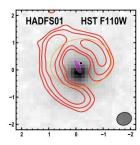
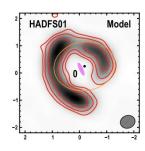
# Ranking Ultimate Frisbee Teams

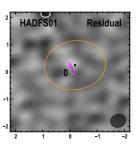
Insight Bayesian Workshop

#### **About Me**

- Senior Data Scientist at CiBO Technologies since December 2017
- Lead Data Scientist at Understory Weather, 2015 2017
- Health Data Science Fellow, Boston, Summer 2015
- Academic history
  - o PhD Astronomy, 2010, University of Arizona
  - Postdoc at Harvard-Smithsonian CfA, 2010 2013
  - o Postdoc at Cornell, 2013 2015









Understory



Astronomy

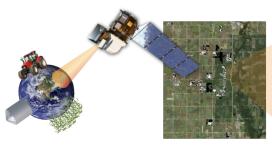
CiBO Technologies is

Planetary-Scale

# Agricultural

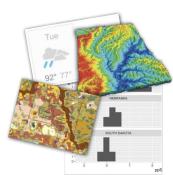


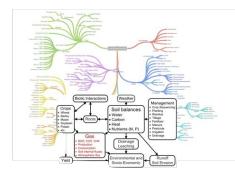
Simulation Optimization











Planetary Scale, Daily Simulations

Sub-field resolution utilizing on-farm and remote sensing

Multi-country, Multi-crop

Thousands of
Variables
&
Millions of data points
per field

Rich Domain Model with Hundreds of Interactions and Outputs

## **Goal of This Workshop**

Walk through a real-world example to show how Bayesian analysis leads to better results!

#### The Problem

- BUDA (Boston Ultimate Disc Alliance) runs recreational ultimate frisbee leagues in the greater
   Boston area
- We have been asked to rank teams for the end-of-season tournament
- Teams self-assign to one of three divisions
  - Div 1 == highest
  - o Div 3 == lowest
- Teams responsible for creating their own schedule
  - Some teams play lots of games, others not so much
  - Some teams play "out of division" games (e.g., Div 1 vs. Div 2)



## Ranking Teams: Win Percentage

- Sort by Win Percentage
- No consideration of number of games
- No consideration of strength of schedule
- Is "Too Drunk to Fail" really a top 5 team?
- Who would win if "AHOC" played "SnakeCountryBromance"?

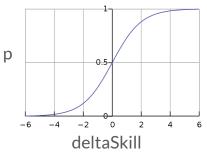
	Division	Wins	Losses	Win Percentage	
Team Name					
AHOC	Div 1	14	0	1.000000	
SnakeCountryBromance	Div 1	5	0	1.000000	
Injustice League	Div 2	14	1	0.933333	
Pink Flamingos	Div 2	10	1	0.909091	
Too Drunk to Fail	Div 3	11	2	0.846154	
Jack's Abby HAOS Lager	Div 2	10	2	0.833333	
Maverick	Div 2	9	2	0.818182	
JuJu Hex	Div 2	11	3	0.785714	
Upstream	Div 2	20	6	0.769231	
Gothrilla	Div 1	12	4	0.750000	



# Ranking Teams: A Bayesian Framework

- Suppose each team has an inherent true skill level, denoted as "skill"
- Consider two teams, Team A and Team B, with skill levels denoted as skillA and skillB, respectively
- In our model, what matters is the difference in skill levels, delta\_skill: delta\_skill = skillA skillB
- We use the logit function to convert deltaSkill to p, the probability that Team A beats Team B

$$p = 1 / (1 + exp(-delta_skill))$$

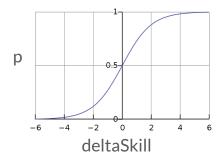




#### A Bayesian Framework: An Example

- Example
  - o skillA = 4.0, skillB = 2.0
  - o delta\_skill = 2.0
  - $\circ$  p = 1 / (1 + exp(-delta\_skill) = 1 / (1 + exp(-2)) = 88.1%

=> We expect Team A to beat Team B 88.1% of the time





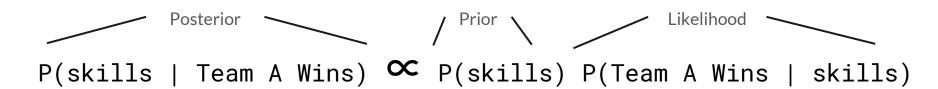
## A Bayesian Framework: The Data

- An ultimate frisbee league has N teams and M game outcomes
- We will use 2016 Boston Ultimate Disc Alliance summer league data with N=67 and M=522
- skills is a vector of length N containing skill for each team in the league
- Each game outcome is binary (i.e., ignore ties) and is denoted "Team A Wins"
- We relate p to the observed outcomes using the Bernoulli distribution

Team A	Team B	Team A Wins	Div A	Div B
AHOC	Tubbs	True	Div 1	Div 2
AHOC	Lady and the BAMF	True	Div 1	Div 2
AHOC	Live Poultry, Fresh Killed (LPFK)	True	Div 1	Div 1
AHOC	BBN	True	Div 1	Div 1
AHOC	JuJu Hex	True	Div 1	Div 2
AHOC	Turtle Boy	True	Div 1	Div 1
AHOC	Upstream	True	Div 1	Div 2
AHOC	TuneSquad	True	Div 1	Div 1
AHOC	Swingers	True	Div 1	Div 1
AHOC	Stonecutters	True	Div 1	Div 1
AHOC	Stonecutters	True	Div 1	Div 1
AHOC	FlowChart	True	Div 1	Div 1
AHOC	Gothrilla	True	Div 1	Div 1
AHOC	Zerg Rush!	True	Div 1	Div 1

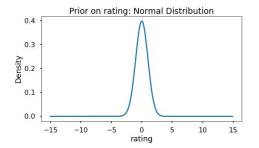


# **Bayes Rule**



#### **Priors**

- To start out, let's assume we know nothing about each team's skill before any games have been played
- Every team is "average"
  - Normal distribution
  - $\circ$  Mean = 0
  - Standard deviation = 1



#### In PyMC3:

- The keyword shape means we will get a vector of skills, one for each team in the dataframe.
- n\_teams is the number of teams in the database

#### **Building delta\_skill**

- We need delta\_skill for every row in the dataframe (i.e., for every game in the season)
- Key insight: we can index skills just like a normal python list
- Plan: assign a number to each team and use that number to index skills

Team A	Team B	Team A Wins	Index A	Index B
AHOC	Gothrilla	True	0	1
AHOC	BBN	True	0	9
AHOC	Stonecutters	True	0	41
AHOC	FlowChart	True	0	2
AHOC	Lady and the BAMF	True	0	28

#### In PyMC3:

#### Calculating p

- p = sigmoid(delta\_skill)
- sigmoid =  $1/(1 + \exp(-x))$

#### In PyMC3:

```
with pm.model() as model:
    skills = pm.Normal(
        'skills', mu=0, sd=1, shape=n_teams)

delta_skill = skills[indexA] - skills[indexB]

p = 1 / (1 + np.exp(-delta_skill))

win = pm.Bernoulli('win', p,
```

observed=team\_A\_wins)

#### **Likelihood Distribution**

- P(Team A Wins | skills) means "What is the likelihood that team A won, given the skill differential between team A and B and our function that converts that differential to the probability that A wins"?
- Team A Wins is a binary outcome
- We use the Bernoulli distribution to model our likelihood. This distribution links a probability to a binary outcome.

Bernoulli Distribution:

http://docs.pymc.io/api/distributions/discrete.html#pymc3.distributions.discrete.Bernoulli

#### In PyMC3:

That's it! We've specified our model. Now we can sample and get the posterior. Let's go to a notebook to see what happens!

#### Let's test it!

First, we'll look at a Jupyter notebook for an example of a simulated season with only 3 teams of known rating.

#### Conclusion

- We looked at different approaches to ranking teams in BUDA ultimate frisbee leagues
- Heuristic approaches are kind of sort of ok, but suffer from problems:
  - subjective
  - o offer no clear path to validation
  - o can't be extended in interesting ways
- In contrast, our Bayesian approach is quantitative, offers direct validation, and can be extended in really interesting ways (e.g., what is the likelihood of AHOC beating SnakeCountryBromance?)
- We looked at two different priors and showed that they have a significant impact on the results
  - This is ok because we stated at the outset very clearly what our priors were

#### **Next steps**

- Ideas
  - Simulate the end-of-season tournament
  - Use accuracy, logloss, or some other metric to optimize the model (watch out for overfitting!)
  - Use data from previous years:
    - to specify prior for this year
    - to implement cross-validation
  - o Incorporate goals-for and goals-against into analysis (Binomial distribution)
- Game scores (for all seasons through 2016) and jupyter notebooks are available
- I'm very interested to see what you come up with!
  - sbussmann@cibotechnologies.com
- CiBO is hosting a Stan meetup on July 24. Please sign up and attend if you have an interest in learning Stan (note: Stan is a probabilistic programming language similar to PyMC3)!

#### Resources

- http://camdavidsonpilon.github.io/Probabilistic-Programming-and-Bayesian-Methods-for-Hacker
   s/
- PyMC3: <a href="http://docs.pymc.io/#learn-bayesian-statistics-with-a-book-together-with-pymc3">http://docs.pymc.io/#learn-bayesian-statistics-with-a-book-together-with-pymc3</a>
- PyMC3 discussion forum (very active, helpful userbase): <a href="https://discourse.pymc.io/">https://discourse.pymc.io/</a>