

stochastic integration techniques. Furthermore, the assumption of dependence between r and x induces additional quadratic co-variation terms to the last formula that must be dealt with, similar to the situation mentioned in Remark 1.1 when A and χ have common jumps. While such more theoretical considerations lie beyond the scope of this more practically oriented article, we still find it important to highlight this issue, as it makes clear that our definition is only an approximation to reality.

3 Distributing assets and whole portfolios

In the logic of the aforementioned section it was important that the asset was subject to reinvestment, in the sense that it is not allowed that cash flows out of the asset, because this outflow would then be forgotten in the analysis. Now we take care about such potential outflows. Special attention is required in this case, because if at some time point u between t and T a certain cash amount² c_u flows out of the asset price A_u , so that the price process jumps down by c_u at time u , then the amount c_u must somehow find its way into the PnL. The simplest possibility is to simply add c_u to the carry gain $P_{(t,T]}^{(A)}(\text{carry})$, and this is essentially what we do. Concretely, we assume a decomposition $t = u_0 < u_1 < \dots < u_m = T$ of the interval $(t, T]$ with u_0, \dots, u_m being potential cash outflow dates (if no cash flows out at time T we assume $c_m = 0$). With A_{u-} denoting the asset price an instant before some cash outflow time point u , we notice that $A_{u_i} = A_{u_i-} - c_{u_i}$, because the (dirty) asset price drops at time u_i by the coupon amount c_{u_i} . With this terminology, the definition of $P_{(t,T]}^{(A)}(\text{carry})$ is enhanced to become

$$P_{(t,T]}^{(A)}(\text{carry}) = \sum_{i=1}^m \frac{\chi_{u_{i-1}} + \chi_{u_i}}{2} \left(\frac{A_{u_i}(r_{u_i}, x_{u_{i-1}}) - A_{u_{i-1}-}(r_{u_i}, x_{u_{i-1}})}{2} + \frac{A_{u_i}(r_{u_{i-1}}, x_{u_i}) - A_{u_{i-1}-}(r_{u_{i-1}}, x_{u_i})}{2} + c_{u_i} \right), \quad (4)$$

and the total PnL is enhanced accordingly as well.

Here it is important to be aware that the FX rate χ enters at all coupon time points u_i , and this is a definition that one should ponder about for a little while. The given formula simply assumes that there is zero PnL between u_i and T arising from the coupon received at u_i , but the PnL on the received EUR amount is “frozen” at time u_i . Intuitively, at time u_i the out-flowing EUR cash amount $c_{u_i} (\chi_{u_{i-1}} + \chi_{u_i})/2$ goes into some other asset and must be monitored in the PnL $P_{(u_i,T]}^{(\tilde{A})}$ for that other asset \tilde{A} . For instance, if nothing is done with this cash and it lays on some cash account during $(u_i, T]$, one must monitor

²Without loss of generality, only concerning terminology, we assume that A is a credit instrument and c_u is a coupon payment at coupon date u , but it could as well be that A is a stock and c_u a dividend payment.