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MATDIP301

Third Semester B.E. Degree Examination, Dec.2013/Jan.2014

Advanced Mathematics – I

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions.

- 1 a. Express the complex number $\frac{(1+i)(1+3i)}{1+5i}$ in the form $x + iy$. (06 Marks)
- b. Find the modulus and amplitude of $\frac{(3-\sqrt{2}i)^2}{1+2i}$. (07 Marks)
- c. Expand $\cos^8 \theta$ in a series of cosines multiples of θ . (07 Marks)
- 2 a. Find the n^{th} derivative of $\sin(ax + b)$. (06 Marks)
- b. If $y = (\sin^{-1} x)^2$, show that $(1-x^2)y_{n+2} - (2n+1)xy_{n+1} - n^2y_n = 0$. (07 Marks)
- c. Find the n^{th} derivative of $\left[\frac{1}{5(x-1)} + \frac{-3/2}{(-\frac{3}{2}-1)(2x+3)} \right]$. (07 Marks)
- 3 a. Using Taylor's theorem, express the polynomial $2x^3 + 7x^2 + x - 6$ in powers of $(x-1)$. (06 Marks)
- b. Using Maclaurin's series, expand $\tan x$ upto the term containing x^5 . (07 Marks)
- c. If $Z = x^3 + y^3 - 3axy$ then prove that $\frac{\partial^2 Z}{\partial y \partial x} = \frac{\partial^2 Z}{\partial x \partial y}$. (07 Marks)
- 4 a. If $u = x \log xy$ where $x^3 + y^3 + 3xy = 1$, find $\frac{du}{dx}$. (07 Marks)
- b. If $z = f(x, y)$ and $x = e^u + e^{-v}$ and $y = e^{-u} - e^v$, prove that $\frac{\partial z}{\partial u} - \frac{\partial z}{\partial v} = x \cdot \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y}$. (07 Marks)
- c. If $u = x + 3y^2 - z^3$, $v = 4x^2yz$, $w = 2z^2 - xy$, find the value of $\frac{\partial(u, v, w)}{\partial(x, y, z)}$ at $(1, -1, 0)$. (07 Marks)
- 5 a. Obtain the reduction formula for $\int \sin^n x \, dx$. (06 Marks)
- b. Evaluate $\int_0^a \frac{x^7 dx}{\sqrt{a^2 - x^2}}$. (07 Marks)
- c. Evaluate $\int_1^2 \int_3^4 (xy + e^y) dy dx$. (07 Marks)
- 6 a. Evaluate $\int_0^1 \int_0^1 \int_0^1 e^{x+y+z} dx dy dz$. (06 Marks)
- b. Find the value of $\left| \left(\frac{1}{2} \right) \right|$. (07 Marks)
- c. Prove that $\beta(m, n) = \frac{\Gamma(m) \Gamma(n)}{\Gamma(m+n)}$. (07 Marks)

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- 7 a. Solve $\frac{dy}{dx} = e^{3x-2y} + x^2 \cdot e^{-2y}$. (06 Marks)
- b. Solve $\frac{dy}{dx} = \frac{x^2 - y^2}{xy}$ which is homogeneous in x and y. (07 Marks)
- c. Solve $\frac{dy}{dx} - \frac{y}{x+1} = e^{3x}(x+1)$. (07 Marks)
- 8 a. Solve $\frac{d^2y}{dx^2} + 5\frac{dy}{dx} + 6y = e^x$. (06 Marks)
- b. Solve $\frac{d^2y}{dx^2} - 3\frac{dy}{dx} + 2y = \sin 2x$. (07 Marks)
- c. Solve $(D^2 - 1)y = x \sin 3x + \cos x$. (07 Marks)

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