

SBGN-ER vs rule-based modeling

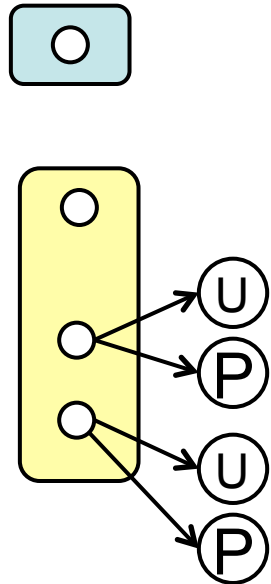
Michael Blinov

Center for Cell Analysis and Modelling
University of Connecticut Health Center

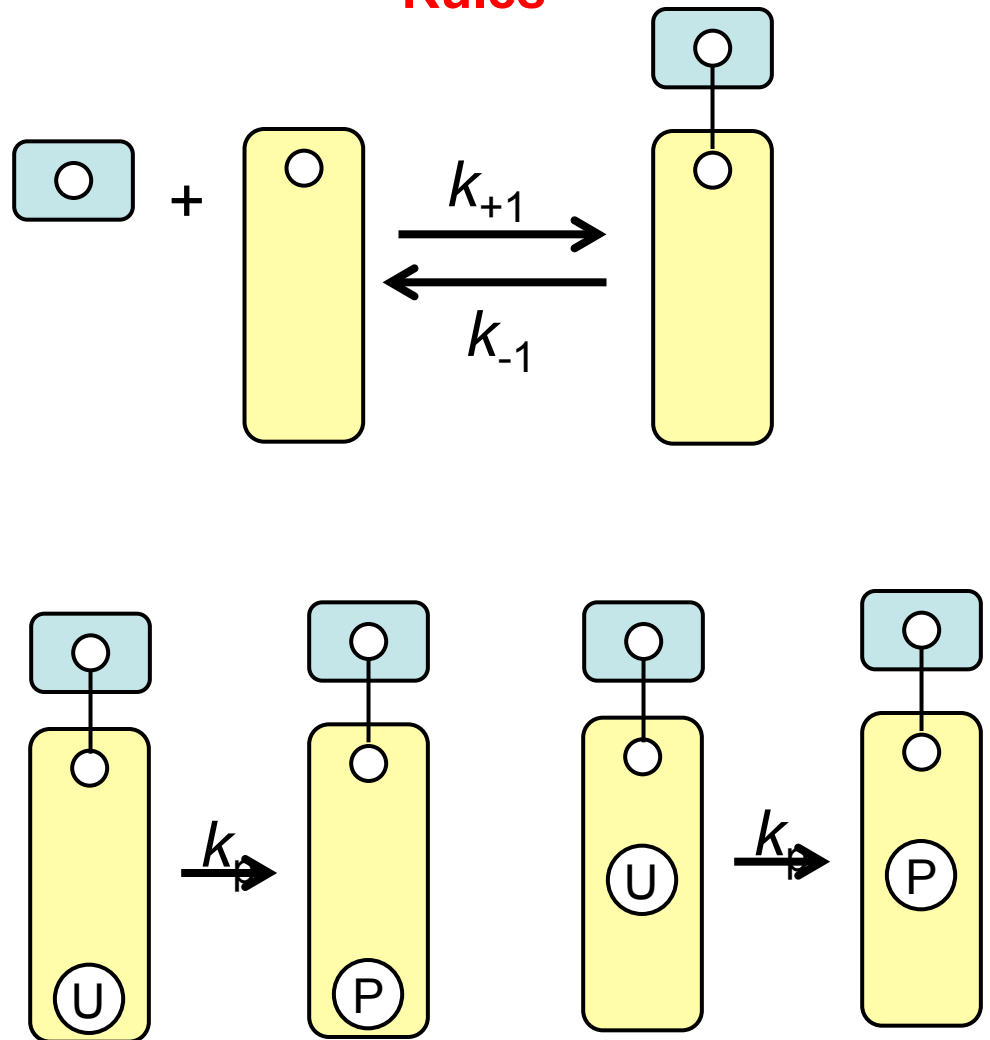
SBGN WORKSHOP, EDINBURGH, April 29th – May 2nd , 2013

Molecules, components and rules

Molecules, binding sites,
components and states

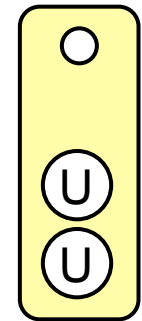


Rules

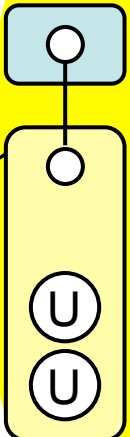
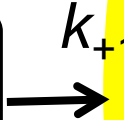
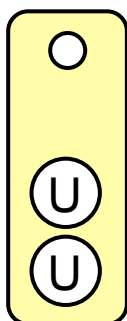
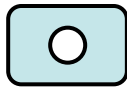


Rules generate reactions and species

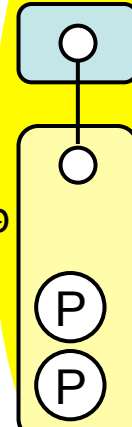
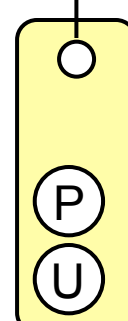
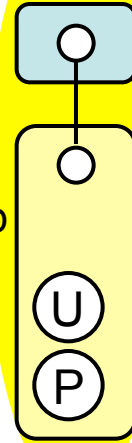
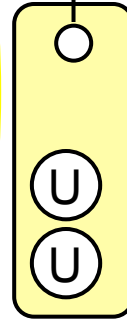
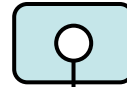
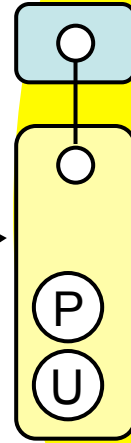
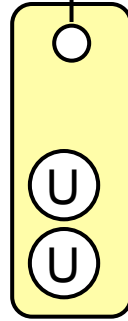
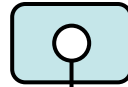
Seed
species: 2
species



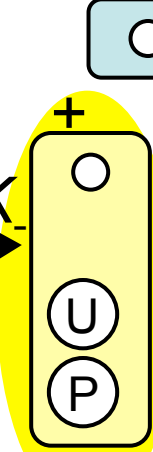
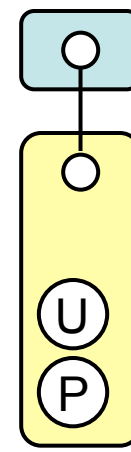
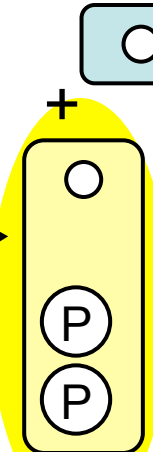
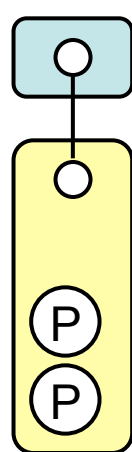
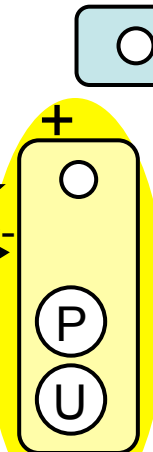
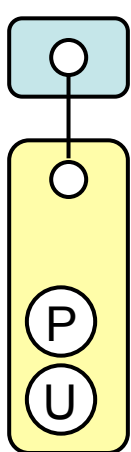
Rule 1 application:
1 reaction, 1 new species



Rule 2 application: 3 reactions, 3 new species

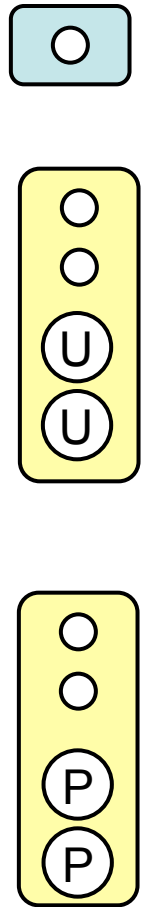


Rule 1R application: 3 reactions, 3 new species

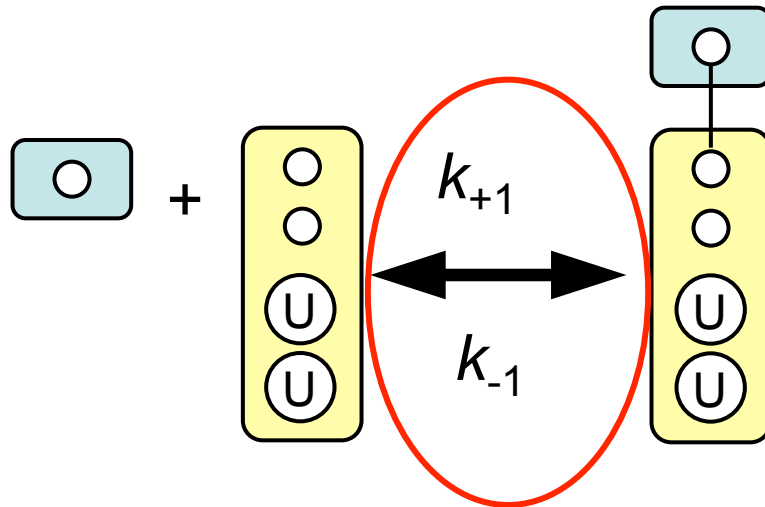


Rules generate reactions and new chemical species

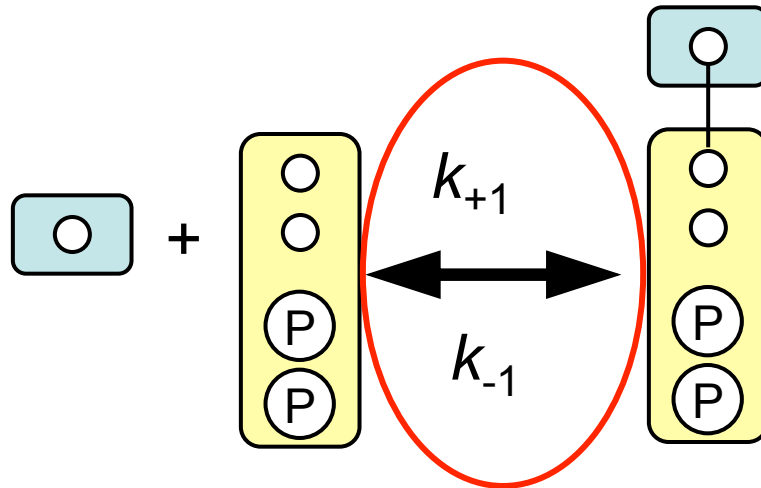
Set
of species



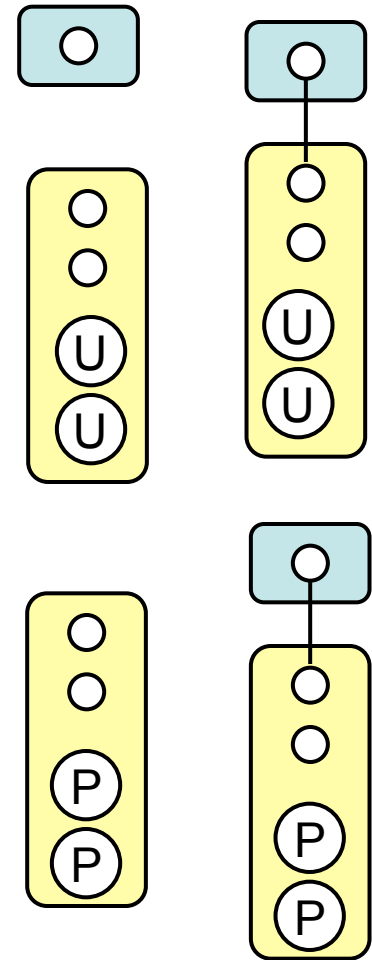
Rule application: reactions



All reactions inherit the same rate law.



New set
of species



Rule-based model generation

Input: initial species \mathbf{S}_0

Input: reaction rules \mathcal{R}



Rules application 1 $\mathcal{R}(\mathbf{S}_0) = \mathbf{R}_0, \mathbf{S}_1$

Rules application 2 $\mathcal{R}(\mathbf{S}_0 \cup \mathbf{S}_1) = \mathbf{R}_1, \mathbf{S}_2$

....

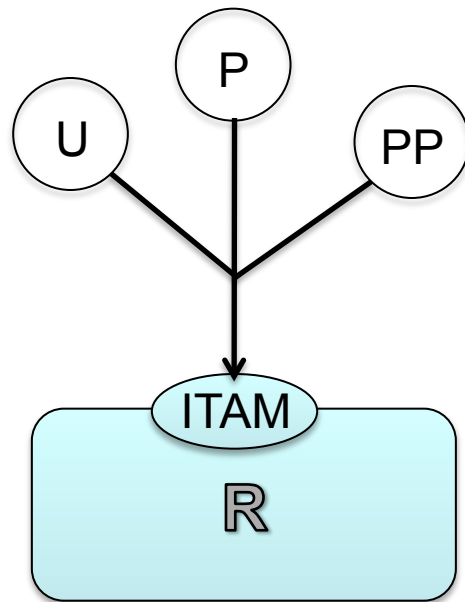
Rules application n $\mathcal{R}(\mathbf{S}_n) = \mathbf{R}_{n+1}, \mathbf{S}_{n+1}$

Termination Terminate if $\mathbf{S}_n = \mathbf{S}_{n+1}$



Model: species \mathbf{S}_n and reactions \mathbf{R}_{n+1}

Models and SBGN-ER are sometimes orthogonal, and annotations can connect them!



$$R(\text{ITAM} \sim U) \leftrightarrow R(\text{ITAM} \sim P) \quad p, d$$

$$R(\text{ITAM} \sim P) \leftrightarrow R(\text{ITAM} \sim PP) \quad 0.1 * p, 0.1 * d$$

$$R(\text{ITAM} \sim PP) \rightarrow R(\text{ITAM} \sim U) \quad 0.01 * d$$

How SBGN-ER can handle combinatorial complexity?

Epidermal growth factor receptor (EGFR)

9 sites $\Rightarrow 2^9=512$ phosphorylation states

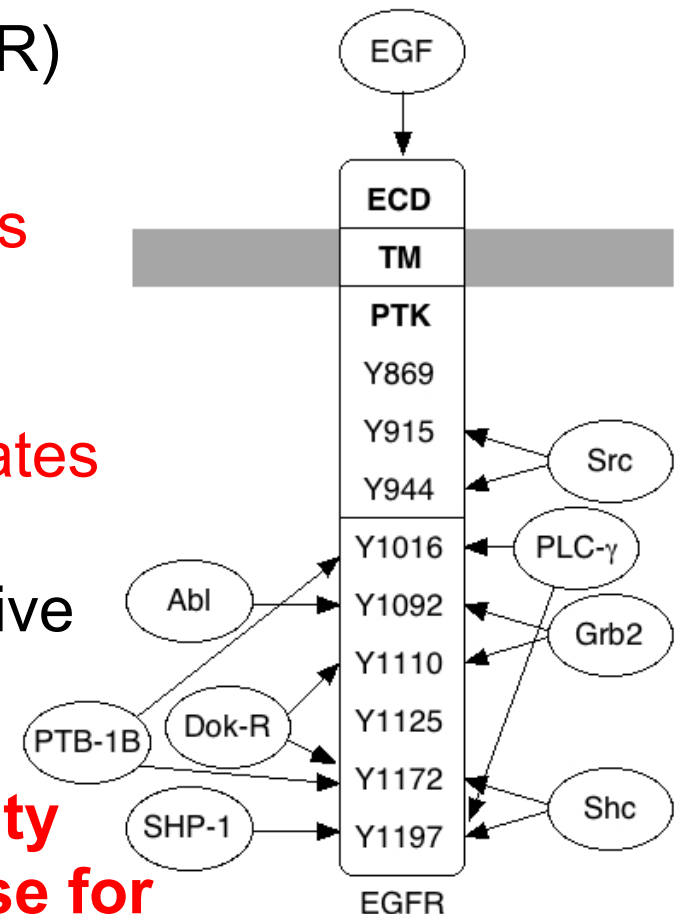
Each site has ≥ 1 binding partner

\Rightarrow more than $3^9=19,683$ total states

EGFR must form *dimers* to become active

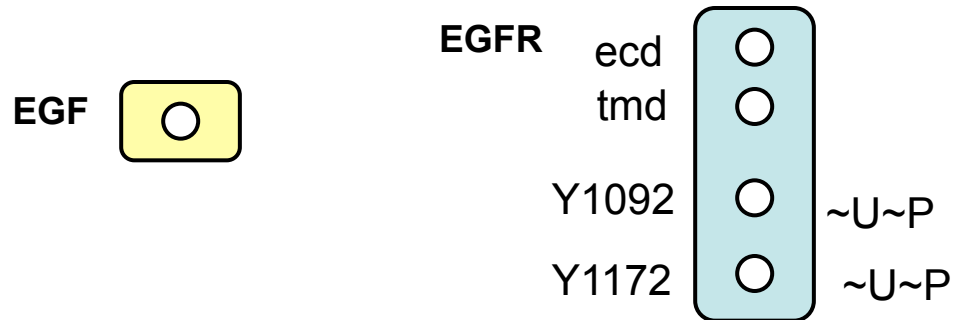
\Rightarrow more than 1.9×10^8 states

...but the number of entities and entity relationships is relatively small – case for SBGN-ER and rule0based modeling.

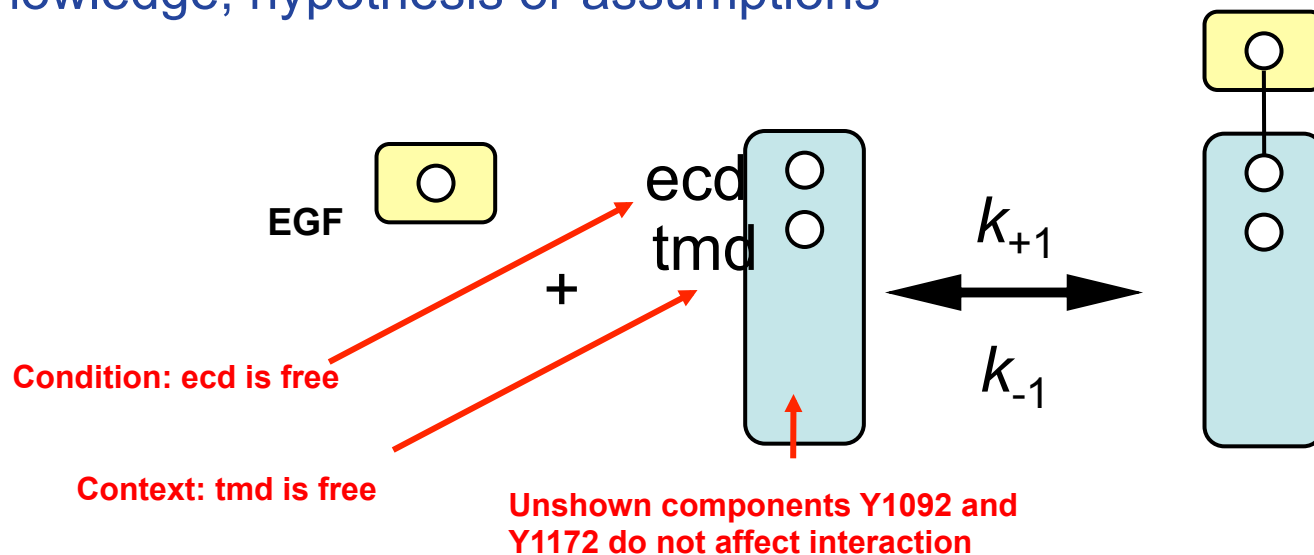


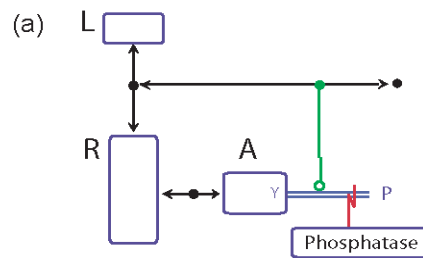
Rule-based approach

Biomolecules represented as collections of functional components

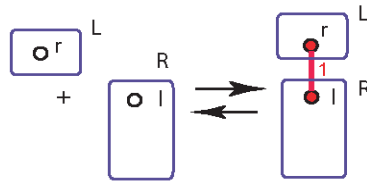


System evolves by reaction rules, that specify which biomolecules and their components affect kinetics of interactions. Rules correspond to knowledge, hypothesis or assumptions

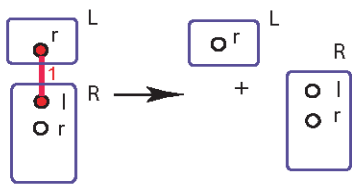
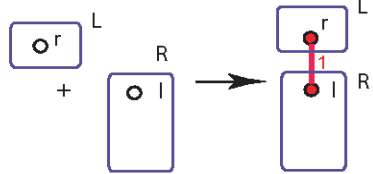




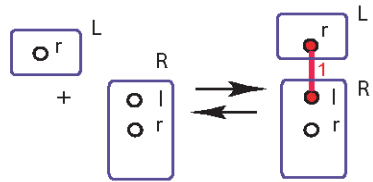
(b1) Ligand-binding independent on dimerization



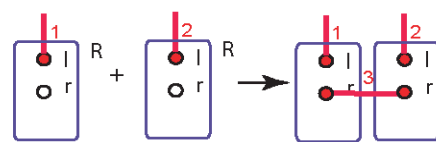
(b2) Ligand binds to any receptor, but can not dissociate in a dimer



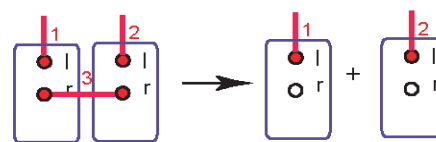
(b3) Ligand can interact with monomers only



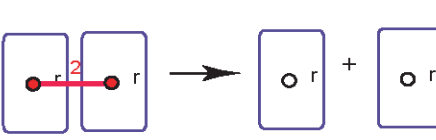
(c1) Dimer formation is ligand-induced



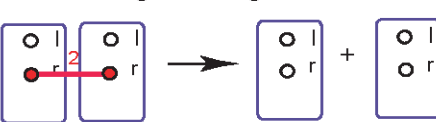
(c2) Dimer can break-up only when both ligands are present



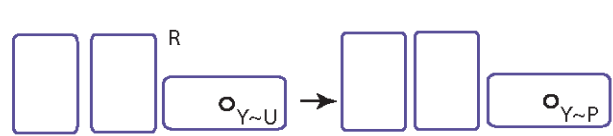
(c2) Dimer break-up is spontaneous



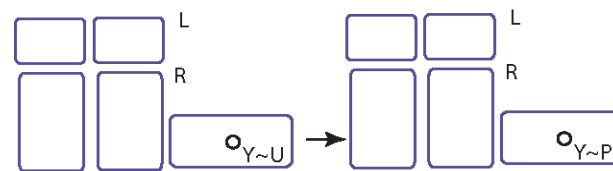
(c4) Dimer can break-up only after both ligand are gone.



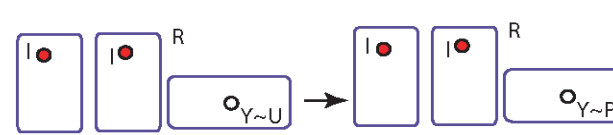
(d1) A is phosphorylated in a dimer



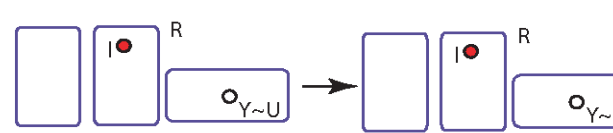
(c2) Phosphorylation requires 2 ligands L



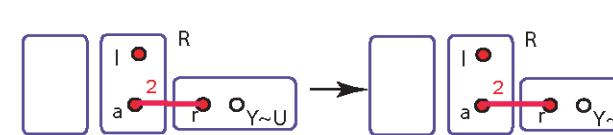
(d3) Phosphorylation requires two ligands



(d4) Phosphorylation requires at least one ligand

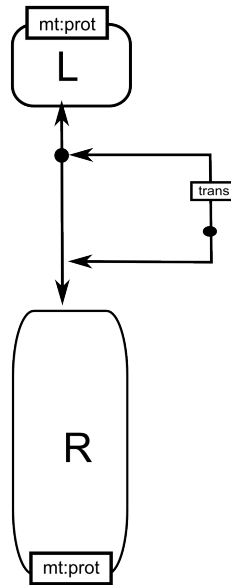


(d5) Explicit requirement which ligand is required

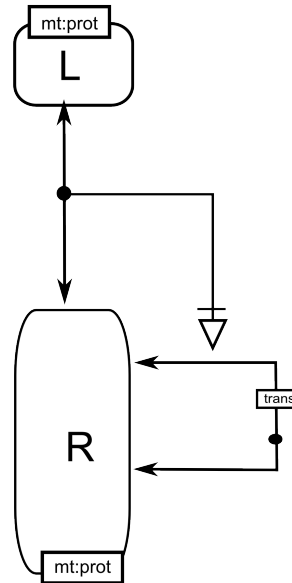


Specifying stoichiometry in ER is a problem...

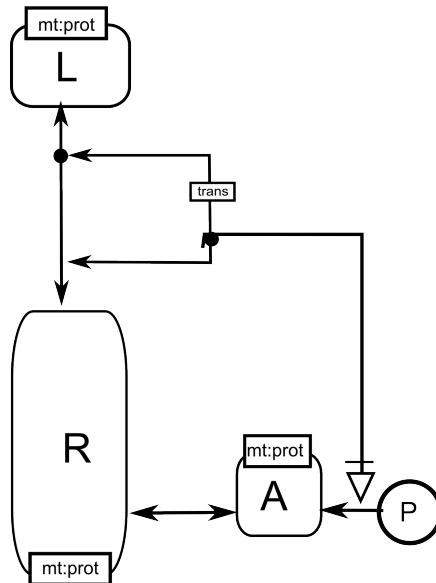
Two ligands are required for dimerization



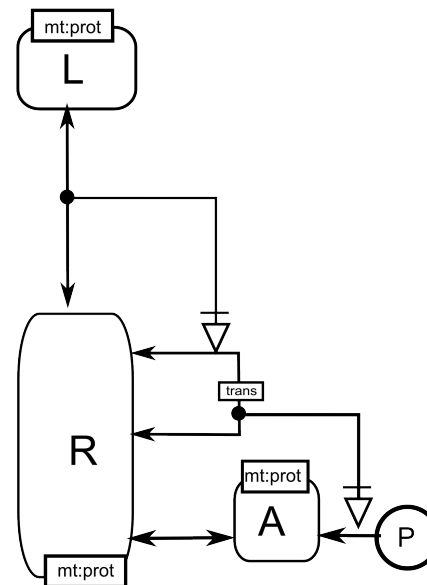
At least one ligand is required for dimerization



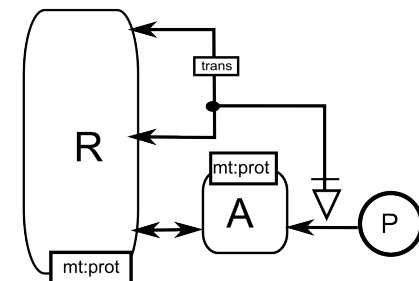
Two ligands are necessary for phosphorylation



One ligand is required for phosphorylation

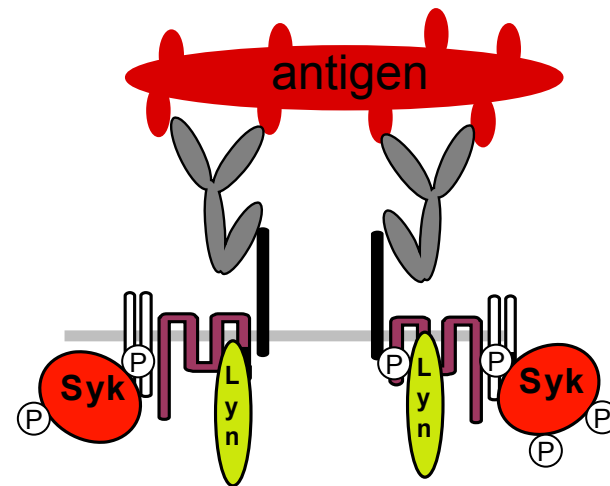


Two receptors are required for phosphorylation

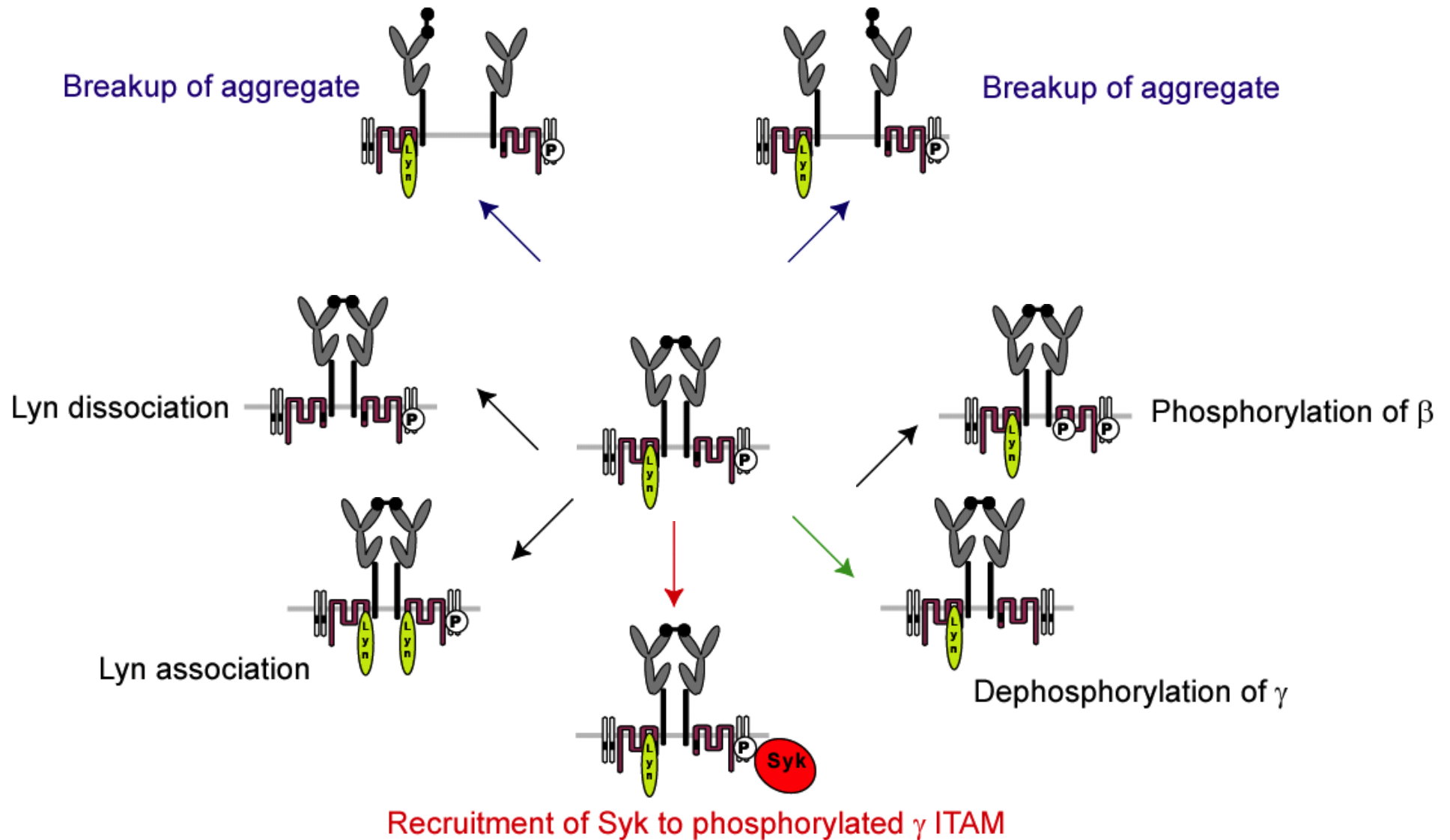


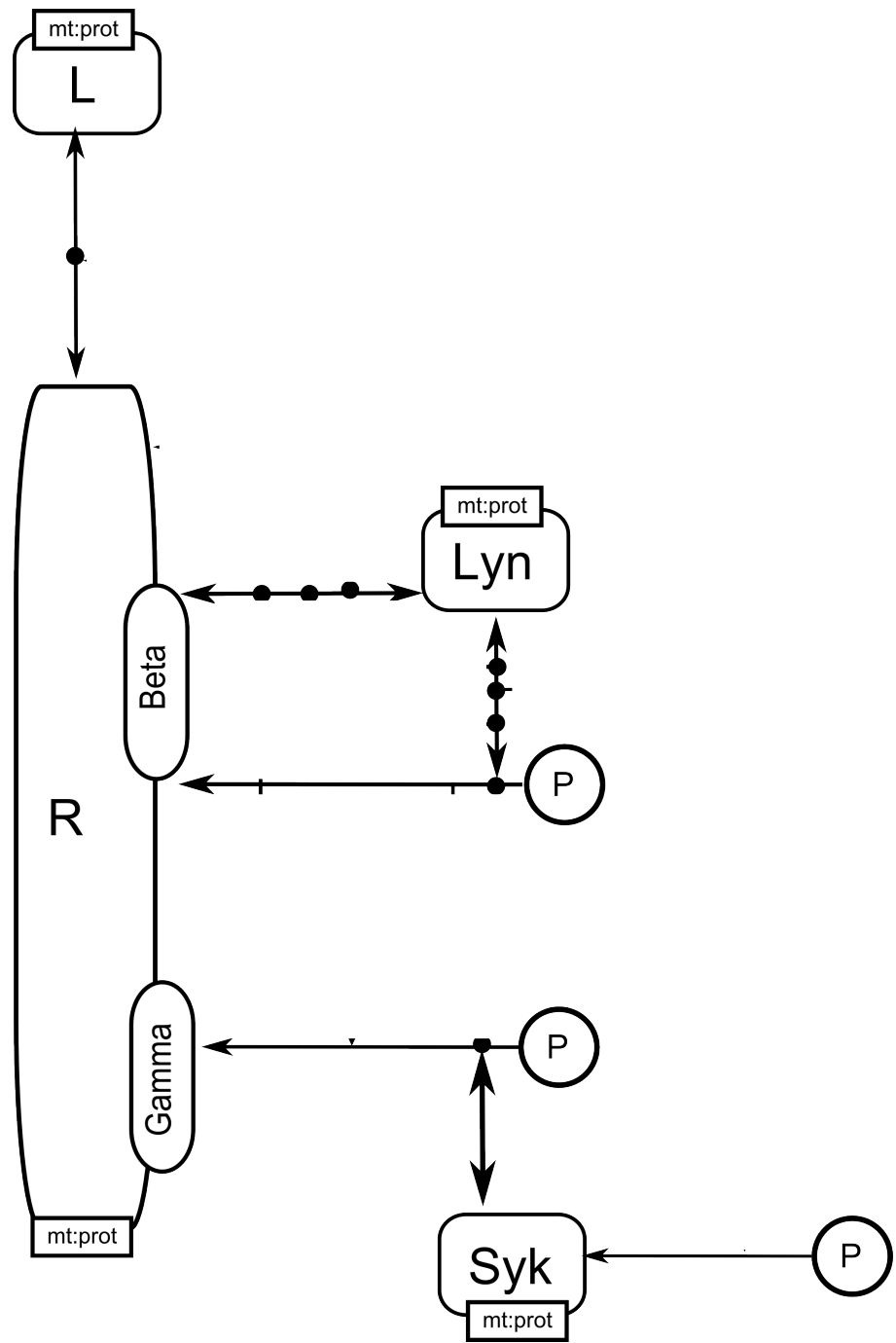
Early Events in FcεRI receptor Signaling

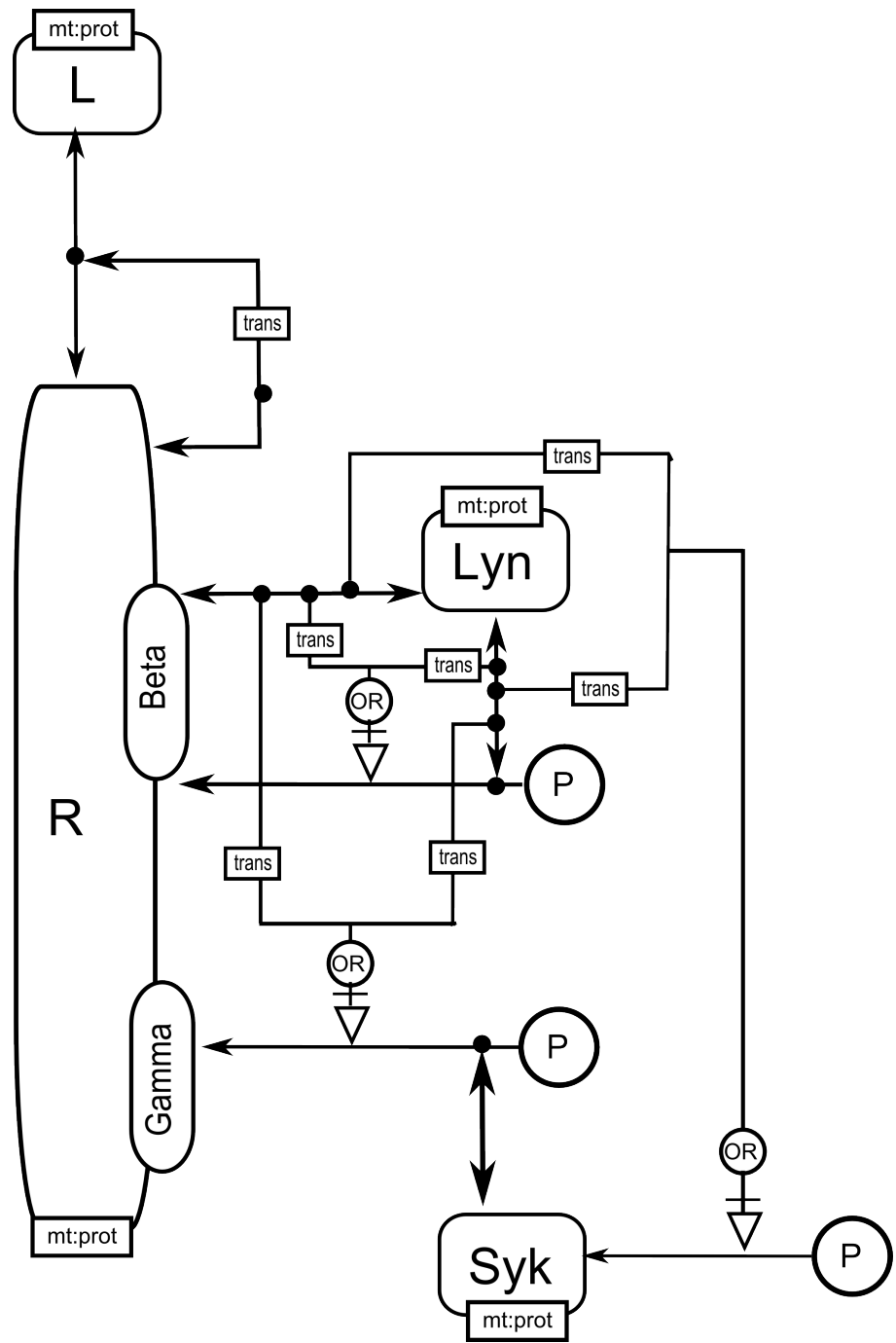
1. Multivalent antigen binds to IgE on cell surface forming aggregates
2. Tyrosine kinase Lyn associates with receptors and **transphosphorylates** ITAM tyrosines
3. Phosphorylated ITAMs recruit Syk and additional Lyn
4. Syk is transphosphorylated by Lyn or Syk
5. Phosphorylation of Syk is critical for downstream events (“activation”)



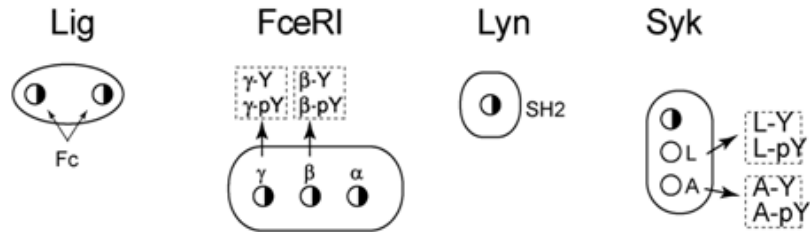
Not a pathway!





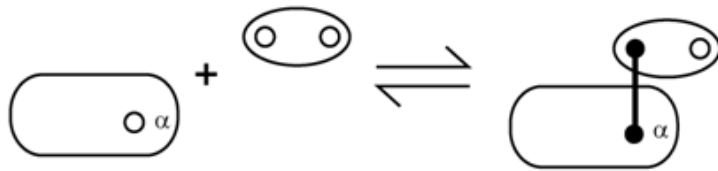


Molecules



Reaction Rules

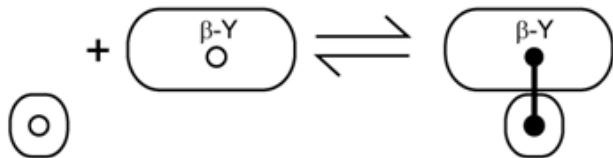
1. Ligand binding



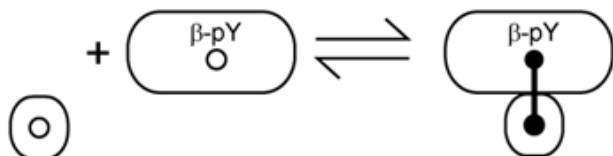
2. Ligand-induced aggregation



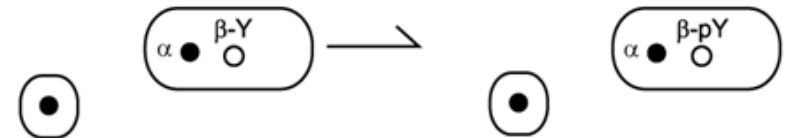
3. Binding of Lyn to unphosphorylated receptor



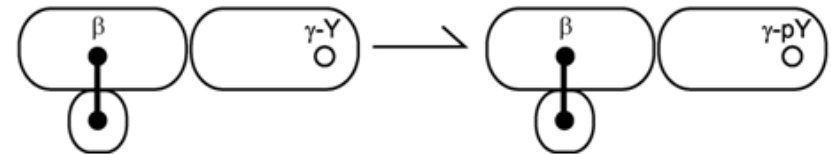
4. Binding of Lyn to phosphorylated receptor



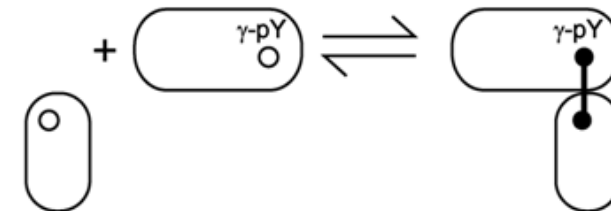
5. Transphosphorylation of β by Lyn



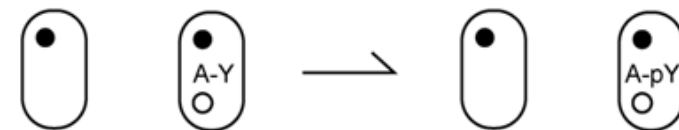
6. Transphosphorylation of γ by Lyn



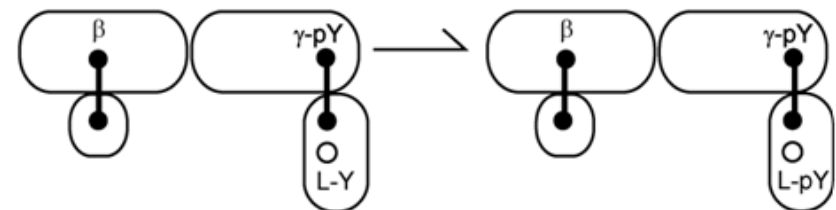
7. Binding of Syk to phosphorylated receptor

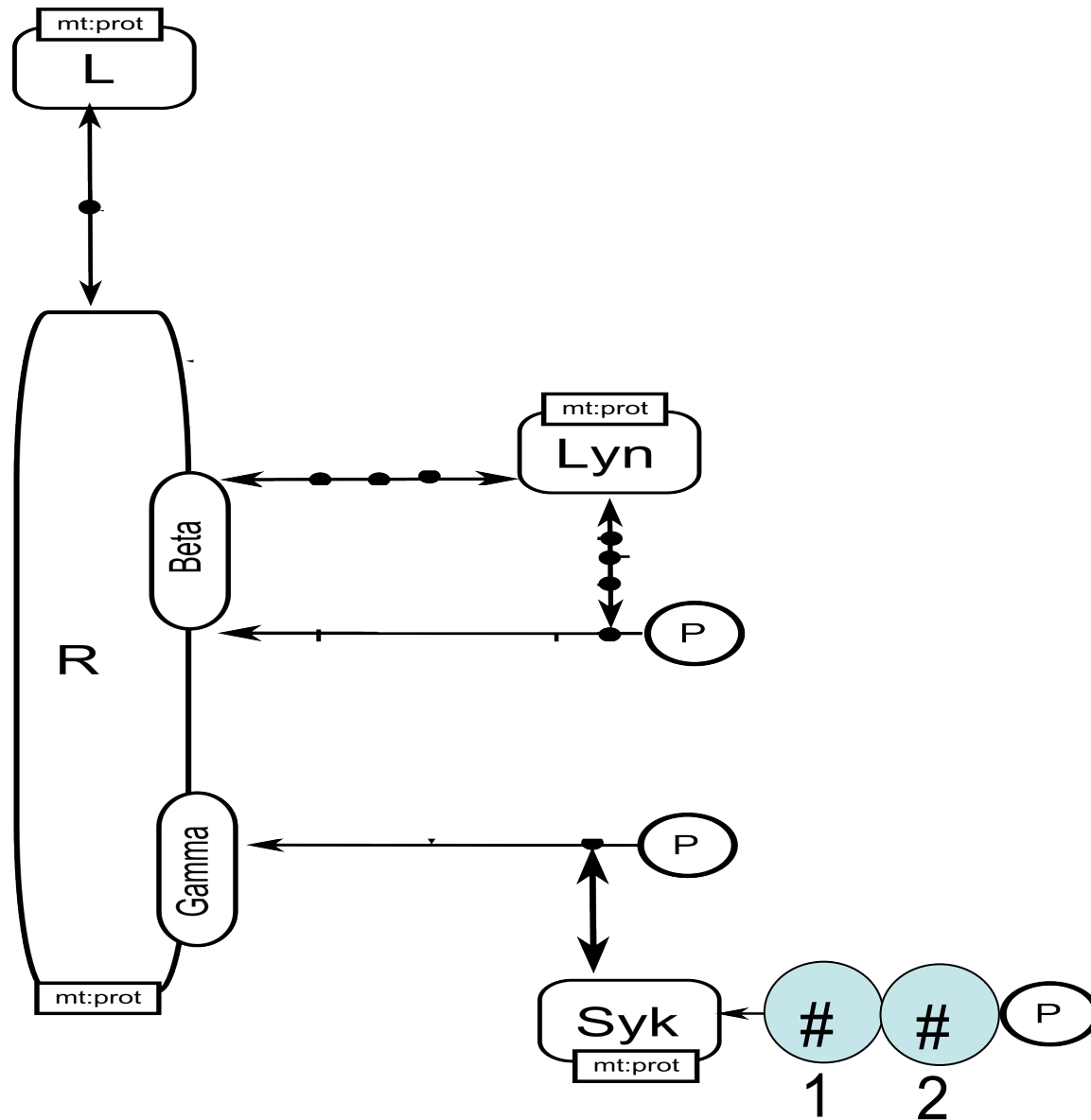


8. Transphosphorylation of Syk by Syk



9. Transphosphorylation of Syk by Lyn



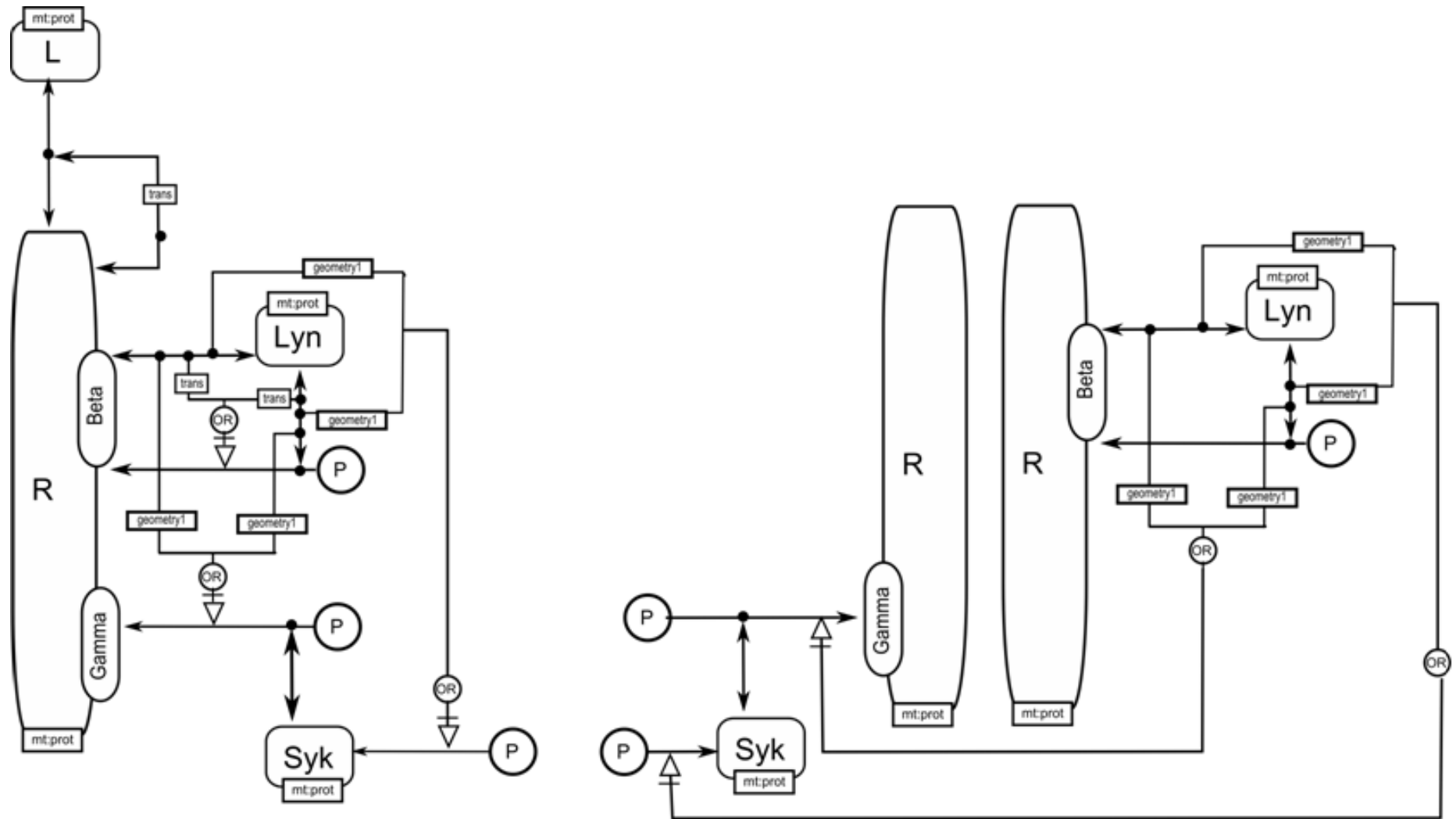


#1: $R().R().Syk(Y \sim U) \rightarrow R().R().Syk(Y \sim P)$

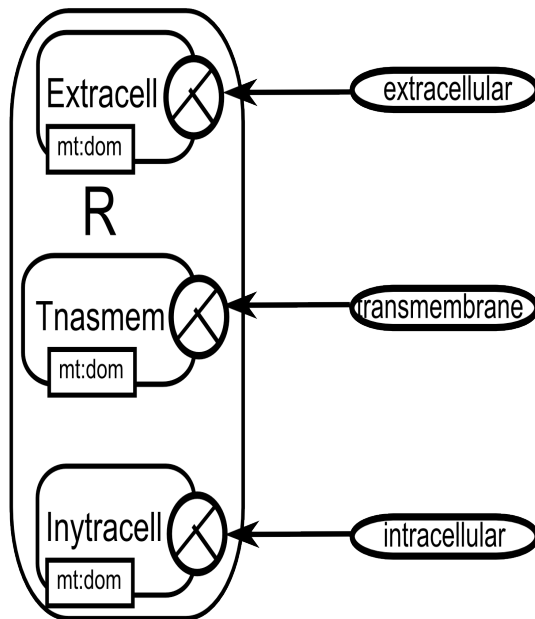
Issues

- Geometry is often essential, but cis and trans are not enough to express it.
- Separate interactions often require different context. Showing it on the same diagram is undesirable. How can we show what is essential and what is context?
- Domains are required.

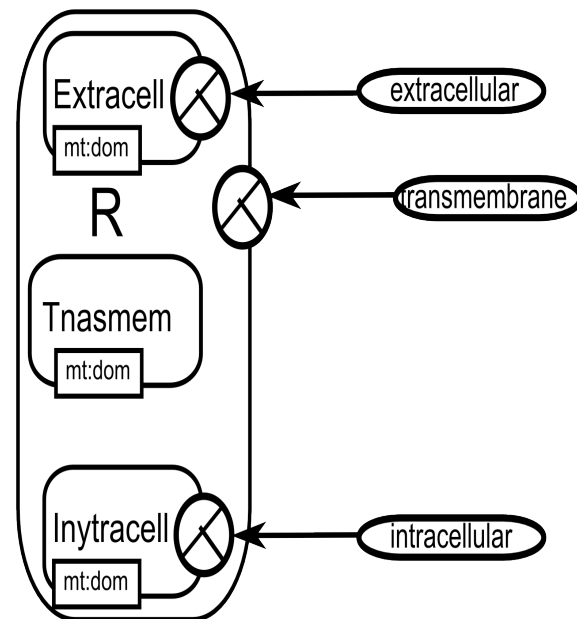
Displaying oligomers



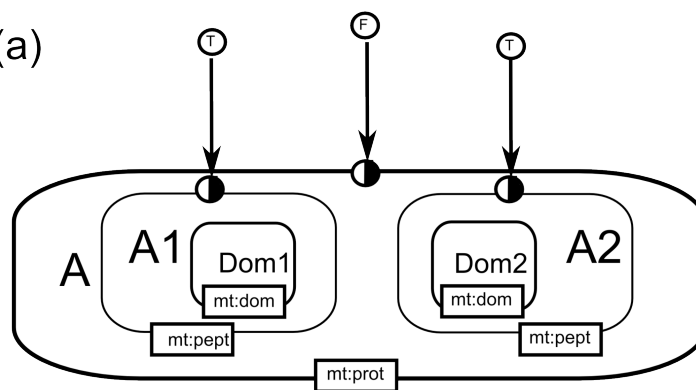
(a)



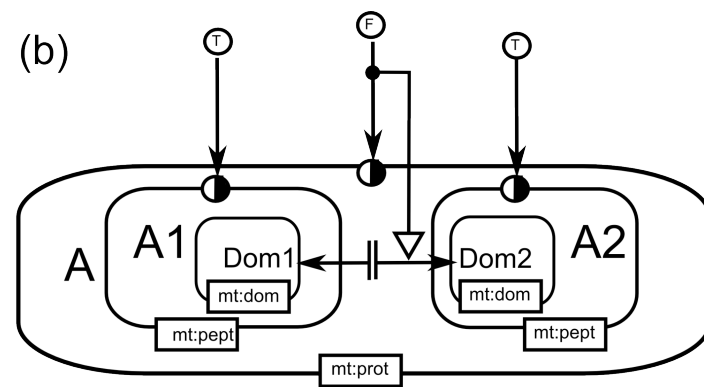
(b)

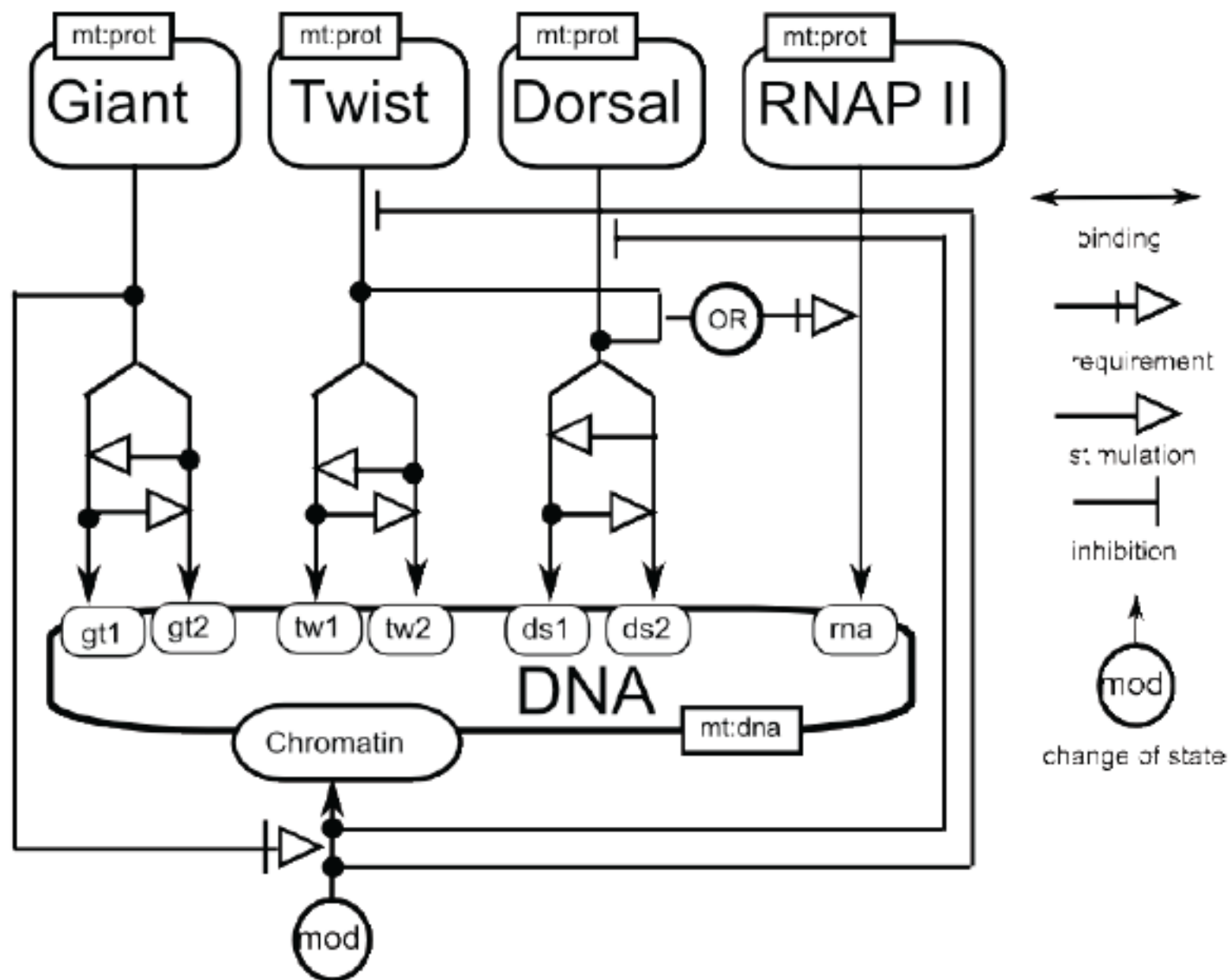


(a)



(b)





Suggestions for SBGN

- Strict rules for annotations!
- Different levels of details (like MIM): Explicit, Heuristic, Combinatorial.
- Separate interactions often require different context. Showing it on the same diagram is undesirable. How can we show what is essential and what is context?
- Think about human vs machine readability.

SBGN-ER

1. SBGN-ER for pathway elements, protein pages, etc.
2. Different levels of details (like MIM): Explicit, Heuristic, Combinatorial.
3. **Logic nodes AND, OR for simultaneous events and making a map more concise - VOTE**
4. Oligomers, topology - submaps
5. Clones
6. **Strict rules for annotations, legends: uncertainty, data - VOTE**
7. Submaps, compositionality
8. Hybrid maps: using PD, ER & AF together, linking different maps