

Outline

- What are mixed models?
- Distinguishing random and fixed effects
- When should we (or shouldn't we) use mixed models?
- · Analytic considerations
- Coding considerations

Why use mixed models?

- Address some problems of fixed effects models:
 - Pseudoreplication
 - Hierarchical data structure
- · Informative:
 - Decompose variation of design into sampling unit
 - Quantify which sampling unit explains most of the variation

Pseudoreplication

- Involves repeated sampling of the same group
 - e.g., Spatial: same area many times,Temporal: same individual many times
- Violates assumption that errors are independent
- · Inflates sample size and df
 - Sample 5 indivs 100 times each
 - -N = 500 or N = 5?

Fixed vs random effects

- · Fixed effects
 - Describe mean of response variable
 - Have meaningful levels
 - Male/female, old/young, types of forest
- Random effects
 - Describe variance of response variable
 - Assumed to represent large population
 - Levels contain little useful information
 - Populations (A,B,C,D), individuals (Aa1,Aa2,Aa3,... Aa100)

Random effects

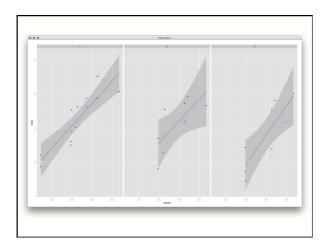
- · Variance components
 - Calculate the variance explained by the randome effects
 - Individual, population, residual
- Best linear unbiased predictors (BLUPs)
 - The deviation from the mean for an individual in a group
 - Extracted from random effects

Why not mixed models?

- Analytically, conceptually, and computationally challenging
- Theory remains poorly understood

 e.g., how many denominator df?
- Many advanced methods for fixed models not yet implemented for mixed models





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Linear mixed model fit by REML ['lmerMod']

Formula: shot ~ prev * count + (1 | moor) + (1 | drive)

Data: GROUSE

REML criterion at convergence: 38.5

Scaled residuals:

Min 1Q Median 3Q Max
-1.39713 -0.55498 0.01077 0.54603 1.47802

Random effects:

Groups Name Variance Std.Dev.
drive (Intercept) 0.04510 0.2124

moor (Intercept) 0.08102 0.2846

Residual 0.13114 0.3621

Number of obs: 29, groups: drive, 12; moor, 5

Fixed effects:

Estimate Std. Error t value
(Intercept) -1.06344 1.93232 -0.550

prev -0.65963 1.04190 -0.633

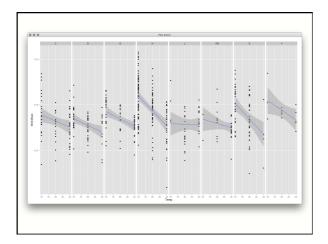
count 0.93763 0.36771 2.550

prev:count 0.04772 0.19226 0.248

Correlation of Fixed Effects:
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```
Linear mixed model fit by REML ['lmerMod']
Formula: Wet.Mass ~ Temp + (Temp | Population) + (1 |
Maternal.Fam) + (1 | Paternal.Fam)
Data: MFLIES

REML criterion at convergence: -4198.8

Scaled residuals:
Min 1Q Median 3Q Max
-3.6319 -0.5534 0.0936 0.6216 2.6972

Random effects:
Groups Name Variance Std.Dev. Corr
Paternal.Fam (Intercept) 4.181e-06 0.002045
Maternal.Fam (Intercept) 1.488e-06 0.001220
Population (Intercept) 2.358e-05 0.004856
Temp 3.764e-08 0.000194 -0.97
Residual 1.139e-05 0.003375
Number of obs: 504, groups: Paternal.Fam, 20; Maternal.Fam, 20; Population, 8
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Fixed effects:

Estimate Std. Error t value

(Intercept) 2.666e-02 2.183e-03 12.214

Temp -4.689e-04 9.068e-05 -5.171

Correlation of Fixed Effects:

(Intr)

Temp -0.937
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