

Announcements

- Quiz I
 - Monday, September 8
 - Lecture 2, Homework 1 & 2
- TA sessions: 7:00 p.m. – 9:00 p.m. (MECC 124)

Date	TA
Sunday	Anupam Khargharia
Monday	Kamilla Volkova
Tuesday	Chi Le
Wednesday	Shivanshu Dwivedi

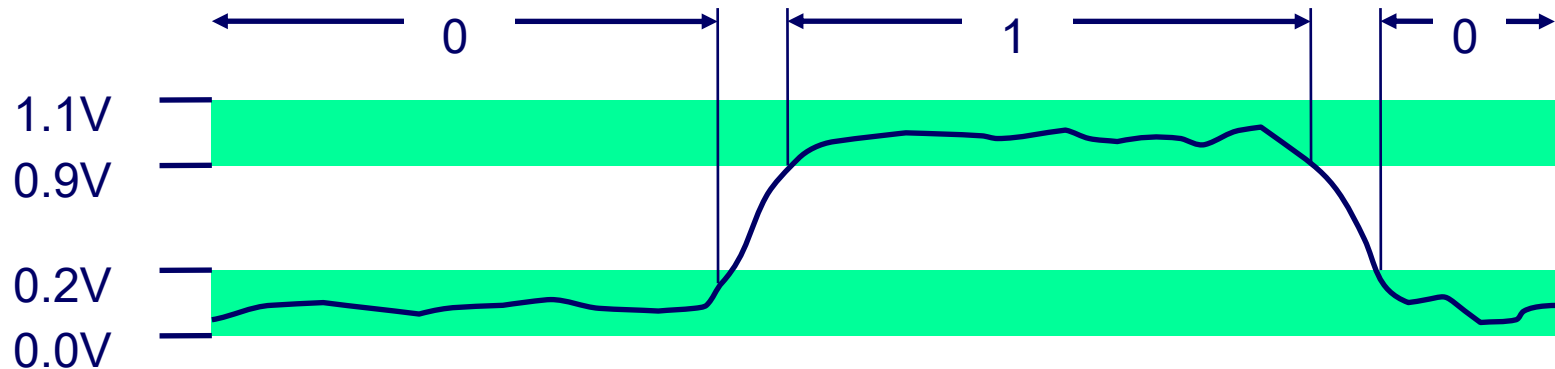
Lecture 2

Bit Operations

CPSC 275
Introduction to Computer Systems

Everything is bit

- Each *bit* is 0 or 1
- By encoding/interpreting sets of bits in various ways
 - Computers determine what to do (instructions) and represent and manipulate numbers, sets, strings, etc.
- Why bits? Electronic Implementation
 - Easy to store with bi-stable elements
 - Reliably transmitted on noisy and inaccurate wires



Encoding Byte Values

- *Byte* = 8 bits
 - Binary 00000000_2 to 11111111_2
 - Decimal: 0_{10} to 255_{10}
 - *Hexadecimal*: Base 16
 - Use characters '0' to '9' and 'A' to 'F'
 - 00_{16} to FF_{16}
 - e.g. write $FAID37B0_{16}$ in C as
0xFAID37B0 or **0xfaId37b0**

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Pop Quiz

- Convert the decimal 199 to hexadecimal.

$$\begin{aligned} 199_{10} &= 11000111_2 \\ &= \underline{C7}_{16} \end{aligned}$$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Pop Quiz

- Convert the binary 1011101_2 to hexadecimal.
 $1011101_2 = \underline{5D}_{16}$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Pop Quiz

- Convert the binary 1011101_2 to hexadecimal.

$$1011101_2 = \underline{5D}_{16}$$

- Convert the hexadecimal $FACE_{16}$ to binary.

$$\underline{FACE}_{16} = \underline{1111101011001110}_2$$

Hex	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

HTML color codes

- HTML color codes are a triplet of the form:

— — — — —
r g b

where each color channel is a hexadecimal.

- Examples

#FF0000 Red	#00FF00 Green	#0000FF Blue
#FFFFFF White	#000000 Black	#808080 Gray
#00FFFF Aqua	#800080 Purple	#FFFF00 Yellow

Octal

- *Octal*: Base 8
 - Binary 000_2 to 111_2
 - Decimal: 0_{10} to 7_{10}
 - Octal constants in C:
 - e.g., write 123_8 as **0123**

Octal	Decimal	Binary
0	0	000
1	1	001
2	2	010
3	3	011
4	4	100
5	5	101
6	6	110
7	7	111

File permissions in Linux

- Every file and directory in Linux is associated with a triplet of the form:

$$\begin{array}{ccccccc} r & w & x & r & w & x & r & w & x \\ \underbrace{\hspace{1cm}} & \underbrace{\hspace{1cm}} & \underbrace{\hspace{1cm}} & & & & & & \\ u & g & o & & & & & & \end{array}$$

where each defines file permission for the user, group, and others, respectively.

- Examples

0755 = **|||0||0|**

The user has full access; group and others have read and execute permissions

Boolean Algebra

- Developed by George Boole in 19th Century
 - Algebraic representation of logic
 - Encode “True” as 1 and “False” as 0

AND

$A \& B = 1$ when both $A=1$ and $B=1$

$\&$	0	1
0	0	0
1	0	1

OR

$A | B = 1$ when either $A=1$ or $B=1$

$ $	0	1
0	0	1
1	1	1

NOT

$\sim A = 1$ when $A=0$

\sim	
0	1
1	0

XOR (Exclusive-Or)

$A \wedge B = 1$ when either $A=1$ or $B=1$, but not both

\wedge	0	1
0	0	1
1	1	0

General Boolean Algebras

- Operate on Bit Vectors
 - Operations applied bitwise

01101001	01101001	01101001	
& 01010101	01010101	^ 01010101	~ 01010101
<hr/>	<hr/>	<hr/>	<hr/>
01000001	01111101	00111100	10101010

Bit-Level Operations in C

- Operations `&`, `|`, `~`, `^` available in C
 - Apply to any “integral” data type
 - `int`, `short`, `char`, `unsigned`, `long`
 - View arguments as bit vectors
 - Arguments applied bit-wise
- Examples (`char` data type)
 - `~0x41 & 0xBE` `~010000012 & 101111102`
 - `0x55 ^ 0x7D` `010101012 ^ 011111012`

Contrast: Logic Operations in C

- Contrast to logical operators: `&&`, `||`, `!`
 - View 0 as “False”
 - Anything nonzero as “True”
 - Always return 0 or 1
- Examples (`char` data type)
 - `0x00 && !0x41 = 0` (short-circuit evaluation)
 - `!0x00 || 0x01 = 1`
 - `0x69 && 0x55 && 0x01 = 1`
 - `0x69 || 0x55 && 0x01 = 1`

