

Radboud University



Statistical inference with cluster permutation testing

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Talk outline

Types of statistics descriptive inferential

Parametric statistics

Non-parametric randomization test

Clustering-based statistics

What types of statistics do we have?



"Data don't make any sense, we will have to resort to statistics."

How do large distributions of "something" behave? Binomial, Normal, Poisson
How can I describe (or summarize) a distribution? Mean, standard deviation, variance, kurtosis
How can I make a decision or draw a conclusion? Inferential statistics, hypothesis testing Inferential parametric statistics

You make N observation and want to find whether some hypothesis "H1" holds

Step 1: Gathering data

Observation	Value
0	2.5
1	-3.2
:	
Ν	2.4



Inferential parametric statistics



Determine probability of *t* under "H0"

 $t = \frac{\mu - \mu_{H0}}{\sigma / \sqrt{N}}$

If the observed t sufficiently unlikely, reject H0 in favour of H1

Inferential parametric statistics





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Types of statistics descriptive inferential

Parametric statistics

Non-parametric randomization test Clustering-based statistics Problem 1: Distribution of the data and test statistic

You make N observation and want to find whether some hypothesis H1 is true.

The first problem is that this requires a *known distribution* of the test statistic.





Problem 2: Multiple comparisons

Typical ERPs

64 channels, 250 timepoints 16.000 datapoints, repeated over conditions and subjects Thousands of parameters and t-values

Chance of false alarm is 5% for every test

With 16.000 data points we expect 800 false alarms in an ERP!

Similar problems for time-frequency ERSPs, connectivity, etc.

Solutions to control the FWER

Bonferroni correction

Reduce the alpha threshold by a factor N, for example from 5% to 2.5% when N=2.

Use the false discovery rate (FDR)

Sort the probabilities and adjust the threshold such that the expected proportion of false alarms is controlled Slightly less conservative than Bonferroni

Use a Monte Carlo approximation of the randomization distribution of the maximum statistic

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Randomization test: general principle

- Independent variable: condition
- Dependent variable: data

H0: the data is **independent** from the condition in which it was observed

The data in the two conditions is **not** different









Distribution of "x" can take any shape



Randomization of independent variable

Hypothesis is about data, not about the specific parameter

The distribution of the statistic of interest "x" is approximated using the Monte-Carlo approach, i.e. by random sampling

H0 is tested by comparing the observed statistic against the randomization distribution

Avoid the multiple comparison problem



The statistic "x" can be anything

- Rather than testing everything, only test the most extreme observation (i.e. the max statistic)
- Compute the randomization distribution for the most extreme statistic over all channels/times/frequencies
- Note that often we compute **two** extrema, one for each tail



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Increasing the sensitivity

Conventional is univariate parametric Our approach is to consider the data Many channels, timepoints, frequencies Massive univariate Multiple comparison problem

EEG is relatively blurry over channels, time, and frequency, so there is quite some structure in the data

Increasing the sensitivity

channel/time/frequency points are not independent and are expected to show similar behaviour

avoid the MCP by comparing the largest observed cluster versus the randomization distribution of the largest clusters

Avoid multiple comparisons

Increase sensitivity

Clustering in time



Clustering in time and frequency



Clustering in time, frequency and space



Toy example

Toy example: Original observation

null hypothesis: condition A = condition B

Condition A	Condition B
S1_a	S1_b
S2_a	S2_b
S3_a	S3_b
S4_a	S4_b
S5_a	S5_b
S6_a	S6_b
S7_a	S7_b
S8_a	S8_b
S9_a	S9_b
S10_a	S10_b

Toy example: 1st permutation

null hypothesis: condition A = condition B



Toy example: 2nd permutation

null hypothesis: condition A = condition B



Toy example: Original observation



Toy example: 1st permutation



Toy example: 1st permutation



Toy example: 2nd permutation



Toy example: 3rd permutation



Toy example: Nth permutation



Assess the likelihood of the *observed max cluster size* given the randomization distribution



General summary

A formal hypothesis can be tested with randomization test

control the chance of false positives

reduce the false negative rate

Multiple comparison problem

ERP - one hypothesis per channel-time

ERSP - one hypothesis per channel-time-frequency

Solution: use one hypothesis for all datapoints

Increase sensitivity

using clusters to capture the structure in the data