

Resolución TP7:

Ejercicio 5 - f

Graficar la región de integración R y e invertir el orden de integración.

$$I = \int_{b-r}^{b+r} \left[\int_{-\sqrt{r^2-(y-b)^2+a}}^{\sqrt{r^2-(y-b)^2+a}} f(x,y) dx \right] dy$$

Resolución:

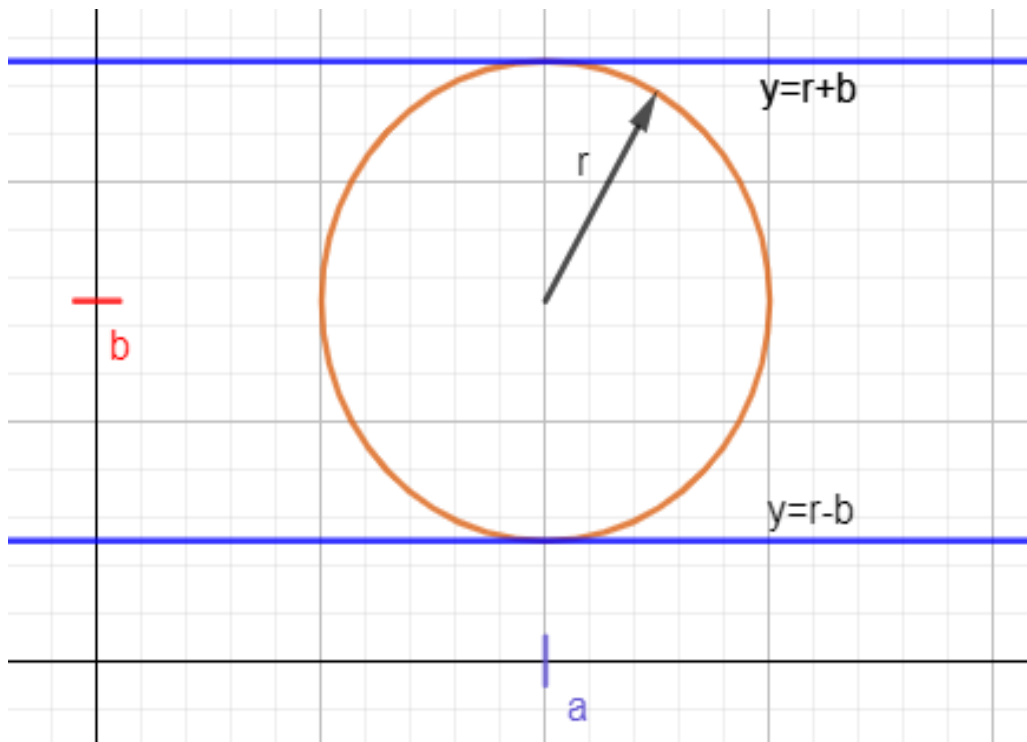
$$\text{de } r(y) = \left[\int_{-\sqrt{r^2-(y-b)^2+a}}^{\sqrt{r^2-(y-b)^2+a}} f(x,y) dx \right] \text{ se deduce}$$

$$-\sqrt{r^2 - (y - b)^2} + a \leq x \leq \sqrt{r^2 - (y - b)^2} + a$$

$$-\sqrt{r^2 - (y - b)^2} \leq x - a \leq \sqrt{r^2 - (y - b)^2}$$

$$(x - a)^2 \leq r^2 - (y - b)^2$$

$$(x - a)^2 + (y - b)^2 \leq r^2$$

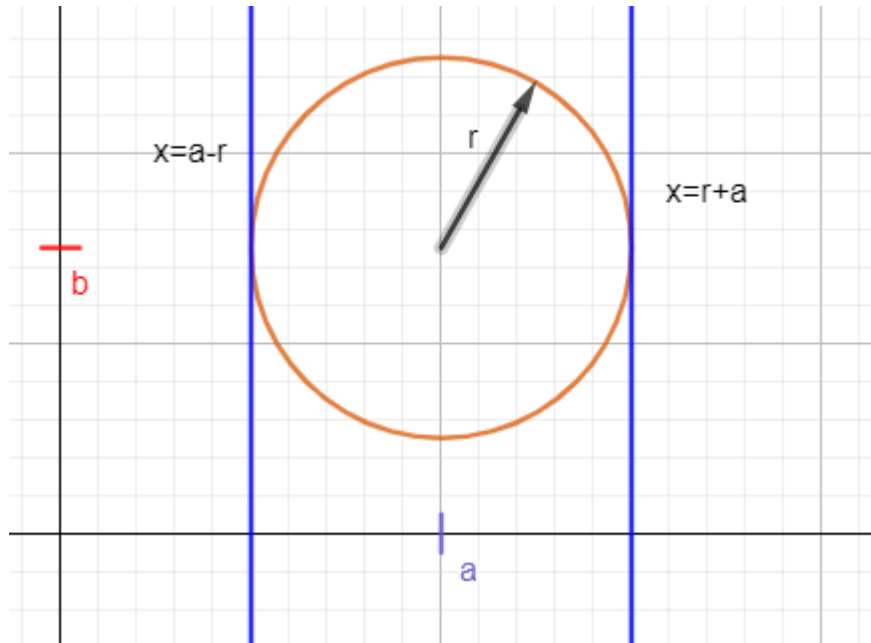


$$(x - a)^2 + (y - b)^2 \leq r^2$$

$$(y - b)^2 \leq r^2 - (x - a)^2$$

$$-\sqrt{r^2 - (x - a)^2} \leq y - b \leq \sqrt{r^2 - (x - a)^2}$$

$$-\sqrt{r^2 - (x - a)^2} + b \leq y \leq \sqrt{r^2 - (x - a)^2} + b$$



Finalmente:

$$I = \int_{a-r}^{a+r} \left[\int_{-\sqrt{r^2 - (x-a)^2} + b}^{\sqrt{r^2 - (x-a)^2} + b} f(x, y) dy \right] dx$$