

Input:  $\mathbf{W}^{h}$ ,  $\boldsymbol{\theta}^{\mathrm{BN}}$ ,  $\mathbf{U}_{\mathbf{W}}$ ,  $\mathbf{U}_{\boldsymbol{\theta}}$ ,  $(\mathbf{x}, \mathbf{y})$ , m,  $\eta$ . Output:  $\mathbf{W}^{h}$ ,  $\boldsymbol{\theta}^{\mathrm{BN}}$ ,  $\mathbf{U}_{\mathbf{W}}$ ,  $\mathbf{U}_{\boldsymbol{\theta}}$ .

1:  $\mathbf{W}^{\mathbf{b}} \leftarrow \operatorname{Sign}(\mathbf{W}^{\mathbf{h}}) \triangleright \operatorname{Computing binary weights}$ 

2:  $\hat{\mathbf{y}}$ , cache  $\leftarrow$  Forward( $\mathbf{x}, \mathbf{W}^{\mathbf{b}}, \boldsymbol{\theta}^{\mathrm{BN}}$ )  $\triangleright$  Perform inference

3:  $C \leftarrow \text{Cost}(\hat{\mathbf{y}}, \mathbf{y}) \triangleright \text{Compute mean loss over the batch}$ 

4:  $(\partial_{\mathbf{W}}C, \partial_{\theta}C) \leftarrow \text{Backward}(C, \hat{\mathbf{y}}, \mathbf{W}^{\mathbf{b}}, \boldsymbol{\theta}^{\text{BN}}, \text{cache})$  $\triangleright \text{Cost gradients}$ 

5:  $(\mathbf{U}_{\mathbf{W}}, \mathbf{U}_{\theta}) \in \mathrm{Adam}(\partial_{\mathbf{W}}C, \partial_{\theta}C, \mathbf{U}_{\mathbf{W}}, \mathbf{U}_{\theta})$ 

6: for Wh in Wh do

7: **if**  $U_W \cdot W^b > 0$  **then**  $\triangleright$ If  $U_W$  prescribes to decrease| $W^b$ | 8:  $W^h \leftarrow W^h - \eta U_W \cdot f_{\text{meta}}(m, W^h)$   $\triangleright$ Metaplastic update

9: else

10:  $W^{h} \leftarrow W^{h} - \eta U_{W}$ 

11: end if

12: end for

13:  $\theta^{\text{BN}} \in \theta^{\text{BN}} - \eta \mathbf{U}_{\theta}$ 

14: return Wh,  $\theta^{BN}$ ,  $U_w$ ,  $U_\theta$