (binary) 100000000000001

Page: (binary) 100 -> (decimal) 4

Offset: (binary) 000000000001 -> (decimal) 1

**3. Consider a logical address space of 64 pages of 1024 words each, mapped onto a physical memory of 32 frames.**

**a. How many bits are there in the logical address?**

**b. How many bits are there in the physical address?**

Answer:

$2^n = 2048 \implies n = 11$  (page size)

Logical -> | 0| 1| 2| 3| 4| 5| 6| 7|  
(pages)

Physical-> | 0| 1| 2| 3| 4| 5| 6| 7| 8| 9|10|11|12|13|14|15|  
(frames)

**a. How many bits are required in the logical address?**

**How many for page number and how many for page offset?**

8 pages \* 2048 bytes = 16,384 bytes total logical memory

$$16,384 = 2^{14} \Rightarrow 14 \text{ bits}$$

8 pages can be accessed with 3 bits ( $2^3 = 8$ )

2048 bytes per page can be access with 11 bits.

Page Number    Page Offset

| 3 bits |    11 bits    |

**b. How many bits are required in the physical address?**

**How many for frame number and how many for page offset?**

16 frames \* 2048 bytes per frame = 32,768 bytes total physical memory

$$32,768 = 2^{15} \Rightarrow 15 \text{ bits}$$

16 pages can be accessed with 4 bits ( $2^4 = 16$ )

2048 bytes per page can be access with 11 bits.

Frame Number    Frame Offset

| 4 bits |    11 bits    |

a. Logical address: 16 bits

b. Physical address: 15 bits

**4. Consider a logical address space of 32 pages with 1024 words per page; mapped onto a physical memory of 16 frames.**

**a. How many bits are required in the logical address?**

**b. How many bits are required in the physical address?**

Answer:

a.  $2^5 + 2^{10} = 15 \text{ bits.}$

b.  $2^4 + 2^{10} = 14 \text{ bits.}$

**5. Consider a paging system with the page table stored in memory.**

**a. If a memory reference takes 200 nanoseconds, how long does a paged memory reference take?**

**b. If we add associative registers, and 75 percent of all page-table references are found in the associative registers, what is the effective memory reference time? (Assume that finding a page-table entry in the associative registers takes zero time if the entry is there.)**

Answer:

a. 400 nanoseconds: 200 nanoseconds to access the page table and 200nanoseconds to access the word in memory.

b. Effective access time =  $0.75 \times (200 \text{ nanoseconds}) + 0.25 \times (400\text{nanoseconds}) = 250 \text{ nanoseconds}$ .

**6. Consider the following segment table:**

Segment	Base	Length
0	219	600
1	2300	14
2	90	100
3	1327	580
4	1952	96

**What are the physical addresses for the following logical addresses?**

**a. 0,430**

**b. 1,10**

**c. 2,500**

**d. 3,400**

**e. 4,112**

Answer:

a. Logical address < Length of the segment

$$430 < 600$$

Add base address with Logical address

$$219 + 430 = 649$$

b. Logical address < Length of the segment

$$10 < 14$$

Add base address with Logical address

$$2300 + 10 = 2310$$

c. Logical address < Length of the segment

$$500 > 100$$

illegal reference, trap to operating system

d. Logical address < Length of the segment

$$400 < 580$$

Add base address with Logical address

$$1327 + 400 = 1727$$

e. Logical address < Length of the segment  
 $112 > 96$

illegal reference, trap to operating system



