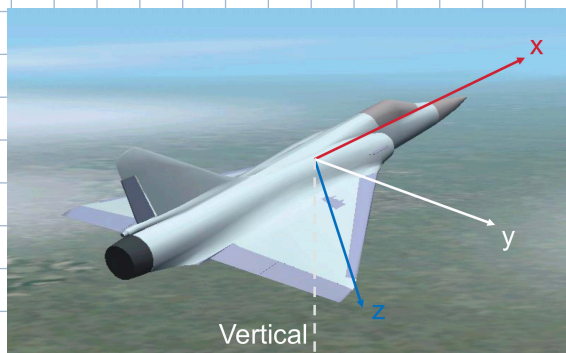
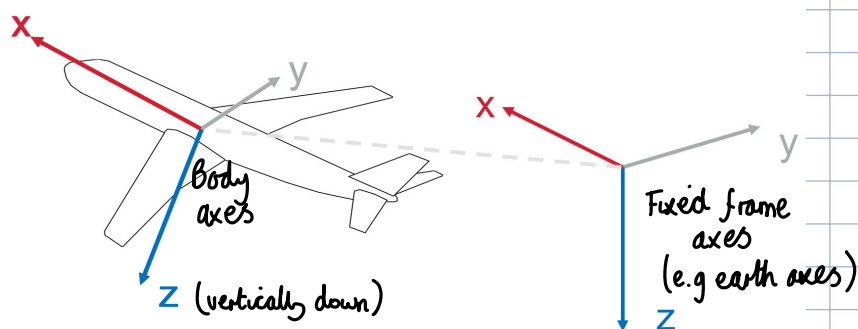


## Body Axes :



Rigid bodies with a distributed mass require a local set of axes attached to the body, with a second set for reference.



Movements of a point mass do not require local set of axes attached to mass.

There are 6 motions of a rigid body - 3 translational, 3 rotational

→ motions are measured relative to reference set of axes → relative motion to where local axes started.

Body axes origin fixed to some easily defined point → CG could be used but may vary throughout flight so not often used

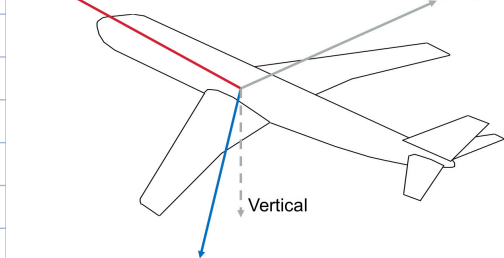
## Body Axes Notation & Sign Conventions :

|        |   |          |   |        |
|--------|---|----------|---|--------|
| $x$    | → | $y$      | → | $z$    |
| roll*  | → | pitch    | → | yaw    |
| $u$    | → | $v$      | → | $w$    |
| $\phi$ | → | $\theta$ | → | $\psi$ |

\*about axis above

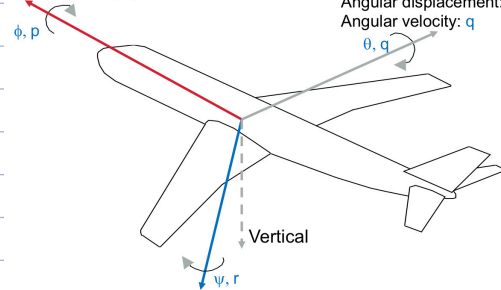
Aircraft velocity:  $U$  (steady) (Note: not  $V$  as you may be used to)  
Aircraft velocity:  $u$  (perturbation)

Aircraft velocity:  $V$  (steady)  
Aircraft velocity:  $v$  (perturbation)



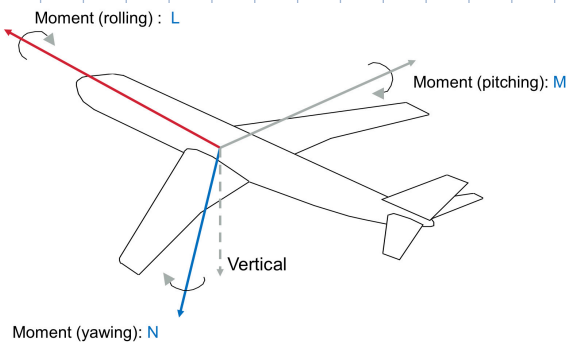
Aircraft velocity:  $W$  (steady)  
Aircraft velocity:  $w$  (perturbation)

Angular displacement:  $\phi$  (roll)  
Angular velocity:  $p$



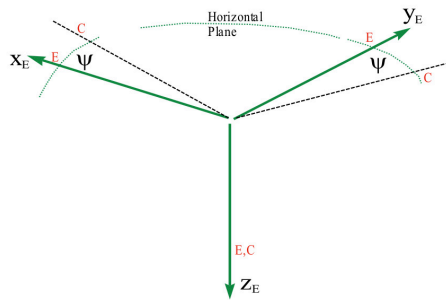
Angular displacement:  $\theta$  (pitch)  
Angular velocity:  $q$

Angular displacement:  $\psi$  (yaw)  
Angular velocity:  $r$

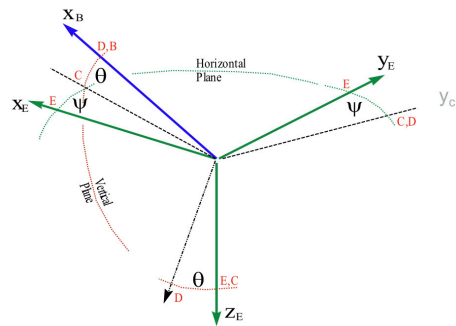


**Euler Angles:** to go from earth axes frame,  $F_E \rightarrow$  body axes frame,  $F_B$   
(via two intermediate frames  $F_C$  &  $F_D$ )

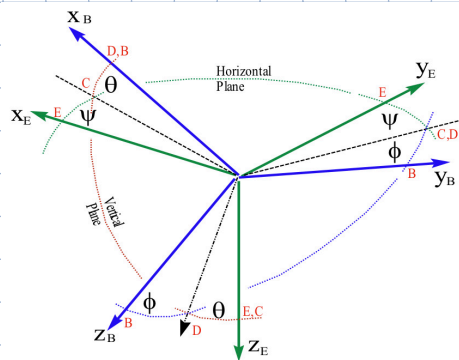
1. Rotation  $\psi$  about  $z_E$  to intermediate frame  $F_C$



2. Rotation  $\theta$  about  $y_C$  to intermediate frame  $F_D$



3. Rotation  $\phi$  about  $x_D$  to body axes frame  $F_B$



## Wind Axes :

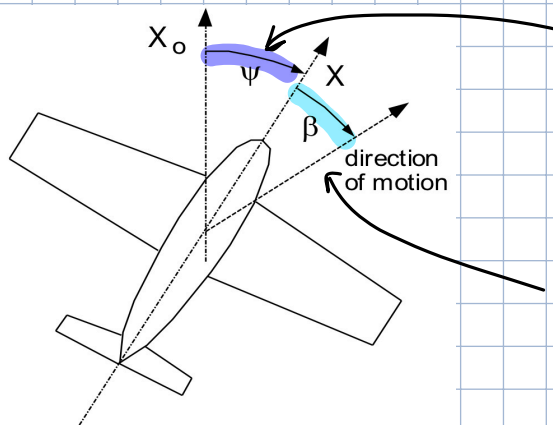
- Orientation of the wind axes usually chosen for convenience of defining aerodynamic forces.
- Origin is fixed at the aircraft reference point
- X-axis points into the wind

## Aerodynamic Incidence Angles : $\alpha$ and $\beta$

- These incidence angles form the basis of aerodynamic forces
- $\psi$  is not included

Sideslip angle

$\psi$  &  $\beta$  are not the same :

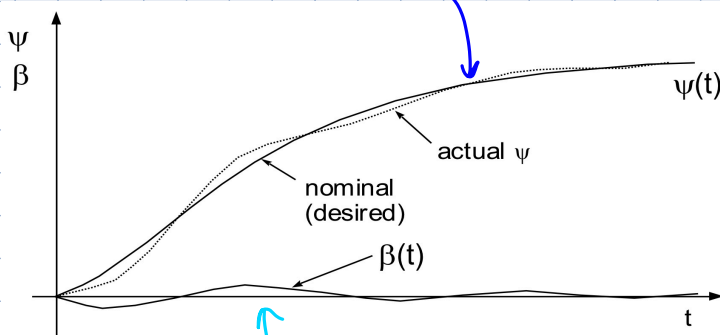


$\psi$  is essentially orientation angle  
→ pointing direction of fuselage reference line compared with previous direction

$\beta$  is difference between direction of motion & pointing direction  
→ 'skidding' to right = +ve sideslip

$\psi$  tends to new steady +ve values

Sideslip incidence  $\beta = \frac{v}{U}$

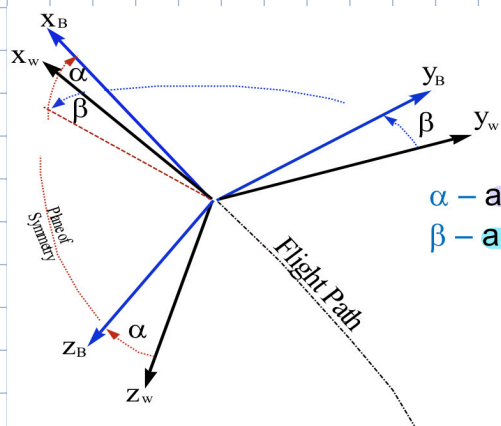


Small yawing oscillations will cause  $\psi(t)$  &  $\beta(t)$  to be quite separate functions

$\beta(t)$  can be  $\approx 0$  throughout

$\beta(t) = 0 =$  coordinated turn

- If atmosphere steady wrt Earth, wind axes are tangent to flight trajectory of aircraft relative to Earth.
- z-wind axis remains in aircraft plane of symmetry although it may tilt forward.
- Only pitch & yaw departures of wind vector are necessary to define wind-induced forces



$\alpha$  - angle of attack  
 $\beta$  - angle of sideslip

angle between  $x_B$  axis and the plane containing the  $y_B$  axis and the velocity vector

angle between velocity vector and plane of symmetry ( $x_B z_B$ )

State Vector : defines where aircraft is & what it's doing

Can use overall resultant velocity,  $V_T$

$$\dot{V}_T = \frac{U\dot{U} + V\dot{V} + W\dot{W}}{V_T}$$

We can also write

$$\dot{\alpha} = \frac{U\dot{W} - W\dot{U}}{U^2 + W^2}$$

and

$$\dot{\beta} = \frac{\dot{V}_T - V\dot{V}_T}{V_T^2 \cos \beta}$$

The state vector is therefore :

$$x^T = [V_T \ \beta \ \alpha \ \phi \ \theta \ \psi \ p \ q \ r \ p_N \ p_E \ h]$$

Stability Axes : (not used in depth on this course)

↳ refer to slides if needed.