## **Chapter 9: Math Operations With Arrays**



To keep track of your work, it is a good idea to work on all of the examples presented in this chapter as part of a new script. I suggest creating and saving a new script called chapter9\_examples.m to

keep track of your work. Make little comments so you can remember what and why you are doing things. LEARNING GOALS

As suggested, we will spend the majority of this chapter learning about how to manipulate arrays to perform complex mathematical operations quickly. To do so we will learn: Element-by-Element Math Operations on Arrays Addition, Subtraction (no dot)

 Multiplication, Division, Exponentiation (dot) MATLAB Built-In Functions for Working with Arrays

min() sum() sort()

Other useful MATLAB Functions

- median()
- o std()
- **Quick Note Warning on Linear Algebra**

o mean()

max()

- The linear algebra capabilities in MATLAB are part of what makes it powerful but because this is an introductory course, linear algebra will not be covered. The reason that I mention it here is because the linear algebra syntax is very similar to what we will learn in this section on element-by-element
- this section (e.g. omitting a single .) that will be hard to notice. Make sure you are being diligent!

## 

corresponding elements are added or subtracted. It is that easy.

**Addition and Subtraction with Arrays** 

and b{11} &b{12} \ b{*21*} &*b*{22} \end{bmatrix} \)

To see it in action, open up MATLAB and define the following four arrays (if you do not remember how

to create these arrays in MATLAB, see Chapter 8). You should notice that I am not showing you the

math operations. It is possible that you can make a tiny mistake when you are practicing problems in

Addition and subtraction of arrays works in the exact way that you think that it would. When you

attempt to use the + (addition) or - (subtraction) operator on arrays of identical size, the

(in this case \( a{11} \) could be any number, \( (a{12} \) could be any number, etc)

\end{bmatrix} \)

Now if we subtract A from B we get:

exact commands to enter these variables into the MATLAB workspace. From now on, I will assume you know how to create vectors and matrices.  $mat1 = \begin{bmatrix} 4 & 12 - 5 & 2.6 \end{bmatrix}$ 

Workspace Name ∠

> mat 1 mat 2

vecl wec2

-6.0000

Figure 9.3: Example of adding matrices in command window

Now that those four arrays are loaded into your Workspace (see figure 9.2 to the right to make sure you are on the same page) you can add or subtract the matrices. Keep these 4 arrays in your Workspace. We will be using them throughout the chapter. First, try adding [mat1] + [mat2] and storing that operation into a new variable called [mat3]. You

Value

Figure 9.2: Before continuing make sure your Workspace variables are identical!

[0,12,24]

[11,36,59]

[4,12;-5,2.6000]

[-10,2.3000;5,7]

1

Notice that it simply adds up the corresponding elements. The 1st row, 1st column of [mat3]contains the value -6 which is just 4 + (-10) which are the values in the 1st row, 1st column of [mat1] and [mat2] respectively. Question 9.1: Subtraction of Vectors Using the variables stored in your workspace, try the following subtraction operation: vec2-vec1 and store it in a new vector called vec3. What is the value of vec3(1)? Remember, arrays must be identical in size Hopefully, you agree that addition and subtraction with arrays is pretty straightforward. If you still need a little practice, I suggest just trying out different combinations of vectors and matrices in

should recall in Chapter 6 that we learned that scalars are just single numbers (as opposed to arrays which are collections of numbers). In the general case if we want to add the number s to the array A:

Adding or subtracting a scalar from an array is even easier than adding or subtracting arrays. You

You should see matlab displays an error Matrix dimensions must agree. The reason MATLAB is

Whenever you see the error Matrix dimensions must agree you should go back and look through

displaying this error to you is because the **dimensions of** mat1 **and** vec1 **are NOT identical.** 

a{11} + {s} &a{12} + {s} \  $a{21} + {s} &a{22} + {s}$ \end{bmatrix} \) You simply add s to every value in the array [A]! Subtraction works the exact same way. Question 9.2: Subtract a scalar

Using the 4 variables still stored in your Workspace, subtract the scalar 4 from mat1 and store

So if we multiply a 2x2 matrix [A] with a 2x2 matrix [B], the output is the multiplication of the corresponding elements. Hopefully you still have the 4 variables still stored in your Workspace. — ♀ STOP & THINK Before continuing, THINK about multiplying mat1 \* mat2 and storing in a new matrix called huh.

What should the value of huh(1,1) be? Do not skip your brain workout! It only takes one second and

Ok, now that you have a prediction for what happens, go ahead and type in >> huh = mat1 \* mat2

into the command window. Your new variable huh should look identical to figure 9.4 below.

the number 20 showing up in huh(1,1)?

multiplication (as are the / and ^ symbols) so we need to specify the . to let MATLAB know we want to perform element-by-element operations. That means that unless you are specifically doing linear algebra, you will want to put a ... before you perform multiplication, division, or exponentiation with arrays. Do not indiscriminately add dots to your equations! Table 9.1 below shows the only times that you need dots. Symbol Description Example you should try Multiplication mat1 .\* mat2 . \* ./ mat1 ./ mat2 Division

Table 9.1: When to use the . operator.

a new section. If you forgot how to do this, a quick recap of Chapter 7 should help.

corresponding values of the evaluated function in a new array called fun.

mathematical operation for every value like this:

 $\Rightarrow$  fun(1) = (-3)^3 - 6\*(-3)^2 + (-3) - 10

 $\Rightarrow$  fun(2) = (-2)^3 - 6\*(-2)^2 + (-2) - 10

reading until you have some ideas about how to proceed.

we can use arrays and array mathematics to solve this problem quickly.

... etc etc... but please **DO NOT DO THIS!** 

—— ♀ STOP & THINK

**Solution:** 

**Step 2)** To solve for the function at every different value of x, you just need to perform the mathematical operations onto the array of x like this: >> fun =  $x.^3 - 6*x.^2 + x - 10$ ; When you are done, the section in your script file should look similar to figure 9.6 below. %% Chapter 8 Challange Problem 1 2 % Created on: 1 July 2019 % By: Samuel Bechara, PhD 3

element in array A. Returns the smallest

>> all = sum(vec1)

>> low2high = sort(mat1)

Adds all the elements in the

array A and returns the

Arranges the elements in

the array in ascending

sum.

order.

**End of Chapter Items** 

Personal Reflection - Chapter 9 This is a completely anonymous submission. The professor will be able to see the responses but the responses will not be attributed to an author. Your participation is required. What do you think about the content of this chapter? Again, there is a lot of new material in this chapter wouldn't you agree? Do you need some more practice before you understand this material? Do

like to see differently? Any feedback is appreciated.

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Request for Feedback - Chapter 9

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some personal reflection about your learning.

This is a completely anonymous submission. The professor will be able to see the responses but the responses will not be attributed to an author. Your participation is required. What did you think of this chapter? Anything stand out as exceptionally good? Anything that you would **Image Citations** 

material. Up until this point, the power of MATLAB has been below the surface. If you recall from Chapter 8, MATLAB stands for MATrix LABoratory. In this chapter, we will learn functions and commands that make use of the most powerful MATLAB features.

In the general case, if we have a matrix A and a matrix B with elements: a{11} &a{12} \ a{21} &a{22} \end{bmatrix} \)

 $([A] - [B] = \left\{ begin\left\{ bmatrix \right\} \right\}$ a{11} - b{11} &a{12} - b{12} \ a{21} - b{21} &a{22} - b{22} We simply subtract the corresponding elements. Addition works the exact same way. It also works the exact same way with vectors (Recall, vectors are 1 dimensional arrays). The main thing to remember is that the arrays [A] and [B] must be the exact same size! TRY IT!

 $vec1 = \begin{bmatrix} 0 & 12 & 24 \end{bmatrix}$  $vec2 = [11 \ 36 \ 59]$ Hint: the first matrix can be input by typing >> mat1 = [4 12; -5 2.6]; but you need to figure out the rest on your own!

 $mat2 = \begin{bmatrix} -10 & 2.35 & 7 \end{bmatrix}$ 

can see the what that looks like in figure 9.3 below. >> mat3 = mat1+mat2 mat3 =

14.3000

9.6000

MATLAB and adding them and subtracting them until you are able to predict what the values of the output will be before you hit enter. Just to make sure you understand when you do make mistakes, make sure that you still have the original 4 arrays in your Workspace (see figure 9.3 above) and try the following in the command window:

your arrays to make sure they are the exact same size!

Adding or Subtracting a Scalar to an Array

>> mat1 + vec1

 $( \{A\} + \{s\} = \beta \{b \in \{b \in A\}\} )$ 

 $([A] * [B] = \left\{ begin\left\{ bmatrix \right\} \right\}$ a{11} \* b{11} &a{12} \* b{12} \

a{21} \* b{21} &a{22} \* b{22}

>> huh = mat1\*mat2

following into the command window:

>> oh\_okay = mat1 .\* mat2

27.6000

18.2000

Now THAT looks like what we are expecting! So what is going on?

Figure 9.5: Now it works?

>> oh\_okay = mat1 \*\* mat2

oh\_okay =

-40.0000

-25.0000

20.0000

63.0000

huh =

\end{bmatrix} \)

Multiplication, Division, and Exponentiation with Arrays If we want to perform element-by-element multiplication (or division, or exponentiation) on arrays it is almost identical to addition or subtraction, with just one tiny difference. What I mean by elementby-element multiplication would look like this in the general case:

in a new matrix called mat4. What is the value of mat4(1,1)?

will make the following example much more compelling.

93.2000

6.7000

Figure 9.4: Did we break MATLAB? So did we break MATLAB? Is MATLAB incapable of doing such a simple mathematical operation? The value of mat(1,1) is 4 and the value of mat2(1,1) is -10 so 4\*-10 should equal -40 so why is

Don't worry, MATLAB is NOT broken. It is simply doing a different type of math than what you are

time, add a . before the \* and lets store the result in a new matrix called oh\_okay . Type the

expecting. I'll explain what is happening in a bit, but for now, try the exact same operation, but this

mat1 .^ 2 Exponentiation ٠,

Lets put this all together in an example in MATLAB. In the script that you have already started, create

Now, Let us consider the function  $(\{f(x)\} = \{x^3\} - \{6x^2\} + \{x\} - \{10\}))$  and say that for whatever reason

we would like to calculate the value of the function at different values of x. Specifically, lets consider

evaluating the function at the following values: -3, -2, -1, 0, 1, 2, 3. Finally, lets store all of the

How can we perform the preceding question in MATLAB? We COULD type out the correct

The above "solution" would be wasting the power of MATLAB and would be extremely tedious. Instead, think about what we have learned and how it relates to this problem. Do not continue

I hope you didn't skip your brain workout. It is important! I hope that you have some inclination that

**Step 1)** define the x array in MATLAB. Notice that the values of x are from -3 to 3 and are equally

spaced by 1. Sound familiar? Sure! Just type in >> x = [-3:3] to define that vector.

Remember that *quick note* at the beginning of the chapter? The reason you need to add the . for

multiplication is to signify element-by-element operations. The \* is reserved for linear algebra

% Description: This problem solves a function fun 4 % for different values of x 5 6 % First, define x array 7 8 x = [-3:3];10 % Next, calculate the function values at each x fun =  $x.^3 - 6*x.^2 + x - 10$ ; 11 Figure 9.6: What your section script should look like. Hopefully, you wrote your comments in your own words. Also notice how the header and comments make it easier to understand what is going on! Question 9.3: Now here is the beauty of MATLAB! For this question, lets consider the preceding example, but this time, redefine x to be from x = 1to x=999 equally spaced by 1. To accomplish this, you should only have to modify two numbers in your script. After running it, you have now created a fun array with 1000 entries! Using this and what you know about MATLAB what is the function value evaluated at x = 257? That is the beauty of MATLAB! You can change one or two numbers, and re-run your script without having to do much work. If you struggled with the question above, it is ok! If you are struggling than

you are learning! But you also need to figure out a plan to make sure that you learn this material. It is

As mentioned in the previous chapter, arrays are the fundamental way to store data in MATLAB. Fun

Because arrays are so fundamental to the way that MATLAB operates, MATLAB comes pre-packaged

with several functions that can perform analysis on arrays. A non-comprehensive (but useful) list of

practice them on the 4 Workspace variables (mat1, mat2, vec1, vec2) that we have been using this

To learn these, I suggest that you create a new section of your chapter8\_examples.m script, and

chapter. Don't forget to read the help text on these functions as well as it can be very helpful!

In table 9.2, A is considered an array (don't forget an array can be a vector or a matrix).

critical to being a successful MATLAB programmer.

these functions is presented in the table below.

sum(A)

sort(A)

fact: a scalar in MATLAB is actually just stored as a 1x1 array!

**MATLAB Functions for Working With Arrays** 

**Function** Description Example you should try Returns the largest max(A)>> maximum = max(mat1) >> minimum = min(mat2) min(A) element in array A.

mean(A)	Returns the average of the elements in array A.	>> average = mean(vec2)
median(A)	Returns the median value of the elements in the array A.	>> med = median(vec1)
std(A)	Returns the standard deviation of the elements in vector A .	>> deviation = std(vec2)
Тал	ble 9.2: A collection of functions tha	t work specifically on arrays.
	ndow type >> help std , read the he	ly on matrices than on vectors. For exar lp text introductory paragraph, then ans
•	, consider a 5x8 matrix stored in the	variable random_man with random valus/are the dimensions of the variable y?