

# Announcements

- Quiz I
  - Monday, September 8
  - Lecture 2, Homework 1 & 2
- TA sessions: 7:00 p.m. – 9:00 p.m. (MECC 124)

Date	TA
Sunday	Anupam Khargharia
Monday	Kamilla Volkova
Tuesday	Chi Le
Wednesday	Shivanshu Dwivedi

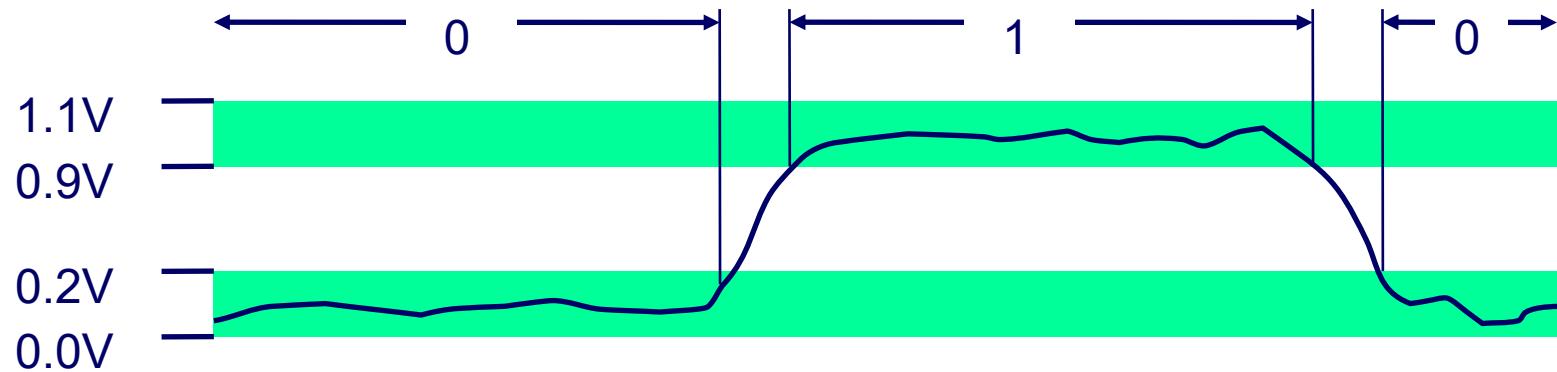
Lecture 2

# Bit Operations

CPSC 275  
Introduction to Computer Systems

# Everything is bit

- Each *bit* is 0 or 1
- By encoding/interpreting sets of bits in various ways
  - Computers determine what to do (instructions) and represent and manipulate numbers, sets, strings, etc.
- Why bits? Electronic Implementation
  - Easy to store with bi-stable elements
  - Reliably transmitted on noisy and inaccurate wires



# Encoding Byte Values

- *Byte = 8 bits*
  - Binary  $00000000_2$  to  $1111111_2$
  - Decimal:  $0_{10}$  to  $255_{10}$
  - *Hexadecimal: Base 16*
    - Use characters ‘0’ to ‘9’ and ‘A’ to ‘F’
    - $00_{16}$  to  $FF_{16}$
    - e.g. write FA1D37B0<sub>16</sub> in C as  
**0xFA1D37B0** or **0xfa1d37b0**

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

# Pop Quiz

- Convert the decimal 199 to hexadecimal.

$$\begin{aligned}199_{10} &= 11000111_2 \\&= \underline{\text{C7}}_{16}\end{aligned}$$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

# Pop Quiz

- Convert the binary  $1011101_2$  to hexadecimal.

$$1011101_2 = \underline{5D}_{16}$$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

# Pop Quiz

- Convert the binary  $1011101_2$  to hexadecimal.

$$1011101_2 = \underline{5D}_{16}$$

- Convert the hexadecimal  $\text{FACE}_{16}$  to binary.

$$\text{FACE}_{16} = \underline{\text{F A C E}}_{16} = \underline{111101011001110}_2$$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

# HTML color codes

- HTML color codes are a triplet of the form:

— — — — —  
r g b

where each color channel is a hexadecimal.

- Examples

#FF0000 Red

#00FF00 Green

#0000FF Blue

#FFFFFF White

#000000 Black

#808080 Gray

#00FFFF Aqua

#800080 Purple

#FFFF00 Yellow

# Octal

- *Octal*: Base 8
  - Binary  $000_2$  to  $111_2$
  - Decimal:  $0_{10}$  to  $7_{10}$
  - Octal constants in C:
    - e.g., write  $123_8$  as **0123**

Octal	Decimal	Binary
0	0	000
1	1	001
2	2	010
3	3	011
4	4	100
5	5	101
6	6	110
7	7	111

# File permissions in Linux

- Every file and directory in Linux is associated with a triplet of the form:

r	w	x	r	w	x	r	w	x
u			g			o		

where each defines file permission for the user, group, and others, respectively.

- Examples

**0755 = 111101101**

The user has full access; group and others have read and execute permissions

# Boolean Algebra

- Developed by George Boole in 19th Century
  - Algebraic representation of logic
    - Encode “True” as 1 and “False” as 0

AND

$A \& B = 1$  when both  $A=1$  and  $B=1$

&	0	1
0	0	0
1	0	1

OR

$A | B = 1$  when either  $A=1$  or  $B=1$

	0	1
0	0	1
1	1	1

NOT

$\sim A = 1$  when  $A=0$

$\sim$	
0	1
1	0

XOR (Exclusive-Or)

$A \wedge B = 1$  when either  $A=1$  or  $B=1$ , but not both

$\wedge$	0	1
0	0	1
1	1	0

# General Boolean Algebras

- Operate on Bit Vectors
  - Operations applied bitwise

$$\begin{array}{rcl} \begin{array}{c} 01101001 \\ \& 01010101 \end{array} & \begin{array}{c} 01101001 \\ | 01010101 \end{array} & \begin{array}{c} 01101001 \\ ^ 01010101 \end{array} \\ \hline \begin{array}{c} 01000001 \\ 01111101 \end{array} & \begin{array}{c} 01111101 \\ 00111100 \end{array} & \begin{array}{c} 01010101 \\ 10101010 \end{array} \end{array}$$

# Bit-Level Operations in C

- Operations `&`, `|`, `~`, `^` available in C
  - Apply to any “integral” data type
    - `int`, `short`, `char`, `unsigned`, `long`
  - View arguments as bit vectors
  - Arguments applied bit-wise
- Examples (`char` data type)

`~0x41 & 0xBE`     $\sim 01000001_2 \& 10111110_2$

`0x55 ^ 0x7D`     $01010101_2 ^ 01111101_2$

# Contrast: Logic Operations in C

- Contrast to logical operators: `&&`, `||`, `!`

- View 0 as “False”
  - Anything nonzero as “True”
  - Always return 0 or 1

- Examples (char data type)

`0x00 && !0x41 = 0` (short-circuit evaluation)

`!0x00 || 0x01 = 1`

`0x69 && 0x55 && 0x01 = 1`

`0x69 || 0x55 && 0x01 = 1`

