

Problem 1.

- (a) Use Equation 10.132 to determine the mass of the W, in terms of  $v = \frac{\mu}{\lambda}$  and  $q = g_w \sqrt{\frac{\hbar c}{4\pi}}$ . Thus, confirm Equation (12.1)
- (b) Use Problem 10.21 and Equation 10.130 to determine the vertex factor for the coupling of the Higgs to a quark or lepton.
- (c) Use Equation 10.136 to determine the vertex factors for the couplings hWW, hZZ, and hhh.

Solution

(a)  $m_A = 2\sqrt{\pi}(\frac{q\mu}{\lambda c^2})$  (10.132)

To get a mass term from a lagrangian, we expand L in powers of  $\phi$  and pick out the term proportional to  $\phi^2$ . (second order in the field).

$$L = \frac{1}{2}(\partial_\mu \phi)(\partial^\mu \phi) + \frac{1}{2}\mu^2 \phi^2 - \frac{1}{4}\lambda^2 \phi^4 \quad (10.108)$$

And we can assume that  $L = T - U$  (10.109)

$$\text{and } U(\phi) = -\frac{1}{2}\mu^2 \phi^2 + \frac{1}{4}\lambda^2 \phi^4 \quad (10.110)$$

$\phi = \frac{\mu}{\lambda}$  (10.111) we assume this as a ground state.

Now, starts from (10.132),  $m_A = 2\sqrt{\pi}(\frac{q\mu}{\lambda c^2})$ ,

This is the mass term for a free gauge field lagrangian (10.131) and was derived from the lagrangian of the spontaneously broken continuous symmetry (chapter 10.8).

$$m_A = 2\sqrt{\pi}(\frac{g_w \sqrt{\hbar c/4\pi} v}{c^2})$$

$$\frac{m_A c^2}{g_w} = 2\sqrt{\pi \hbar c/4\pi} = \frac{1}{2}\sqrt{\hbar c} v \rightarrow \sqrt{\hbar c} v = \frac{2m_A c^2}{g_w} = 246 \text{ GeV}$$

the vertex factor is  $2iM_m^2 c^2 g^{\mu\nu} / \hbar^2 v$  : one higs + 2 Ws or 2 Zs.

Problem 2.

- (a) Calculate the decay rate for  $h \rightarrow f + \bar{f}$  (where  $f$  is a quark or lepton), in the MSM.

$$\left[ \text{Answer} : \frac{\alpha_w}{8\hbar} m_h c^2 \left(\frac{2m_f}{M_W}\right)^2 \left[1 - \left(\frac{2m_f}{m_h}\right)^2\right]^{3/2} \right]$$

- (b) If  $m_h = 120 \text{ GeV}/c^2$ , what are the branching ratios  $\Gamma(b\bar{b})/\Gamma(c\bar{c})$  and  $\Gamma(b\bar{b})/\Gamma(\tau^+\tau^-)$ ? [Include a factor of 3, for color, in the case of quarks.]