

2nd Order RC Circuit

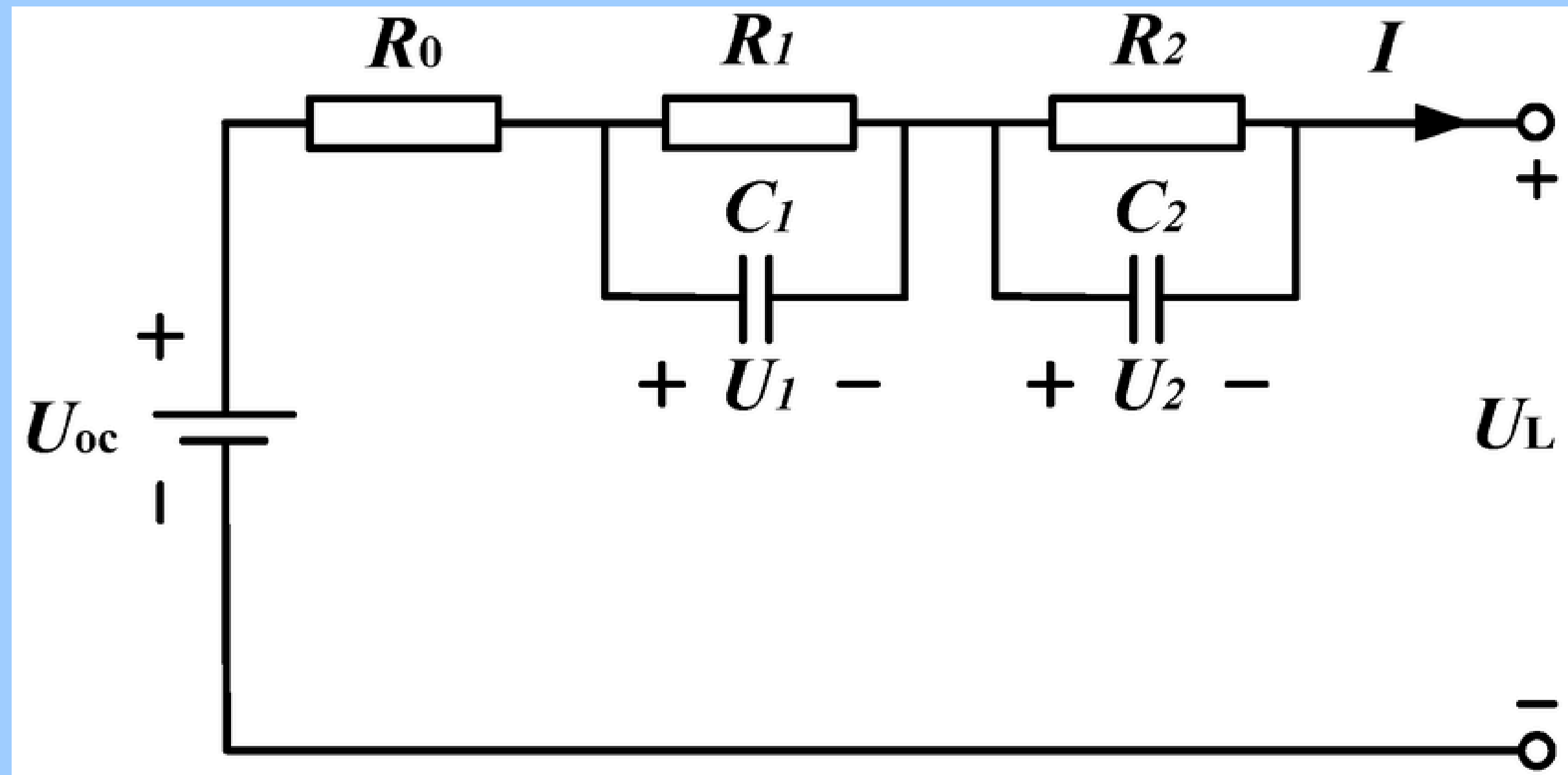


Second Order RC Circuit Using Laplace Transform

- A second-order circuit contains two independent energy storage elements
- In RC circuits, energy storage elements are capacitors
- Two capacitors \Rightarrow second-order system

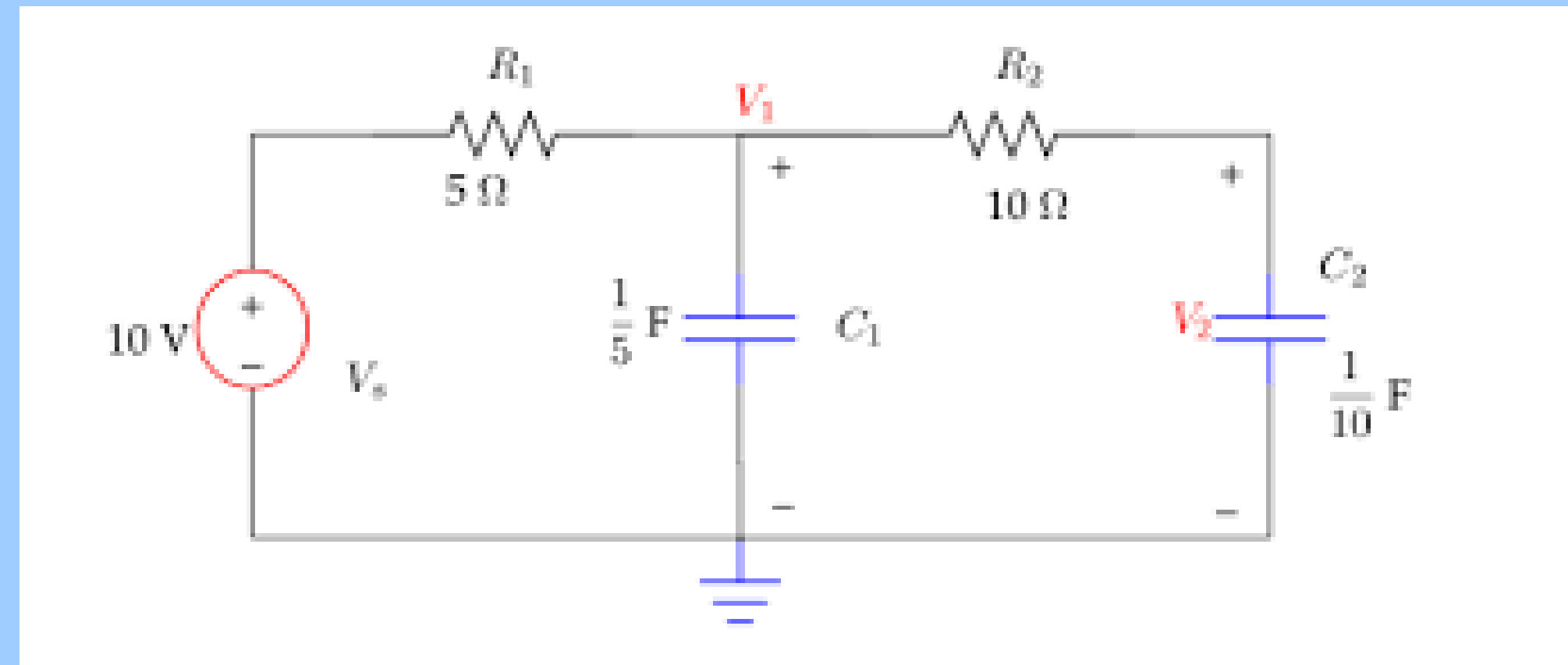
Laplace Transform:

- Converts differential equations to algebra
- Simplifies analysis of higher-order circuits



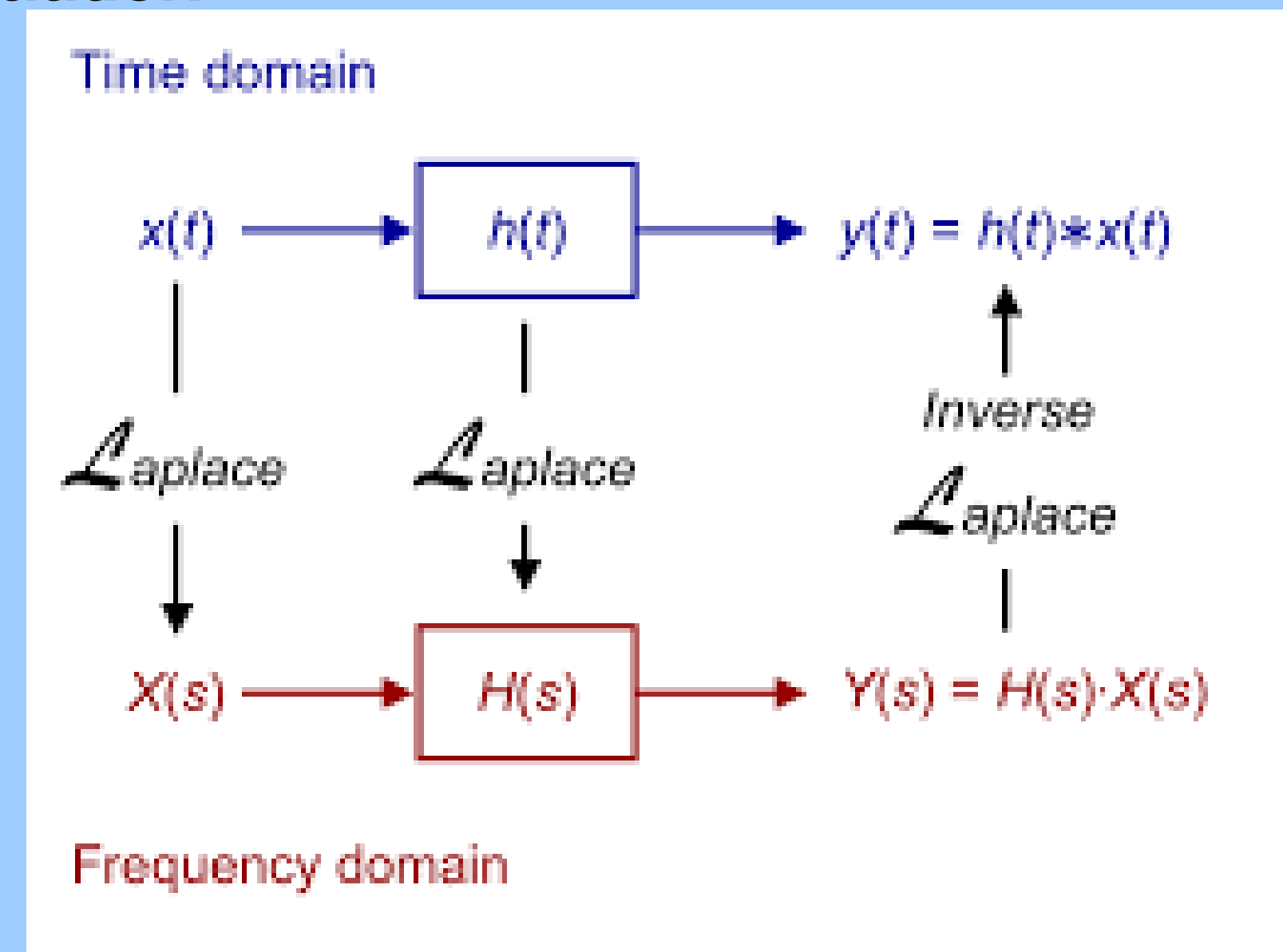
Basic Second-Order RC Circuit Structure

- Contains:
Resistors: R_1, R_2
Capacitors: C_1, C_2
- Input: $V_i(t)$, Output: $V_o(t)$
- Two capacitors \Rightarrow two energy storage states
- Leads to a second-order differential equation



Why Use Laplace Transform?

- Time domain equations include derivatives:
- $i(t) = C dv(t)/dt$, $d\{sqr{v(t)}}/{dtsquare} i(t) = C$
- Two capacitors \rightarrow second-order differential equation
- Laplace Transform:
- Converts differentiation to multiplication by s
- Handles initial conditions
- Makes algebraic circuit equations



Laplace Domain Model of Second-Order RC

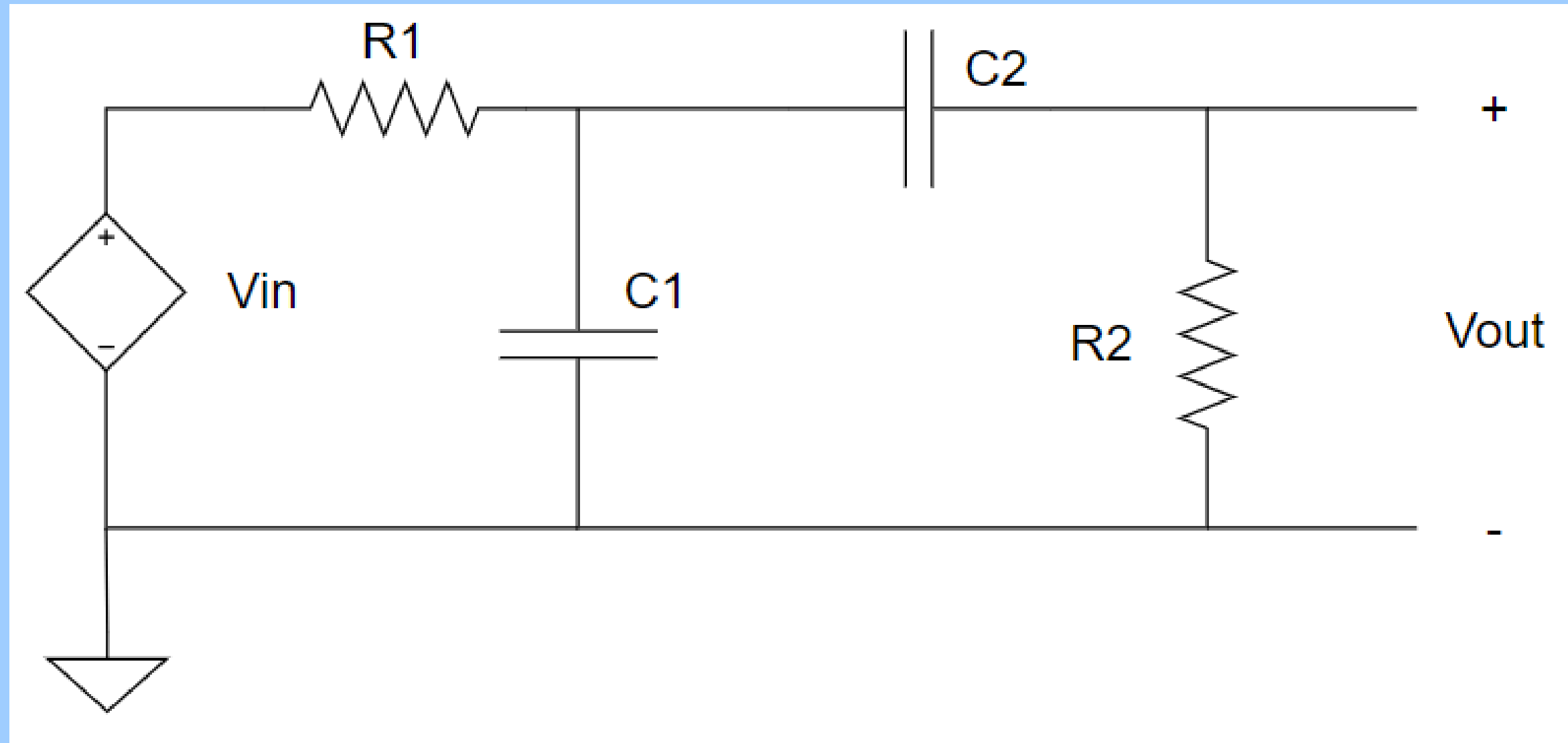
- Impedance in s-domain:
 $Z_R=R$, $Z_C=1/sC$
- Solve using voltage division or mesh equations
- Final transfer function:
 $H(s)=V_o(s)/V_i(s)=K/s^2+as+b$

Where:

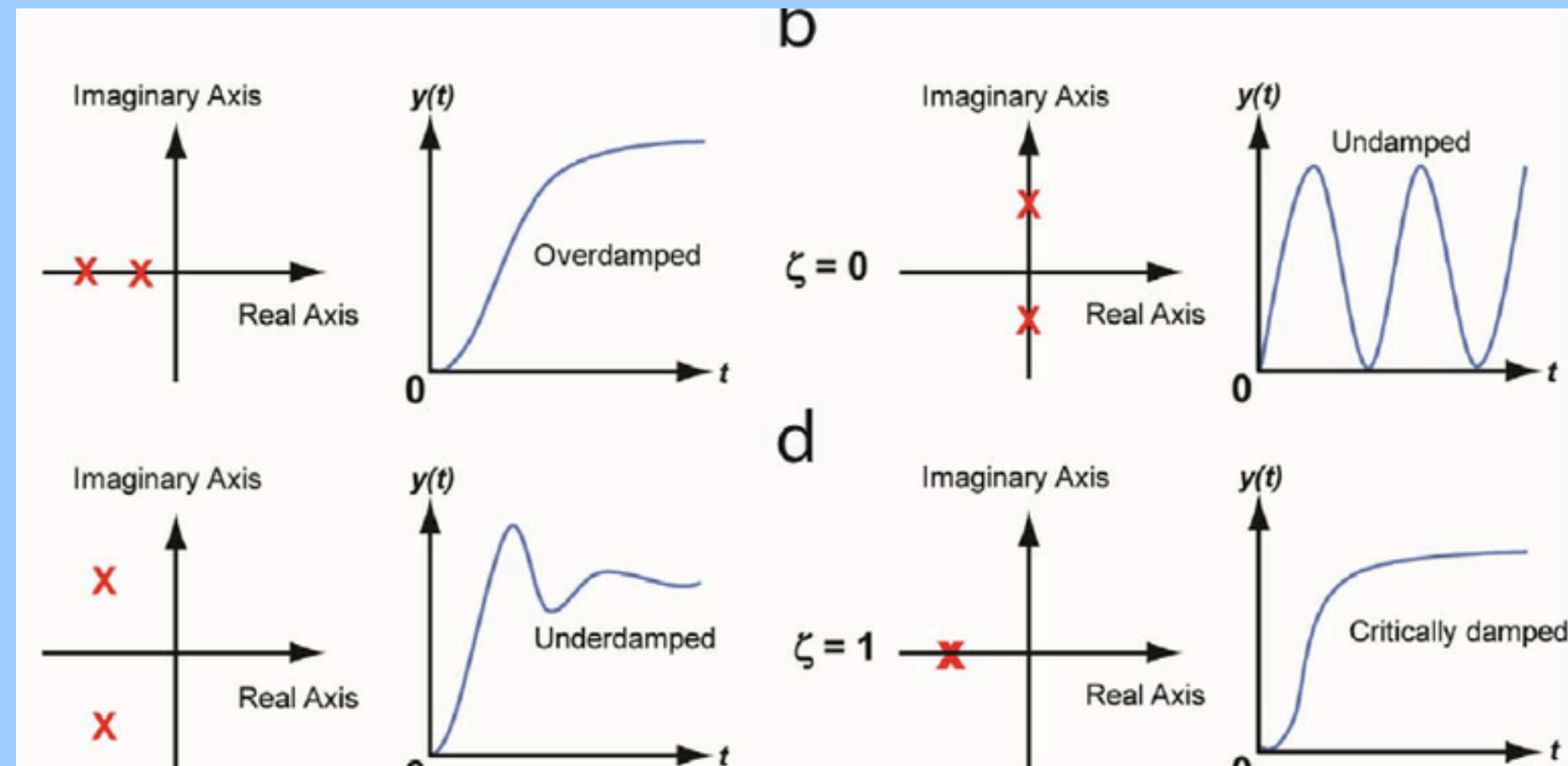
- a =sum of resistive & capacitive terms
- b = product of resistive and capacitive terms

Conclusion:

Highest power of s is 2 \Rightarrow second-order circuit



- **Denominator:**
 $s^2 + as + b = 0$
- **Roots determine behavior:**
 - Real & distinct \Rightarrow Overdamped
 - Real & equal \Rightarrow Critically damped
- Complex conjugate \Rightarrow Underdamped
- RC networks usually show overdamped/critically damped behavior (no oscillation)
- **Key Insight:**
- Response shaped by two poles



Frequency Response & Practical Uses

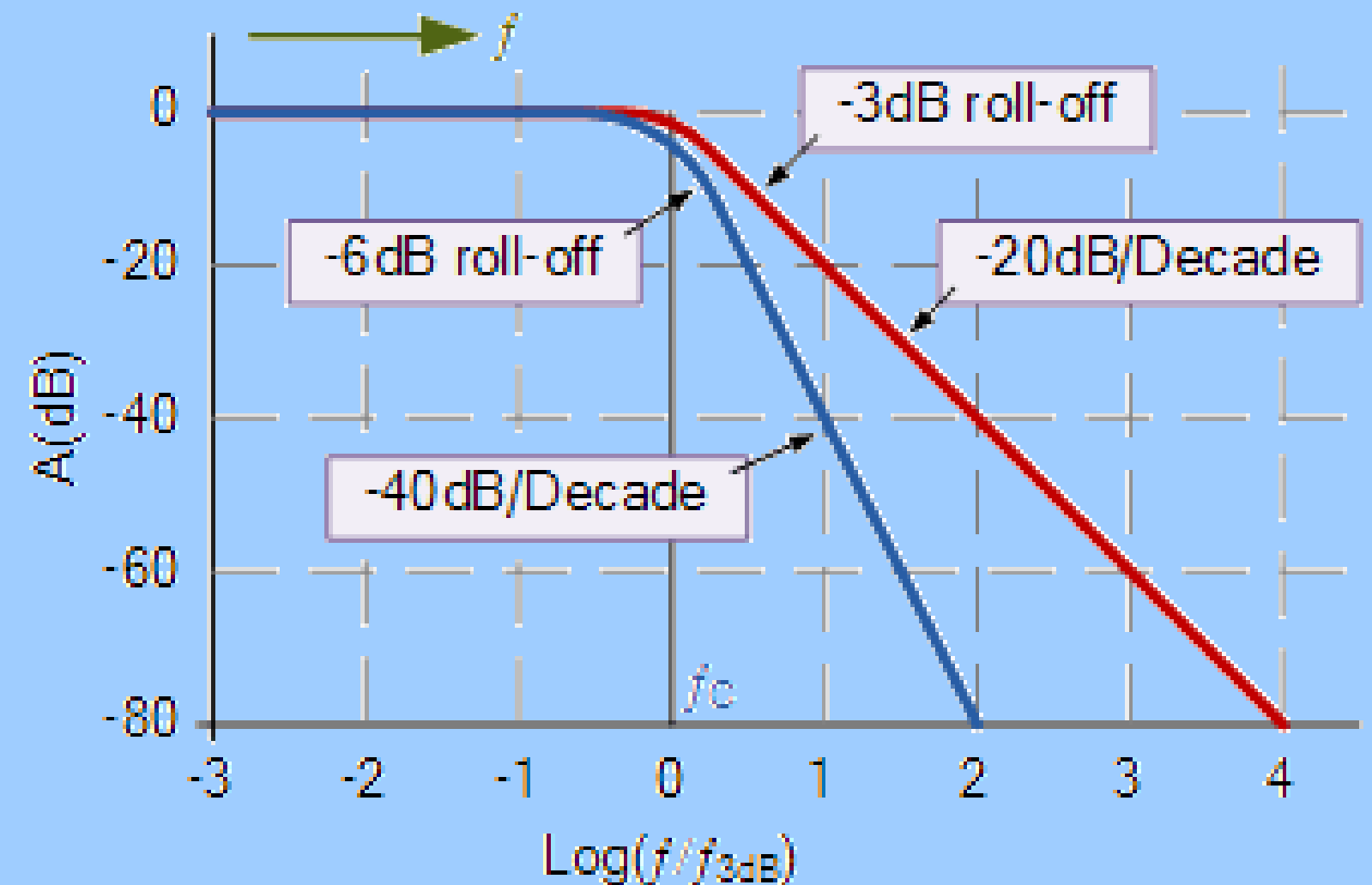
- Second-order RC can be: Low-pass, High-pass
- Band-pass depending on configuration
- Compared to first order: Steeper attenuation

Better filtering

- Roll-off: -40 dB/decade

Applications

- Power supply noise filtering
- Audio signal conditioning
- Communication circuits



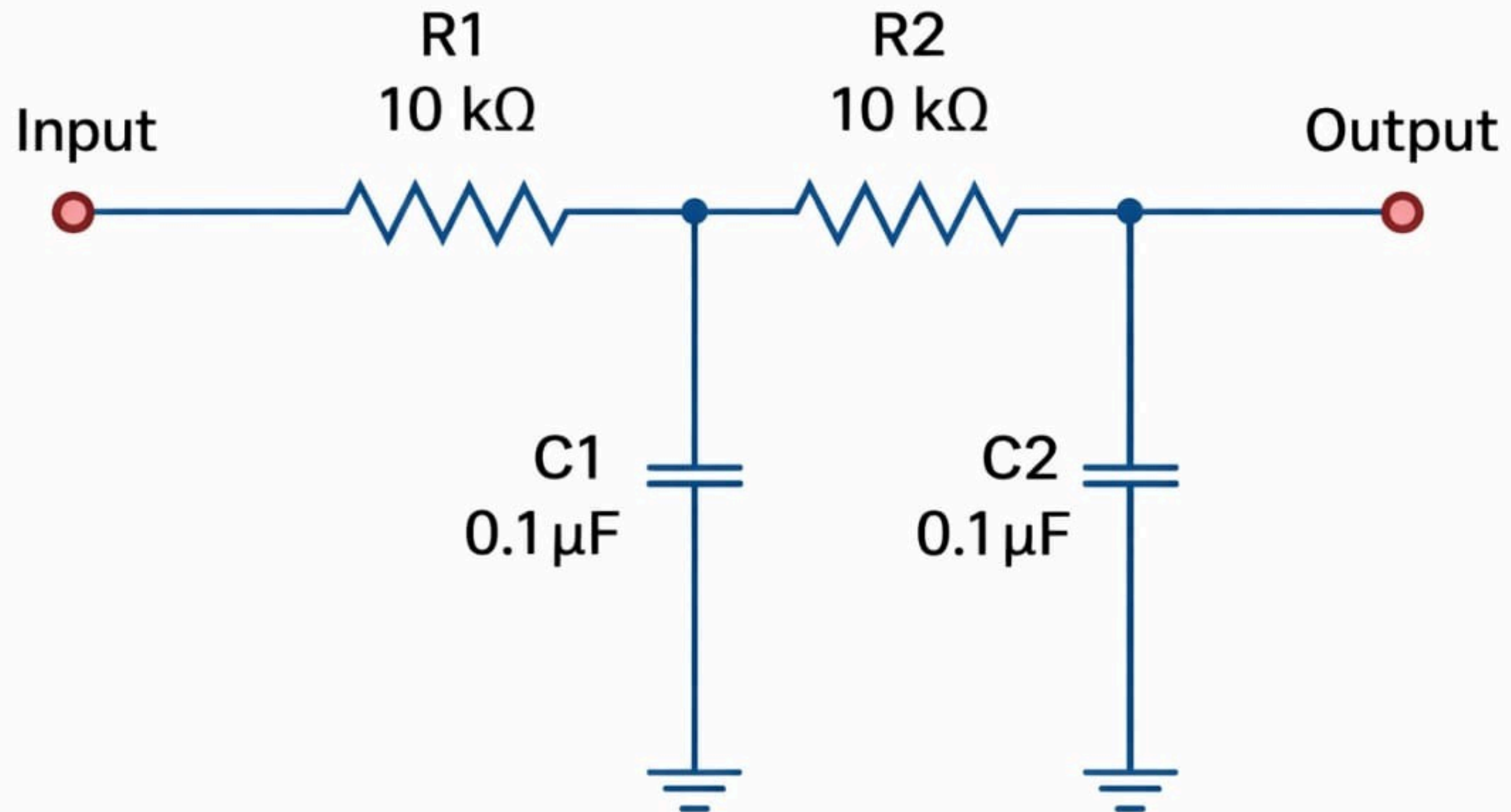
Application :Passive Noise Reduction Using Second Order RC Circuit

- **Noise is an unwanted high-frequency signal present in electrical systems**
- **Passive noise reduction uses R and C elements only**
- **Second order RC circuits provide:**
- **Better noise attenuation than first order circuits**
- **Sharper frequency roll-off**
- **Laplace Transform is used to:**
- **Model noise filtering behavior mathematically**
- **Analyze system response efficiently**

Objective

- **To demonstrate how a second-order RC**
- **circuit reduces noise using Laplace Transform**

Second-Order RC Low-Pass Filter Circuit



Second Order RC Low-Pass Filter Configuration

Circuit consists of:

- Two resistors: R_1, R_2
- Two capacitors: C_1, C_2
- Two cascaded RC sections

Each RC section contributes:

- One pole

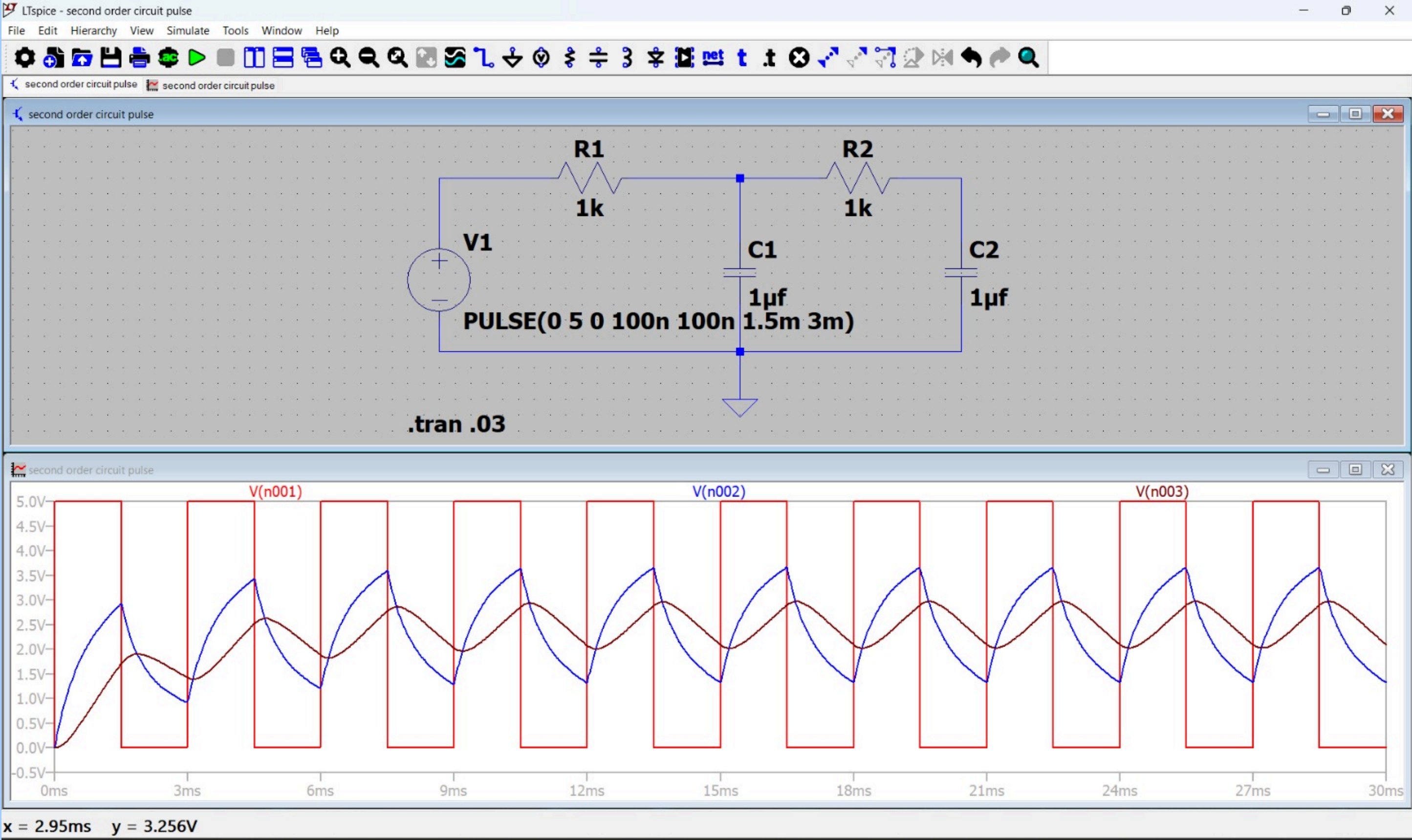
Total system order:

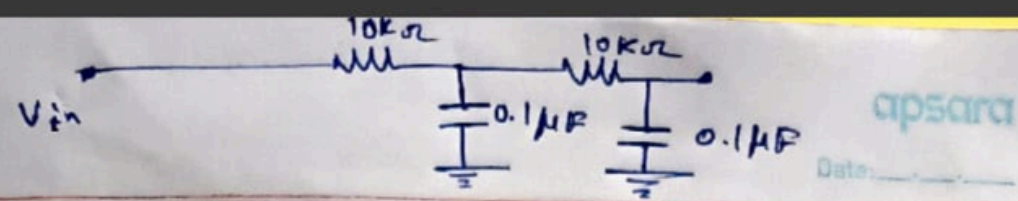
- Two poles → second-order system

Filtering Action

- Low-frequency signals pass with minimal attenuation
- High-frequency noise is significantly reduced

Simulation and theoretical approach





Given in

| parameter | value |
|----------------|--------------------------|
| Input voltage | 1.5 V _{pp} |
| Frequency | 1.5 KHz |
| Output voltage | 40 mV _{pp} |
| R | 10 kΩ |
| C | 0.1 μF |
| Circuit | 2 nd Order RC |

Theoretical Calculation

$$f_c = \frac{\text{Cutoff frequency}}{2\pi RC} = \frac{1}{2\pi \times (10k) (0.1\mu F)} = 159 \text{ Hz}$$

Frequency ratio

$$\frac{f}{f_c} = \frac{1500}{159} \approx 9.43$$

Gain of 2nd order RC filter.

$$= |H(j\omega)| = \frac{1}{1 + (\omega RC)^2}$$

$$= \frac{1}{1 + (9.43)^2}$$

$$= \frac{1}{1 + 88.9} \approx 0.011$$

Expected Output voltage

$$V_{out} = 1.5 \times 0.0111$$

$$V_{out} = 0.0267 \text{ V} \approx 27 \text{ mV}$$

Practical value (we got)

$$V_{out} = 40 \text{ mV}$$

The variation is due to Capacitor tolerance of $\pm 20\%$