

Bubble sort

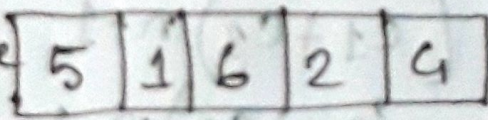
① Sorting with the first element (Index=0) compare the current element with the next element of the array.

② If the current element is greater than the next element of the array, swap them.

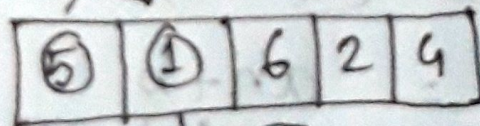
③ If the current element is less than the next element, Repeat ①.

Let's consider array with values $\{5, 1, 6, 2, 4\}$

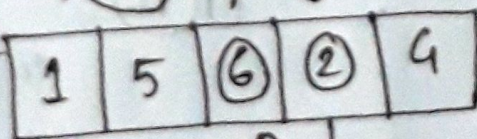
$5 > 1$, so interchange



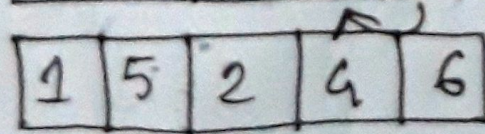
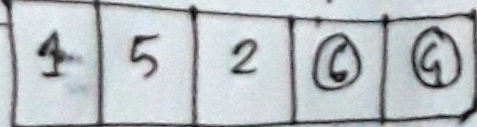
$5 > 6$, No swapping



$6 > 2$, interchange



$6 > 4$, interchange



$$\begin{aligned}
 T(n) &= (c_1 + c_3)n - 1 + c_3(1 + 2 + 3 + \dots + n - 1) \\
 &= (c_1 + c_3)n - 1 + c_3 \cdot \frac{n(n-1)}{2} \\
 &= an^2 + b^2 + c \\
 &= O(n^2)
 \end{aligned}$$

Average case: $O(n^2)$

Best case: when the array is already sorted. The inner loop won't execute.

$$\begin{aligned}
 T(n) &= (c_1 + c_3)n - 1 \\
 &= (c_1 + c_3)n - 1 \\
 &= an + b \\
 &= O(n)
 \end{aligned}$$