

Figure 6: Fourth step of encryption.

The last step involves adding some number of transitions under letters from the alphabet  $\{0,1\}$  between states belonging to the same copy of a public key in  $\mathcal{B}$ . In that case we have added transition  $\rho(9a,0)=10a$  (first copy), transitions  $\rho(7b,1)=10b$  and  $\rho(8b,1)=3b$  (second copy) and transition  $\rho(12c,0)=7c$  (third copy).

## 4 Basic decryption

For that section we assume that we have a ciphertext automaton  $\mathcal{B} = (P, \Sigma, \rho)$  constructed from a public key  $\mathcal{A} = (Q, \Sigma, \delta)$ , and that we know a private key w which is a carefully synchronizing word for the automaton  $\mathcal{A}$ . First we state a lemma.

**Lemma 1.** Let  $Q.w = q_l$ . After removing letters  $x \in \{0, 1\}$  from automaton  $\mathcal{B}$  we have that  $P.w = \{q_l^1, q_l^2, ..., q_l^{|u|+1}\}$ .