

Q1

5 Points

Q1.1

1 Point

Assuming the alphabet size is R , what is the *amortized* runtime of the DFA construction step in the KMP string-matching algorithm over k searches when searching for the same pattern string (of length m) over k different text strings (each of length n)?

- ☒ $\Theta\left(\frac{mR}{k}\right)$
- ☐ $\Theta\left(\frac{nR}{k}\right)$
- ☐ $\Theta(mR)$
- ☐ $\Theta(kR)$

Q1.2

1 Point

Assuming the alphabet size is R , what is the *amortized* runtime of the DFA construction step in the KMP string-matching algorithm over k searches when searching for k different pattern strings (each of length m) over the same text string (of length n)?

- ☐ $\Theta\left(\frac{mR}{k}\right)$
- ☐ $\Theta\left(\frac{nR}{k}\right)$
- ☒ $\Theta(mR)$
- ☐ $\Theta(kR)$

Q1.3

1 Point

All brute-force algorithms have exponential worst-case runtime.

- ☐ True
- ☒ False

Q1.4

1 Point

Which of the following text-pattern pairs results in the worst-case runtime for the Boyer-Moore string-matching algorithm?

- ☒ text = XXXXXXXXXXXXXXXXXXXXXXXXXXXX and pattern = YXXXXXX
- ☐ text = XXXXXXXXXXXXXXXXXXXXXXXXXXXX and pattern = XXXXXY
- ☐ text = XYXYXZXXXXXXXXXXXXXXXX and pattern = XYXYZ
- ☐ text = ABCDVABCDWABCDXABCDYABCDZ and pattern = ABCDE

Q1.5

1 Point

Which of the following text-pattern pairs results in the worst-case runtime for the brute-force string-matching algorithm?

- ☐ text = XXXXXXXXXXXXXXXXXXXXXXXXXXXX and pattern = YXXXXXX
- ☒ text = XXXXXXXXXXXXXXXXXXXXXXXXXXXX and pattern = XXXXXY
- ☐ text = XYXYXZXXXXXXXXXXXXXXXX and pattern = XYXYZ
- ☐ text = ABCDVABCDWABCDXABCDYABCDZ and pattern = ABCDE

Q2

6 Points


Q2.1

2 Points

Consider the following open-addressing hash table, with $h(x) = x \bmod 11$. Also, consider the following keys (in order): 17, 24, 30, 37, 13, 18.

Linear Probing	
Index	Key
0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

Assume that linear probing is being used for collision resolution. Draw the table after the keys shown above are inserted in the given order.

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Q2.2

1 Point

What is the total number of collisions in the previous question?

1

Q2.3

2 Points

Consider the following open-addressing hash table, with $h(x) = x \bmod 11$. Also, consider the following keys (in order): 17, 24, 30, 37, 13, 18.

Double Hashing	
Index	Key
0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

Assume that double hashing is being used for collision resolution, with $h_2(x) = (x \bmod 7) + 1$. Show the table after the keys shown above are inserted in the given order. For each collision indicate the value(s) of $h_2(x)$ for the colliding key x .

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Q2.4

1 Point

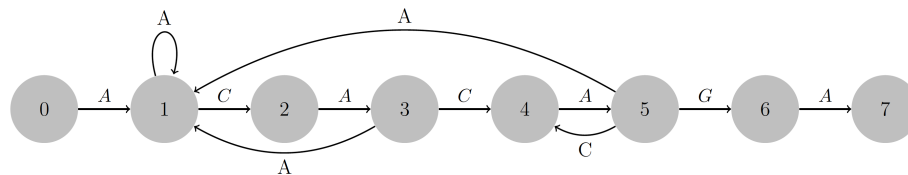
What is the total number of collisions in the previous question?

2

Q3

13 Points

The KMP string-matching algorithm computes the first index i of a text string txt of length n such that each of the m characters in the substring of txt starting at i matches the corresponding character in a pattern string pat of length m . Consider the below DFA, which resulted from pre-processing a particular pattern string. Answer the following questions using the given DFA.



Q3.1

1 Point

The pattern string is

ACACAGA

Q3.2

1 Point

The length of the pattern string is:

7

Q3.3

1 Point

Assuming the characters that appear in the pattern string are the only characters that appear in the alphabet, then the alphabet size R =

3

Q3.4

1 Point

If the DFA is in state 4, then the last four characters processed from the text string are

ACAC

Q3.5

1 Point

If the last six characters processed from the text string are ACACAC, then the DFA is in which state?

- ☐ 0
- ☐ 1
- ☐ 2
- ☐ 3
- ☒ 4
- ☐ 5
- ☐ 6
- ☐ 7

Q3.6

1 Point

Assume the 2-dimensional array `dfa[][]` is used to represent the above DFA. What is the value of `dfa[2]['A']`?

3

Q3.7

1 Point

The runtime of DFA construction in terms of m , n , and R is

$O(Rn)$

Q3.8

1 Point

What is the restart state after a mismatch in the sixth character of the pattern, that is, after matching ACACA?

4

Q3.9

3 Points

Construct the DFA for the following pattern. Draw the DFA **and** represent it as a 2-d array `dfa[m]`.

pattern = ACTACACTA

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Q3.10

1 Point

Given the below code for the KMP search algorithm, assuming a match was found starting from index 7 and the pattern string is 10 characters-long. What is the values of `i` right after the `for` loop?

```
public int kmp_search(String pat, String txt){
    int m = pat.length();
    int n = txt.length();
    int i, j;
    for (i = 0, j = 0; i < n && j < m; i++)
        j = dfa[j][txt.charAt(i)];
    if (j == m) return i-m;
    return n;
}
```

`i =`

8

Q3.11

1 Point

Given the below code for the KMP search algorithm, assuming a match was found starting from index 7 and the pattern string is 10 characters-long. What is the values of `j` right after the `for` loop?

```
public int kmp_search(String pat, String txt){
    int m = pat.length();
    int n = txt.length();
    int i, j;
    for (i = 0, j = 0; i < n && j < m; i++)
        j = dfa[j][txt.charAt(i)];
    if (j == m) return i-m;
    return n;
}
```

`j =`

10

Q4

13 Points

Consider the mismatched character heuristic of the Boyer-Moore string matching algorithm. The pattern string is ABRACADABRA. Answer the following questions.

Q4.1

1 Point

`right['A'] =`

10

Q4.2

1 Point

`right['B'] =`

8

Q4.3

1 Point

`right['C'] =`

4

Q4.4

1 Point

`right['D'] =`

6

Q4.5

1 Point

`right['E'] =`

-1

Q4.6

1 Point

`right['R'] =`

9

Q4.7

1 Point

Assume that the text string is `ABRAZADABRACADABRA`. What is the value of `j` (the index over the pattern string)? right before comparing the character `z` in the text.

4

Q4.8

1 Point

Assume that the text string is `ABRAZADABRACADABRA`. What is the value of `i` (the index over the text string)? right before comparing the character `z` in the text.

0

Q4.9
1 Point

Assume that the text string is `ABRAZADABRACADABRA`. What is the value of `j` (the index over the pattern string)? right after comparing the character `z` in the text.

10

Q4.10
1 Point

Assume that the text string is `ABRAZADABRACADABRA`. What is the value of `i` (the index over the text string)? right after comparing the character `z` in the text.

5

Q4.11
3 Points

For the pattern and text strings shown above, state and justify **using a drawing** how many total character comparisons must be done in order to match the pattern shown within the text string.

▼ 4.11.png Download

The diagram illustrates the process of matching the pattern string "ABRACADABRA" (in blue) against the text string "ABRAZADABRACADABRA" (in blue). A third instance of "ABRACADABRA" is shown in pink below the text string. Orange arrows and handwritten notes indicate the movement of indices: "j - right" points to the second 'A' of the pink string, and "i - left" points to the 'Z' in the blue text string. On the right side, a green tally of 14 comparisons is shown, with vertical lines grouped in sets of 4, 3, 3, and 4.

Homework 2

GRADED

STUDENT
Sushruti Bansod

TOTAL POINTS

27.5 / 37 pts

QUESTION 1

(no title)	5 / 5 pts
1.1 (no title)	1 / 1 pt
1.2 (no title)	1 / 1 pt
1.3 (no title)	1 / 1 pt
1.4 (no title)	1 / 1 pt
1.5 (no title)	1 / 1 pt

QUESTION 2

(no title)	3 / 6 pts
2.1 (no title)	2 / 2 pts
2.2 (no title)	1 / 1 pt
2.3 (no title)	0 / 2 pts
2.4 (no title)	0 / 1 pt

QUESTION 3

(no title)	9.5 / 13 pts
3.1 (no title)	1 / 1 pt
3.2 (no title)	1 / 1 pt
3.3 (no title)	1 / 1 pt
3.4 (no title)	1 / 1 pt
3.5 (no title)	1 / 1 pt
3.6 (no title)	1 / 1 pt
3.7 (no title)	0 / 1 pt
3.8 (no title)	0 / 1 pt
3.9 (no title)	2.5 / 3 pts
3.10 (no title)	0 / 1 pt
3.11 (no title)	1 / 1 pt

QUESTION 4

(no title)	10 / 13 pts
4.1 (no title)	1 / 1 pt
4.2 (no title)	1 / 1 pt
4.3 (no title)	1 / 1 pt
4.4 (no title)	1 / 1 pt
4.5 (no title)	1 / 1 pt
4.6 (no title)	1 / 1 pt
4.7 (no title)	1 / 1 pt
4.8 (no title)	1 / 1 pt
4.9 (no title)	1 / 1 pt
4.10 (no title)	1 / 1 pt
4.11 (no title)	0 / 3 pts

- 0 pts Correct

✓ - 3 pts Incorrect

- 1.5 pts Partial correct