

\*This coding assignment was discussed with Haoyuan Zheng, Yuquan Hu and Yuan Zhou.

P1a:

i	a(i)	alpha(i)	theta(i)	d(i)
0	0	0	None	None
1	0.033	$\pi/2$	$\theta(1)+\pi/2$	0.1
2	0.155	0	$\theta(2)+\pi/2$	0
3	0.135	0	$\theta(3)$	0
4	0	$\pi/2$	$\theta(4)+\pi/2$	0
5	0	0	$\theta(5)$	0

P2a:

(1) Homogeneous matrices first:

Handwritten equations for homogeneous transformation matrices:

$$H_1^0 = \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 & 0 & 0 \\ \sin \theta_1 & \cos \theta_1 & 0 & 0 \\ 0 & 0 & 1 & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_2^1 = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 & 0 & a_1 \\ 0 & 0 & -1 & 0 \\ \sin \theta_2 & \cos \theta_2 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_3^2 = \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & a_2 \\ \sin \theta_3 & \cos \theta_3 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_4^3 = \begin{bmatrix} \cos \theta_4 & -\sin \theta_4 & 0 & a_3 \\ \sin \theta_4 & \cos \theta_4 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

(2) By multiplying them together (Forward Kinematics), we get the homogeneous transform matrix:

```
[ [ (-sin(theta2)*sin(theta3)*cos(theta1) + cos(theta1)*cos(theta2)*cos(theta3))*cos(theta4) + (-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*sin(theta4)
  -(-sin(theta2)*sin(theta3)*cos(theta1) + cos(theta1)*cos(theta2)*cos(theta3))*sin(theta4) + (-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*cos(theta4)
  sin(theta1)
  -0.135*sin(theta2)*sin(theta3)*cos(theta1) + 0.135*cos(theta1)*cos(theta2)*cos(theta3) + 0.155*cos(theta1)*cos(theta2) + 0.33*cos(theta1) ]
[ (-sin(theta1)*sin(theta2)*sin(theta3) + sin(theta1)*cos(theta2)*cos(theta3))*cos(theta4) + (-sin(theta1)*sin(theta2)*cos(theta3) - sin(theta1)*sin(theta3)*cos(theta2))*sin(theta4)
  -(-sin(theta1)*sin(theta2)*sin(theta3) + sin(theta1)*cos(theta2)*cos(theta3))*sin(theta4) + (-sin(theta1)*sin(theta2)*cos(theta3) - sin(theta1)*sin(theta3)*cos(theta2))*cos(theta4)
  -cos(theta1)
  -0.135*sin(theta1)*sin(theta2)*sin(theta3) + 0.135*sin(theta1)*cos(theta2)*cos(theta3) + 0.155*sin(theta1)*cos(theta2) + 0.33*sin(theta1) ]
[ (-sin(theta2)*sin(theta3) + cos(theta2)*cos(theta3))*sin(theta4) + (sin(theta2)*cos(theta3) + sin(theta3)*cos(theta2))*cos(theta4)
  (-sin(theta2)*sin(theta3) + cos(theta2)*cos(theta3))*cos(theta4) - (sin(theta2)*cos(theta3) + sin(theta3)*cos(theta2))*sin(theta4)
  0
  0.135*sin(theta2)*cos(theta3) + 0.155*sin(theta2) + 0.135*sin(theta3)*cos(theta2) + 0.1 ]
[ 0 0 0 1 ] ]
```

(3) By differentiating theta1, theta2, theta3, theta4, theta5 correspondly in the homogeneous matrix and concatenate the result matrices together, we get the jacobian matrix:

```
[ [ -0.2175*(sin(theta1)*sin(theta2)*sin(theta3) - sin(theta1)*cos(theta2)*cos(theta3))*sin(theta4) + 0.2175*(sin(theta1)*sin(theta2)*cos(theta3) + sin(theta1)*sin(theta3)*cos(theta2))*cos(theta4)
  0.2175*(sin(theta2)*sin(theta3)*cos(theta1) - cos(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*sin(theta4)
  0.2175*(sin(theta2)*sin(theta3)*cos(theta1) - cos(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*sin(theta4)
  -0.2175*(-sin(theta2)*sin(theta3)*cos(theta1) + cos(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*sin(theta4)
  0 ]
[ -0.2175*(-sin(theta2)*sin(theta3)*cos(theta1) + cos(theta1)*cos(theta2)*cos(theta3))*sin(theta4) + 0.2175*(-sin(theta2)*cos(theta1)*cos(theta3) - sin(theta3)*cos(theta1)*cos(theta2))*cos(theta4)
  0.2175*(sin(theta1)*sin(theta2)*sin(theta3) - sin(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta1)*sin(theta2)*cos(theta3) - sin(theta1)*sin(theta3)*cos(theta2))*sin(theta4)
  0.2175*(sin(theta1)*sin(theta2)*sin(theta3) - sin(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta1)*sin(theta2)*cos(theta3) - sin(theta1)*sin(theta3)*cos(theta2))*sin(theta4)
  -0.2175*(-sin(theta1)*sin(theta2)*sin(theta3) + sin(theta1)*cos(theta2)*cos(theta3))*cos(theta4) - 0.2175*(-sin(theta1)*sin(theta2)*cos(theta3) - sin(theta1)*sin(theta3)*cos(theta2))*sin(theta4)
  0 ]
[ 0
  -0.2175*(-sin(theta2)*sin(theta3) + cos(theta2)*cos(theta3))*sin(theta4) + 0.2175*(-sin(theta2)*cos(theta3) - sin(theta3)*cos(theta2))*cos(theta4)
  -0.2175*(-sin(theta2)*sin(theta3) + cos(theta2)*cos(theta3))*sin(theta4) + 0.2175*(-sin(theta2)*cos(theta3) - sin(theta3)*cos(theta2))*cos(theta4)
  -0.2175*(-sin(theta2)*sin(theta3) + cos(theta2)*cos(theta3))*sin(theta4) - 0.2175*(sin(theta2)*cos(theta3) + sin(theta3)*cos(theta2))*cos(theta4)
  0 ] ]
```