

Q1. A unit feedback system has the transfer function of 05

$$G(s) = \frac{40K}{s(s+4)(s+10)}$$

- a. Construct Bode diagrams for  $K=1$ .
- b. Determine the phase and gain margins of the system.
- c. Determine the value for the static gain  $K$  such that the system has a gain margin of 10dB. Find the corresponding steady state errors.
- d. From Bode diagrams determine the value for the static gain  $K$  such that the phase margin is  $45^\circ$ . Determine the damping ratio and the natural frequency for the obtained value of  $K$ .
- e. Draw the Nyquist diagram and determine the value of  $K$  for the system stability.

Q2. A unit feedback system with transport delay has the transfer function 05

$$G(s) = \frac{10Ke^{-0.5s}}{(s+4)(s+10)} \quad \text{Approximate time delay as } e^{-Ts} \approx 1/(1+Ts)$$

- a. Plot on the same figure the Bode diagrams for the system with and without transport delay for  $K=1$ . Comment on system stability.
- b. Plot the unit step response of the system for both cases and compare the results (steady state errors, transient response parameters).
- c. Determine the value of the static gain  $K$  that gives a steady state unit step error of 0.02 for both the approximated system and the original system without time delay.
- d. Design phase-lag, phase-lead, and phase-lag-lead controllers to achieve a steady state error of  $e_{ss} \leq 0.05$  and a phase margin  $P_m \geq 50^\circ$  for the approximated system.
- e. Draw the exact phase Bode diagrams of the compensated systems, including the time delay, and check the values obtained for the phase margins (Use MATLAB).