Collision Avoidance in Swarm Robots using ORCA (Optimal Reciprocal Collision Avoidance)

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***Abstract*— This paper explains our approach of implementation of a global path planner algorithm along with ORCA(Optimal Reciprocal Collision Avoidance) for collision avoidance in Swarm Robots. Swarm robotics is all about controlling a large number of simple robots and in general any algorithm deployed to control these swarm bots are independent of the fact that how many number of robots are active on the platform. Our project is to implement ORCA algorithm for obstacle avoidance along with the use of any commonly available global planner algorithm such as A*. This implementation will take into consideration both dynamic and static obstacles present in the environment.**

Keywords: ORCA, Collision Avoidance, Swarm Robots, Local Planning Algorithm, Dynamic Obstacles

I. INTRODUCTION

Exploration using a robot is a difficult task in itself, whether it may be on a known terrain or an unknown terrain. Known environments can include inside of a building or a warehouse etc. Unknown environments can include a forest area, extraterrestrial planetary surface etc. Exploration becomes much more difficult when there are unidentified obstacles and resources in the unexplored region. The harder part is not to differentiate between an obstacle and a resource, but to get around an obstacle without losing its path and efficiency. The process becomes more involved. when along with static obstacles, dynamic obstacles are also at play. The only difference between exploring a known space from an unknown space is the availability of a map (a known environment with pre-defined constraints). Hence exploring an unknown environment becomes a complex job with all these intertwined involved processes. We mainly want to emulate the exploratory behavior of a swarm, preferably three to four, in an extraterrestrial environment. Exploration obviously includes obstacle avoidance from static obstacles and collision avoidance between the robots. It is assumed that all robots communicate with the server and not with each other, therefore each robot can be assumed to act independently[1]. A simple exploratory algorithm such as ray algorithm or spiral algorithm will be used. As robots can not directly communicate with each other we are using ORCA (Optimal Reciprocal Collision Avoidance) algorithm, which is specially designed for such systems. ORCA uses the concept of velocity obstacles (velocity space), where required conditions for the collision-free motion are derived using linear programming. Basically the problem is reduced into a low-dimensional linear program[1].

II. LOCAL PLANNERS

Local planners focus on updating the robot's trajectory based on the data coming from its sensors. The resulting robot motion is both a function of the robots current or recent sensor readings and its goal position and relative location to the goal position.The obstacle avoidance algorithms being discussed depend on a global map and the robot's current location relative to the that map(not ORCA). Diverse range of obstacle avoidance algorithms are discussed in the following sections.

1) Bug algorithm: This is one of the most simplest local planning algorithms. The idea here is that the robot must follow the contour of an obstacle. There are two types of Bug algorithms namely - Bug1 and Bug2.
In Bug1 the robot encircles the obstacle first, determines the best leave point from the obstacle boundary(one with the minimum distance to goal) and then sets off. Bug1's approach is not efficient but can assure robot will reach any reachable target or goal point.
Bug2 algorithm is an improved version of Bug1 in which the robot encircles the obstacle's boundary but does not do so entirely rather, departs immediately when it has a clear way towards the goal.

2) Vector Field Histogram: Borenstein together with Koren developed the Vector Field Histogram (VFH)[5].
The drawbacks of Bug algorithm is that it's output relied on the recent sensor's readings. This is an issue as in some cases the robot's latest sensor readings were not sufficient for performing obstacle avoidance. The VFH overcomes this issue by creating a local map. It uses the concept of occupancy grids that contain relatively recent sensor readings.
For performing obstacle avoidance it creates a polar histogram. The x-axis of which represents the angle at which the obstacle was found and the y-axis represents the probabilities that the obstacle was actually there based on the occupancy grid's values. Using the histogram the steering direction is determined. All the free spaces large enough for the robot to pass through are identified and then a cost is assigned to each of those. Ultimately the free passage with the lowest cost is chosen.

3) Probabilistic Velocity Obstacle(PVO) and Occupancy Grids: This approach consists of reactive obstacle avoidance in dynamic uncertain environment. The algorithm factors in the uncertainty generated due to noise coming from sensors as well as from an erroneous description of a model of the environment[8].
The algorithm relies on occupancy grids that are extremely sensitive to changes in the surroundings of the robot.
The algorithm works in the velocity space by computing the probabilities to collision. Kinematic and dynamic constraints are also considered and they help in determining the reach-

able velocities.
Based on the time to collision a navigation algorithm is constructed and control inputs are chosen accordingly that are considered to steer the robot in a safe direction within the current interval of time.

4) ORCA: ORCA stands for Optimal Reciprocal Collision Avoidance that as the name suggests finds the best or optimal velocity for a swarm of robots placed in a cluttered environment. It avoids obstacles easily and can be scaled to any number of robots in a swarm[1].
The algorithm works by creating certain admissible velocities for each robot called Collision Avoidance velocities which as their name suggests ensures the robot does not collide with other moving robots/obstacles. These velocities are computed for one robot relative to the approaching robot/obstacle. Each robot has its velocity space that tells it which velocities to take for a time t such that it(and the approaching robot) stay collision free for that period.
It can avoid both static and dynamic obstacles. It is perfect for decentralized swarms as the robots do not need to communicate with each other and thus inter-communication issues and the associated complexities are avoided. It provides a sufficient condition for multiple robots to avoid collisions among one another, and thus can guarantee collision-free navigation for many robots in a cluttered workspace. It achieves convincing motions that are smooth and collision-free. It takes care of the common problem among other obstacle avoidance algorithms called asteroid avoidance which deals with avoiding obstacles that have comparable or greater velocities than the robot.

III. ASSUMPTIONS

- It is assumed that all robots communicate with the server and not with each other, therefore each robot can be assumed to act independently.
- We assume that the robots move in plane R^2 .
- All the robots are circular in shape.
- The Robots are holonomic, i.e., they can move in any direction.
- Preferable velocity for all the robots is

$$V_{robot}^{pref} = V_{robot}^{max}$$

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- Sensing and Perception is one of the most important part of ORCA, as robots observe the position and velocity of other robots. Hence the sensor data is assumed to be robust and noiseless.
- Robots are able to accurately observe each others current position and velocity (which are external parameters) done through sensing and perception.

IV. METHOD

A. Pseudo Code

```
input list of robots (LR), t: time step
loop
    for all A in LR do
        get position and velocity of A
        compute "n" nearest neighbors "NN" in LR for each A
        for all B in NN do
            get position and velocity for B
            construct the velocity obstacle VO_A|B
            construct ORCA_A|B
        end for
        construct ORCA_A from the intersection of all ORCA_A|B
        compute preferred velocity for A
        compute new velocity for A in ORCA_A that is closest to the preferred
        velocity using 2D linear programming
        if 2D linear programming is infeasible then
            print "solution infeasible"
        end if
    end for
    for all A in LR do
        set velocity to new velocity for A and position to old position + t*new
    velocity
    end for
end loop
```

The basic approach is as follows -
Each robot A will continuously sense and act with a time step dt. With each iteration the robot A will obtain the radius, current position and optimization velocity of other robots(nearest neighboring ones). The robot A then infers the permitted velocities $ORCA_{A|B}$. The set of all permitted velocities of A with respect to all other neighbor robots is obtained from the intersection of half-plane of permitted velocities. This is given by the following equation -

$$ORCA_A^\tau = D(0, v_A^{max}) \bigcap \bigcap_{B \neq A} ORCA_{A|B}^\tau$$

The new velocity of A is then chosen based on the how close it is to the preferred velocity. This relationship can be shown by the following optimization equation -

$$v_A^{new} = min||v - v_A^{pref}||$$

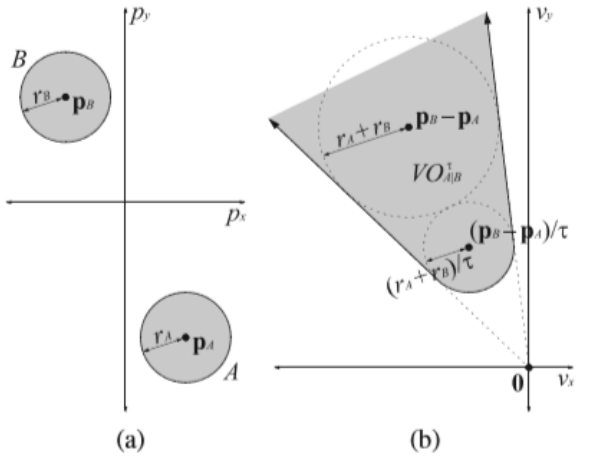
The velocity v_A^{new} is found via 2D linear programming. If a solution is not found then an error is reported. This velocity is then updated as the current velocity of the robot and correspondingly the current position is updated as well. The cycle then simply repeats.

B. Theoritical Explanation

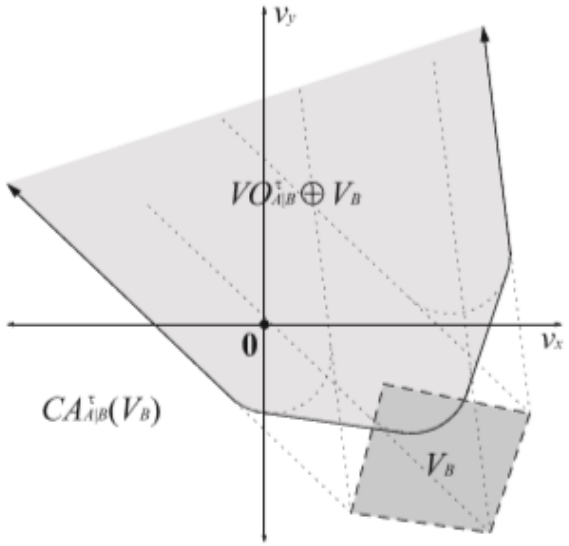
- In order to show decentralized/decoupled swarm behaviour, we will take 4-6 robots working independently towards their goal. Decentralized swarm means that each robot though working in collaboration, works

independently towards its goal. There is no chain of command, robot receives no information about the position and velocity of the other robot, and decides its position and velocity independently unlike centralized swarms.

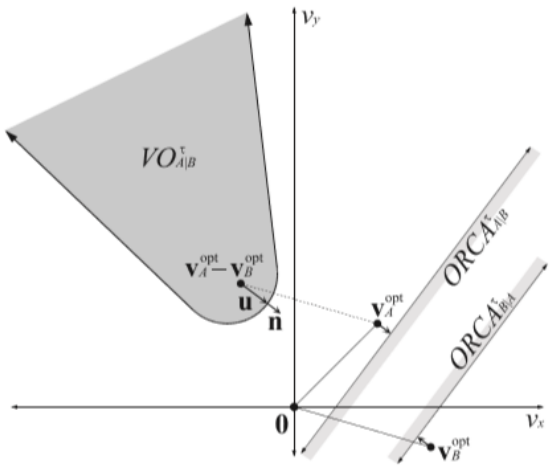
- All robots are put on a collision course by giving them a colliding path generated through A*.
- Determine and plot the velocity obstacle for each robot with respect to the other robot in the velocity space.



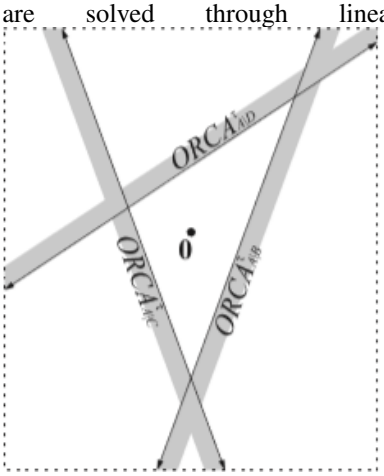
- In the above figures[1] (a) is the configuration of two robots A and B. (b) is the The velocity obstacle $VO^{\tau}_{A|B}$ (gray) which can geometrically interpreted as a truncated cone with its apex at the origin (in velocity space) and its legs tangent to the disc of radius $r_A + r_B$ centered at $p_B - p_A$. The amount of truncation depends on the value of τ , the cone is truncated by an arc of a disc of radius $(r_A + r_B)/\tau$ centered at $(p_B - p_A)/\tau$[1].
- This velocity obstacle $VO^{\tau}_{A|B}$ is the velocity obstacle of A induced by B. Similarly there will be a velocity obstacle $VO^{\tau}_{B|A}$ of B induced by A. The velocity obstacles $VO^{\tau}_{A|B}$ and $VO^{\tau}_{B|A}$ will be symmetric about origin[1].
- Then the Minkowski sum of each robot velocity obstacle is found with each other robot[1].



- The above figure is the Minkowski sum (light gray) of $VO^{\tau}_{A|B}$ and V_B (selected robot B velocity). The set of collision-avoiding $CA^{\tau}_{A|B}(V_B)$ is the complement of the Minkowski sum[1].
- if $v_A - v_B \in VO^{\tau}_{A|B}$, or equivalently if $v_B - v_A \in VO^{\tau}_{B|A}$, then A and B will collide at some moment before time τ if they continue moving at their current velocity. Conversely, if$v_A - v_B \notin VO^{\tau}_{A|B}$, robot A and B are guaranteed to be collision-free for at least τ time[1].
- Hence $CA^{\tau}_{A|B}(V_B)$ and $CB^{\tau}_{B|A}(V_A)$ are the collision avoided velocity of A induced by B and B induced by A respectively.
- Hence the pair V_A and V_B of velocities for A and B are called reciprocally collision avoiding if $V_A \subseteq CA^{\tau}_{A|B}(V_B)$ and $V_B \subseteq CB^{\tau}_{B|A}(V_A)$. If $V_A = CA^{\tau}_{A|B}(V_B)$ and $V_B = CB^{\tau}_{B|A}(V_A)$, we call V_A and V_B reciprocally maximal[1].
- There are infinitely many pairs of sets V_A and V_B that obey these requirements, but among those we select the pair that maximizes the amount of permitted velocities close to optimization velocities v^{opt}_A for A and v^{opt}_B for B. We denote these velocities sets as $ORCA^{\tau}_{A|B}$ for A and $ORCA^{\tau}_{B|A}$ for B[1].
- Derive and plot the half planes equation for optimum velocities such as $ORCA^{\tau}_{A|B}$ and $ORCA^{\tau}_{B|A}$.



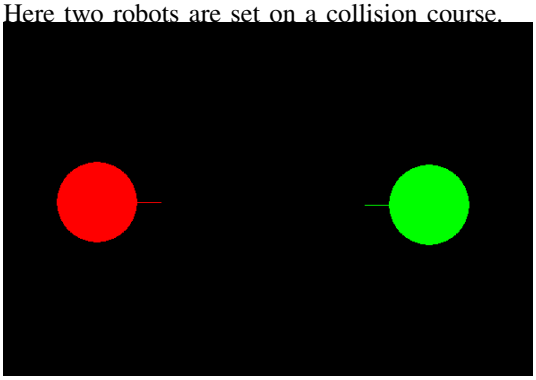
- The above figure[1] shows the half plane plots for $ORCA^{\tau}_{A|B}$ for A and $ORCA^{\tau}_{B|A}$ for B.
- All the corresponding half-plane equations are solved through linear programming.



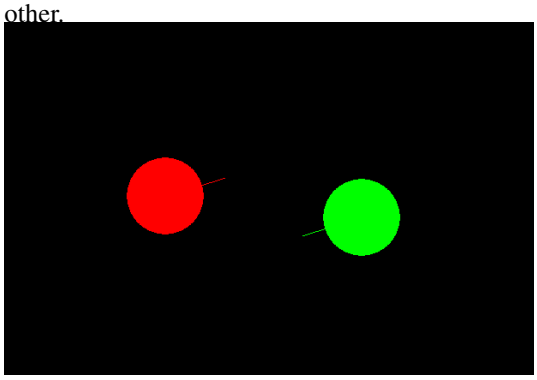
- The above steps are repeated until the robots reach each of their goal destination.

V. RESULT

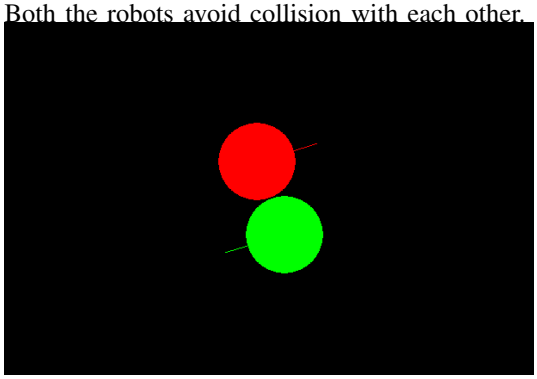
- The ORCA was implemented for a cluster of 2 and 4 robots separately, the outputs of which have been shown as follows in a sequential manner. The pictures represent the swarm robots initially at rest, moving towards each other, about to collide with each other, avoiding collision and lastly moving away from one another.
- Here two robots are set on a collision course.



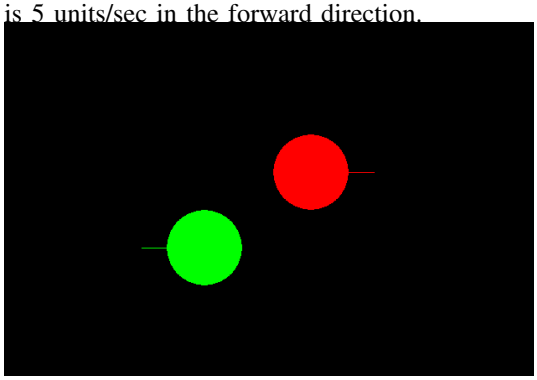
- We can see that the two robot turns, one in left direction and one in right direction when they comes close to each other.



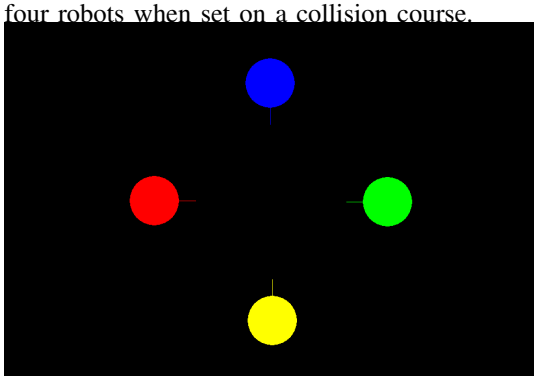
- Both the robots avoid collision with each other.



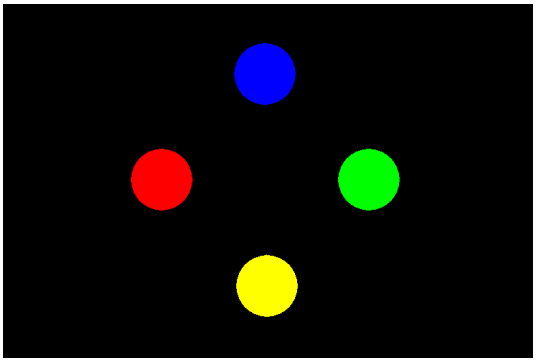
- Both robots now move with their preferred velocity once the collision is avoided. Preferred velocity of each robot is 5 units/sec in the forward direction.



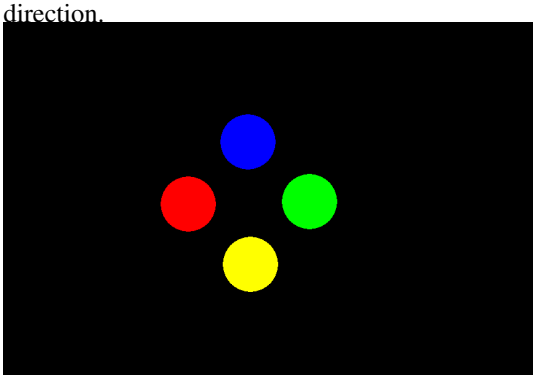
- Here, in the below image OCRA is implemented on four robots when set on a collision course.



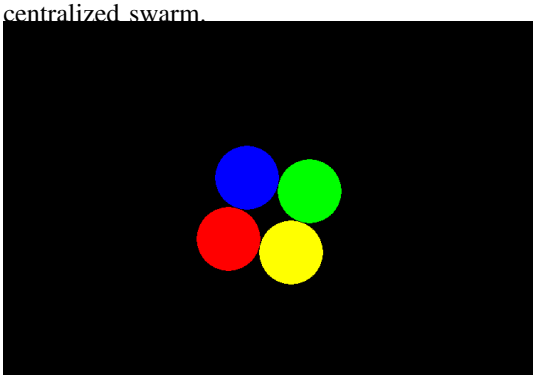
- Robots approach each other from four different directions



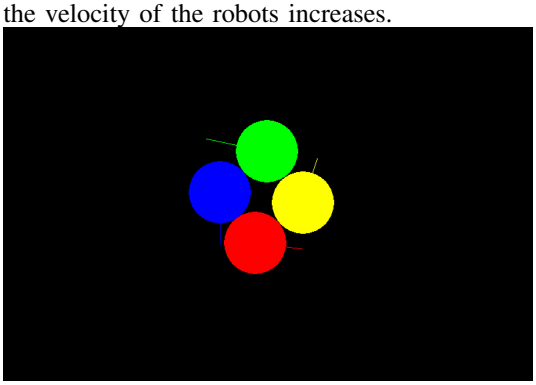
- In the subsequent image we can see that the velocity vector is not visible as it very close to zero, in both x,y direction.



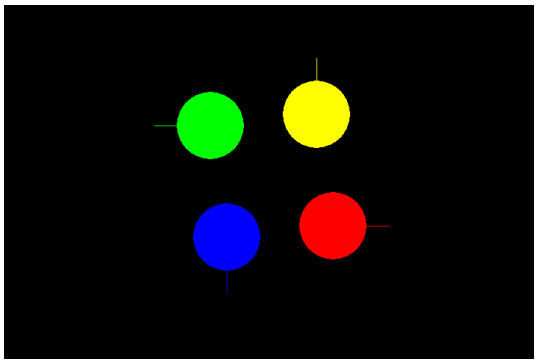
- Robots stop and start rotating in anti-clockwise direction. This kind of behaviour is interesting as a decentralized swarm shows a behaviour similar to a centralized swarm.



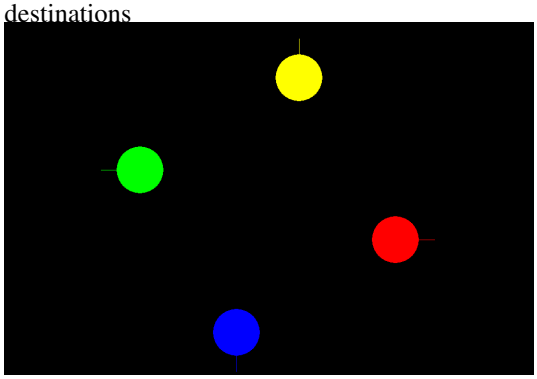
- Robots rotates more in anti-clockwise direction and now we can see that the velocity vector of three robots i.e. the velocity of the robots increases.



- Each robot now moves with their preferred velocity, 5 units/sec in forward direction.



- Collision is avoided and robots reach their respective destinations



VI. Conculsion and Future Scope

To summarize, we have implemented a local planning algorithm called ORCA in order to perform obstacle avoidance in a swarm of robots (3-4). The proposed work can be used for solving real-world problems such as search and rescue, extraterrestrial exploration missions etc where these robots would be left in an unexplored region to gather useful data and report to a remotely situated human controller.
Now that we have implemented a local planning algorithm like ORCA for a swarm of robots, the next step would be to integrate it with a global planning algorithm like A-star to completely define a path planner for the swarm robots. Currently our implementation uses simple robot shapes like circle or discs, the algorithm could be extended to include various types of robot shapes/sizes. In future we could scale this approach to account for robots kinematics and dynamics, and also combine path planning in both velocity space and Cartesian space. Lastly, the current implementation only accounts for 2-D environments. In future this approach could be extended to 3-D.

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