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Oregon Center for Optical,  
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# A Single Photon Detector Design based on a First Order Dissipative Phase Transition

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## Model

**A driven dissipative first order phase transition: Nonlinear Kerr Model**

$$\hat{H} = -\Delta \hat{a}^\dagger \hat{a} + \frac{U}{2} \hat{a}^\dagger \hat{a}^\dagger \hat{a} \hat{a} + F(\hat{a}^\dagger + \hat{a})$$

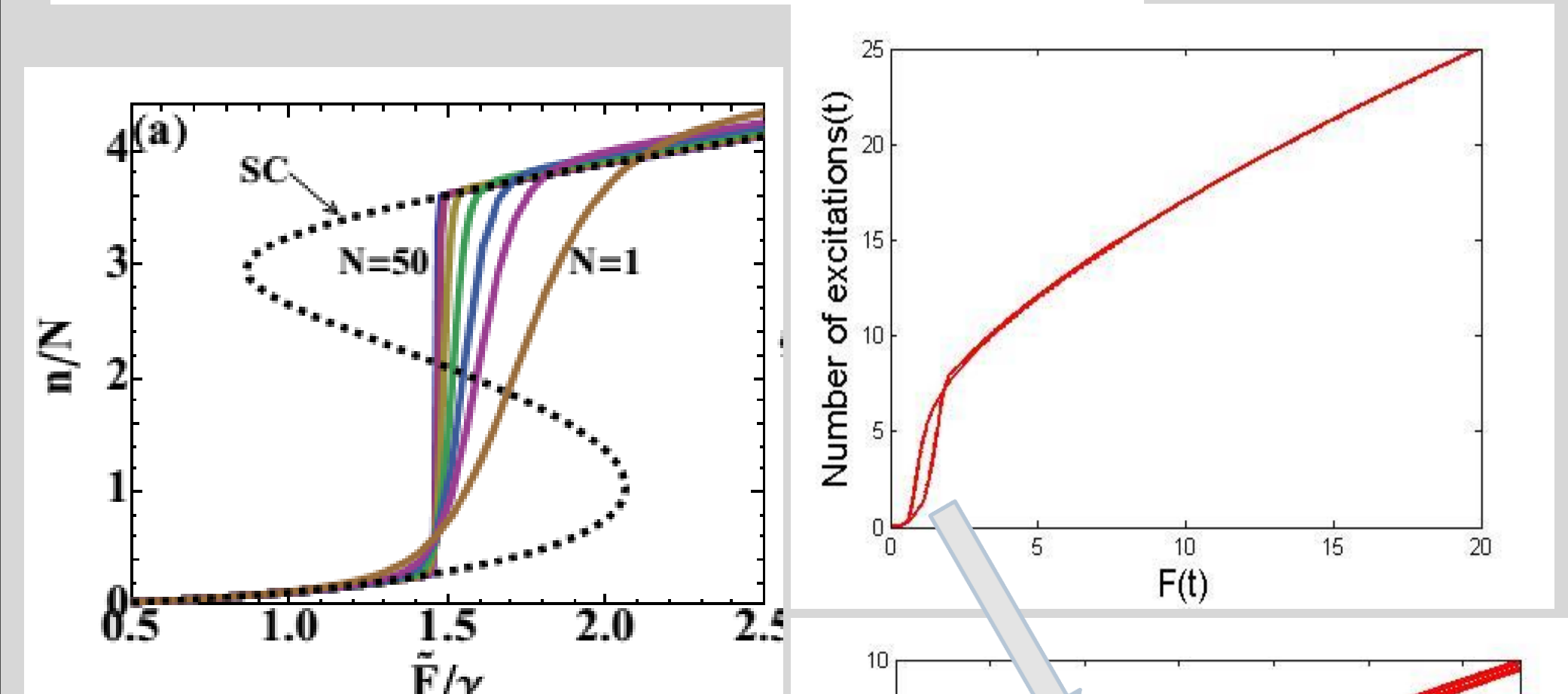
1. Single-site critical phenomena: dynamical optical hysteresis in the Kerr model.

Storme, F. (2017). *Dissipative phase transitions in open quantum lattice systems* (Doctoral dissertation, Université Paris Diderot (Paris 7), Sorbonne Paris Cité).

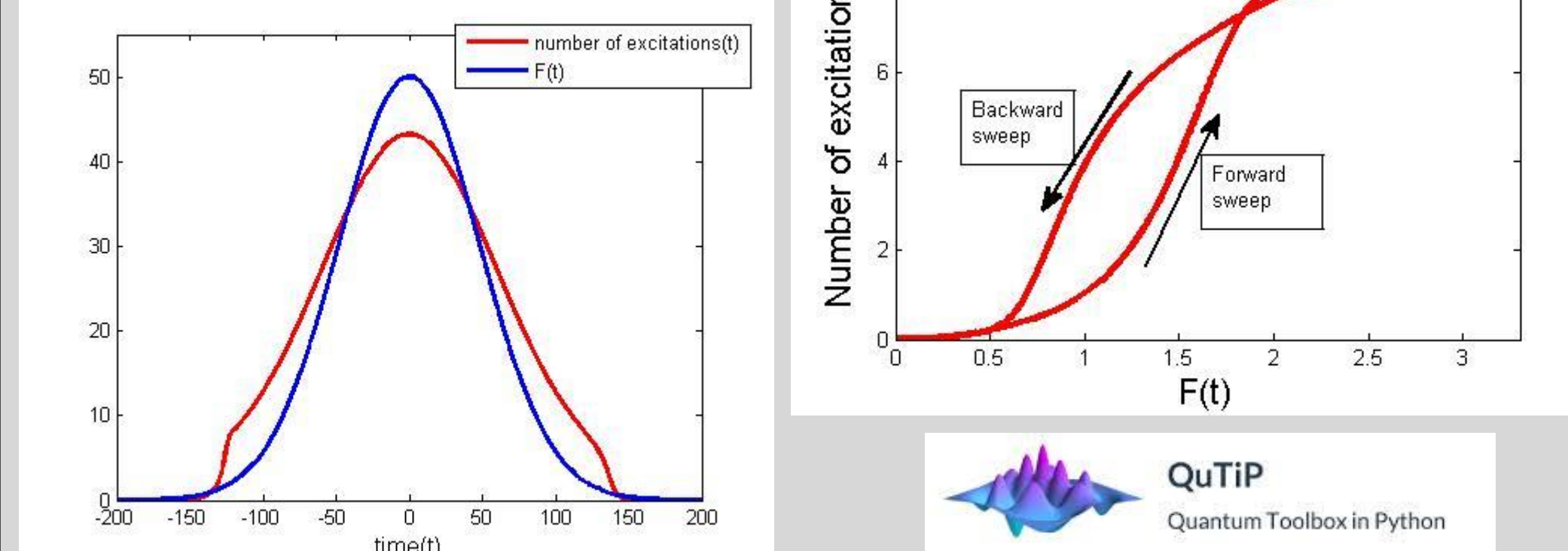
2. A superconducting, ladder-type artificial atom, a transmon, strongly coupled to a waveguide

Gasparinetti et al. (2019). Two-Photon Resonance Fluorescence of a Ladder-Type Atomic System. *arXiv preprint arXiv:1901.00414*.

$$\partial_t \hat{\rho} = -i[\hat{H}, \hat{\rho}] + \frac{\gamma}{2} (2\hat{a} \hat{\rho} \hat{a}^\dagger - \hat{a}^\dagger \hat{a} \hat{\rho} - \hat{\rho} \hat{a}^\dagger \hat{a})$$



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$$H = -\Delta b^\dagger b + \frac{U}{2} b^\dagger b^\dagger b b + \hat{F}(b^\dagger + b) + H_{ph-F}$$

$$H_{ph-F} = \sqrt{\kappa} \phi(t) |F_1\rangle \langle F_0| + H.C.$$

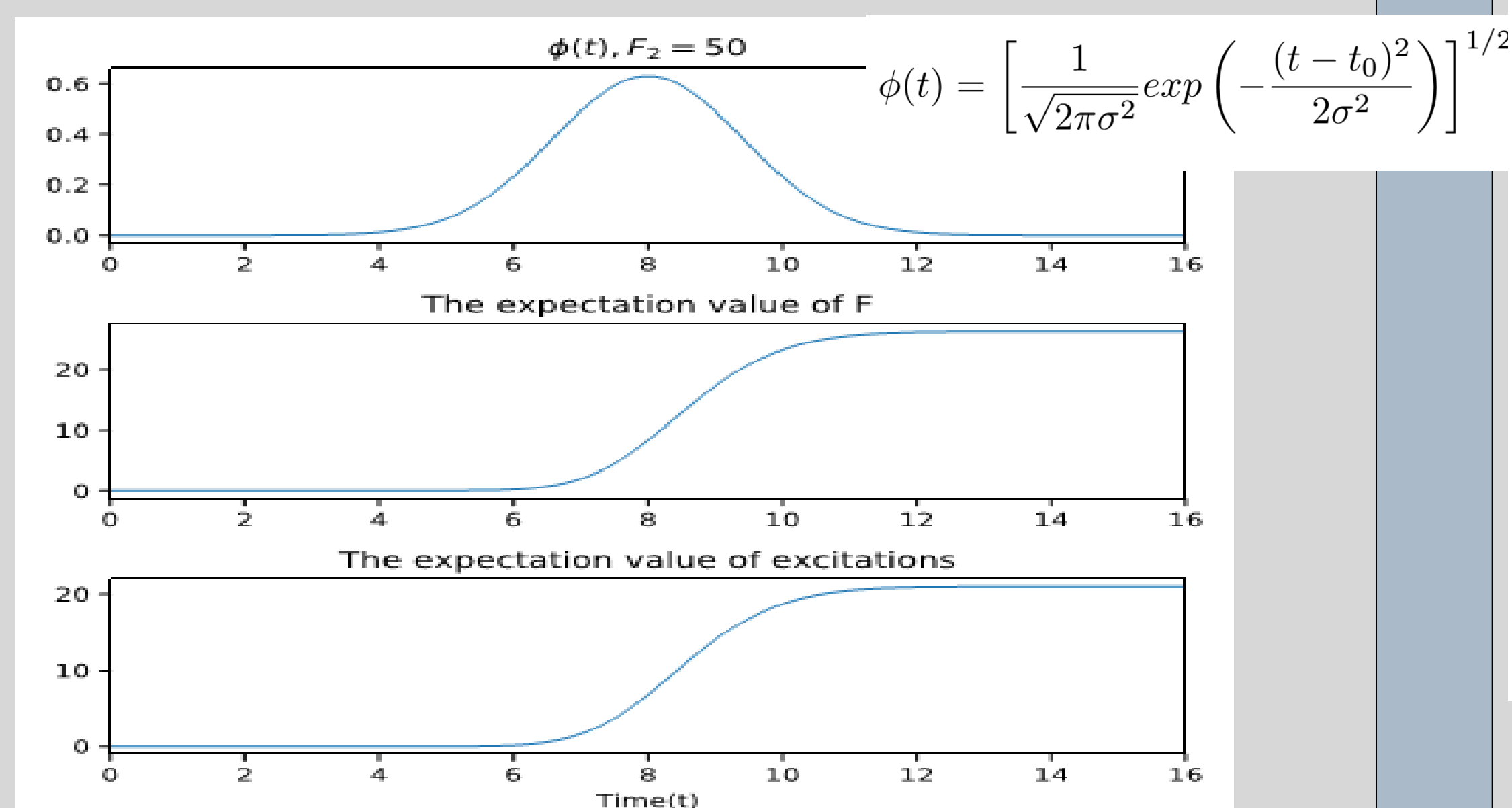
$$\hat{F} = F_0 |F_0\rangle \langle F_0| + F_1 |F_1\rangle \langle F_1| + F_2 |F_2\rangle \langle F_2|$$

$$\dot{\rho} = -\frac{i}{\hbar} [H, \rho] + \mathcal{L}_A + \mathcal{L}_B + \mathcal{L}_C + \mathcal{L}_D + \mathcal{L}_E$$

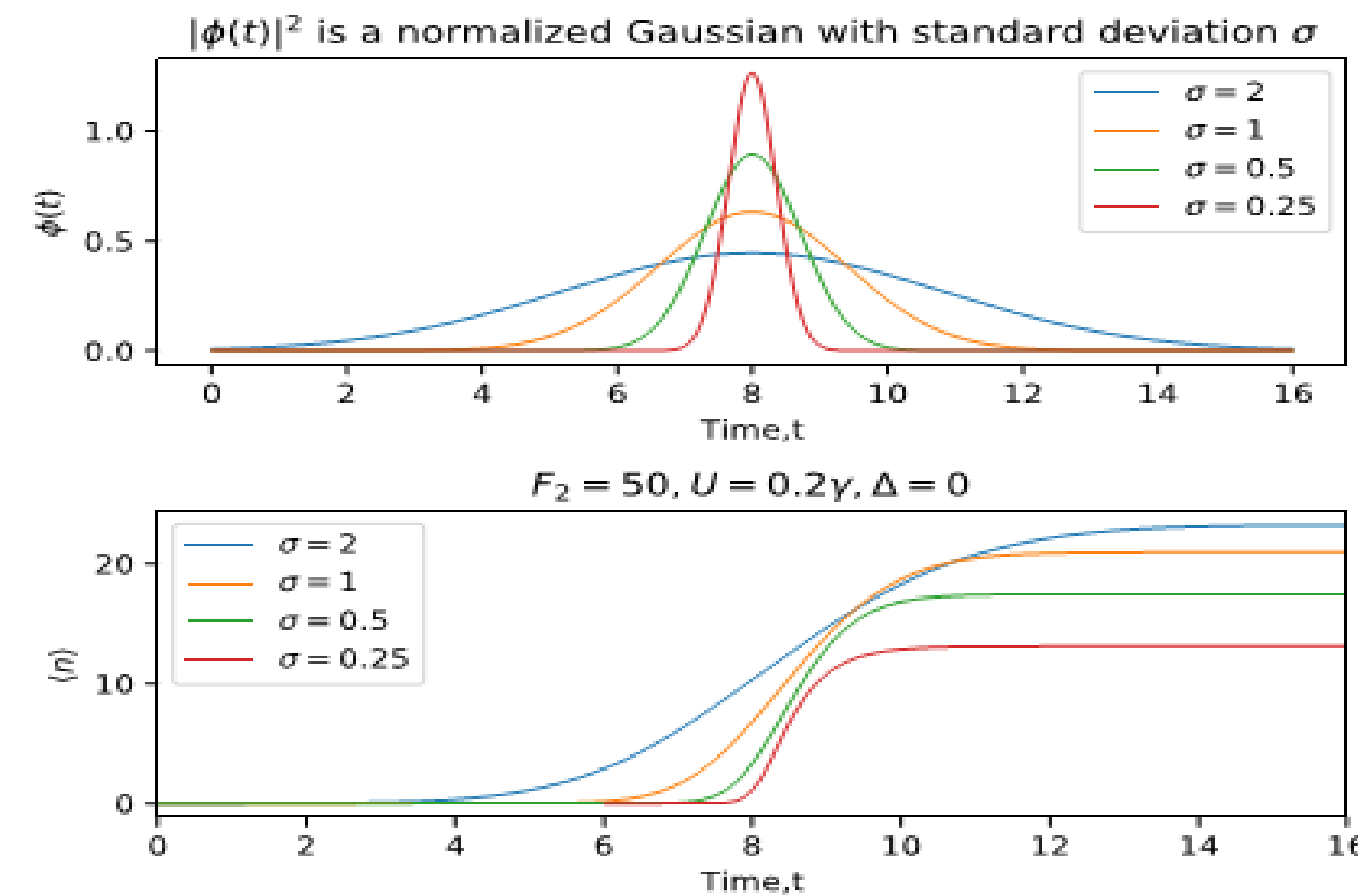
$$\mathcal{L}_X = X \rho X^\dagger - \frac{1}{2} X^\dagger X \rho - \frac{1}{2} \rho X^\dagger X$$

$$A = \sqrt{\gamma b}, B = \sqrt{\kappa p_{1,0}} |F_0\rangle \langle F_1|, C = \sqrt{\kappa(1-p_{1,0})} |F_1\rangle \langle F_0|,$$

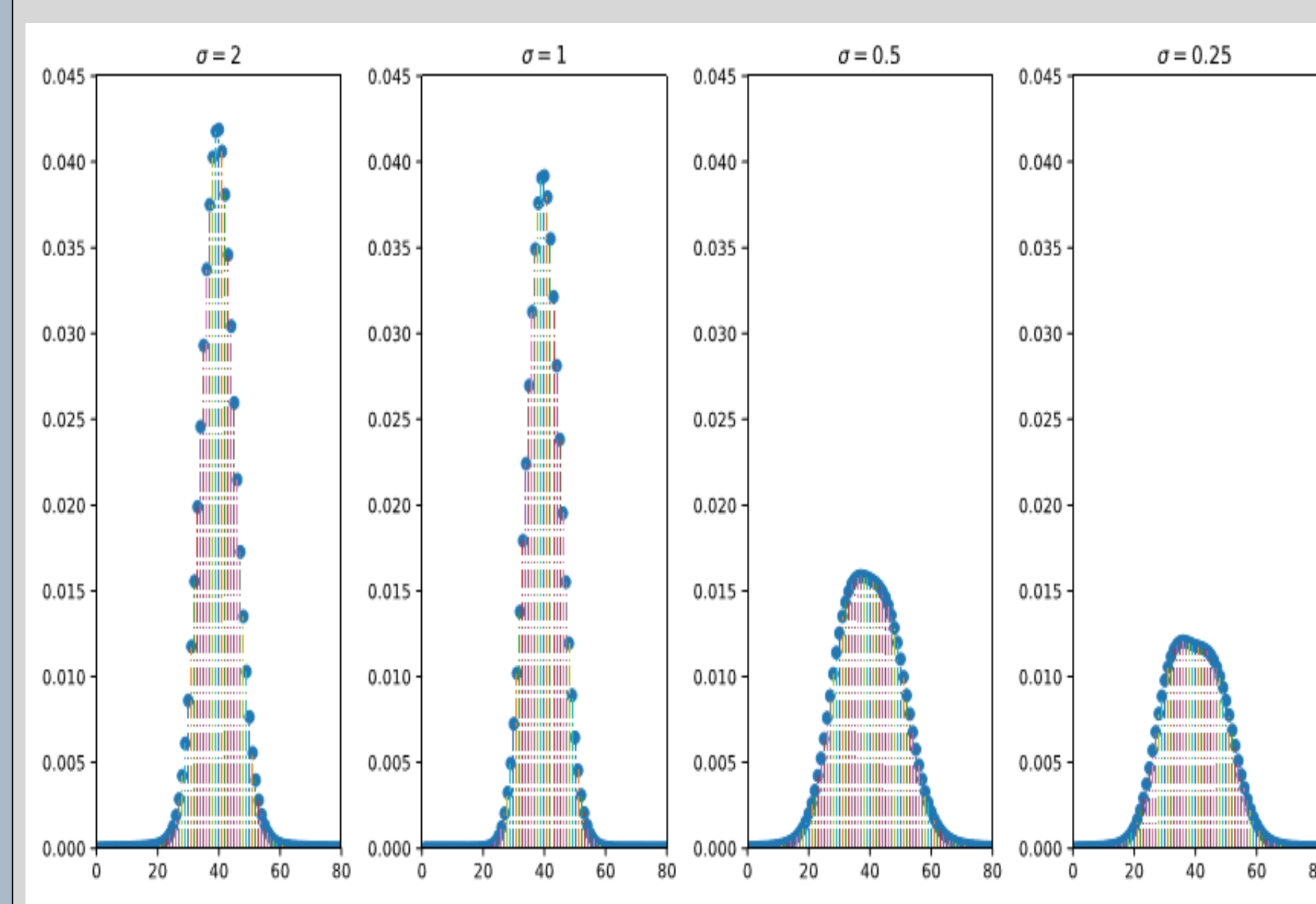
$$D = \sqrt{\lambda p_{1,2}} |F_1\rangle \langle F_2|, E = \sqrt{\lambda(1-p_{1,2})} |F_2\rangle \langle F_1|$$



## Effect of Photon Wave-function width on the average dynamics

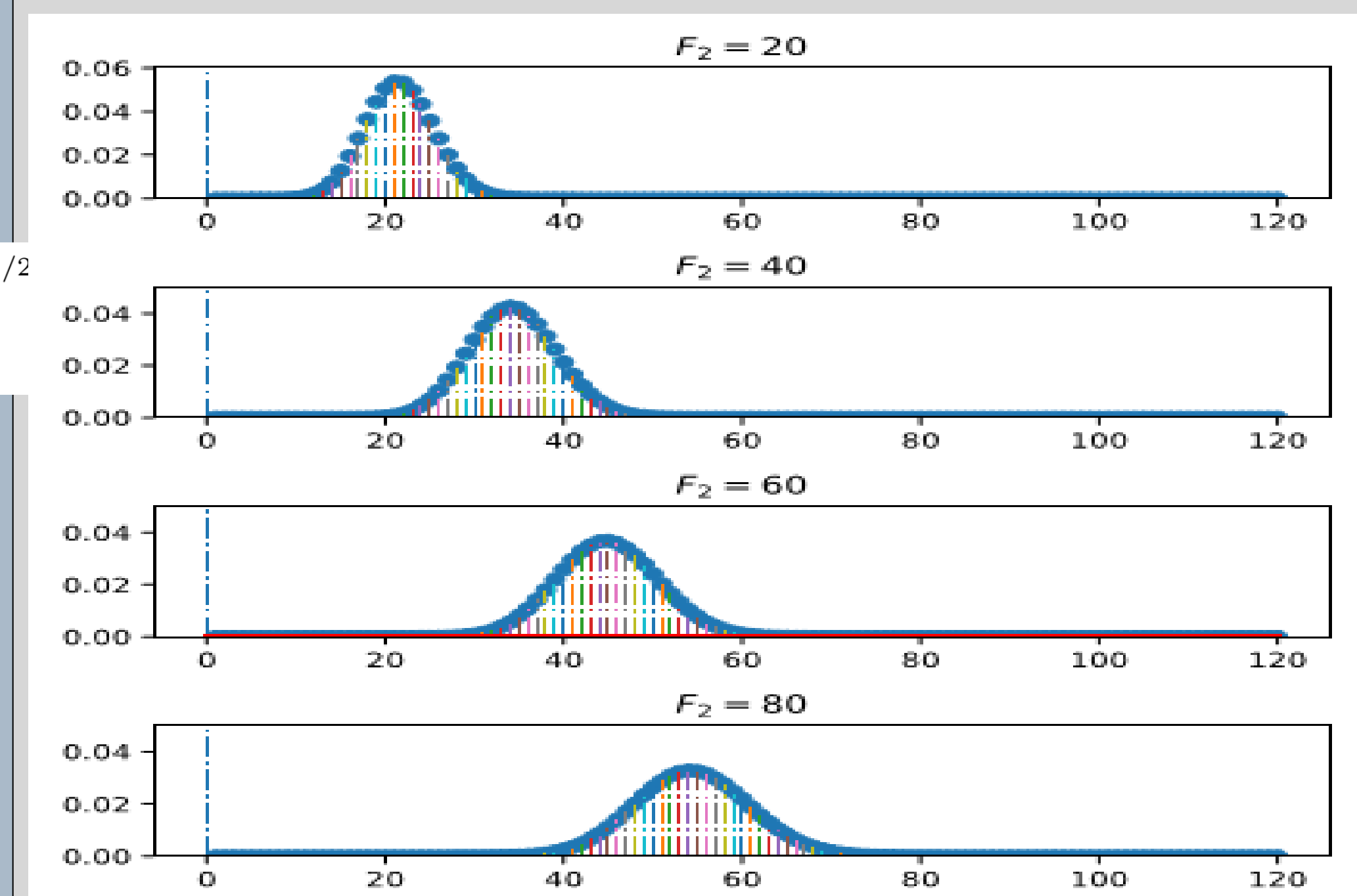


Comparison of probability distribution of excitation numbers in the steady state for different widths of the photon wave-function

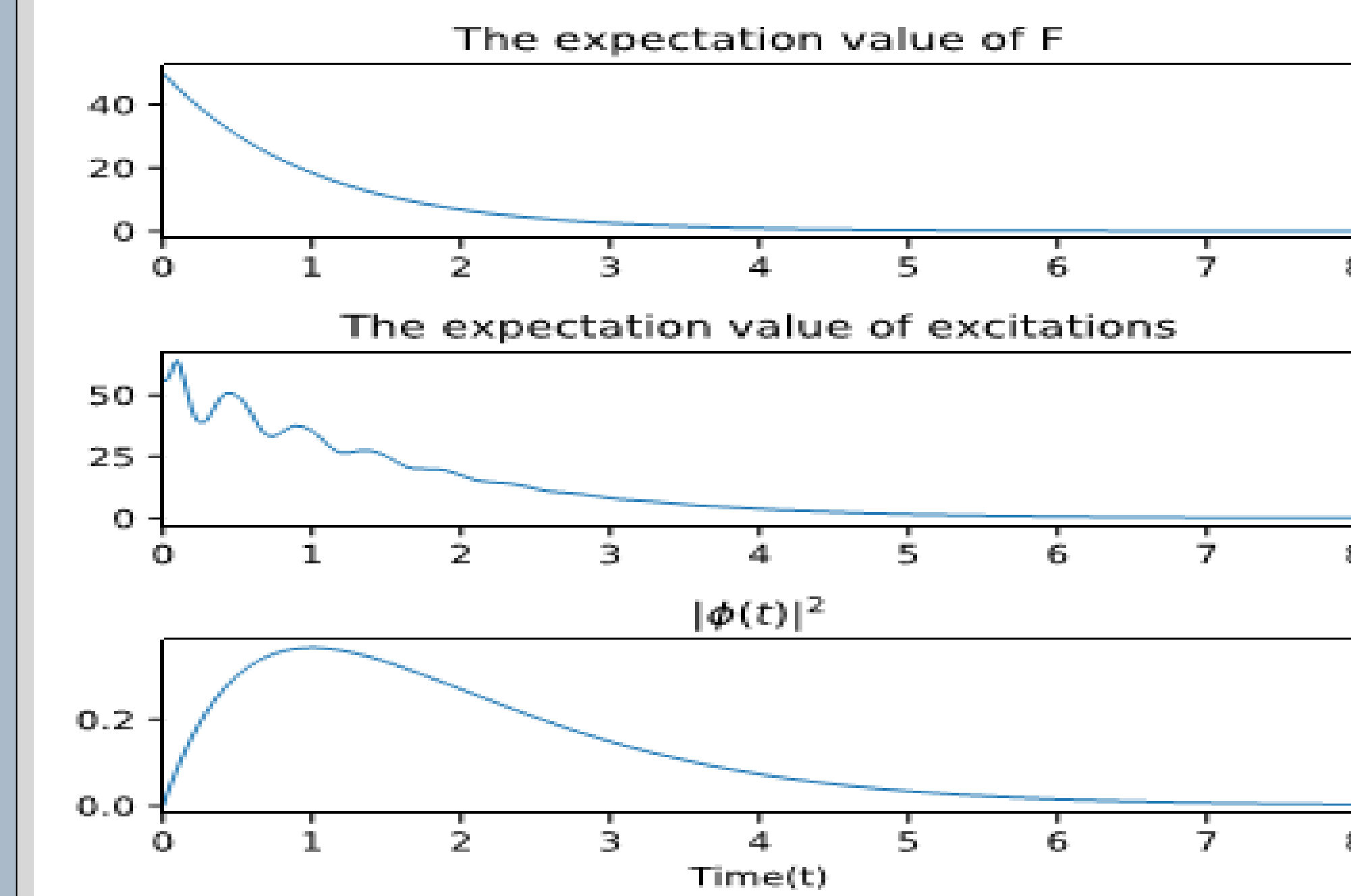


## Effect of the values of F2

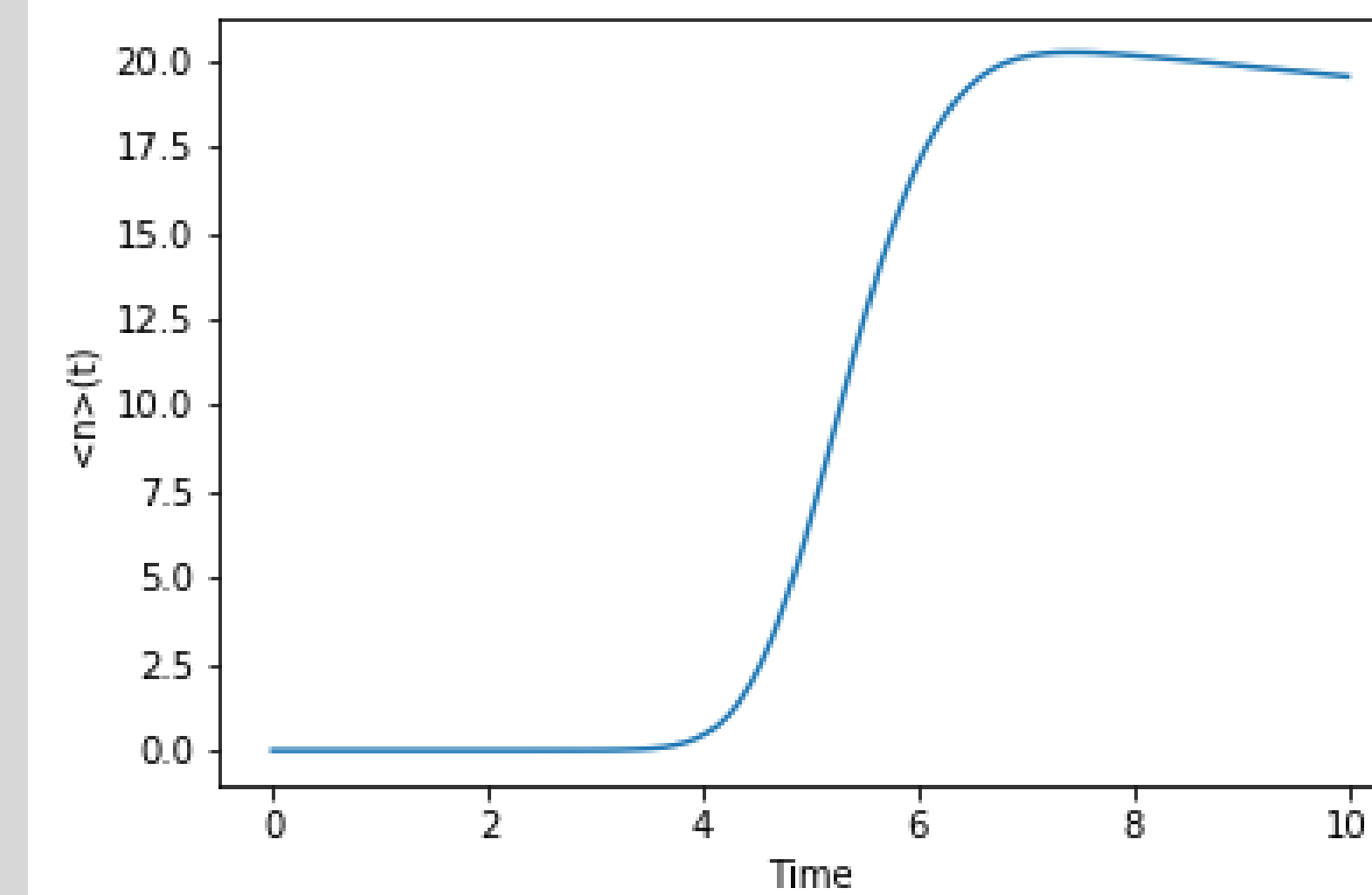
Comparison of probability distribution of excitation numbers in the steady state for different values of F2



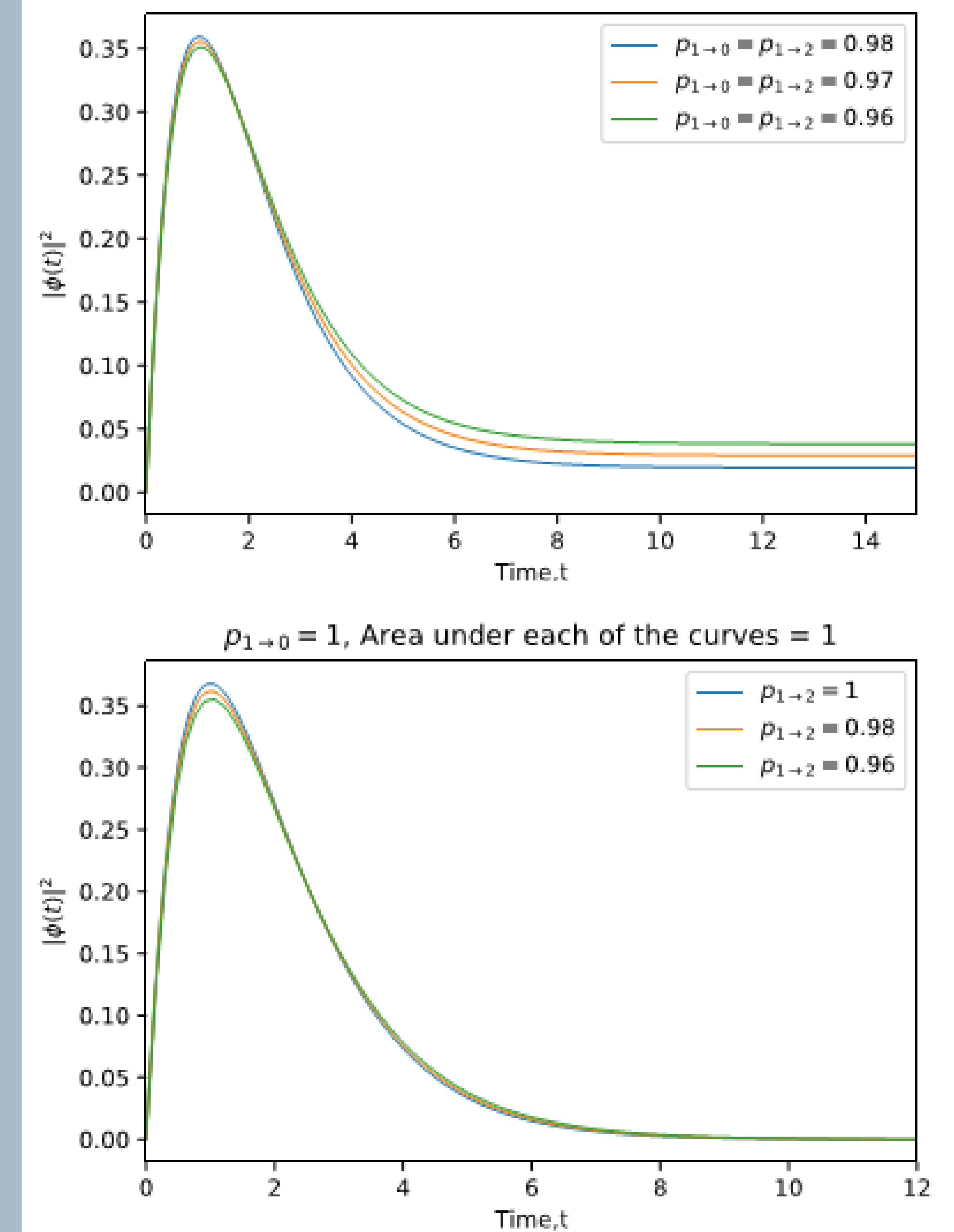
## Calculation of the modulus squared Photon Wave function



The wigner function develops a bimodality close to the onset of the steady state in the average dynamics



## Effects of thermal fluctuations



The calculated photon wave-function reveals the nature of the final equilibrium.

## Properties of the steady state of the average dynamics

