

SN1a, solutions

3.

©tidal accelerations on the surface of the red giant (radius r_1 , mass m_1) by the white dwarf (r_2, m_2) in distance d :

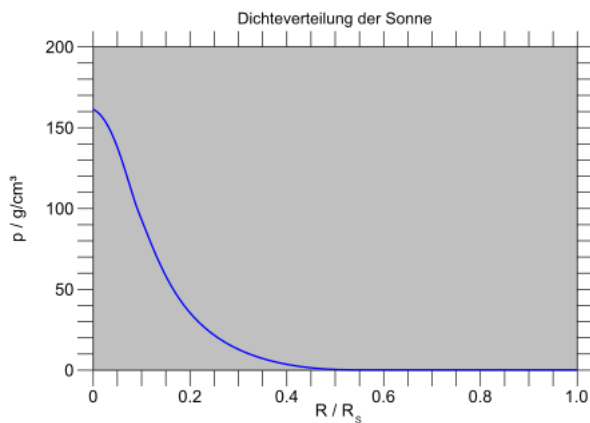
$$\text{!} \quad da = g \cdot m_2 \left(\frac{1}{(d-r_1)^2} - \frac{1}{(d+r_1)^2} \right) \quad da = m_2 \left(\frac{1}{(d-r_1)^2} - \frac{1}{(d+r_1)^2} \right) \cdot g$$

$$da = \frac{4 \cdot g \cdot m_2}{d^3} \cdot r_1 \quad da = \frac{4 \cdot g \cdot m_2 \cdot r_1}{d^3}$$

©when da is greater than the surface-acceleration of the red giant it bursts:

$$\text{solve} \left(da = \frac{g \cdot m_1}{r_1^2}, d \right) \quad d = \frac{m_2^{\frac{1}{3}} \cdot r_1 \cdot 2^{\frac{2}{3}}}{m_1^{\frac{1}{3}}}$$

4.



$$\int_0^r (4 \cdot \pi \cdot \rho_0 \cdot x^2) dx \quad \frac{4 \cdot \rho_0 \cdot \pi \cdot r^3}{3}$$

©for the sun is $a \sim 9$ and at sunradius r ρ_0 is about 0, therefore you can integrate at ∞ .

$$\text{©} \quad \int_0^\infty \left(4 \cdot \pi \cdot \rho_0 \cdot e^{\frac{-a}{r} \cdot x} \cdot x^2 \right) dx = 4 \pi \cdot \rho_0 \cdot \left(\frac{r}{a} \right)^3 \int_0^\infty (e^{-x} \cdot x^2) dx = 8 \frac{\pi \cdot \rho_0}{a^3} \cdot r^3$$

5. Number N of Electrons is equal to the number of Protons, $m_e \cdot N = m$ is the mass of the star.

Therefore, every electron has the space $dr^3 = V/N = V \cdot m_e / m = m_e / \rho_0$ with proton mass m_p . The Fermi-Energy is:

$$dE = \hbar^2 / (8\pi^2 \cdot m \cdot dr^2) = \hbar^2 / (8\pi^2 \cdot m_e \cdot dr^2) = \hbar^2 / (8\pi^2 \cdot m_e) \cdot (\rho_0 / m_e)^{2/3}$$

and if it is much greater than the thermal Energy the gas is „entartet“.

From gas-theory we know $p = n \cdot k_B \cdot T$ with particle density $n = N/V$ and Boltzmann constant, and the thermal Energy is $E = 1.5 \cdot k_B \cdot T$. Then $p = 2/3 \cdot n \cdot E$ and we suppose it is valid for Fermi-Energy, too.

Then follows the estimated equation.

$$p(h) = \int_0^h (\rho \cdot g(r-x)) dx \text{ with } g(x) = \frac{g \cdot m(r)}{r^2} \text{ gives for the pressure at the center}$$

$$p = \frac{3 \cdot g \cdot m^2}{8 \cdot \pi \cdot r^4}$$

Compare with the „Entartung“ pressure you get the law

$r \sim m^{-(1/3)}$

If the Star gets more mass it shrinks.