

## EECE 2160 – Embedded Design: Enabling Robotics

## Homework #3

Assigned: Sat., Oct. 12, 2024. Due Sun., Oct. 20, at 11:59pm on Canvas

5 Problems 100 points total

*Show your work!***Problem 1.** (30 points, 10 points each)

Design a circuit that will tell whether a given month has 31 days in it. The month is specified by a 4-bit input  $A_{3:0}$ . For example, if the inputs are 0001, the month is January, if the inputs are 1100 the month is December. The circuit output  $Y$  should be HIGH only when the month specified by the inputs has 31 days in it.

- Draw the truth table
- Draw the simplified equation
- Draw the circuit diagram using the simplified equation

Hints:

Use a Karnaugh Map for simplification

Take advantage of “don’t cares,” see lecture 4 slide 32 – 34.

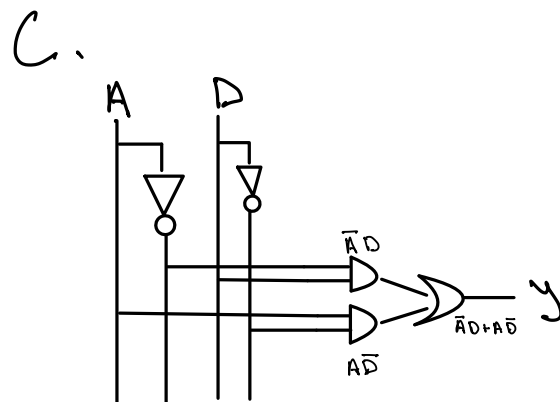
A.

month	a	b	c	d	Y
1	0	0	0	1	1
2	0	0	1	0	0
3	0	0	1	1	1
4	0	1	0	0	0
5	0	1	0	1	1
6	0	1	1	0	0
7	0	1	1	1	1
8	1	0	0	0	1
9	1	0	0	1	0
10	1	0	1	0	1
11	1	0	1	1	0
12	1	1	0	0	1

B.

AB \ CD	00	01	11	10
00	X	1	1	0
01	0	1	1	0
11	1	X	X	X
10	1	0	0	1

$\bar{A}D + A\bar{D} = Y$



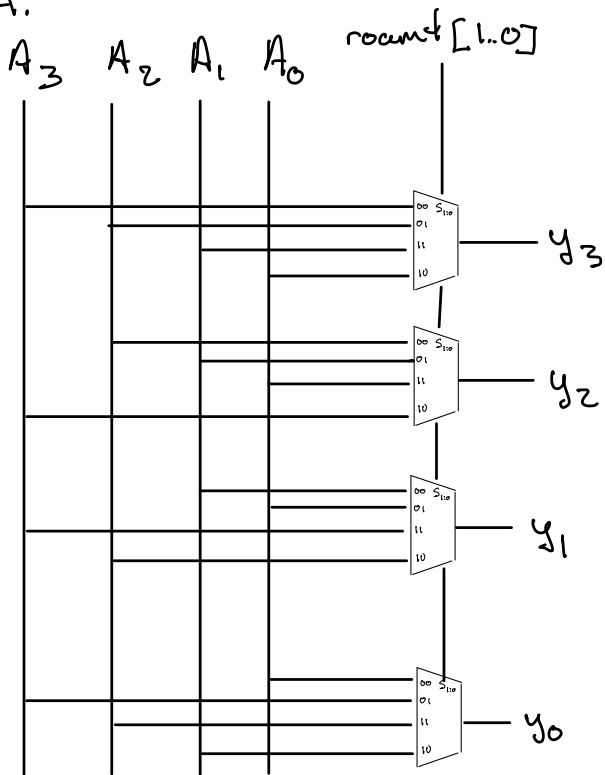
**Problem 2.** (20 points, 10 points each)

Design 4-bit left and right rotators. There should be a 2-bit input named *roamt* that determines how many bits to rotate.

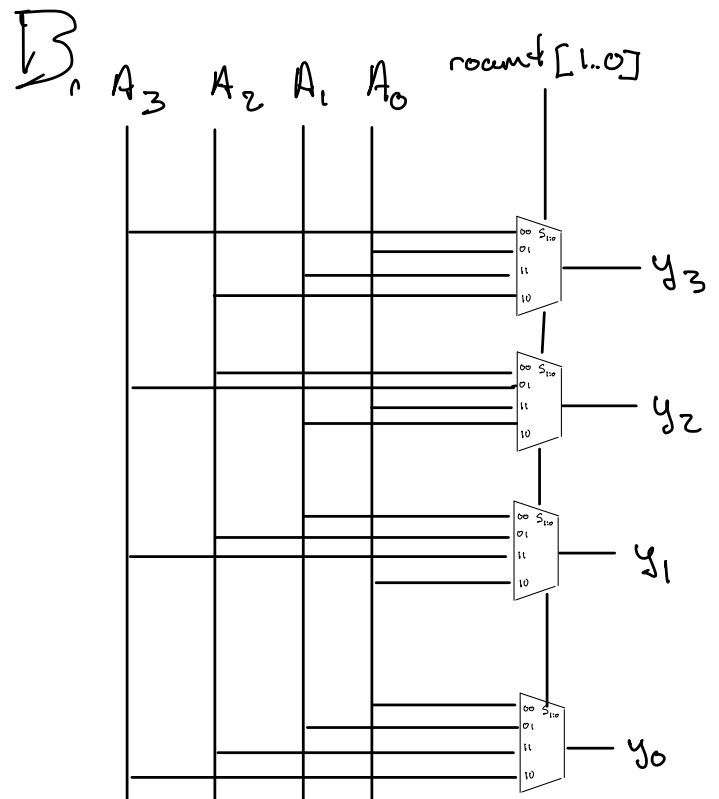
- 4-bit left rotator: sketch a schematic of your design
- 4-bit right rotator: sketch a schematic of your design

Hint: look at design of left and right shifters

A.

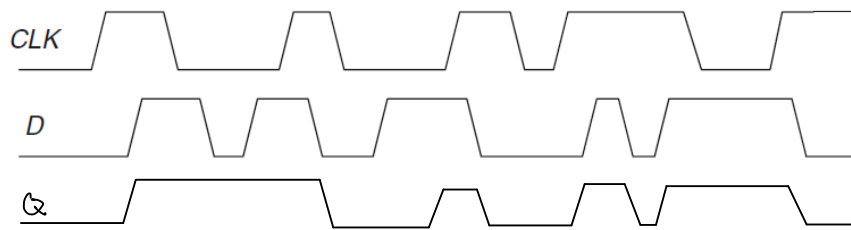


B.

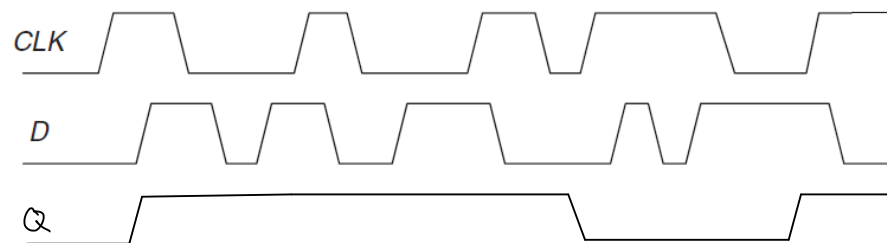


**Problem 3.** (10 points total, 5 points each)

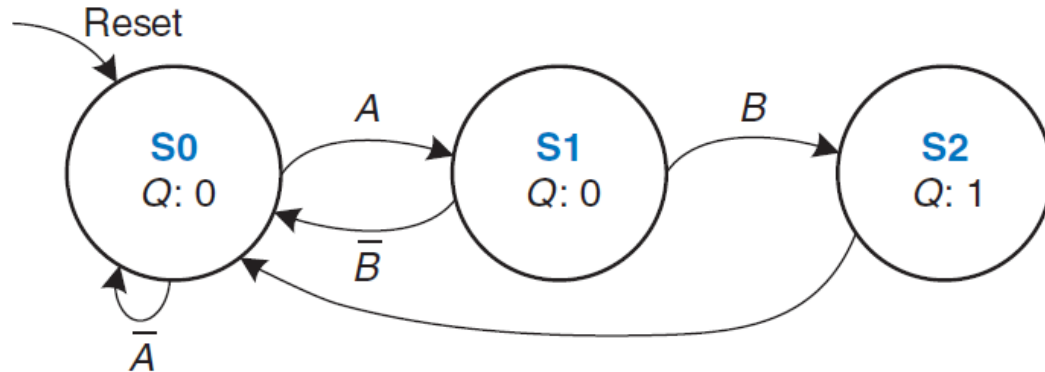
- a. For the following waveforms, sketch the output  $Q$  of a D-Latch:



- b. For the following waveforms, sketch the output  $Q$  of a D-Flip-Flop



**Problem 4.** (20 points) Consider this Moore-type Finite State Machine represented by the state transition diagram below.



Use binary encodings

- (8 points) Write the following:
  - State encoding table
  - State transition table (using state and input encodings)
- (2 points) Write the output table (using state and output encodings)
- (2 points) Write Boolean equations for (simplification optional):
  - The next state logic
  - The output logic
- (8 points) Sketch a schematic (circuit diagram) of the Finite State Machine.

A.

i.

$S_1$	$S_2$	A	B	$S_1'$	$S_2'$
0	0	0	x	0	0
0	0	1	x	0	1
0	1	x	0	0	0
0	1	x	1	1	0
1	0	x	x	0	0

ii.

State	Encoding
S0	00
S1	01
S2	10

B.

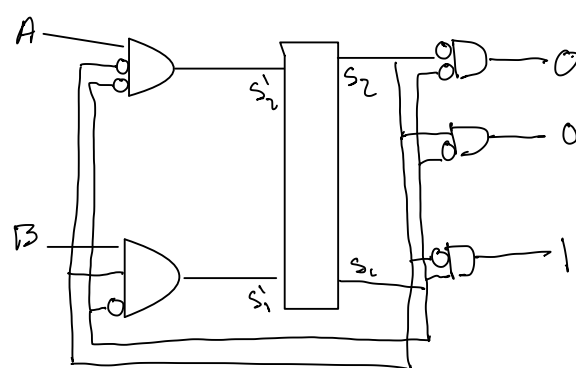
$S_1$	$S_2$	Q
0	0	0
0	1	0
1	0	1

C.

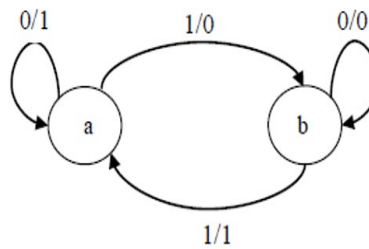
$$S_1' = \bar{S}_1 S_2 B$$

$$S_2' = \bar{S}_1 \bar{S}_2 A$$

D.



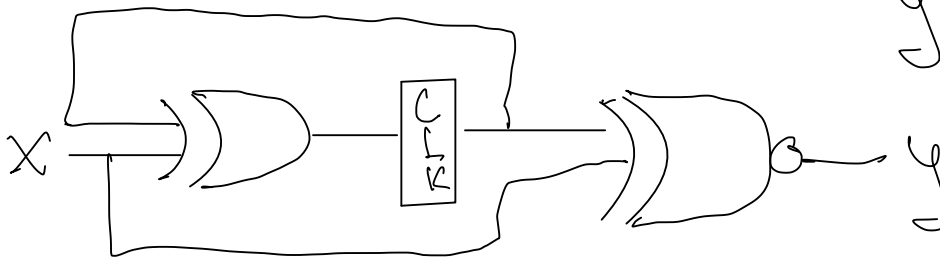
**Problem 5.** (20 points total, 10 points each) Design a sequential logic circuit to implement the following state diagram of a Mealy-type Finite State Machine.



a. Fill-in the state table (table has more rows than needed)

Current State	Input	Next State	Output
Q	X	Q*	Y
0	0	0	1
0	1	1	0
1	0	1	0
1	1	0	1

b. Draw the schematic diagram of the circuit.



$$Q^* = Q \oplus X$$

$$Y = Q \odot X$$