$\mathbf{Q}\mathbf{1}$

This method will return the given singly linked list in the reverse order. It acts by rearranging pointers. Head and tail pointers are correctly set.

```
/* Java/pseudocode to reverse the elements of a singly-linked list */
reverseSLL(list)
  prevNode = null
  currNode = list.head
  nextNode = null

while(currNode != null) // list traversal
  nextNode = currNode.next
  currNode.next = prevNode
  prevNode = currNode
  currNode = nextNode

list.tail = list.head
  list.head = prevNode

return list
```

$\mathbf{Q2}$

For both unordered lists and arrays, one must iterate through each element in the list/array until the value is found. It is assumed that the order of the unordered list/array is completely random, in which case the average number of nodes accessed in a search will be n/2.

For an ordered array (random access), a binary search can be employed to search for a particular node. The time complexity of binary search is $O(\log 2 n)$ or simply $O(\log n)$. The best case is (1); however, the average performance of binary search is $(\log n)$. Thus, the average number of nodes accessed will be $\log n$.

For an ordered list, average number of nodes accessed would depend on the implementation namely whether list is random or sequential access. From the Java API on binarySearch (https://docs.oracle.com/javase/7/docs/api/java/util/Collections.html)

This method runs in $\log(n)$ time for a "random access" list (which provides near-constant-time positional access). If the specified list does not implement the RandomAccess interface and is large, this method will do an iterator-based binary search that performs O(n) link traversals and $O(\log n)$ element comparisons.

Thus, the average number of nodes for a sequential access list will be n/2, and for a random access list log n.

$\mathbf{Q3}$

This question is deceptively tricky because there are several different cases to evaluate.

```
/* Java/pseudocode to interchange the mth and nth elements of a singly-linked list */
swap(list,m,n)
  curr = list.head
  prevM = null
  currM = null
  nextM = null
  prevN = null
  currN = null
  nextN = null
  if(curr == M) // case head --> m
     currM = curr
     nextM = curr.next
  if(curr == N) // case head --> n
     currN = curr
     nextN = curr.next
  while(curr != null) // list traversal
     if(curr.next == M)
        prevM = curr
        currM = curr.next
        nextM = curr.next.next
     if(curr.next == N)
        prevN = curr
        currN = curr.next
       nextN = curr.next.next
     curr = curr.next
  if(prevM == null) // case head --> m
     list.head = currN
     currN.next = nextM
     prevN.next = currM
     currM.next = nextN
  else if(prevM == null) // case head --> n
     list.head = currM
     currM.next = nextN
     prevM.next = currN
     currN.next = nextM
  else
     prevM.next = currN // m-1 --> n
     currN.next = nextM // n --> m+1
     prevN.next = currM // n-1 --> m
     currM.next = nextN // m --> n+1
```

```
/* Java/pseudocode to implement the deque as a doubly-linked list (not circular, no
   header) with InsertLeft and DeleteRight methods */
public class Deque
  private Node head = null // left
  private Node tail = null // right
  private class Node
     Node left
     Node right
     Item data
     Node (Item data, Node left, Node right)
        this.data = data
        this.left = left
        this.right = right
  boolean isEmpty()
     if(head == null AND tail == null)
        return true
        return false
  void insertLeft(Item data)
     Node node = new Node(data, null, head) // data, left (head), right (tail)
     head = node
  Item deleteRight()
     if(isEmpty())
        throw exception
     else
        Node temp = tail
        tail.left.right = tail.right // set node n-1 next to null
        tail = tail.left // set tail to node n-1
        return temp
```

$\mathbf{Q5}$

```
/* Java/pseudocode to implement the deque as a doubly-linked circular list with a header
    and InsertRight and DeleteLeft methods. */
public class Deque

private class Node
    Node left // head
    Node right // tail
    Item data

Node(Item data, Node left, Node right)
    this.data = data
    this.left = left // head
    this.right = right // tail

Node header = new Node(null,null,null)
```

```
boolean isEmpty()
  if(head == null AND tail == null)
     return true
  else
     return false
void insertRight(Item data)
  if(isEmpty())
     Node node = new Node(data, node, node) // points to itself
     Node node = new Node(data, header.left, header.right)
     header.right.right = node
     node.right = header.left
     header.right = node
Item deleteRight()
  if(isEmpty())
     throw exception
     Node temp = header.left // temp = first (head) node
     header.right.right = header.left.right // set trail node next to header.next
     header.left = header.left.right // update where header head points to
     return temp
```

$\mathbf{Q6}$

My answer to this question does require additional working out, but these are the basics.

```
/* Java/pseudocode for hybrid implementation of list capable of handling multiple
    stacks/queues */
public class HybridArray{
   private int size;
   Node[] data = new Node[size];
   Stack free = new Stack(size);
   public HybridArray(int size){
       this.size = size;
       for(int i = 0; i < size; i++){</pre>
           free.push(i);
   }
   // Implement stack as an array
   private class Stack{
       private int arr[];
       private int size;
       private int top = 0;
       private Stack(int size){
           this.size = size;
```

```
arr = new int[size];
   }
   private void push(int element){
       if(top == size) {
           System.out.println("Invalid.");
       else {
           arr[top] = element;
           top++;
   }
   private int pop(){
       if (isEmpty()){
           System.out.println("Invalid.");
       return arr[top-1];
   }
   private boolean isEmpty(){
       if (top == 0) {
           return true;
       return false;
   }
}
// Implement node to hold data and pointer
private class Node{
   int data;
   int next;
   private Node(int data, int next){
       this.data = data;
       this.next = next;
}
// Methods to push and pop to/from the free index stack
public int freeIndex(){
   if(free.isEmpty()){
       System.out.println("Invalid.");
   return free.pop();
}
public void returnFree(int index){
   free.push(index);
}
// Stack methods
public void push(int data, int next){
```

```
int freeIndex = free.pop(); // obtain an index from the free index stack
       Node node = new Node(data, 0)
       data[freeIndex] = node;
   }
   public Node pop(){
       if(data.isEmpty()){
           throw exception;
       }
       node = startNode
       while(node.next != 0){ // traverse array to find last node in stack
          prevNode = node;
          node = data[node.next];
       }
       data[prevNode].next = 0; // set pointer of new last item to 0
       returnFree(node); // return the index to the free index stack
       return data[node];
   }
   // Queue methods
   public void add(int data, int next){
       int freeIndex = free.pop(); // obtain an index from the free index stack
       Node node = new Node(data, 0)
       data[freeIndex] = node;
   }
   public void remove(){
       temp = startNode;
       startNode = startNode.next; // set new startNode to the next element in queue
       returnFree(temp); // return the index to the free index stack
       return data[temp];
   }
}
```