

the primordial Spectrum, which could (in principle) be identified as a fingerprint on the temperature distribution of the microwave background.

It remains as a future investigation objective to determine how general the proposed scenario is, for example by considering more general cosmological models like the Bianchi Universes [35]. Clearly, these cosmological frameworks can be reconciled to the isotropic late Universe by the inflationary de-Sitter phase [36], whose associated Spectrum should have a corrected morphology

which is expected to be similar to the one presented here.

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