

$$(2) \quad \underline{e^{ax} \sin(bx+c)}$$

$$\text{let } y = e^{ax} \sin(bx+c)$$

$$y_1 = e^{ax} b \cos(bx+c) + a e^{ax} \sin(bx+c)$$

$$= e^{ax} \{ b \cos(bx+c) + a \sin(bx+c) \}$$

putting $a = r \cos \theta$ and $b = r \sin \theta$ where r and θ are constants.

$$r = \sqrt{a^2 + b^2} \quad \& \quad \theta = \tan^{-1} \frac{b}{a} \quad \text{where } r \& \theta \text{ are constants.}$$

$$\therefore y_1 = e^{ax} r \{ \sin \theta \cos(bx+c) + \cos \theta \sin(bx+c) \}$$

$$= r e^{ax} \sin(bx+c+\theta)$$

$$y_2 = r e^{ax} b \cos(bx+c+\theta) + r e^{ax} a \sin(bx+c+\theta)$$

$$= r e^{ax} r \sin \theta \cos(bx+c+\theta) + r e^{ax} r \cos \theta \sin(bx+c+\theta)$$

$$= r e^{ax} \sin(bx+c+2\theta)$$

$$y_n = r^n e^{ax} \sin(bx+c+n\theta)$$

$$\therefore y_n = (a^2 + b^2)^{n/2} e^{ax} \sin(bx+c+n \tan^{-1} \frac{b}{a})$$

$$\mathcal{D}^n [e^{ax} \sin(bx+c)] = (a^2 + b^2)^{n/2} e^{ax} \sin(bx+c+n \tan^{-1} \frac{b}{a})$$

if $a=1$, $b=1$ and $c=0$, then:

$$y = e^x \sin x \& y_n = 2^{n/2} e^x \sin \left(x + \frac{n\pi}{4} \right)$$

$$\left[\because r = \sqrt{2} \quad \& \theta = \pi/4 \right]$$