

Cube root of

$$1+i$$

$$z = x+iy = 1+i$$

$$\arg z = \tan^{-1} \left(\frac{y}{x} \right) = \tan^{-1} \left(\frac{1}{1} \right) = \pi/4$$

$$r = \sqrt{x^2 + y^2} = \sqrt{1+1} = \sqrt{2}$$

$$z = 1+i = (+, +) \text{ is in 1st quadrant}$$

$$\theta = \pi = \pi/4$$

$$z = \sqrt{2} \left[\cos(\pi/4) + i \sin(\pi/4) \right]$$

$$\text{or } z = \sqrt{2} \left[\cos\left(\frac{2k\pi + \pi}{4}\right) + i \sin\left(\frac{2k\pi + \pi}{4}\right) \right]$$

$$z = 2^{1/2} \left[\cos\left(\frac{8k+1}{4}\right) + i \sin\left(\frac{8k+1}{4}\right) \right]$$

$$z^{1/3} = 2^{1/6} \left[\cos\left(\frac{8k+1}{4}\right) + i \sin\left(\frac{8k+1}{4}\right) \right]^{1/3}$$

$$z_k = 2^{1/6} \left[\cos\left(\frac{8k+1}{12}\right) + i \sin\left(\frac{8k+1}{12}\right) \right] \quad 0, 1, 2$$

$$z_0 = 2^{1/6} \left[\cos\left(\frac{\pi}{12}\right) + i \sin\left(\frac{\pi}{12}\right) \right]$$

$$z_1 = 2^{1/6} \left[\cos\left(\frac{9\pi}{12}\right) + i \sin\left(\frac{9\pi}{12}\right) \right]$$

$$z_2 = 2^{1/6} \left[\cos\left(\frac{17\pi}{12}\right) + i \sin\left(\frac{17\pi}{12}\right) \right]$$