

# 1. Greeting

## 1 Greeting

2 TD2: Exc19

3 TD2: Exc23

4 TD2: Exc24

5 TD2: Exc25

6 TD2: Exc26

7 TD2: Exc27

*Khmer TeX User Group*

## Introduction to Show Beamer Theme

OL Say

Khmer TeX Users Group

April 05, 2020

## 2. TD2: Exc19

- 1 Greeting
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- 4 TD2: Exc24
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- 6 TD2: Exc26
- 7 TD2: Exc27

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- 19 Let  $X$  be the number of working pumps before the third non-working pump is found. Then,  $X \sim \text{Neg}(r = 3, p = 0.2)$ . Let  $T$  be the total time (in minute) for testing and repairing the pumps. Then  $T = 10X + 3(30) = 10X + 90$ . Thus,

$$\begin{aligned} E(T) &= E(10X + 90) = 10E(X) + 90 \\ &= 10 \left( \frac{r(1-p)}{p} \right) + 90 = 10 \left( \frac{3(0.8)}{0.2} \right) + 90 = \dots \end{aligned}$$

$$\begin{aligned} V(T) &= V(10X + 90) = 10^2 V(X) \\ &= 100 \times \frac{r(1-p)}{p^2} = 100 \left( \frac{3(0.8)}{(0.2)^2} \right) = \dots \end{aligned}$$

### 3. TD2: Exc23

- 1 Greeting
- 2 TD2: Exc19
- 3 TD2: Exc23**
- 4 TD2: Exc24
- 5 TD2: Exc25
- 6 TD2: Exc26
- 7 TD2: Exc27

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- 23 Let  $X$  be the number of failed diodes among the 200 diodes. Then,  
 $X \sim \text{Bin}(n = 200, p = 0.01)$
- a  $E(X) = np = (200)(0.01) = 2$  and  
 $\sigma_X = \sqrt{npq} = \sqrt{(200)(0.01)(0.99)} = \dots$
- b Since  $n$  is large,  $p$  is small and  $np = 2 < 5$  then  $X$  is approximately Poisson distributed. That is  $X \sim \text{Poi}(\lambda = \mu_X = 2)$ .

$$P(X \geq 4) = 1 - P(X < 4) \approx 1 - \sum_{x=0}^3 \frac{e^{-2} 2^x}{x!} = \dots$$

- © Let  $Y$  be the number of boards among the five selected boards that works. Then,  $Y \sim \text{Bin}(n = 5, p = P(X = 0))$ . Since

$$p = P(X = 0) \approx \frac{e^{-2}2^0}{0!} = e^{-2} \approx 0.1353$$

$$q = 1 - p = 1 - e^{-2} \approx 0.8647$$

Then,  $P(Y = y) = \binom{5}{y}(0.1353)^y(0.8647)^{5-y}$  and

$$P(Y \geq 4) = P(Y = 4) + P(Y = 5) = \dots$$

## 4. TD2: Exc24

- ① Greeting
- ② TD2: Exc19
- ③ TD2: Exc23
- ④ **TD2: Exc24**
- ⑤ TD2: Exc25
- ⑥ TD2: Exc26
- ⑦ TD2: Exc27

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- 24 The set of possible values of  $X$  is  $D = \{x \in \mathbb{N} : x \geq 0\}$  and  $a > 0$ .

$$\begin{aligned} \sum_{x \geq 0} xP(X = x) &= \sum_{0 \leq x < a} xP(X = x) + \sum_{x \geq a} xP(X = x) \\ &\geq \sum_{x \geq a} xP(X = x) \end{aligned}$$

But  $\sum_{x \geq a} xP(X = x) \geq \sum_{x \geq a} aP(X = x)$  then

$$\sum_{x \geq 0} xP(X = x) \geq \sum_{x \geq a} aP(X = x)$$

$$E(X) \geq aP(X \geq a)$$

Therefore,  $P(X \geq a) \leq \frac{E(X)}{a}$ .

## 5. TD2: Exc25

- 1 Greeting
- 2 TD2: Exc19
- 3 TD2: Exc23
- 4 TD2: Exc24
- 5 TD2: Exc25**
- 6 TD2: Exc26
- 7 TD2: Exc27

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25 We have  $a > 0$ .

$$\begin{aligned} P(|X - E(X)| \geq a) &= P([X - E(X)]^2 \geq a^2) \\ &\leq \frac{E([X - E(X)]^2)}{a^2} \\ &= \frac{E[(X - \mu_X)^2]}{a^2} \\ &= \frac{V(X)}{a^2} \end{aligned}$$

Thus,  $P(|X - E(X)| \geq a) \leq \frac{V(X)}{a^2}$ .

## 6. TD2: Exc26

- 1 Greeting
- 2 TD2: Exc19
- 3 TD2: Exc23
- 4 TD2: Exc24
- 5 TD2: Exc25
- 6 TD2: Exc26**
- 7 TD2: Exc27

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- 26 We know that  $Y$  is the number of customers per day at a sales counter. The distribution of  $Y$  is not known.

$$\begin{aligned} P(16 < Y < 24) &= P(-4 < Y - 20 < 4) \\ &= P(|Y - 20| < 4) \\ &= 1 - P(|Y - 20| \geq 4) \\ &\geq 1 - \frac{V(Y)}{4^2} \\ &= 1 - \frac{2^2}{4^2} = 0.75 \end{aligned}$$

Thus, we infer that  $P(16 < Y < 24) \geq 0.75$ .

## 7. TD2: Exc27

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- 3 TD2: Exc23
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- 7 TD2: Exc27**

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27 We know that  $X$  is random with  $\mu_X = 11$  and  $V(X) = 9$ .

a Find a lower bound for  $P(6 < X < 16)$

$$\begin{aligned} P(6 < X < 16) &= P(-5 < X - 11 < 5) = P(|X - \mu_X| < 5) \\ &= 1 - P(|X - \mu_X| \geq 5) \geq 1 - \frac{V(X)}{5^2} \\ &= 1 - \frac{9}{5^2} = \frac{16}{25} \end{aligned}$$

Thus, a lower bound of  $P(6 < X < 16)$  is  $\frac{16}{25}$ .

b Find value of  $C$  such that  $P(|X - 11| \geq C) \leq 0.09$ . We know that

$$P(|X - 11| \geq C) \leq \frac{V(X)}{C^2} = \left(\frac{3}{C}\right)^2$$

To have  $P(|X - 11| \geq C) \leq 0.09$ , we let  $\left(\frac{3}{C}\right)^2 \leq 0.09$ .

That is  $C \geq 10$ .