goal: compare & combine optimal controller and estimator for linear systems with Gaussian noise

ref: Sterge/ Ch 5.3

duality - i.e. comparison of LQ controller & KF estimator

consider $X_{SH} = A_S X_S + B_S U_S + S_S = \mathbb{E}[S_S] = 0$, $Cov[S_S] = \mathbb{Q}_S$ $Y_S = C_S X_S + Y_S = \mathbb{E}[Y_S] = 0$, $Cov[Y_S] = \mathbb{E}[Y_S] = \mathbb$

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$$P_{S} = (A_{S} - B_{S}K_{S})^{T}R_{S1}(A_{S} - R_{S}K_{S})$$

$$+ C_{S}^{T}R_{S}K_{S} + G_{S}$$

$$+ C_{S}^{T}R_{S}K_{S} + G_{S}^{T}K_{S} + G_{S}^{T}K_{S}^{T$$

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minimizes $E\left[\underset{s=0}{\overset{t}{\sum}} \times_{\xi} C_{\xi} \times_{\xi} + u_{\xi}^{T} R_{s} u_{s}\right]$ where expectation is taken with respect to $\{s_{s}\}, \{y_{s}\}$ — terms "separation poinciple" in stochastic optimal cantol (or "certainty equivalence")