

1:  $\hat{\mathbf{W}}^{\mathbf{b}} \leftarrow \operatorname{Sign}(\mathbf{W}^{\mathbf{h}}) \triangleright \operatorname{Computing binary weights}$ 2:  $\hat{\mathbf{y}}$ , cache  $\leftarrow \operatorname{Forward}(\mathbf{x}, \mathbf{W}^{\mathbf{b}}, \boldsymbol{\theta}^{\operatorname{BN}}) \triangleright \operatorname{Perform inference}$ 

Output: Wh,  $\theta^{BN}$ , Uw, U $_{\theta}$ .

3:  $C \leftarrow \text{Cost}(\hat{\mathbf{y}}, \mathbf{y}) \triangleright \text{Compute mean loss over the batch}$ 4:  $(\partial_{\mathbf{w}} C, \partial_{\boldsymbol{\theta}} C) \leftarrow \text{Backward}(C, \hat{\mathbf{y}}, \mathbf{W}^{\mathbf{b}}, \boldsymbol{\theta}^{\text{BN}}, \text{cache})$ 

⊳Cost gradients

Input:  $\mathbf{W}^{\mathbf{h}}$ ,  $\boldsymbol{\theta}^{\mathrm{BN}}$ ,  $\mathbf{U}_{\mathbf{W}}$ ,  $\mathbf{U}_{\boldsymbol{\theta}}$ ,  $(\mathbf{x}, \mathbf{y})$ , m,  $\eta$ .

5:  $(\mathbf{U}_{\mathbf{W}}, \mathbf{U}_{\theta}) \in \operatorname{Adam}(\partial_{\mathbf{W}}C, \partial_{\theta}C, \mathbf{U}_{\mathbf{W}}, \mathbf{U}_{\theta})$ 6: for  $W^{h}$  in  $W^{h}$  do

7: **if**  $U_W \cdot W^b > 0$  **then**  $\triangleright$ If  $U_W$  prescribes to decrease  $|W^b|$  8:  $W^h \leftarrow W^h - \eta U_W \cdot f_{\text{meta}}(m, W^h) \triangleright$ Metaplastic update

9: else

10:  $W^{\text{h}} \leftarrow W^{\text{h}} - \eta U_W$ 

11: end if 12: end for

13:  $\theta^{\text{BN}} \in \theta^{\text{BN}} - \eta \mathbf{U}_{\theta}$ 14: **return**  $\mathbf{W}^{\mathbf{h}}$ ,  $\theta^{\text{BN}}$ ,  $\mathbf{U}_{\mathbf{W}}$ ,  $\mathbf{U}_{\theta}$