

1. Definition (BFS)

Breadth-First Search (BFS) is a graph/tree traversal algorithm that explores all nodes **level by level**, using a **queue**.

It guarantees the **shortest path** in **unweighted** graphs by visiting closer nodes before deeper ones.

2. Solution Approach (Short)

1. Create a **queue** and a **visited** array/set.
2. Mark the **start node** as visited and push it into the queue.
3. While the queue is not empty:
 - Pop the front node
 - Visit all its neighbors
 - If a neighbor is unvisited → mark visited + enqueue
4. Continue until all reachable nodes are processed (or target is found).

3. Hint (General BFS Tips)

- Use a **queue** (FIFO) — that's the core of BFS.
- Always maintain a **visited** set to avoid loops.
- BFS naturally finds the **shortest path** in unweighted graphs.
- Perfect for: levels, distances, grids, connectivity, shortest path.

4. Pseudocode (C++ Style)

```
void BFS(int start, vector<vector<int>>& graph) {  
    int n = graph.size();  
    vector<bool> visited(n, false);  
    queue<int> q;  
  
    visited[start] = true;  
    q.push(start);  
  
    while (!q.empty()) {  
        int node = q.front();
```

```

q.pop();

// process node
cout << node << " ";

for (int nbr : graph[node]) {
    if (!visited[nbr]) {
        visited[nbr] = true;
        q.push(nbr);
    }
}
}
}

```

5. Hint :

- Queue → FIFO → Level order traversal
- Use adjacency list for efficiency (not matrix).
- In grids: check boundaries + use direction array.
- BFS = shortest path in unweighted graphs → No need for Dijkstra.

6. Time Complexity

| Scenario | Time Complexity | Space Complexity |
|---------------------------------|-----------------|------------------|
| Graph BFS ($V + E$) | $O(V + E)$ | $O(V)$ |
| Tree (N nodes) | $O(N)$ | $O(N)$ |
| Grid ($N \times M$) | $O(NM)$ | $O(NM)$ |
| Adjacency Matrix Graph $O(V^2)$ | | $O(V)$ |