

# An energetically consistent vertical mixing parameterization in CCSM4

Søren B. Nielsen<sup>a,\*</sup>, Markus Jochum<sup>a</sup>, Carsten Eden<sup>b</sup>, Roman Nuterman<sup>a</sup>

<sup>a</sup>*Climate and Computational Geophysics, Niels Bohr Institute, University of  
Copenhagen, Copenhagen, Denmark*

<sup>b</sup>*Institut für Meereskunde, University of Hamburg*

---

## Abstract

An energetically consistent stratification-dependent vertical mixing parameterization is implemented in the Community Climate System Model 4 and forced with energy conversion from the barotropic tides to internal waves. The structures of the resulting dissipation and diffusivity fields are compared to observations, and the fidelity of the resulting temperature fields is assessed. Compared to existing biases in the control simulation, differences in surface fields are small, showing that the surface climate state is relatively robust to the choice of mixing parameterization. The thermocline structure, however, depends greatly on the details of the vertical mixing parameterizations, where the new energetically consistent parameterization results in low thermocline diffusivities and a sharper and shallower thermocline. It is also investigated if the ocean state is more sensitive to a change in forcing if the energetically consistent scheme is used compared to a tidal mixing parameterization with fixed background diffusivity. In particular we find that the Atlantic Meridional Overturning Circulation is more sensitive to changes in the Southern Ocean wind stress with the former. However, in line with previous results, changes to Southern Ocean upwelling are still largely compensated by changes to the diabatic upwelling in the Indo-Pacific basin.

*Keywords:* Diapycnal mixing, Numerical mixing, Parameterizations, Internal wave breaking

---

## 1. Introduction

Mechanical energy is needed to return the deep waters that are formed at high latitudes to the surface (see e.g. [Sandström, 1908](#)). It has been

---

\*Corresponding author. Address: Juliane Maries Vej 30, 2100 Copenhagen, Denmark  
Email address: [soeren.nielsen@nbi.ku.dk](mailto:soeren.nielsen@nbi.ku.dk) (Søren B. Nielsen)

hypothesized that this mechanical energy is provided by the breaking of internal waves to small scale turbulence (Munk, 1966; Munk and Wunsch, 1998). This hypothesis has been supported by numerical studies (Bryan, 1987; Marotzke, 1997). Yet, despite its importance, small scale turbulence in the ocean interior is still represented through diffusivity, fixed in time and space. More recently, this so called background diffusivity will be amplified near the bottom to mimic tidally induced mixing (e.g. Bryan and Lewis, 1979; St. Laurent et al., 2002). However, for large parts of the ocean, away from the boundary layers, the vertical diffusivity is dominated by the background diffusivity.

The value of this background diffusivity is obtained by a combination of observations and model optimization. Using spatially-varying maps of diffusivity to match global observations rather than a constant global value has been shown to improve climate models (Harrison and Hallberg, 2008; Jochum, 2009). However, while using a constant diffusivity can yield pre-industrial or present day simulations in good agreement with observations, the reliability of these parameterizations is questionable for different climate states. The model of Osborn (1980) suggests that vertical diffusivity,  $\kappa$ , is a function of locally dissipated energy from the internal wave field,  $\epsilon$ , and the Brunt-Väisälä frequency,  $N$ ,

$$\kappa \propto \frac{\epsilon}{N^2}. \quad (1)$$

Because both variables are likely to change as climate changes, we expect changes in diffusivities and therefore in ocean circulation, heat and carbon storage and uptake. Furthermore, present tidal mixing parameterizations have problems of representing observed dissipation rates due to assumptions regarding the propagation and dissipation of internal wave energy (Waterhouse et al., 2014; MacKinnon et al., 2017; Kunze, 2017).

The focus of this study is how climate is affected when using an energetically consistent mixing parameterization rather than using fixed background diffusivities. Studies suggest that the parameterization of interior mixing affects the simulations of pre-industrial climate (e.g. Jayne, 2009; Melet et al., 2013). In particular, changes in the localization of dissipation of internal wave energy has consequences in regions of deep water formation as well as for thermocline structure (Melet et al., 2013, 2016). Previous studies mainly focus on steady state properties of the ocean; here we perform a simple experiment to assess to what degree the ocean response to changed forcing is affected by the choice of parameterization.

67 The topic of interest for this experiment is the strength of the Atlantic  
 68 Meridional Overturning Circulation (AMOC). The AMOC is a measure of  
 69 the volume transport from the Southern Hemisphere to the Northern, often  
 70 referred to as the "ocean conveyor belt", with sinking waters in the North At-  
 71 lantic being replaced by sub-tropical surface waters through the Gulf Stream.  
 72 This circulation gives rise to an Atlantic heat transport from the Southern  
 73 to the Northern hemisphere. The driving mechanisms of the AMOC have  
 74 been investigated and discussed throughout the last decades (see e.g. the  
 75 review by [Kuhlbrodt et al., 2007](#)). In particular, buoyancy fluxes, diapycnal  
 76 mixing rates and Southern Ocean wind stress have all been suggested to play  
 77 important or even dominating roles. These also impact the strength of the  
 78 Antarctic Circumpolar Current (ACC) ([Gent et al., 2001](#)). Several numerical  
 79 studies have implicated a direct dependency of overturning to the value of di-  
 80 apycnal diffusivity ([Bryan, 1987](#); [Marotzke, 1997](#)). Yet, many studies require  
 81 mixing values larger than observed to sustain the observed rate of overturning  
 82 ([Toggweiler and Samuels, 1995](#); [Polzin et al., 1997](#); [Ledwell et al., 1998](#)).

83 In the mid 1990's it was pointed out that Southern Ocean winds and  
 84 the sill at the Drake Passage were potentially dominating global ocean up-  
 85 welling, sometimes referred to as the "Drake Passage Effect" ([Toggweiler and  
 86 Samuels, 1995](#)). Even near the limit of no vertical diffusion, the Drake Pas-  
 87 sage Effect was discovered to sustain an observed overturning ([Toggweiler  
 88 and Samuels, 1998](#)). In a more recent study, [Munday et al. \(2013\)](#) found  
 89 the overturning to be less sensitive to wind forcing as horizontal resolution  
 90 increased due to the explicit generation of Southern Ocean eddies, although a  
 91 sensitivity remained. Additionally, the overturning was found to be sensitive  
 92 to the choice of diapycnal diffusivity regardless of model resolution. All these  
 93 results were obtained by forcing an ocean model with prescribed buoyancy  
 94 forcing.

95 In contrast to these studies [Jochum and Eden \(2015\)](#) found that in a  
 96 realistic coupled climate model the AMOC is robust to changes in South-  
 97 ern Ocean wind stress: Changes to Southern Ocean winds and upwelling are  
 98 compensated by diabatic upwelling in the Indo-Pacific basin. Their study,  
 99 however, used a fixed vertical diffusivity, so that changed mixing rates due to  
 100 changed ocean stratification are not present, possibly leading to an overesti-  
 101 mation of the Indo-Pacific compensation. Here we will revisit this idea and  
 102 check if their results still hold if a fixed-energy, rather than a fixed-diffusivity  
 103 parameterization is used.

104 The paper is structured as follows: In section 2 current ideas about di-

105 apycnal mixing and its parameterizations are briefly reviewed, and an en-  
 106 ergetically consistent parameterization (IDEMIX, [Olbers and Eden, 2013](#))  
 107 and its implementation in an ocean model are described. In Section 3 the  
 108 results of model simulations with the standard mixing parameterization and  
 109 with IDEMIX are compared in two sets: three coupled simulations (includ-  
 110 ing a sensitivity study), and six forced simulations, comparing the response  
 111 of the ocean to changes in the wind stress under the two different mixing  
 112 schemes. In Section 4 the results are summarized and discussed in context  
 113 to modelling, climate and future prospects.

## 114 2. Methods

### 115 2.1. Vertical mixing in ocean models

116 Diapycnal (from hereon simply vertical) mixing in the ocean in level coor-  
 117 dinate ocean general circulation models is generally represented as a vertical  
 118 diffusion of tracers. This process represents the conversion of small scale  
 119 turbulent kinetic energy into potential energy and is important in setting  
 120 the global pycnocline structure ([Munk, 1966](#)). It is often recognized that  
 121 an average global value of  $10^{-4} \text{ m}^2\text{s}^{-1}$  is required to maintain the observed  
 122 global stratification ([Munk and Wunsch, 1998](#)).

123 The energy input needed to maintain the observed ocean stratification has  
 124 been estimated to be approximately 2 terawatts (TW), partitioned between  
 125 winds and tides ([Munk and Wunsch, 1998](#); [Egbert and Ray, 2000](#); [Jayne and](#)  
 126 [St. Laurent, 2001](#); [Nycander, 2005](#)). Wind energy enters the ocean through  
 127 the work winds do on the surface ocean, with a large fraction driving the  
 128 time-mean circulation, eventually dissipating to mesoscale eddies, and some  
 129 through direct generation of near-inertial waves (NIWs, see e.g. [Jochum et al.,](#)  
 130 [2013](#)), of which only a fraction leaves the mixed-layer. Energy from mesoscale  
 131 eddies is lost through numerous processes, including bottom and lateral fric-  
 132 tion and generation of lee waves over rough topography in a similar way as  
 133 tidal energy loss ([Nikurashin and Ferrari, 2010](#)). Estimates of dissipation  
 134 and diffusivity from Argo float finestructure measurements support the rela-  
 135 tionship between vertical mixing and dissipation of barotropic tides as well  
 136 as geostrophic motions ([Whalen et al., 2012](#); [Pollmann et al., 2017](#)).

137 With the recognition of the importance of tides and their signature bot-  
 138 tom enhanced mixing, parameterizations have been developed for tidally in-  
 139 duced mixing near the bottom. One such parameterization is the one by

140 [St. Laurent et al. \(2002\)](#). This parameterization calculates a bottom en-  
 141 hanced diffusivity based on the local energy flux from tides to internal waves  
 142 (taken from the model of tidal dissipation by [Jayne and St. Laurent, 2001](#)),  
 143 by assuming that a fraction,  $q$ , of the energy that is locally converted from  
 144 barotropic to internal tides is dissipated locally through a vertical distribu-  
 145 tion function which ensures bottom enhanced mixing, whereas the remaining  
 146 energy radiates away and contributes to background mixing (for details, see  
 147 [Simmons et al., 2004](#); [Jayne, 2009](#)). The mathematical expression becomes

$$\kappa = \kappa_b + \frac{q\Gamma E_{F,t}(x,y)F(z)}{\rho N^2}, \quad (2)$$

148 where  $\kappa_b$  is the background diffusivity,  $\Gamma = 0.2$  is the mixing efficiency and  
 149  $q = 1/3$  is the fraction of the energy flux from barotropic tides to inter-  
 150 nal waves,  $E_{F,t}$ , that dissipates locally, with the local dissipation being dis-  
 151 tributed vertically by an exponential decay function,  $F(z)$  and  $\rho$  being the  
 152 density.

153 One key uncertainty is the fixed vertical decay scale,  $F(z)$ , for the dissipa-  
 154 tion of internal wave energy. This choice often does not match observations  
 155 ([Kunze, 2017](#)), and it has been shown that the choice of a vertical dissipation  
 156 profile is important for setting the ocean state ([Melet et al., 2013](#)). Further-  
 157 more, the globally constant value of locally dissipated energy in Eq. 2,  $q$ ,  
 158 relies on sparse observations and there is little justification that one value is  
 159 representative of the entire ocean ([Waterhouse et al., 2014](#)). Recent work has  
 160 now provided a theoretical background to take a step in parameterizing small  
 161 scale turbulence through directly computed values for dissipated energy, as  
 162 described below.

## 163 2.2. IDEMIX

164 A recent paper proposes the model Internal Wave Dissipation, Energy and  
 165 Mixing (IDEMIX, [Olbers and Eden, 2013](#)), to be implemented in a global  
 166 ocean model. Although extensions to the model have been developed ([Eden  
 167 and Olbers, 2014](#)), we will here use the first version as described in [Olbers and  
 168 Eden \(2013\)](#) due to the simplicity and as the main focus is how the ocean  
 169 and climate responds when the vertical mixing is defined from a constant  
 170 energy flux compared to a fixed background diffusivity in space and time.

171 Through a set of assumptions and simplifications, IDEMIX calculates  
 172 the total internal wave energy,  $E$ , as well as the dissipation of internal wave

173 energy,  $\epsilon_{IW}$ .  $E$  is calculated by solving a single differential equation obtained  
 174 from the spectral radiation balance of a weakly interacting wave field:

$$\frac{\partial E}{\partial t} - \frac{\partial}{\partial z} \left( c_0 \tau_v \frac{\partial c_0 E}{\partial z} \right) - \nabla_h \cdot v_0 \tau_h \nabla_h v_0 E = -\epsilon_{IW} + \mathcal{S}, \quad (3)$$

175 where the second and third terms on the l.h.s. are the vertical and horizontal  
 176 transport of  $E$ , respectively.  $\mathcal{S}$  represents the sum of local sources of internal  
 177 wave energy.

178 IDEMIX has been discussed in several papers already, (Olbers and Eden,  
 179 2013; Eden et al., 2014; Eden and Olbers, 2014; Pollmann et al., 2017) and  
 180 will therefore only be summarized briefly here. In order to arrive at Eq. 3,  
 181 upward and downward propagating waves are first treated separately, and  
 182 the wave energy is integrated over all wave numbers in each vertical wave  
 183 number half-space. Equations for the sum of energy,  $E$ , and difference,  $\Delta E$ ,  
 184 of the two half-spaces are then simplified by assuming approximate symme-  
 185 try in vertical wave number,  $m$ , and that nonlinear wave-wave interactions  
 186 work to eliminate  $\Delta E$  through an exponential relaxation with decay scale  $\tau_v$ .  
 187 The wave speed is also assumed to have the same value for the upward and  
 188 downward propagating waves,  $c_0$ . The value of  $c_0$  can be found by assuming  
 189 a Garrett-Munk (GM) like internal wave energy spectrum. The third term  
 190 on the l.h.s. of Eq. 3 represents the lateral propagation of energy, with  $v_0$   
 191 a horizontal average group velocity and  $\tau_h$  a relaxation time for horizontal  
 192 anisotropies (similar to  $\tau_v$ ).

193 The model is closed on the r.h.s. of Eq. 3 by setting

$$\epsilon_{IW} = \mu_0 f_e \frac{m_\star^2}{N^2} E^2, \quad (4)$$

194 which represents the energy flux at high vertical wavenumber (a combination  
 195 of calculations of McComas and Müller, 1981; Heyney et al., 1986) with  $m_\star$   
 196 the bandwidth in vertical wavenumber and  $\mu_0$  a constant (McComas and  
 197 Müller, 1981). Finally,  $f_e = f_{\text{arccosh}}(N/f)$ .

198 The dissipation of energy is then related to a vertical diffusivity through  
 199 the Osborn (1980) model:

$$\kappa = \frac{\delta}{1 + \delta} \frac{\epsilon_{IW}}{N^2} = \frac{\delta}{1 + \delta} \mu_0 f_e \frac{E^2}{c_\star^2 N^2}, \quad (5)$$

200 where the relation  $m_\star = N/c_\star$  is used with  $c_\star = \frac{1}{j_\star \pi} \int_{-h}^0 N(z) dz$ , with  $j_\star$  the  
 201 modal bandwidth of the GM-model.

### 2.3. Model and Implementation

Eq. 3 is implemented in the ocean component of the Community Climate System Model 4 (CCSM4, [Gent et al., 2011](#)), the Parallel Ocean Program (POP2, [Danabasoglu et al., 2012](#)) following the implementation of [Eden et al. \(2014\)](#) with the parameter values suggested by [Olbers and Eden \(2013\)](#):  $\mu_0 = 4/3$ ,  $\delta = 0.2$ ,  $j_\star = 10$ ,  $\tau_v = 1$  day and  $\tau_h = 10$  days. First, Eq. 3 is solved with a tri-diagonal solver without the lateral propagation term, which is then added explicitly to the solution afterwards. Diffusivities obtained through Eq. 5 are capped at a minimum of  $10^{-7} \text{ m}^2\text{s}^{-1}$  (molecular level) and a maximum of  $10^{-2} \text{ m}^2\text{s}^{-1}$ .

A total of 9 experiments are carried out using the coarse resolution version of CCSM4 ([Shields et al., 2012](#)). The ocean component uses a horizontal nominal  $3^\circ$  resolution with 60 vertical layers of increasing thickness. In the surface layers are 10 m thick, ranging to several hundred meters in the deepest ocean. First, a coupled control simulation using the  $T31 \times 3$  configuration, CONT, is run for 500 years using a latitudinal dependent background diffusivity ( $0.01 \text{ cm}^2\text{s}^{-1}$  at Equator,  $0.3 \text{ cm}^2\text{s}^{-1}$  at  $30^\circ\text{N/S}$  and  $0.17 \text{ cm}^2\text{s}^{-1}$  elsewhere, [Jochum, 2009](#)) with bottom-enhanced diffusivity calculated from Eq. 2. This is then compared to a similar 500 year long run where the background and tidal induced diffusivities are replaced by the IDEMIX module, referred to as IDE, forced with only the conversion of barotropic to baroclinic tides using the same forcing as CONT ([Jayne and St. Laurent, 2001](#); [St. Laurent et al., 2002](#); [Jayne, 2009](#)). Analysis is carried out for the years 450-499.

One extra sensitivity simulation, IEDDY, includes an additional energy source from mesoscale eddies as calculated from the simple dissipation form of [Eden and Greatbatch \(2008\)](#), where mesoscale eddy energy is converted to internal wave energy by

$$\epsilon_{eddy} = 0.1L^2\sigma^3, \quad (6)$$

with  $L$  being the minimum of the first baroclinic Rossby radius of deformation and the Rhines scale, and  $\sigma = f\mathbf{u}_z/N$  is the Eady growth rate. This parameterization of eddy forcing adds energy to the internal waves everywhere in the ocean, in particular near eddying currents such as the ACC, western boundary currents and the Tropics (see e.g. figure 1d of [Eden et al., 2009](#)).

Eddy forcing of IDEMIX can be implemented in different ways ([Eden et al., 2014](#)). Here we choose the simplest form of local injection in Eq. 3.



238 This may not be the ideal implementation, but the reasoning behind the  
 239 simulation is to see what effect adding more energy to the parameterization  
 240 has, not how the choice of injection optimizes the simulations (here we refer  
 241 the reader to [Eden et al., 2014](#); [Pollmann et al., 2017](#)). The background for  
 242 the sensitivity experiment comes from the fact that IDEMIX falls short of  
 243 explaining observed dissipation rates without mesoscale eddy forcing ([Poll-  
 244 mann et al., 2017](#)). However, as CONT is only forced with tidal forcing, the  
 245 main comparison experiment, IDE, is also forced with tides only. For an en-  
 246 ergetically consistent implementation the eddy forcing should be calculated  
 247 from the used thickness diffusivity (in our simulations calculated according  
 248 to [Danabasoglu and Marshall, 2007](#)). Other ways to implement other energy  
 249 would be from estimates of lee wave energy fluxes ([Nikurashin and Ferrari,  
 250 2011](#); [Melet et al., 2014](#)). Our implementation compares with the horizontal  
 251 structure of such estimates. The choice of Eq. 6 is based on the simplicity  
 252 from the fact that it is already directly implemented in POP2 ([Eden and  
 253 Greatbatch, 2008](#); [Eden et al., 2009](#)). IEDDY will be used only when dis-  
 254 cussing adding extra forcing to the IDEMIX parameterization. Note that the  
 255 simple additional energy source by Eq. 6 is most likely an overestimation of  
 256 the effect of eddies (as discussed in [Eden et al., 2014](#)).

257 In order to revisit the Indo-Pacific upwelling discussed by [Jochum and  
 258 Eden \(2015\)](#), a set of three ocean/ice simulations with COREv2 Normal  
 259 Year Forcing ([Large and Yeager, 2004](#)) with a sea surface salinity restoring  
 260 timescale of one month are performed for both parameterizations of mixing.  
 261 Each set consists of a 500 year control simulation, CONTF and IDEF. Each  
 262 control simulation is accompanied by branched runs from year 300: One  
 263 where winds over the Southern Ocean south of 35°S are shut off by multi-  
 264 plying the wind stress with a value  $p = 0$ , CONTF00 and IDEF00, and one  
 265 where the Southern Ocean winds are increased by 50% by setting  $p = 1.5$ ,  
 266 CONTF15 and IDEF15. Between 35 and 25°S  $p$  is reduced linearly to 1.  
 267 The wind profiles are depicted in Fig. 1. Each branch is run for 200 years.  
 268 The forced simulation are analyzed for years 490-499. The model setups are  
 269 summarized in table 1.

270 Reducing the background diffusivity in simulations using IDEMIX comes  
 271 with the risk of making the model more prone to numerical noise, but this  
 272 has been found only to pose issues in marginal seas (e.g. the Baltic and  
 273 Caspian Seas, which only span few grid points and are not connected to the  
 274 major basins in the coarse resolution POP2), for which reason the background  
 275 diffusivities in these basins are set to the same value in IDEMIX simulations



276 as in the control simulations.

277 Section 3 first considers the coupled simulations and response in climate,  
278 and then deals with the two sets of forced simulations.

### 279 3. Results

#### 280 3.1. Coupled simulations

281 We begin by assessing the differences between the two coupled simula-  
282 tions, CONT and IDE, beginning with the diffusivities followed by the dif-  
283 ferences in climatology. Global maps of the diffusivities (in this case only  
284 background diffusivities and tidal mixing as calculated by Eq. 2 in CONT  
285 and diffusivities as calculated by Eq. 3 and 5 in IDE) are presented in Fig. 2,  
286 averaged over three depth intervals: 0.2-1 km, 1-2 km and 2-4 km. The up-  
287 per 200 m have been excluded because mixed and boundary layer diffusivities  
288 in IDE contaminate the signal of the thermocline structure due to the low  
289 stratifications within these. The pattern of bottom enhanced diffusivity due  
290 to topography is the same for the two simulations at all depths. This is ex-  
291 pected as both parameterizations have the same tidal energy induced at the  
292 same bottom cells. The difference is in how the energy is distributed globally,  
293 as only 1/3 of the energy is dissipated locally in CONT and the rest is not  
294 considered but assumed to contribute to the background diffusivity, whereas  
295 IDE injects all the energy and distributes it through Eq. 3. CONT is largely  
296 characterized by the latitudinal dependent background diffusivity (Jochum,  
297 2009), whereas IDE is characterized strongly by the bottom topography and  
298 displays a more heterogeneous diffusivity pattern. The diffusivities have been  
299 observed to be heterogeneous (Whalen et al., 2012; Pollmann et al., 2017),  
300 although the pattern here does lack much of the observed structure, likely  
301 due to only using tidal energy as forcing. In all depth intervals, IDE has large  
302 regions of reduced diffusivities compared to CONT. In the upper layer, the  
303 three major basins all have smaller diffusivities in IDE than CONT, show-  
304 ing a tendency for very small thermocline diffusivities. However, regions of  
305 larger diffusivities are also present, which is particularly connected to regions  
306 of weak stratification in the high latitudes and over rough topography. Be-  
307 tween 1-2 km in the Equatorial band, the Pacific and the South Australia  
308 Basin have lower diffusivities than the imposed background level in CONT,  
309 which is also valid for the 2-4 km interval. These regions are associated with  
310 abyssal plains with very low tidal energy input to the internal waves. The  
311 diffusivities close to rough topography, on the other hand, are generally the

312 same magnitude or somewhere even larger in IDE. This suggests that more  
 313 energy is dissipated locally (or at least very close to injection) in IDE than  
 314 the 1/3 used in CONT, and that the horizontal propagation of  $E$  is very  
 315 weak compared to the vertical propagation term and the dissipation.

316 The left panel of Fig. 3 shows the distribution of grid points with a  
 317 specific diffusivity. It is evident that where CONT has a very narrow peak  
 318 around diffusivities just above  $10^{-5} \text{ m}^2\text{s}^{-1}$ , IDE has a more broad distribution  
 319 of diffusivities, but also has distinct peaks at the two cut-off ends of the  
 320 spectrum. Note that there is almost an order magnitude more points at the  
 321 higher end of the spectrum in IDE than CONT due to the global dependency  
 322 on stratification throughout the water column and not just near the bottom,  
 323 which increases the diffusivity greatly in the surface layers within the mixed  
 324 layer. The histogram also displays that a large number of grid points in IDE  
 325 have diffusivities smaller than in CONT. From Fig. 2 we can infer that these  
 326 points are in particular located in the Tropics and Sub-Tropics over abyssal  
 327 plains and are not only confined to the deep ocean but also the upper parts  
 328 of the ocean below the mixed and boundary layers.

329 On the right panel of Fig. 3 globally averaged profiles of the diffusiv-  
 330 ities are plotted. Solid lines indicate diffusivities over rough topography  
 331 (defined here as bathymetry slopes larger than 0.01), and dashed lines indi-  
 332 cate diffusivities over smooth topography. Only water columns with depths  
 333 greater than 500 m are included. This shows that CONT has up to an order  
 334 magnitude larger diffusivities than IDE in the very deep ocean over smooth  
 335 topography. This is a result of the deep ocean points which have very little  
 336 injection of tidal energy in the abyssal plains, causing many points to be of  
 337 small magnitude in IDE (see Fig. 2) in the deep ocean, in contrast to the  
 338 rather large background diffusivity in CONT. Between 1-4 km depth, the two  
 339 models have very similar global profiles. In the upper 200 m the stratification  
 340 dependency in IDE shows up in very large diffusivities.

341 The global power consumption to raise the potential energy due to vertical  
 342 mixing is estimated as the global integral

$$\mathcal{P} = \int_V \kappa \rho \frac{\partial b}{\partial z} dV, \quad (7)$$

343 where  $b = g\delta\rho/\rho_0$  is buoyancy, which yields a total of 0.26 TW for CONT  
 344 of which 0.12 TW is dissipated below 500 m, and 0.30 TW for IDE of which  
 345 only 0.08 TW is dissipated below a depth of 500 m.

346 The vertical distribution of dissipated energy per unit volume divided  
 347 by the density of water, yielding the dissipation per unit mass, is shown in  
 348 Fig. 4 for CONT (black) and IDE (red) along with a global composite of  
 349 fine-structure estimates (Kunze, 2017, magenta line). The dashed red curve  
 350 is calculated directly from Eq. 4, whereas solid curves are calculated by  
 351 dividing the integrand of Eq. 7 with the mixing efficiency. This estimate is  
 352 derived as no direct estimate of dissipation is calculated in CONT. Unstably  
 353 stratified grid points are omitted as assumptions for fine structure as well  
 354 as parameterizations are not valid under these conditions. As can be seen,  
 355 using diffusivity and stratification to derive the dissipation in IDE (solid red)  
 356 underestimates the amount of dissipation calculated by Eq. 4 (dashed red).  
 357 Both parameterizations show too much dissipation in the deep regions of the  
 358 ocean and in particular at mid-depth, but dissipation in CONT is more in  
 359 line with observations above 1 km, where the dissipation rate in IDE is too  
 360 small and does not resemble fine-structure estimates. That both models have  
 361 too much dissipation in the deep ocean suggests too much deep dissipation  
 362 of tidal energy. For IDE, discrepancies with observations might be related  
 363 to either a poor representation of propagation of energy or missing energy  
 364 sources in the upper ocean. To investigate the latter, the sensitivity study  
 365 IEDDY has been carried out, where conversion of mesoscale eddy energy to  
 366 internal wave energy is added in Eq. 3. The resulting dissipation profile (from  
 367 Eq. 4) is added in Fig. 4 as the dashed blue line. It is seen that eddy energy  
 368 forcing increases the interior dissipation rates in particular in the upper 2  
 369 km. A different choice of implementation of mesoscale eddy dissipation may  
 370 alter this distribution, but this is beyond the scope of this study. It should  
 371 be noted that the fine-structure estimates sample mostly the major ocean  
 372 basins whereas the model estimates are global averages. Furthermore, the  
 373 uncertainty is large in the deep ocean where observations are sparse (Kunze,  
 374 2017).

375 The average AMOC strength at 26°N is 14.3 Sverdrups ( $1 \text{ Sv} = 10^6 \text{ m}^3\text{s}^{-1}$ )  
 376 for CONT and 13.4 Sv for IDE. Thus, the different dissipation in IDE is ac-  
 377 companied by a weaker AMOC. This may be a reflection in changed mixing  
 378 in waters associated with deep water formation (Melet et al., 2016), although  
 379 the AMOC reduction is not necessarily a direct result of the mixing param-  
 380 eterization but could be due to feedbacks in buoyancy or wind forcing from  
 381 the atmosphere. However, wintertime convection depths in the North At-  
 382 lantic are shallower in IDE than CONT, suggesting the AMOC reduction to  
 383 be caused by reduced production of North Atlantic Deep Water (not shown).

384 Changes in the surface fields are generally small. Fig. 5 shows the sea  
 385 surface temperature (SST) difference between IDE and CONT. Note that  
 386 CONT has several biases (discussed in [Shields et al., 2012](#)), the most promi-  
 387 nent ones being related to the western boundary currents and the upwelling  
 388 regions such as the Benguela system west of southern Africa, where the am-  
 389 plitude of the biases are larger in IDE than CONT. The root-mean-squared  
 390 error (RMSE) for CONT is 1.67 and somewhat larger for IDE with a RMSE  
 391 of 1.90 (reduced to 1.80 in IEDDY, not shown).

392 Superimposed on the upper panel of Fig. 5 is the 15% sea ice concentra-  
 393 tion lines for CONT (black) and IDE (red). The two lines almost coincide,  
 394 with IDE having a slightly more northward extent of sea ice in the Southern  
 395 Ocean, and a slightly more southward extent in the Bering Sea. The North  
 396 Atlantic sea ice extent is comparable, but sea ice concentrations are greater  
 397 within parts of the ocean in IDE, most remarkably in the Baffin Bay (not  
 398 shown). The sea ice extent is already too large in CONT ([Shields et al.,](#)  
 399 [2012](#)), but is stable within the two parameterization schemes.

400 The lower panel of Fig. 5 shows the precipitation difference between IDE  
 401 and CONT. Differences are confined to the Tropics. Two major patterns are  
 402 visible. The first is an increase in precipitation in the double-ITCZ seen over  
 403 the Pacific and Atlantic. These changes are rather small and related to the  
 404 modest increase in SST in the upwelling regions. The biggest change occurs  
 405 over the Indian Ocean and the Indonesian seas, related to a difference in SST  
 406 in the same region. This precipitation pattern is related to the diffusivity in  
 407 the Banda Sea region ([Jochum and Potemra, 2008](#)). In CONT, this region  
 408 has enhanced background vertical diffusivity made to match observations of  
 409 a large tidally induced mixing in the region, which causes a reduction in the  
 410 SST which heavily influences precipitation. This mixing is not captured in  
 411 IDE, which may either be due to a too low energy input from tides or in the  
 412 way the energy propagates into the region in the IDEMIX parameterization.

413 Fig. 6 shows the meridional distribution of temperature difference be-  
 414 tween the two simulations, overlaid with contours ( $5^{\circ}\text{C}$  intervals) from CONT  
 415 (dashed), IDE (solid) and World Ocean Atlas 2009 (WOA, [Locarnini et al.,](#)  
 416 [2010](#), dotted). A large difference in the simulations is in the thermocline.  
 417 IDE has a sharper and shallower thermocline which causes temperatures to  
 418 be cooler between 100 and 1000 m depth. This is seen in particular in the  
 419 waters between 5 and 15  $^{\circ}\text{C}$  which are shallower in IDE compared to both  
 420 CONT and observations, causing the temperature stratification to be in less  
 421 agreement with observations. At mid-depth, however, IDE is closer to ob-

422 servations seen in the close agreement with the observed 5°C isotherm. The  
 423 rest of the global ocean has temperature differences with amplitude less than  
 424 0.5°C. The large differences between CONT and IDE occur in the upper km  
 425 which is also the region of the largest discrepancy in dissipated energy in Fig.  
 426 4, and in the region of small diffusivities in the Pacific and Atlantic, causing  
 427 a reduced diffusion of heat from the surface, making the deep ocean largely  
 428 colder and lifting the isotherms relatively to CONT. Evidently, the amount  
 429 of energy used for mixing, but also its distribution vertically and horizontally,  
 430 plays a major role in setting the thermocline structure (in agreement with  
 431 earlier studies such as Bryan, 1987; Samelson, 1998; Melet et al., 2016).

### 432 3.2. Forced experiments

433 We now turn to the forced simulations with changed wind stress. Re-  
 434 sulting diffusivities, SSTs and thermocline structure are similar as for the  
 435 coupled simulations (not shown) and will not be discussed further, as the  
 436 focus of the forcing experiments is how the ocean responds to changes in  
 437 forcing.

438 As can be seen in Fig. 1, the wind stress for  $p = 1.5$  peaks at almost 0.2  
 439 N/m<sup>2</sup> compared to 0.13 for  $p = 1.0$ . This change in wind stress alters the  
 440 wind stress curl over the Southern Ocean and forces increased Ekman driven  
 441 upwelling. For  $p = 0$ , the wind stress curl is zero and the corresponding  
 442 Ekman driven upwelling is zero.

443 The residual meridional overturning circulations (RMO, from hereon  
 444 simply MOC), defined as the sum of the Eulerian mean and the eddy-  
 445 induced overturning streamfunctions for the Atlantic (AMOC) and Indo-  
 446 Pacific (PMOC, calculated as the global MOC subtracted the AMOC, min-  
 447 imum overturning north of 35S) averaged over the last 10 model years are  
 448 listed in Table 4. The AMOC strength at 26°N is plotted in Fig. 7. CONTF  
 449 has an AMOC strength of 15.7 Sv after 300 years and 15.8 Sv after 500 years  
 450 compared to 13.5 Sv at both times in IDEF, suggesting that although not  
 451 nearly equilibrated, the model is stable enough for our purposes. Also, the  
 452 weaker AMOC seen in the coupled runs is also reflected in the forced runs.  
 453 As with coupled runs, shallow North Atlantic boundary layer depths in IDE  
 454 suggest a reduced production of North Atlantic Deep Water to be the cause  
 455 of this.

456 As can be seen, increasing (decreasing) winds results in an initial, quick  
 457 response where the AMOC increases (decreases) over the first 30 years. After  
 458 this initial, transient response, a more gradual increase (decrease) follows.

459 The initial relative increase in AMOC strength in CONTF15 is 9% after 30  
 460 years of perturbation and by the end in year 500 the AMOC strength has  
 461 increased by 18%. For IDEF15 relative to IDEF the values are 12% and 24%,  
 462 respectively. Correspondingly for  $p = 0.0$  the values of CONTF00 relative to  
 463 CONTF are a 16% and 26% decrease in AMOC strength, and for IDEF00 the  
 464 decrease corresponds to 18% and 31% relative to IDEF. It follows that the  
 465 relative sensitivity towards changing wind stress is larger in simulations with  
 466 the Olbers and Eden (2013) parameterization, whereas the absolute values  
 467 are comparable.

468 The PMOC for the six experiments is plotted in Fig. 8 along with the  
 469 average depth of the  $\sigma_\theta = 27.7 \text{ kg m}^{-3}$  isopycnal. The relative increase in  
 470 strength of the upwelling (PMOC in Table 4) for IDEF00 is 194%, and the  
 471 relative reduction in IDEF15 is 17%. For CONTF00 and CONTF15 these  
 472 numbers are 106% and 27%, respectively. The absolute changes in PMOC  
 473 in experiments with  $p = 0$  compares roughly to the strength of the AMOC  
 474 in the corresponding runs.

475 Thus, as in Jochum and Eden (2015), simulations without any wind stress  
 476 over the Southern Ocean yield an enhanced upwelling in the Indo-Pacific,  
 477 which at least in part compensates the missing upwelling in the Southern  
 478 Ocean and sustains an AMOC at least for several centuries following the  
 479 beginning of the wind stress perturbation.

480 The  $27.7 \text{ kg m}^{-3}$  isopycnal shoals 200-300 m in the Pacific and deepens  
 481 in the Southern Ocean in both experiments with  $p = 0$ , compared to sim-  
 482 ulations with  $p = 1$ , flattening and shallowing the isopycnal. For  $p = 1.5$   
 483 the isopycnal steepens over the Southern Ocean and deepens by up to 200  
 484 m at  $40^\circ\text{S}$  and about 100 m north of this latitude. Thus, while the relative  
 485 changes in streamfunction are different with the two parameterizations, the  
 486 impact of the winds on the pycnocline depth is very similar in the two cases.  
 487 Thus, despite diffusivities depending on the stratification, the Indo-Pacific  
 488 overturning response in IDEF simulations is, in absolute sense, comparable  
 489 to the response in CONTF simulations.

#### 490 4. Summary and discussion

491 Three coupled ocean, atmosphere and sea ice (including a sensitivity run)  
 492 and six forced ocean/sea ice simulations, have been carried out to assess the  
 493 impact of the vertical mixing parameterization IDEMIX (Olbers and Eden,  
 494 2013) in the ocean component of CCSM4. The coupled simulations, CONT,

495 IDE and the sensitivity study IEDDY, are run for 500 years and the forced  
 496 CONTF and IDEF are run for 300 years, at which time wind stress perturba-  
 497 tions over the Southern Ocean are performed and simulations are run for 200  
 498 years more. It has been shown that the way in which the dissipation of energy  
 499 is localized globally impacts the ocean state and related climate (in agreement  
 500 with earlier studies such as [Samelson, 1998](#); [Melet et al., 2013](#)). The most  
 501 prominent differences occur in setting the thermocline depth. Reduced ther-  
 502 mocline diffusivities cause less heat to be mixed downward, causing a sharper  
 503 and shallower thermocline, consistent with other studies ([Melet et al., 2016](#)).  
 504 The relationship between thermocline structure and diffusivities implies that  
 505 large differences in heat and carbon storage can occur over long timescales  
 506 depending on the mixing parameterization, something that is left for future  
 507 studies to assess.

508 For the coupled simulations minor changes are observed in the SSTs and  
 509 precipitation fields. The representation of precipitation and SSTs in IDE is  
 510 worse than in CONT. However, compared to the already existing biases in  
 511 CONT, the differences between IDE and CONT are small. Also, the overall  
 512 climate state is very comparable in the two runs. The SST differences in  
 513 IDE are adding to already existing biases, which implies that with improved  
 514 parameterizations of vertical mixing the biases might be reduced.

515 The Benguela upwelling system is one area in the model with an already  
 516 existing bias that gets worse in IDE. The nature of the bias has been studied  
 517 and is thought to be a result of several processes ([Xu et al., 2014](#); [Harlaß  
 518 et al., 2015](#)). In particular, vertical mixing has been suggested to be one of  
 519 the contributing mechanisms in generating temperature biases in POP2 ([Xu  
 520 et al., 2014](#)). Our results support this hypothesis and suggest that either  
 521 energy forcing or propagation is not adequately represented in the region. It  
 522 is also possible that a more realistic description of vertical mixing enhances  
 523 the SST bias because a previous compensation with other model errors is  
 524 relaxed. The same holds for other model biases, highlighting the need for  
 525 more careful representation of vertical mixing in climate models.

526 While the errors in surface fields are larger in IDE than CONT in some  
 527 areas, IDEMIX is developed from physical principles, whereas the existing  
 528 parameterization uses the background mixing to match diffusivities to obser-  
 529 vations, which may not hold in studies of paleoclimate or future predictions.  
 530 It is furthermore interesting to note that while both simulations are missing  
 531 energy sources from e.g. mesoscale eddies, the contribution from these is  
 532 easily implemented as forcing terms in IDEMIX if one can calculate the en-



533 energy transfer to the internal wave field, whereas the existing model requires a  
 534 new parameterization for each energy source that needs to be included. Us-  
 535 ing IDEMIX, the problem is reduced to the investigation of how and where  
 536 energy enters the internal wave field (Eden et al., 2014).

537 The large amount of grid points with diffusivities below  $10^{-6} \text{ m}^2 \text{ s}^{-1}$  in  
 538 IDE seen in Fig. 2 and in the left panel of Fig. 3 may not be realistic, but  
 539 suggest that more energy forcing to the internal wave field is needed. Our  
 540 sensitivity study, IEDDY, is preliminary, but indicates that adding energy  
 541 sources in IDEMIX might indeed bring the simulation closer to observed esti-  
 542 mates of dissipation rates in the thermocline and thus improve climate simu-  
 543 lations. However, this requires careful treatment of each individual source of  
 544 internal wave energy. For instance, for coarse resolution ocean models, tidal  
 545 energy may be put in too deep in the water column which might in turn affect  
 546 overturning strengths (Schmittner and Egbert, 2014). Other improvements  
 547 might be found by separate treatment of low mode internal waves (Eden and  
 548 Olbers, 2014).

549 Finally, the present results show that trapped waves and their dissipation  
 550 in the Banda Sea is not well represented in the current parameterization of  
 551 IDEMIX. It is not clear how such waves, which are unresolved in climate  
 552 models, and their associated dissipation should be parameterized and im-  
 553 plemented in IDEMIX, but as with the case of the Banda Sea, these are of  
 554 climatic importance and other areas might exist where similar wave dissipa-  
 555 tion is important in setting the mixing strength.

556 With regards to the forced simulations, we find that the relative impor-  
 557 tance of the Southern Ocean wind stress on AMOC strength is larger in IDEF  
 558 than CONTF, whereas absolute changes are similar. It is therefore likely  
 559 that the difference in relative importance of winds is a result of the changed  
 560 background state and its associated weaker AMOC observed in IDEF. Both  
 561 parameterizations find a similar compensation in the Indo-Pacific when the  
 562 wind stress is shut off over the Southern Ocean, in agreement with Jochum  
 563 and Eden (2015). A key difference compared to their results is that without  
 564 wind stress the AMOC is declining toward a weak state, whereas they found  
 565 the AMOC to be independent of the wind stress. However, the nature of  
 566 forced ocean/ice experiments do not allow for atmospheric feedbacks which  
 567 might modify this result (Rahmstorf and England, 1997).

## 568 Acknowledgements

569 This study was supported by The Danish Council for Independent Re-  
570 search, Natural Sciences, 4002-00397. Simulations were done with support  
571 from the High Performance Computing Centre at the University of Copen-  
572 hagen. The authors would also like to thank Eric Kunze for fine structure  
573 estimates of internal wave dissipation and Nils Brüggemann and Dirk Olbers  
574 for helpful comments.

## 575 References

- 576 Bryan, F., 1987. Parameter sensitivity of primitive equation ocean gen-  
577 eral circulation models. *J. Phys. Oceanogr.* 17, 970–985. doi:[10.1175/  
578 1520-0485\(1987\)017<0970:PSOPEO>2.0.CO;2](https://doi.org/10.1175/1520-0485(1987)017<0970:PSOPEO>2.0.CO;2).
- 579 Bryan, K., Lewis, L., 1979. A water mass model of the world ocean. *J.*  
580 *Geophys. Res.* 84, 2503–2517. doi:[10.1029/JC084iC05p02503](https://doi.org/10.1029/JC084iC05p02503).
- 581 Danabasoglu, G., Bates, S., Briegleb, B., Jayne, S., Jochum, M., Large, W.,  
582 Peacock, S., Yeager, S., 2012. The ccsm4 ocean component. *J. Climate*  
583 25, 1361–1389. doi:[10.1175/JCLI-D-00091.1](https://doi.org/10.1175/JCLI-D-00091.1).
- 584 Danabasoglu, G., Marshall, J., 2007. Effects of vertical variations of thickness  
585 diffusivity in an ocean general circulation model. *Ocean Modell.* 18, 122–  
586 141.
- 587 Eden, C., Czeschel, L., Olbers, D., 2014. Toward energetically consis-  
588 tent ocean models. *J. Phys. Oceanogr.* 44, 3160–3184. doi:[10.1175/  
589 JPO-D-13-0260.1](https://doi.org/10.1175/JPO-D-13-0260.1).
- 590 Eden, C., Greatbatch, R., 2008. Towards a mesoscale eddy closure. *Ocean*  
591 *Modell.* 20, 223–239. doi:[10.1016/j.ocemod.2007.09.002](https://doi.org/10.1016/j.ocemod.2007.09.002).
- 592 Eden, C., Jochum, M., Danabasoglu, G., 2009. Effects of different closures  
593 for thickness diffusivity. *Ocean Modell.* 26, 47–59.
- 594 Eden, C., Olbers, D., 2014. An energy compartment model for propagation,  
595 nonlinear interaction, and dissipation of internal gravity waves. *J. Phys.*  
596 *Oceanogr.* 44, 2093–2106. doi:[10.1175/JPO-D-13-0224.1](https://doi.org/10.1175/JPO-D-13-0224.1).

597 Egbert, G., Ray, R., 2000. Significant dissipation of tidal energy in the  
598 deep ocean inferred from satellite altimeter data. *Nature* 405, 775–778.  
599 doi:[10.1038/35015531](https://doi.org/10.1038/35015531).

600 Gent, P.R., Danabasoglu, G., Donner, L.J., Holland, M.M., Hunke, E.C.,  
601 Jayne, S.R., Lawrence, D.M., Neale, R.B., Rasch, P.J., Vertenstein, M.,  
602 Worley, P.H., Yang, Z.L., Zhang, M., 2011. The community climate system  
603 model version 4. *J. Climate* 24, 4973–4991. doi:[10.1175/2011JCLI4083.1](https://doi.org/10.1175/2011JCLI4083.1).

604 Gent, P.R., Large, W.G., Bryan, F.O., 2001. What sets the mean transport  
605 through drake passage. *J. Geophys. Res.* 106, 2693–2712. doi:[10.1029/](https://doi.org/10.1029/2000JC900036)  
606 [2000JC900036](https://doi.org/10.1029/2000JC900036).

607 Harlaß, J., Latif, M., Park, W., 2015. Improving climate model simulation  
608 of tropical atlantic sea surface temperature: The importance of enhanced  
609 vertical atmospher model resolution. *Geophys. Res. Lett.* 42, 2401–2408.  
610 doi:[10.1002/2015GL063310](https://doi.org/10.1002/2015GL063310).

611 Harrison, M., Hallberg, R., 2008. Pacific subtropical cell response to reduced  
612 equatorial dissipation. *J. Phys. Oceanogr.* 38, 1894–1912. doi:[10.1175/](https://doi.org/10.1175/2008JP03708.1)  
613 [2008JP03708.1](https://doi.org/10.1175/2008JP03708.1).

614 Heyney, F., Wright, J., Flatté, S., 1986. Energy and action flow through  
615 the internal wave field: An eikonal approach. *J. Geophys. Res.* 91 (C7),  
616 8487–8495. doi:[10.1029/JC091iC07p08487](https://doi.org/10.1029/JC091iC07p08487).

617 Jayne, S., 2009. The impact of abyssal mixing parameterizations in an ocean  
618 general circulation model. *J. Phys. Oceanogr.* 39, 1756–1775. doi:[10.1175/](https://doi.org/10.1175/2009JP04085.1)  
619 [2009JP04085.1](https://doi.org/10.1175/2009JP04085.1).

620 Jayne, S., St. Laurent, L., 2001. Parameterizing tidal dissipation over  
621 rough topography. *Geophys. Res. Lett.* 28 (5), 811–814. doi:[10.1029/](https://doi.org/10.1029/2000GL012044)  
622 [2000GL012044](https://doi.org/10.1029/2000GL012044).

623 Jochum, M., 2009. Impact of latitudinal variations in vertical diffusivity  
624 on climate simulations. *J. Geophys. Res.* 114, C01010. doi:[10.1029/](https://doi.org/10.1029/2008JC005030)  
625 [2008JC005030](https://doi.org/10.1029/2008JC005030).

626 Jochum, M., Briegleb, B., Danabasoglu, G., Large, W., Norton, N., Jayne,  
627 S., Alford, M., Bryan, F., 2013. The impact of oceanic near-inertial waves  
628 on climate. *J. Climate* 26, 2833–2844. doi:[10.1175/JCLI-D-12-00181.1](https://doi.org/10.1175/JCLI-D-12-00181.1).

- 629 Jochum, M., Eden, C., 2015. The connection between southern ocean winds,  
630 the atlantic meridional overtuning circulation, and indo-pacific upwelling.  
631 J. Climate 28, 9250–9257. doi:[10.1175/JCLI-D-15-0263.1](https://doi.org/10.1175/JCLI-D-15-0263.1).
- 632 Jochum, M., Potemra, J., 2008. Sensitivity of tropical rainfall to banda sea  
633 diffusivity in the community climate system model. J. Climate 21, 6445–  
634 6454. doi:[10.1175/2008JCLI2230.1](https://doi.org/10.1175/2008JCLI2230.1).
- 635 Kuhlbrodt, T., Griesel, A., Montoya, M., Levermann, A., Hofmann, M.,  
636 Rahmstorf, S., 2007. On the driving processes of the atlantic merid-  
637 ional overturning circulation. Rev. Geophys. 45, RG2001. doi:[10.1029/  
638 2004RG000166](https://doi.org/10.1029/2004RG000166).
- 639 Kunze, E., 2017. Internal-wave-driven mixing: Global geography and bud-  
640 gets. Journal of Physical Oceanography 47, 1325–1345. doi:[10.1175/  
641 JPO-D-16-0141.1](https://doi.org/10.1175/JPO-D-16-0141.1).
- 642 Large, W., Yeager, S., 2004. Diurnal to decadal global forcing for ocean and  
643 sea-ice models: the data sets and flux climatologies. NCAR.
- 644 Ledwell, J., Watson, A., Law, C., 1998. Mixing of a tracer in the pycnocline.  
645 Journ. Geophys. Res. 103, 21499–21529. doi:[10.1029/98JC01738](https://doi.org/10.1029/98JC01738).
- 646 Locarnini, R., Mishonov, A., Antonov, J., Boyer, T., Garcia, H., Baranova,  
647 O., Zweng, M., Johnson, D., 2010. World Ocean Atlas 2009, Volume 1:  
648 Temperature. NOAA Atlas NESDIS 68.
- 649 MacKinnon, J.A., et al., 2017. Climate process team on internal-wave  
650 driven ocean mixing. Bull. Am. Meteorol. Soc. In Press. doi:[10.1175/  
651 BAMS-D-16-0030.1](https://doi.org/10.1175/BAMS-D-16-0030.1).
- 652 Marotzke, J., 1997. Boundary mixing and the dynamics of three-dimensional  
653 thermohaline circulation. J. Phys. Oceanography 27, 1713–1728. doi:[10.  
654 1175/1520-0485\(1997\)027<1713:BMATDO>2.0.CO;2](https://doi.org/10.1175/1520-0485(1997)027<1713:BMATDO>2.0.CO;2).
- 655 McComas, C., Müller, P., 1981. Time scales of resonant interactions among  
656 oceanic internal waves. J. Phys. Oceanogr. 11, 139–147. doi:[10.1175/  
657 1520-0485\(1981\)011<0139:TSORIA>2.0.CO;2](https://doi.org/10.1175/1520-0485(1981)011<0139:TSORIA>2.0.CO;2).
- 658 Melet, A., Hallberg, R., Legg, S., Nikurashin, M., 2014. Sensitivity of the  
659 ocean state to lee wave-driven mixing. J. Phys. Oceanogr. 44, 900–921.  
660 doi:[10.1175/JPO-D-13-072.1](https://doi.org/10.1175/JPO-D-13-072.1).

- 661 Melet, A., Hallberg, R., Legg, S., Polzin, K., 2013. Sensitivity of the ocean  
662 state to the vertical distribution of internal-tide-driven mixing. *J. Phys.*  
663 *Oceanogr.* 43, 602–615. doi:[10.1175/JPO-D-12-055.1](https://doi.org/10.1175/JPO-D-12-055.1).
- 664 Melet, A., Legg, S., Hallberg, R., 2016. Climate impacts of parameterized  
665 local and remote tidal mixing. *J. Climate* 29, 3473–3500. doi:[10.1175/  
666 JCLI-D-15-0153.1](https://doi.org/10.1175/JCLI-D-15-0153.1).
- 667 Munday, D., Johnson, H., Marshall, D., 2013. Eddy saturation of equili-  
668 brated circumpolar currents. *J. Phys. Oceanogr.* 43, 507–532. doi:[10.  
669 1175/JPO-D-12-095.1](https://doi.org/10.1175/JPO-D-12-095.1).
- 670 Munk, W., 1966. Abyssal recipes. *Deep Sea Res.* 13, 707–730. doi:[10.1016/  
671 0011-7471\(66\)90602-4](https://doi.org/10.1016/0011-7471(66)90602-4).
- 672 Munk, W., Wunsch, C., 1998. Abyssal recipes ii: energetics of tidal and  
673 wind mixing. *Deep Sea Res.* 45, 1977–2010. doi:[10.1016/S0967-0637\(98\)  
674 00070-3](https://doi.org/10.1016/S0967-0637(98)00070-3).
- 675 Nikurashin, M., Ferrari, R., 2010. Radiation and dissipation of internal waves  
676 generated by geostrophic motions impinging on small-scale topography:  
677 Theory. *J. Phys. Oceanogr.* 40, 1055–1074. doi:[10.1175/2009JP04199.1](https://doi.org/10.1175/2009JP04199.1).
- 678 Nikurashin, M., Ferrari, R., 2011. Global energy conversion rate from  
679 geostrophic flows into internal lee waves in the deep ocean. *Geophys. Res.*  
680 *Letters* 38, L08610. doi:[10.1029/2011GL046576](https://doi.org/10.1029/2011GL046576).
- 681 Nycander, J., 2005. Generation of internal waves in the deep ocean by tides.  
682 *J. Geophys. Res.* 110, C10028. doi:[10.1029/2004JC002487](https://doi.org/10.1029/2004JC002487).
- 683 Olbers, D., Eden, C., 2013. A global model for the diapycnal diffusivity  
684 induced by internal gravity waves. *J. Phys. Oceanogr.* 43, 1759–1779.  
685 doi:[10.1175/JPO-D-12-0207.1](https://doi.org/10.1175/JPO-D-12-0207.1).
- 686 Osborn, T., 1980. Estimates of the local rate of vertical diffusion from  
687 dissipation measurements. *J. Phys. Oceanogr.* 10, 83–89. doi:[10.1175/  
688 1520-0485\(1980\)010<0083:EOTLR0>2.0.CO;2](https://doi.org/10.1175/1520-0485(1980)010<0083:EOTLR0>2.0.CO;2).
- 689 Pollmann, F., Eden, C., Olbers, D., 2017. Evaluating the global internal  
690 wave model idemix using finestructure methods. *J. Phys. Oceanogr.* 47,  
691 2267–2289.

- 692 Polzin, K., Toole, J., Ledwell, J., Schmitt, R., 1997. Spatial variability of  
693 turbulent mixing in the abyssal ocean. *Science* 276, 93+96. doi:[10.1126/  
694 science.276.5309.93](https://doi.org/10.1126/science.276.5309.93).
- 695 Rahmstorf, S., England, M., 1997. Influence of southern hemisphere winds  
696 on north atlantic deep water flow. *J. Phys. Oceanogr.* 27, 2040–2054.  
697 doi:[10.1175/1520-0485\(1997\)027<2040:I0SHW0>2.0.CO;2](https://doi.org/10.1175/1520-0485(1997)027<2040:I0SHW0>2.0.CO;2).
- 698 Samelson, R., 1998. Large-scale circulation with locally enhanced vertical  
699 mixing. *J. Phys. Oceanogr.* 28, 712–726. doi:[10.1175/1520-0485\(1998\)  
700 028<0712:LSCWLE>2.0.CO;2](https://doi.org/10.1175/1520-0485(1998)028<0712:LSCWLE>2.0.CO;2).
- 701 Sandström, J., 1908. Dynamische verusche mit meerwasser. *Annals in Hy-*  
702 *drodynamic Marine Meteorology* 1, 6–23.
- 703 Schmittner, A., Egbert, G., 2014. An improved parameterization of tidal  
704 mixing. *Geosci. Model Dev.* 7, 211–224. doi:[10.5194/gmd-7-211-2014](https://doi.org/10.5194/gmd-7-211-2014).
- 705 Shields, C., Bailey, D., Danabasoglu, G., Jochum, M., Kiehl, J., Levis, S.,  
706 Park, S., 2012. The low-resolution ccsm4. *J. Climate* 25, 3993–4014.  
707 doi:[10.1175/JCLI-D-11-00260.1](https://doi.org/10.1175/JCLI-D-11-00260.1).
- 708 Simmons, H., Jayne, S., St. Laurent, L., Weaver, A., 2004. Tidally driven  
709 mixing in a numerical model of the ocean general circulation. *Ocean Mod-*  
710 *ell.* 6, 245–263. doi:[10.1016/S1463-5003\(03\)00011-8](https://doi.org/10.1016/S1463-5003(03)00011-8).
- 711 St. Laurent, L., Simmons, H., Jayne, S., 2002. Estimating tidally driven  
712 mixing in the deep ocean. *Geophys. Res. Letters* 29(23), 2106. doi:[10.  
713 1029/2002GL015633](https://doi.org/10.1029/2002GL015633).
- 714 Toggweiler, J., Samuels, B., 1995. Effects of drake passage on the global  
715 thermohaline circulation. *Deep-Sea Res.* 42, 477–500. doi:[10.1016/  
716 0967-0637\(95\)00012-U](https://doi.org/10.1016/0967-0637(95)00012-U).
- 717 Toggweiler, J., Samuels, B., 1998. On the ocean’s large-scale circulation  
718 near the limit of no vertical mixing. *J. Phys. Oceanogr.* 28, 1832–1852.  
719 doi:[10.1175/1520-0485\(1998\)028<1832:OT0SLS>2.0.CO;2](https://doi.org/10.1175/1520-0485(1998)028<1832:OT0SLS>2.0.CO;2).
- 720 Waterhouse, A.F., et al., 2014. Global patterns of diapycnal mixing from  
721 measurements of the turbulent dissipation rate. *J. Phys. Oceanogr.* 44,  
722 1854–1872. doi:[10.1175/JPO-D-13-0104.1](https://doi.org/10.1175/JPO-D-13-0104.1).

- 723 Whalen, C., Talley, L., MacKinnon, J., 2012. Spatial and temporal variability  
724 of global ocean mixing inferred from argo profiles. *Geophys. Res. Let.* 39,  
725 L18612. doi:[10.1029/2012GL053196](https://doi.org/10.1029/2012GL053196).
- 726 Xu, Z., Chang, P., Richter, I., Kim, W., Tang, G., 2014. Diagnosing southeast  
727 tropical atlantic sst and ocean circulation biases in the cmip5 ensemble.  
728 *Clim Dyn* 43, 3123–3145. doi:[10.1007/s00382-014-2247-9](https://doi.org/10.1007/s00382-014-2247-9).



Table 1: Summary of model setups. Case explanation: OCN: ocean/sea ice. FULL: fully coupled.  $p$  is the SO wind multiplication factor

	Case	Mixing	$p$
CONT	FULL	<a href="#">St. Laurent et al. (2002)</a>	–
IDE	FULL	<a href="#">Olbers and Eden (2013)</a>	–
IEDDY	FULL	<a href="#">Olbers and Eden (2013)</a> ; <a href="#">Eden and Greatbatch (2008)</a>	–
CONTF00	OCN	<a href="#">St. Laurent et al. (2002)</a>	0.0
CONTF	OCN	<a href="#">St. Laurent et al. (2002)</a>	1.0
CONTF15	OCN	<a href="#">St. Laurent et al. (2002)</a>	1.5
IDEF00	OCN	<a href="#">Olbers and Eden (2013)</a>	0.0
IDEF	OCN	<a href="#">Olbers and Eden (2013)</a>	1.0
IDEF15	OCN	<a href="#">Olbers and Eden (2013)</a>	1.5

Table 2: Absolute strength in overturning circulations in the forced simulations. All units in Sv ( $1 \text{ Sv} = 10^6 \text{ m}^3 \text{ s}^{-1}$ ).

	AMOC	PMOC
CONTF00	11.7	-21.4
CONTF	15.8	-10.3
CONTF15	18.5	-7.5
IDEF00	9.5	-14.8
IDEF	13.5	-5.0
IDEF15	16.6	-4.1

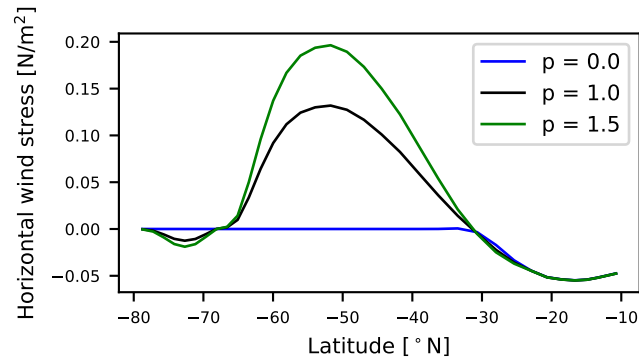


Figure 1: The horizontal wind stress over the Southern Ocean in the three experiments of each set of forced simulations.

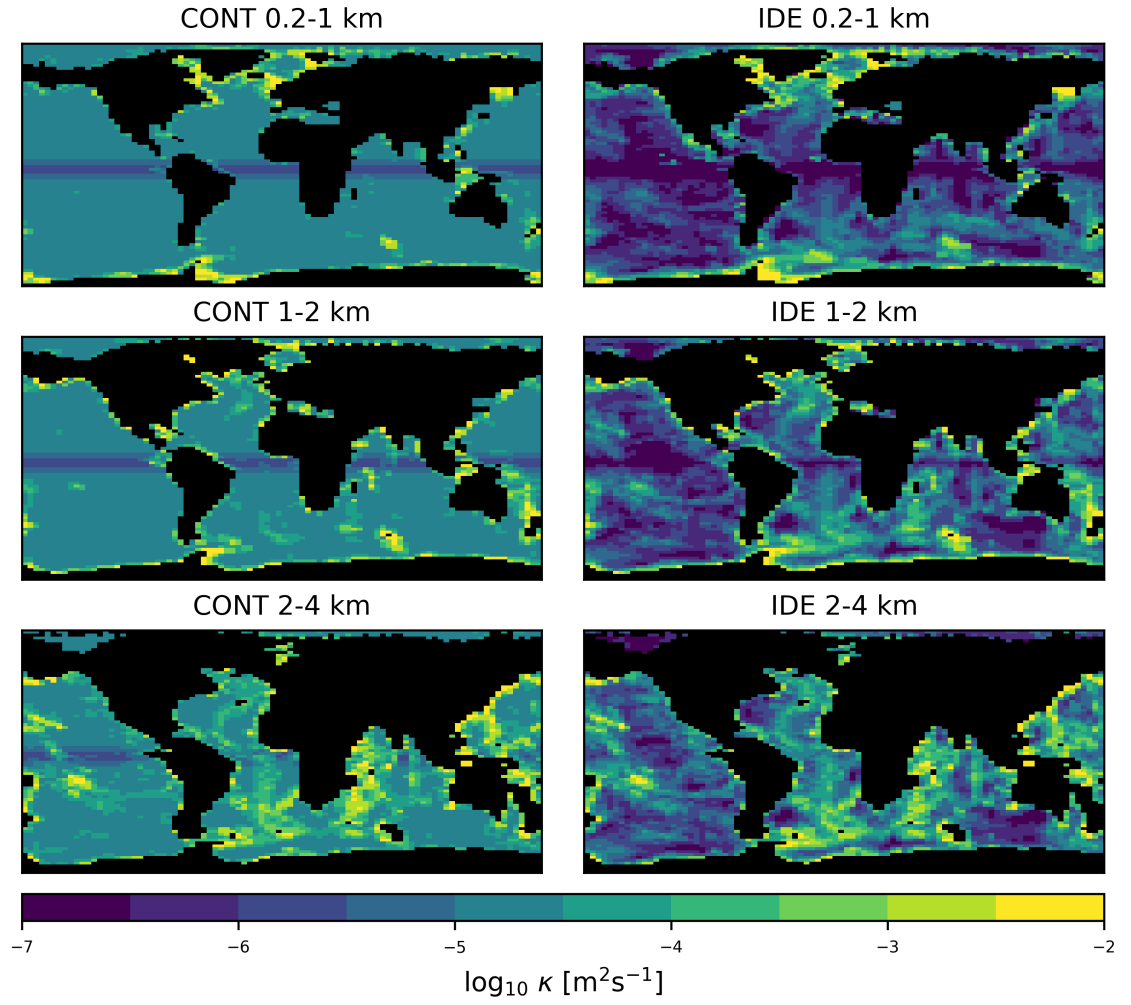


Figure 2: Global map of diffusivities for CONT (left column) and IDE (right column) averaged over 0.2-1 km depth (upper row), 1-2 km depth (middle row) and 2-4 km depth (bottom row).

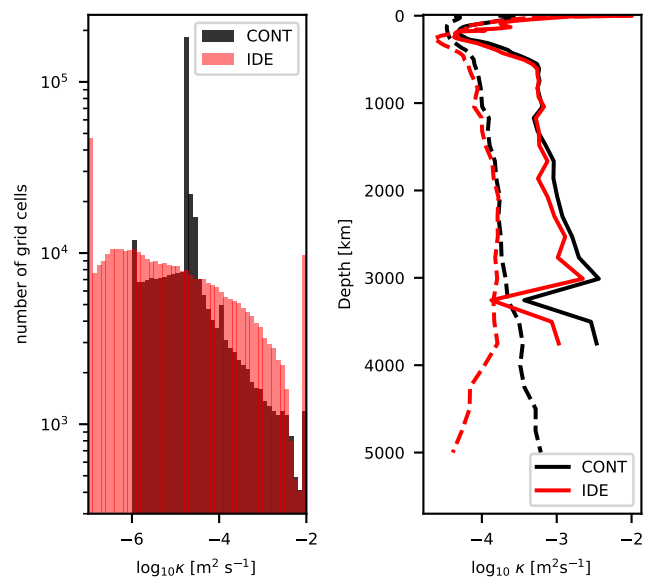


Figure 3: Left: Histogram of diffusivities in CONT (black) and IDE (pink). Red indicates the overlap of the two. Note the logarithmic vertical axis. Right: Globally averaged vertical diffusivity profile for CONT (black) and IDE (red). Solid lines indicate diffusivities over rough topography (slopes larger than 0.01) and dashed indicate smooth topography.

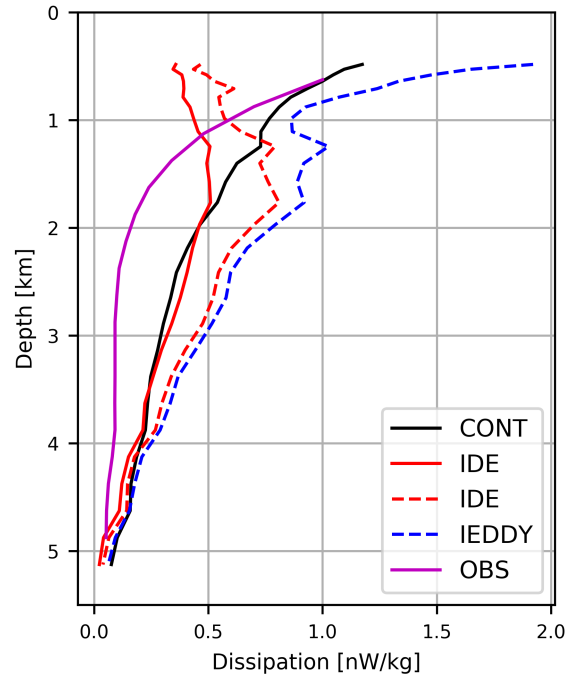


Figure 4: Globally integrated dissipation of energy for CONT (solid black), IDE (solid red) and observations (Kunze, 2017, solid magenta). The red dashed curve represents IDE evaluated using Eq. 4. The dashed blue line represents IEDDY where extra energy forcing is added to Eq. 3, evaluated using Eq. 4.

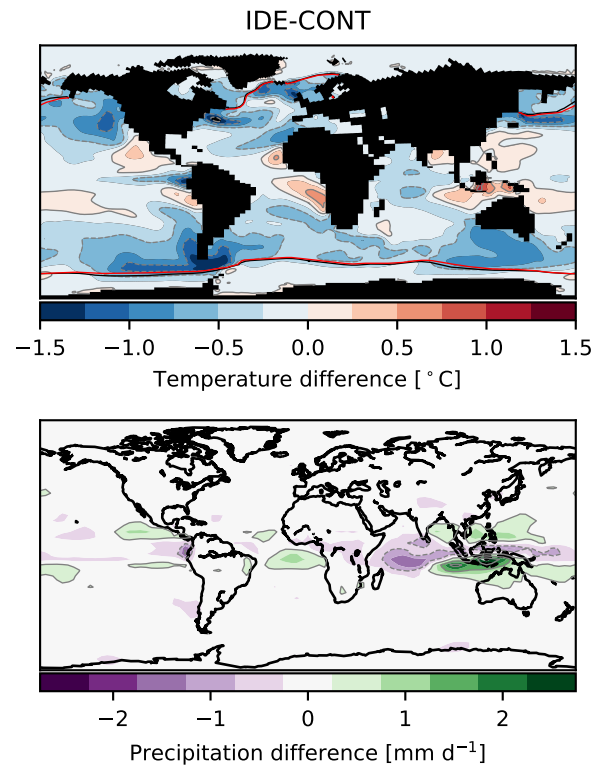


Figure 5: SST (upper) and precipitation (lower) difference between IDE and CONT.



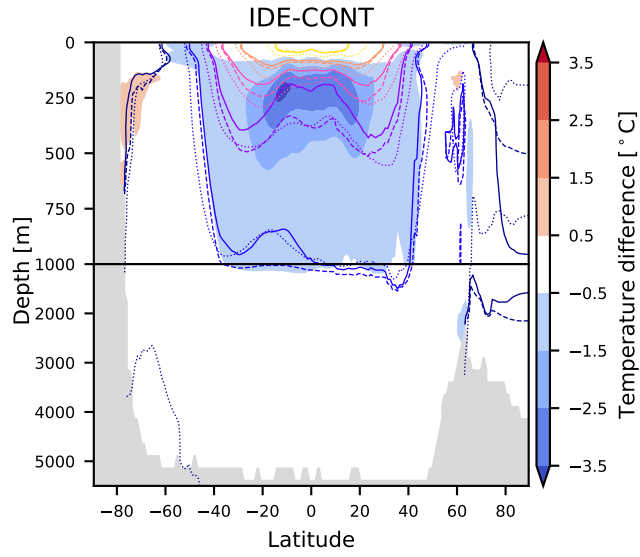


Figure 6: Difference between zonally averaged temperature in IDE and CONT. Overlying contours are zonally averaged potential temperature of CONT (dashed), IDE (full) and WOA (dotted). Contour interval is  $5^{\circ}\text{C}$ , ranging from  $0^{\circ}\text{C}$  (dark blue in polar regions) to  $25^{\circ}\text{C}$  (yellow). Note the non-linear vertical axis at 1000 m.

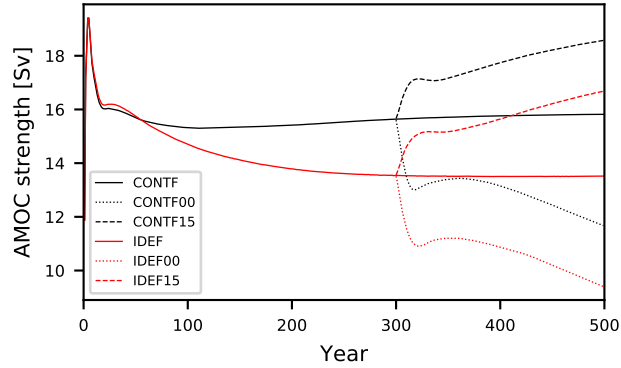


Figure 7: AMOC strength (in Sv) at  $26^{\circ}\text{N}$  in the forced simulations. Wind stress perturbations start at year 300.

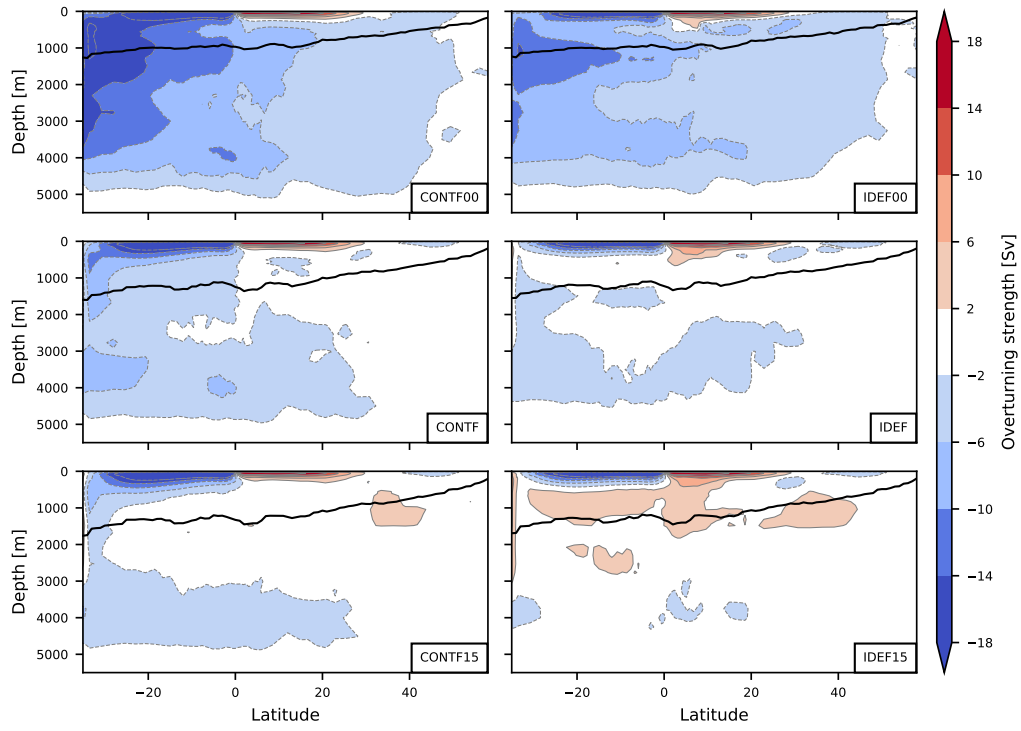


Figure 8: Indo-Pacific overturning stream function for the six forced experiments. Contour interval is 4 Sv. The black line denotes the average depth of the  $\sigma = 27.7$  isopycnal.