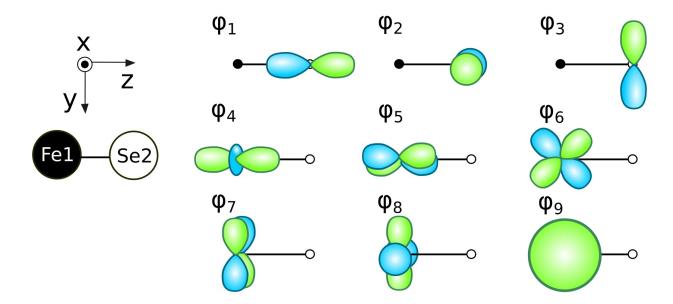
Model Hamiltonian for the FeSe molecule

Localized orbitals:



Model:

$$H = E_0 + \sum_i \varepsilon_i n_i + \sum_{i,j,\eta} t_{ij} c_{i,\eta}^{\dagger} c_{j,\eta} + \text{h.c.} + \sum_i U_i n_{i,\uparrow} n_{i,\downarrow} + \sum_{i,j} V_{ij} n_i n_j + \sum_{i,j} J_{ij} \boldsymbol{S_i} \cdot \boldsymbol{S_j}$$

Orbital energies $(n_i = c^{\dagger}_i c_i)$

$arepsilon$ s $n_{arphi 9}$	$oldsymbol{arepsilon} d\sigma n_{arphi^4}$	$\varepsilon d (n_{\varphi 4} + n_{\varphi 5} + n_{\varphi 6} + n_{\varphi 7} + n_{\varphi 8})$
$ε$ ρ σ $n_{φ1}$	$\varepsilon d\pi (n_{\varphi 5} + n_{\varphi 6})$	$\boldsymbol{\varepsilon p} (n_{\varphi 1} + n_{\varphi 2} + n_{\varphi 3})$
$\varepsilon p\pi (n_{\omega 2} + n_{\omega 3})$	$\varepsilon d\delta (n_{\varphi 7} + n_{\varphi 8})$	

Symmetry-allowed hoppings

$$t\sigma \ \Sigma_{\eta} \ (c^{\dagger}_{\varphi 1,\eta} \ c_{\varphi 4,\eta} + h.c.)$$

$$t\sigma ps \ \Sigma_{\eta} \ (c^{\dagger}_{\varphi 1,\eta} \ c_{\varphi 9,\eta} + h.c.)$$

$$t\sigma ll \ \Sigma_{\eta} \ (c^{\dagger}_{\varphi 1,\eta} \ c_{\varphi 9,\eta} + h.c.)$$

$$t\sigma ll \ \Sigma_{\eta} \ (c^{\dagger}_{\varphi 1,\eta} \ c_{\varphi 4,\eta} + c^{\dagger}_{\varphi 1,\eta} \ c_{\varphi 9,\eta} + h.c.)$$

Self-repulsion

$$\begin{array}{ll} \textbf{\textit{Up}} \; (n_{\varphi 1,\uparrow} n_{\varphi 1,\downarrow} + n_{\varphi 2,\uparrow} n_{\varphi 2,\downarrow} + n_{\varphi 3,\uparrow} n_{\varphi 3,\downarrow}) & \textbf{\textit{Ud}} \delta \; (n_{\varphi 7,\uparrow} n_{\varphi 7,\downarrow} + n_{\varphi 8,\uparrow} n_{\varphi 8,\downarrow}) \\ \textbf{\textit{Ud}} \sigma \; n_{\varphi 4,\uparrow} n_{\varphi 4,\downarrow} & \textbf{\textit{Ud}} \; \Sigma_{i=4}{}^8 n_{\varphi i,\uparrow} n_{\varphi i,\downarrow} \\ \textbf{\textit{Ud}} \pi \; (n_{\varphi 5,\uparrow} n_{\varphi 5,\downarrow} + n_{\varphi 6,\uparrow} n_{\varphi 6,\downarrow}) & \textbf{\textit{U}} \; \Sigma_{i=1}{}^9 n_{\varphi i,\uparrow} n_{\varphi i,\downarrow} \end{array}$$

Couloumb interaction

$$\textit{Vpd} \ \Sigma_{i=1}{}^{3} \Sigma_{j=4}{}^{8} n_{\phi i} n_{\phi j} \qquad \qquad \textit{Vps} \ \Sigma_{i=1}{}^{9} n_{\phi i} n_{\phi 9}$$

Exchange

$$\mathbf{J} \sum_{i=4}^{8} \sum_{j>i} S_{\varphi i} S_{\varphi j}$$