

# CSE548/AMS542 Fall 2018 Analysis of Algorithms

Jie Gao\*

September 4, 2018

Due **September 16th** 9pm. Each problem, unless specified otherwise, has a maximum of 10 points. Avoid too many details. A succinct and clean proof is the best. You may use the algorithms we covered in class without referring to the details.

We may select a random subset of the problems to grade.

## Homework 1

1. Textbook [Kleinberg & Tardos] Chapter 2, page 69, problem #8.
2. Textbook [Kleinberg & Tardos] Chapter 3, page 107, problem #4 .
3. Textbook [Kleinberg & Tardos] Chapter 3, page 107, problem #11 .
4. List the following functions in increasing asymptotic order. Between each adjacent functions in your list, indicate whether they are asymptotically equivalent ( $f(n) \in \Theta(g(n))$ ), you may use the notation that  $f(n) \equiv g(n)$  or if one is strictly less than the other ( $f(n) \in o(g(n))$ ) and use the notation that  $f(n) \prec g(n)$ .

$$\begin{array}{ccccc} 5n^3 + \log n & 2^n & 3^{n/2} & 2^{n/3} & \sqrt{\lg n} \\ \ln n & 2^{\sqrt{\lg n}} & \min\{n^2, 1045n\} & \sum_{i=1}^n i^{77} & n^{\ln 4} \\ \lfloor n^2/45 \rfloor & \lceil n^2/45 \rceil & n^2/45 & \lg \sqrt{n} & \lg \lg n \\ \sum_{i=1}^n 1/i & \sum_{i=1}^n 1/i^2 & \sum_{i=1}^n (i^2 + 5i)/(6i^4 + 7) & \ln(n!) & (\lg n)^{\sqrt{\lg n}} \end{array}$$

5. An Euler tour of a graph  $G$  is a closed walk through  $G$  that traverses every edge of  $G$  exactly once.
  - (a) Prove that a connected graph  $G$  has an Euler tour if and only if every vertex has even degree.
  - (b) Describe and analyze an algorithm to compute an Euler tour in a given graph, or correctly report that no such tour exists.
6. Prove that any connected acyclic graph with  $n \geq 2$  vertices have at least two vertices with degree 1. Notice that you should not use any known properties of trees and your proof should follow from the definitions directly.

---

\*Department of Computer Science, Stony Brook University, Stony Brook, NY 11794, USA, [jgao@cs.stonybrook.edu](mailto:jgao@cs.stonybrook.edu).