

Types of recursion

(1) Tail recursion: (Every call at run time)

```
void any(int n) {
```

```
    if(n > 0) {
```

```
        cout << n;
```

```
        any(n-1);
```

```
    }
```

```
}
```

```
any(3);
```

Time $\rightarrow O(n)$
Space $\rightarrow O(n)$ } (A)

→ recursive call at the end of condition

→ Tail recursion

→ space: 4 stacks will be created (n+1) (recursion uses stack)

(A) So it is better to modify a tail recursion into a loop as the loop will have space complexity as $O(1)$.

(2) Head recursion: (Every call at returning time)

```
void any(int n) {
```

```
    if(n > 0) {
```

```
        any(n-1);
```

```
    }
```

```
}
```

→ recursive call at the start of condition

→ Head recursion

(3) Tree recursion

```
void something (int n) {
```

```
    if (n > 0) {
```

```
        cout << n;
```

```
        something (n-1);
```

```
        something (n-1);
```

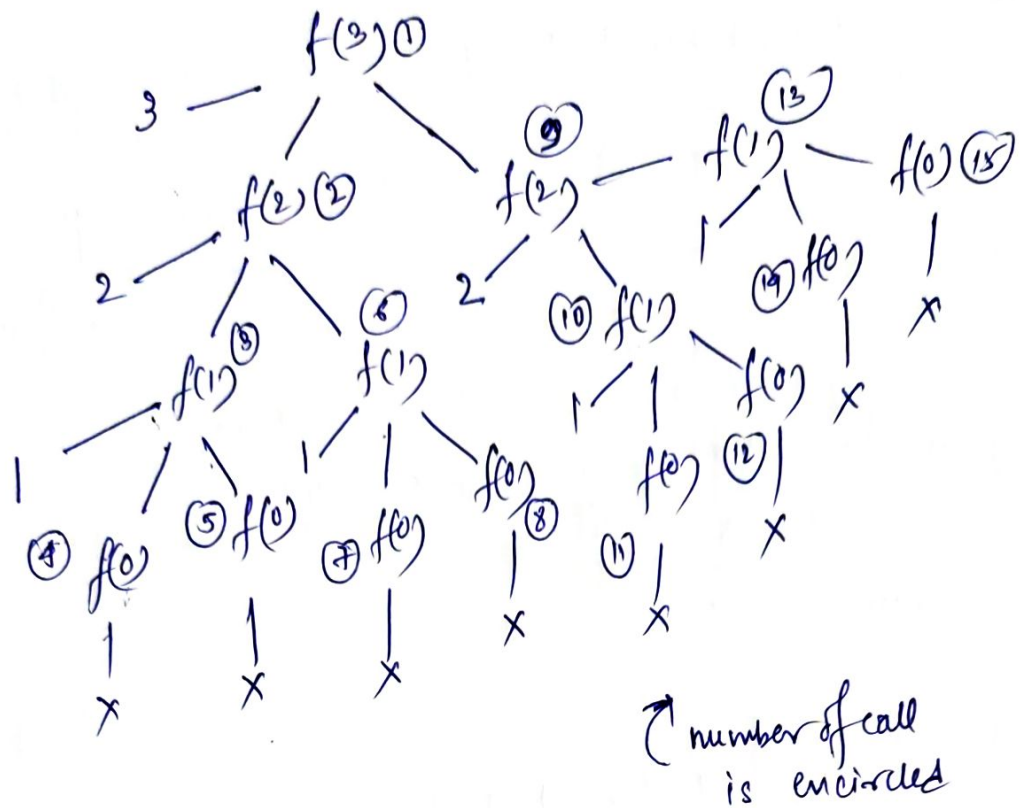
```
    }
```

```
}
```

]

Calling the recursive function more than two times is c/a tree recursion

Something $() \approx f()$



O/P $\rightarrow 3 \ 2 \ 1 \ 1 \ 2 \ 1 \ 1$

Time complexity $\rightarrow 1 + 2 + 4 + 8 = 15$
 $2^0 + 2^1 + 2^2 + 2^3$

$$\sum_{i=0}^n 2^i = 2^0 + 2^1 + 2^2 + \dots + 2^n = 2^{n+1} - 1$$

So, ~~$O(2^n)$~~ $O(2^n)$

space complexity $\rightarrow O(n)$

• Indirect Recursion

```
void A(int n) {
```

```
    if (n > 1) {
```

```
        B(n-1);
```

```
    }
```

```
void B(int n) {
```

```
    if (n > 1) {
```

```
        A(n-3);
```

```
    }
```

```
}
```

Eg. void funA(int n)

```
{ if (n > 0)
```

```
{ cout << n;
  funB(n-1);
```

```
}
```

```
void funB(int n)
```

```
{ if (n > 1)
```

```
{ cout << n;
  funA(n/2);
```

```
}
```

```
}
```

funA(20)

20

funB(19)

19

funA(9)

$19/2 = 9 \text{ int}$

9

funB(8)

8

funA(4)

4

funB(3)

3

funA(1)

1

funB(0)

X

Nested Recursion

Eg.

```
void func (int n)
```

```
{ if (n < 4)
```

```
{ return
```

```
func (func(n+1));
```

```
}
```

```
}
```

```
int func (int n)
```

```
{ if (n > 100)
```

```
return n-10;
```

```
else
```

```
return
```

```
func(func(n+1));
```

```
}
```

```
func(98)
```

func(98) = 91

↓

func(func(98+1));

func(99)

99

func(99)

↓

func(func(99+1));

func(100)

100

↓

func(100)

func(101)

101

func(func(100+1));

↓

func(101)

↓

91. → Ans