

The Place of the Local Group in the Cosmic Web

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The influence of cosmological environment on the properties of large-scale structures has been extensively discussed in previous works, following this direction we aim to determinate a possible influence on the kinematic properties of our Local Group of Galaxies. We use the Bolshoi simulation in the current time (z=0), with a comovil volume of 256 Mpc³h³ and a BDM catalog of dark matter halos and subhalos systems. Quantification of the environment is made using the velocity tensor scheme (Vweb) and the potential tensor scheme (Tweb). We detect LG like systems using gravitational isolations criteria and imposing observational constrains in the halos pair systems. To build a more faithful sample of LG systems we detect large-scale void regions using a FOF scheme and select a subsample of LG systems near to those void regions. Finally we calculate the kinematic properties of each sample to determinate correlations with their environment selection criteria. We find a significative bias in the radial velocity and the specific energy of LG systems, whereas the specific angular momentum and the tangential velocity don't seem to have important bias.

Motivation

The coagulation-fragmentation equations describe the evolution of a large number of clusters which can stick together or break. Here we deal with the discrete version.

$$c_j \equiv \text{number density of}$$

clusters of size j

$$b_{jk} \equiv$$
 rate of occurrence of $a_{jk} \equiv$ rate of occurrence of reaction $j + k \rightarrow j, k$ reaction $j \rightarrow j + k$

$$\frac{d}{dt}c_{j} = \frac{1}{2} \sum_{k=1}^{j-1} a_{k,j-k} c_{k} c_{j-k} \qquad \text{Coagulation gain}$$

$$-\sum_{k=1}^{\infty} a_{jk} c_{j} c_{k} \qquad \text{Coagulation loss}$$

$$+\sum_{k=j+1}^{\infty} b_{j,k-j} c_{k} \qquad \text{Fragmentation gain}$$

$$-\frac{1}{2} \sum_{k=1}^{j-1} b_{k,j-k} c_{j} \qquad \text{Fragmentation loss}$$

The generalized Becker-Döring system is the special case where a_{jk} and b_{jk} are zero whenever $\min\{j,k\} > N$ for some N. For N=1 the system is the Becker-Döring system.

Asymptotic Behavior

The study of the long-time behavior of solutions to these equations is expected to be a model of physical processes such as phase transition. Under certain general conditions which include a detailed balance we can ensure the existence of equilibrium states. In these conditions, there is a critical mass $\rho_s \in]0, \infty[$ such that any solution that initially has mass $\rho_0 \leq \rho_s$ will converge for large times, in a certain

strong sense, to an equilibrium solution with mass ρ_0 . On the other hand, any solution with mass above ρ_s converges (in a weak sense) to the only equilibrium with mass ρ_s ; this weak convergence can then be interpreted as a phase transition in the physical process modelled by the equation.

Convergence in this weak sense means that a fixed part of the total mass of particles is found to be forming larger and larger clusters as time passes and the mean size of clusters goes to infinity. The physical interpretation of this, depending on the context, can be a change of phase or the apparition of crystals, for example.

Below critical mass
$$\rightarrow$$
 { Trend to equilibrium Strong convergence}

Over critical mass \rightarrow { Large clusters created Weak convergence}

Previous results

Becker-Döring	Ball, Carr, Penrose
system	[1, 2] (1986-88)
Generalized Becker-Döring	Carr, da Costa
(rapidly decaying initial data)	[4] (1994)
Generalized Becker-Döring	da Costa
(small initial data)	[5] (1998)

Sketch of the proof

Our proof is a generalization of a method used in unpublished notes by Ph. Laurençot and S. Mischler [6], inspired by the proof of uniqueness of solutions to the Becker-Döring equation in [7].

It is known that, under common assumptions, there is always at least weak convergence to a certain equilibrium state; the problem reduces to show that for an initial density under the critical one solutions converge strongly to the equilibrium with the same density. To prove this, it is enough to show that the tails of the solutions are small enough, so that strong convergence holds. The following estimate, roughly stated here, is the key of our proof:

Main estimate

If $c = \{c_j\}_{j\geq 1}$ is a solution to the generalized Becker-Döring equations with density below the critical one, then there is some sequence r_i (which tends to zero as $i \to \infty$) such that the tails of the solution have mass below r_i ; this is,

$$\sum_{k=i}^{\infty} k c_k(t) \le r_i$$

for all times t after some time t_0 .

The proof of this consists mainly of an estimate obtained by differentiating the quantity $H_i := (G_i - r_i)_+$ (the positive part of $G_i - r_i$), proving with a differential inequality that it must remain zero for all times starting from a certain t_0 .

References

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