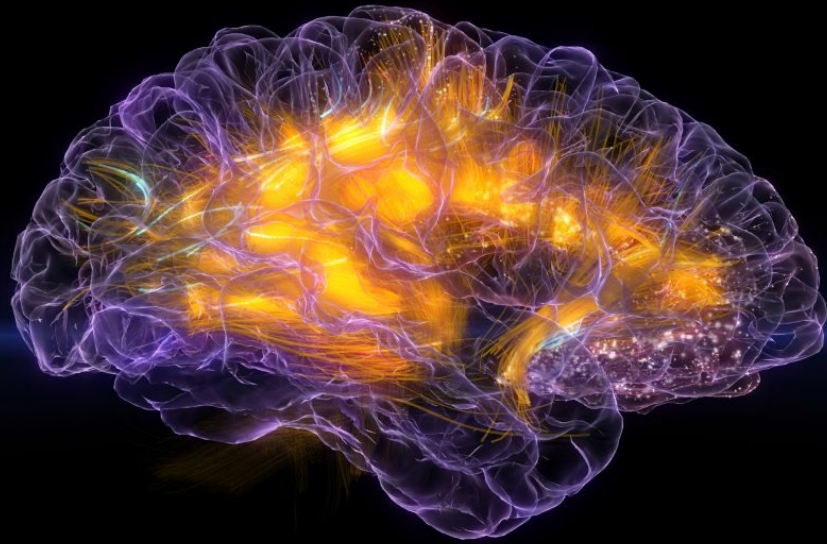
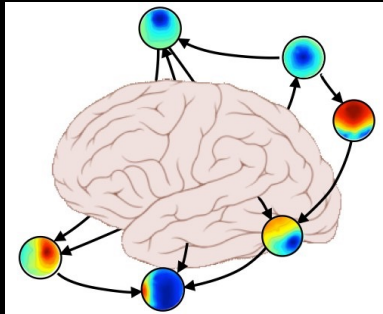


# Connectivity analysis

Aspet, 2023



Tim Mullen



# SIFT

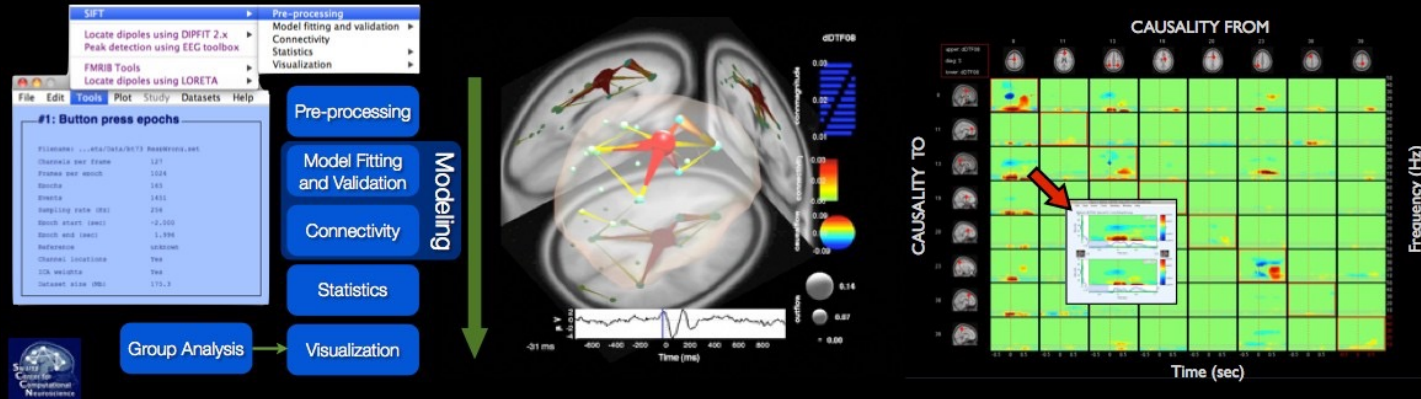
Source Information Flow Toolbox

<http://sccn.ucsd.edu/wiki/SIFT>

Mullen, et al, *Journal of Neuroscience Methods* (in prep, 2012)

Mullen, et al, *Society for Neuroscience*, 2010

Delorme, Mullen, Kothe et al, *Computational Intelligence and Neuroscience*, vol 12, 2011



- A toolbox for (source-space) electrophysiological information flow and causality analysis (single- or multi-subject) integrated into EEGLAB
- Emphasis on vector autoregression and time-frequency domain approaches
- Standard and novel interactive visualization methods for exploratory analysis of connectivity across time, frequency, and spatial location



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  - EEGLAB Wiki
  - MoBI Lab Wiki
  - SCCN Wiki Home

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  - SIFT
  - MoBILAB
  - MPT

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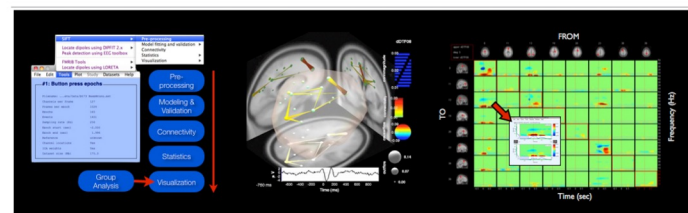
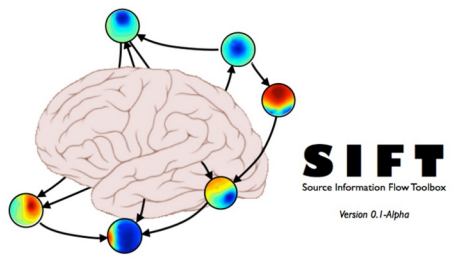
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# SIFT



**Contents** [hide]

- 1 Welcome to the repository for the Source Information Flow Toolbox (SIFT)
  - 1.1 SIFT Downloads
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- 2 SIFT Online Handbook and User Manual

## Welcome to the repository for the Source Information Flow Toolbox (SIFT)

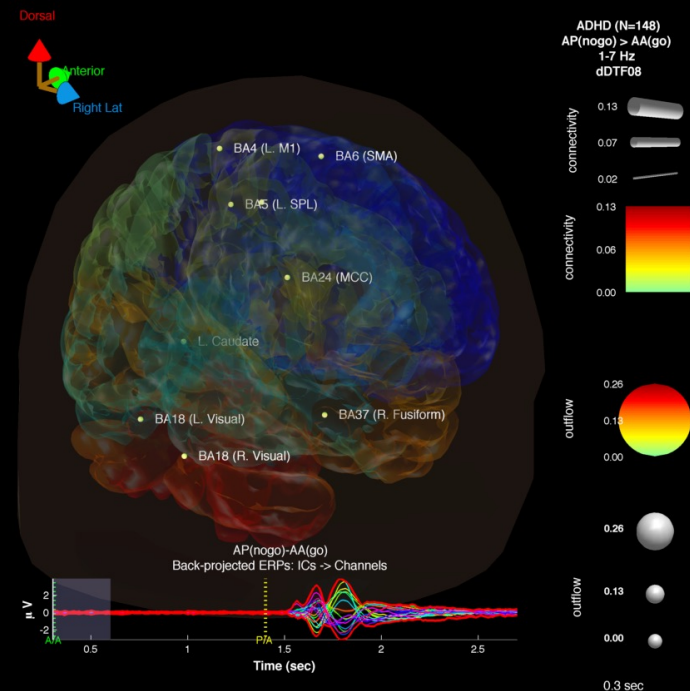
Developed and Maintained by: Tim Mullen (SCCN, INC, UCSD)  
Web: <http://www.antilipsi.net>  
Email: <Tim's first name> (at) sccn (dot) ucsd (dot) edu

SIFT is an EEGLAB-compatible toolbox for analysis and visualization of multivariate causality and information flow between sources of electrophysiological (EEG/ECOG/MEG) activity. It consists of a suite of command-line functions with an integrated Graphical User Interface for easy access to multiple features. There are currently four modules: data preprocessing, model fitting and connectivity estimation, statistical analysis, and visualization.



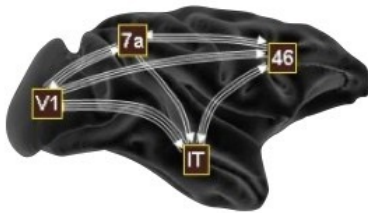
# The Dynamic Brain

- A key goal: To model temporal changes in neural dynamics and information flow that index and predict task-relevant changes in cognitive state and behavior
- Open Challenges:
  - Non-invasive measures (source inference)
  - Robustness and Validity (constraints statistics)
  - Scalability (multivariate)
  - Temporal Specificity / Non stationarity / Single-trial (dynamics)
  - Multi-subject Inference
  - Usability and Data Visualization (software)



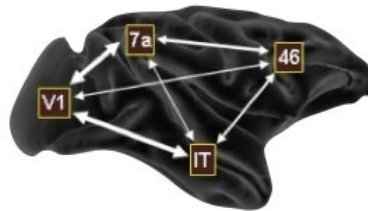
(Bullmore and Sporns, *Nature*, 2009)

### Structural



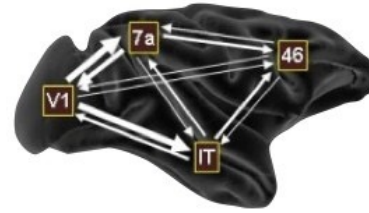
state-invariant,  
anatomical

### Functional



dynamic, state-dependent,  
correlative, symmetric

### Effective

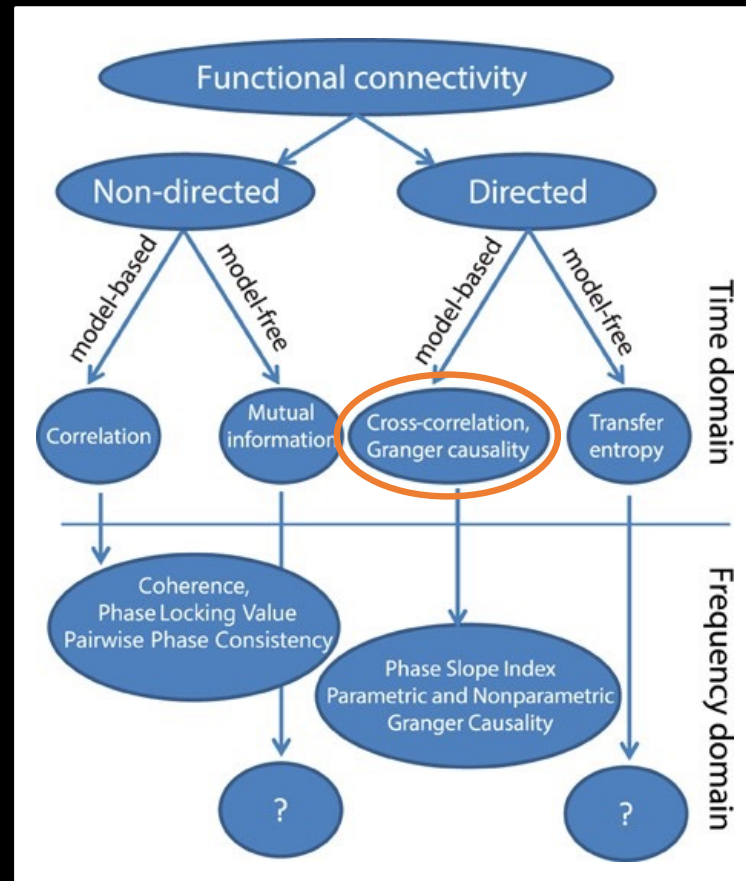


dynamic, state-dependent,  
asymmetric, causal,  
information flow

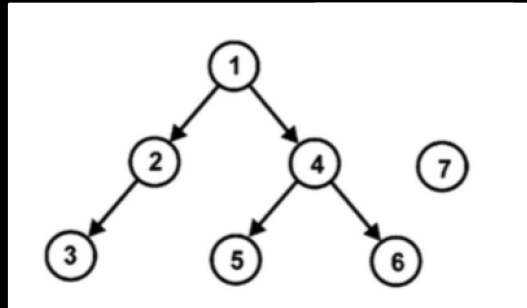
Hours-Years

milliseconds-seconds

Temporal Scale



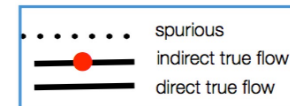
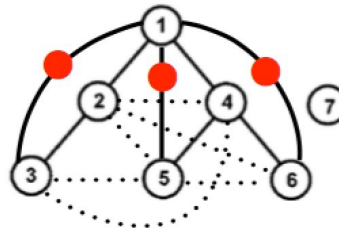
Bastos AM, Schoffelen J-M: **A Tutorial Review of Functional Connectivity Analysis Methods and Their Interpretational Pitfalls.** *Front Sys Neurosci* 2016, 9:413.



Coherency

$$C_{ij}(f) = \frac{S_{ij}(f)}{\sqrt{S_{ii}(f)S_{jj}(f)}}$$

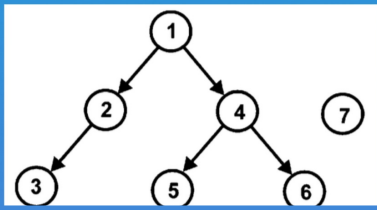
(Bendat and Piersol, 1986)



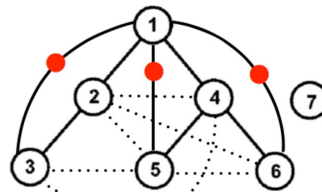
Bivariate measures such as coherence (but also original GC), find spurious connections between nodes if they share a common input.



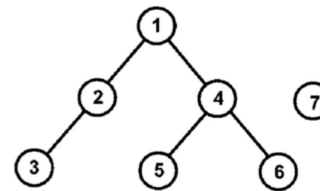
## Ground Truth



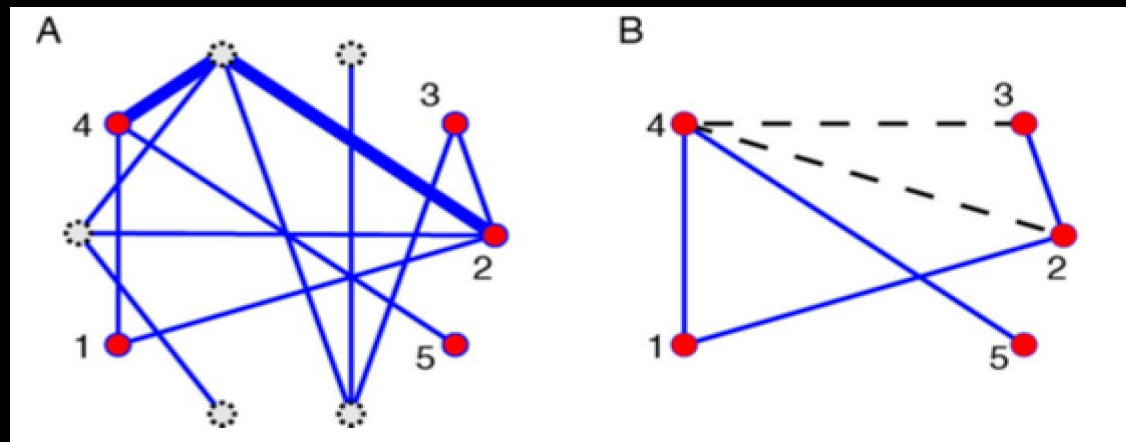
## Coherence



## Partial coherence



## A deeper problem – unobserved nodes



With EEG, it's unavoidable that there will be contributing network nodes (e.g. thalamus) that we cannot observe.

We also can't be sure ICA will identify all important sources...

# Granger-causality

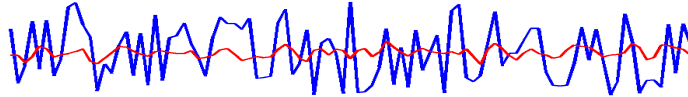


- A measure of *statistical* causality based on prediction.
- Widely used in time-series econometrics.
- Nobel Prize in economics, 2003.

*If a signal A causes a signal B, then knowledge of the past of both A and B should improve the predictability of B, as compared to knowledge of B alone.*

AR Models (prediction of future of a signal by its past)

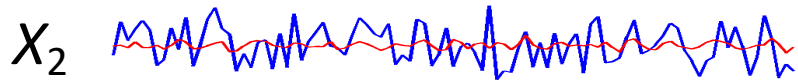
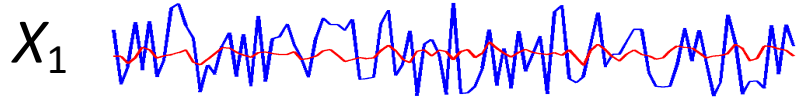
$X_1$



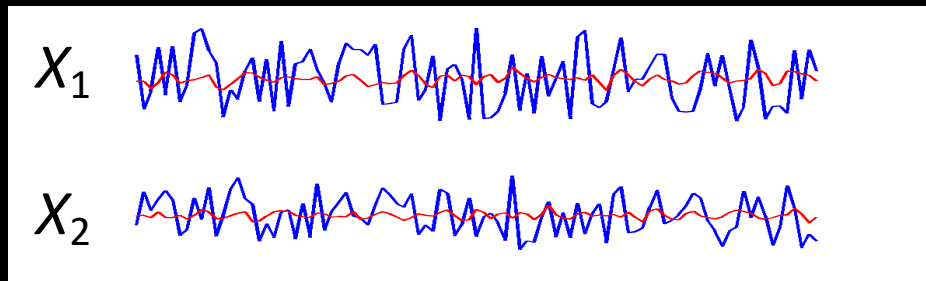
$$X_1(t) = -0.5X_1(t-1) + 0.3X_1(t-2) + 0.1X_1(t-3) \dots$$



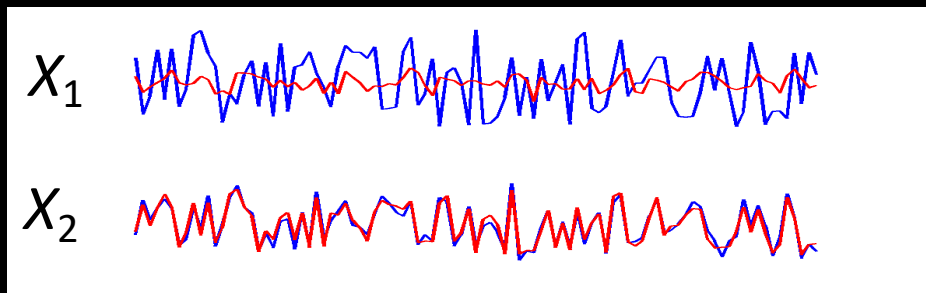
AR Models (prediction of future of a signal by its past)



AR Models (prediction of future of a signal by its past)

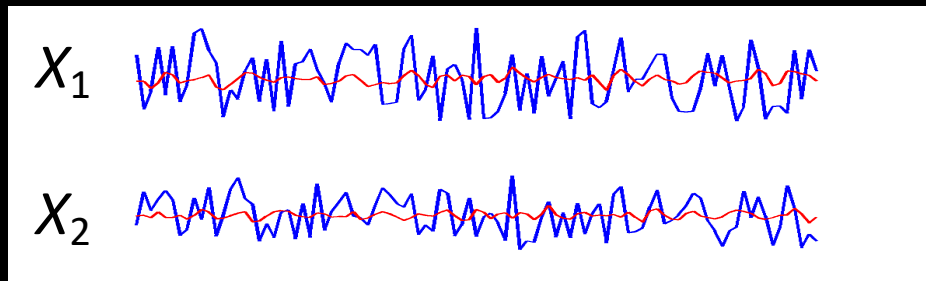


VAR Models (prediction of future of a signal by its past + the other signal's past)

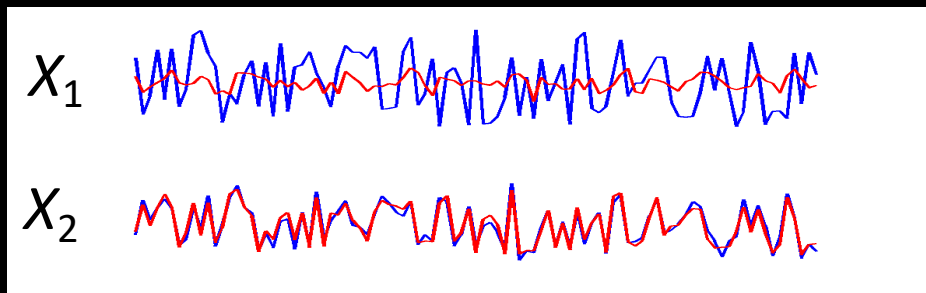


Incorporating information about  $X_1$  improves the prediction of  $X_2$ ! We say " $X_1$  granger causes  $X_2$ "

AR Models (prediction of future of a signal by its past)



VAR Models (prediction of future of a signal by its past + the other signal's past)

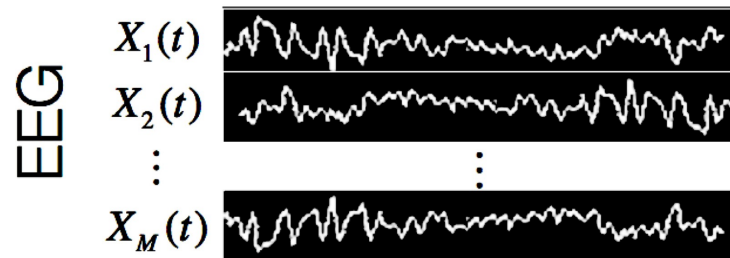


$$X_1(t) = -0.5X_1(t-1) + 0.3X_2(t-1) + \dots$$

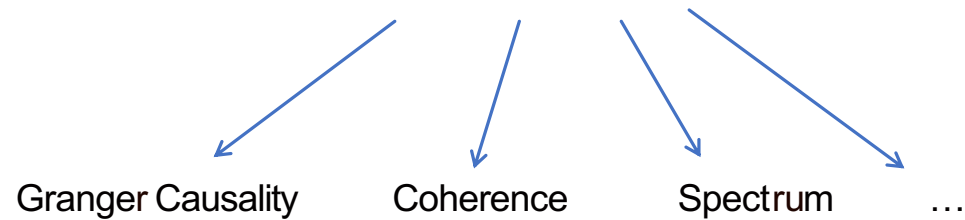
$$X_2(t) = -5X_1(t-1) - 0.1X_2(t-1) + \dots$$

Incorporating information about  $X_1$  improves the prediction of  $X_2$ ! We say " $X_1$  granger causes  $X_2$ "

# Vector Autoregressive (VAR / MAR / MVAR) Modeling



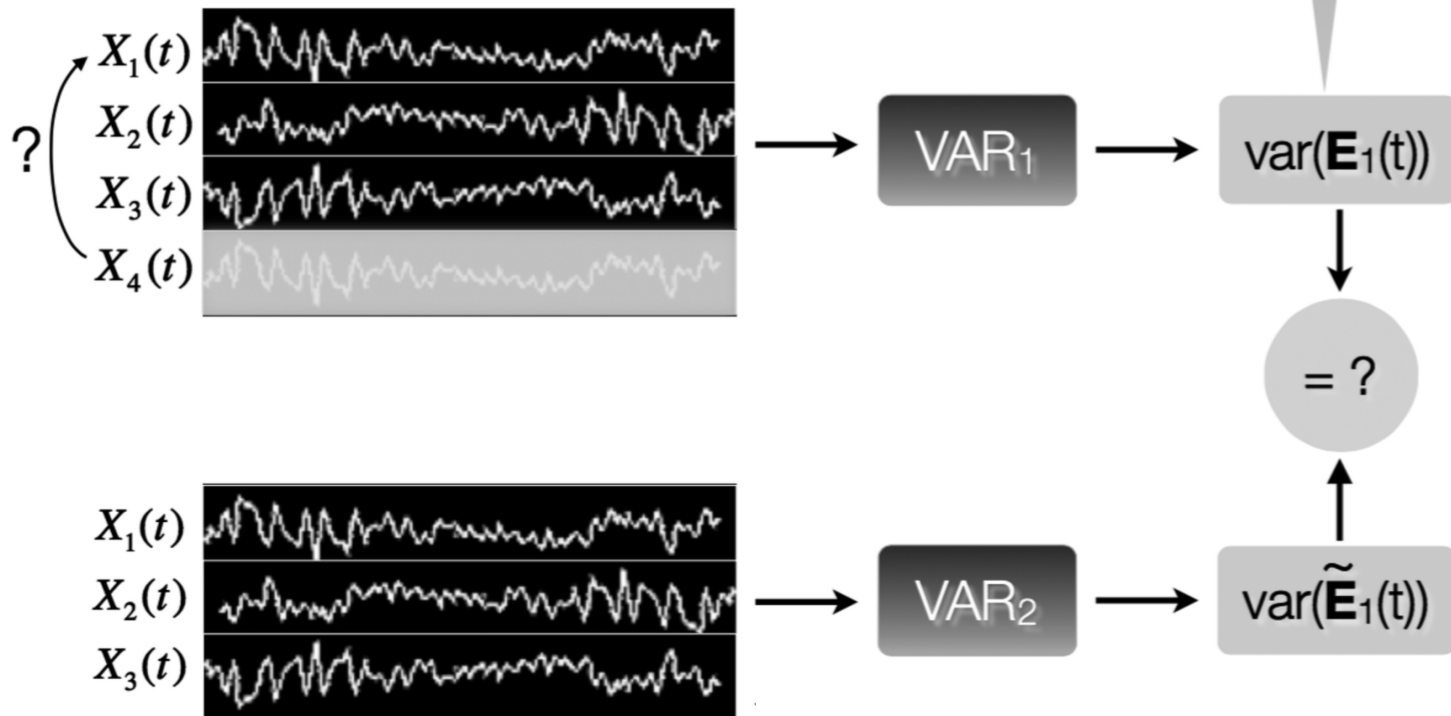
VAR



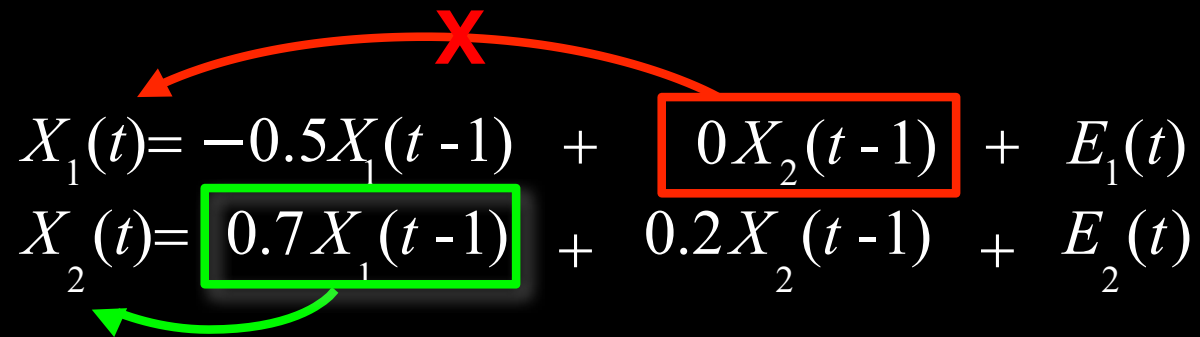


# Granger Causality

Does  $X_4$  granger-cause  $X_1$ ?  
(conditioned on  $X_2, X_3$ )



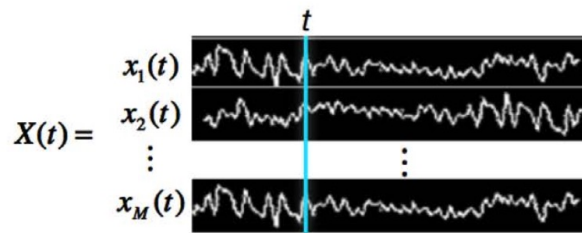
## Granger-causality quiz

$$\begin{aligned} X_1(t) &= -0.5X_1(t-1) + \boxed{0X_2(t-1)} + E_1(t) \\ X_2(t) &= \boxed{0.7X_1(t-1)} + 0.2X_2(t-1) + E_2(t) \end{aligned}$$


Which causal structure does this model correspond to?

- a)  b)  c) 

# The Linear Vector Auto-regressive (VAR) Model



Ordinary Least-Squares

VAR[p] model

$$\mathbf{X}(t) = \sum_{k=1}^p \mathbf{A}^{(k)}(t) \mathbf{X}(t-k) + \mathbf{E}(t)$$

model order

random noise process

M-channel data vector  
at current time  $t$

M x M matrix of (possibly time-varying)  
model coefficients indicating variable  
dependencies at lag  $k$

multichannel data  $k$   
samples in the past

$$\mathbf{A}^{(k)}(t) = \begin{pmatrix} a_{11}^{(k)}(t) & \dots & a_{1M}^{(k)}(t) \\ \vdots & \ddots & \vdots \\ a_{M1}^{(k)}(t) & \dots & a_{MM}^{(k)}(t) \end{pmatrix}$$

$$\mathbf{E}(t) = N(0, \mathbf{V})$$

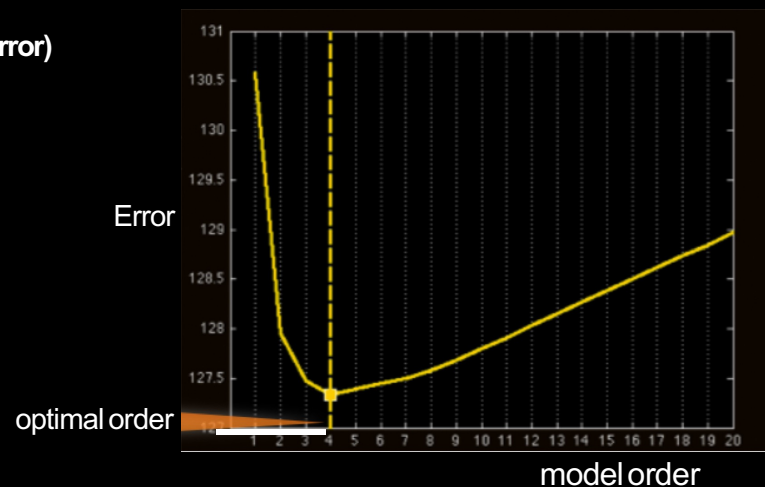
# Selecting a VAR Model Order

- Model order is typically determined by minimizing information criteria such as Akaike Information Criterion (AIC) for varying model order (p):

$$\text{AIC}(p) = 2\log(\det(V)) + M2p/N \quad \leftarrow \text{Penalizes high model orders (parsimony)}$$

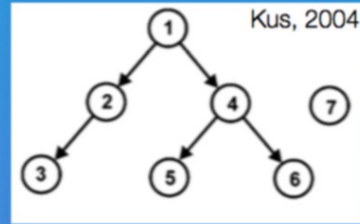
↑  
entropy rate (amount of prediction error)

- Optimal model order depends on sampling rate (higher sampling rate often requires higher model orders)





## Ground Truth



### Functional

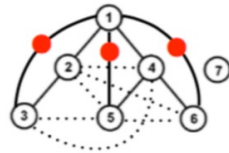
### Effective

Bivariate

Coherency

$$C_{ij}(f) = \frac{S_{ij}(f)}{\sqrt{S_{ii}(f)S_{jj}(f)}}$$

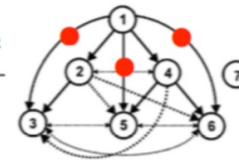
(Bendat and Piersol, 1986)



Granger-Geweke Causality

$$F_{ij}(f) = \frac{\Sigma_{jj} - (\Sigma_{ij}^2 / \Sigma_{ii})}{S_{ii}(f)} |H_{ij}(f)|^2$$

(Geweke, 1982; Bressler et al., 2007)

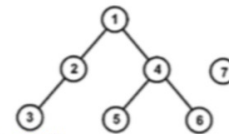


Multivariate

Partial Coherence

$$P_{ij}(f) = \frac{S_{ij}^{-1}(f)}{\sqrt{S_{ii}^{-1}(f)S_{jj}^{-1}(f)}}$$

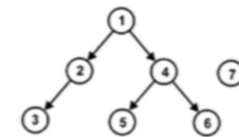
(Bendat and Piersol, 1986; Dalhaus, 2000)



Partial Directed Coherence

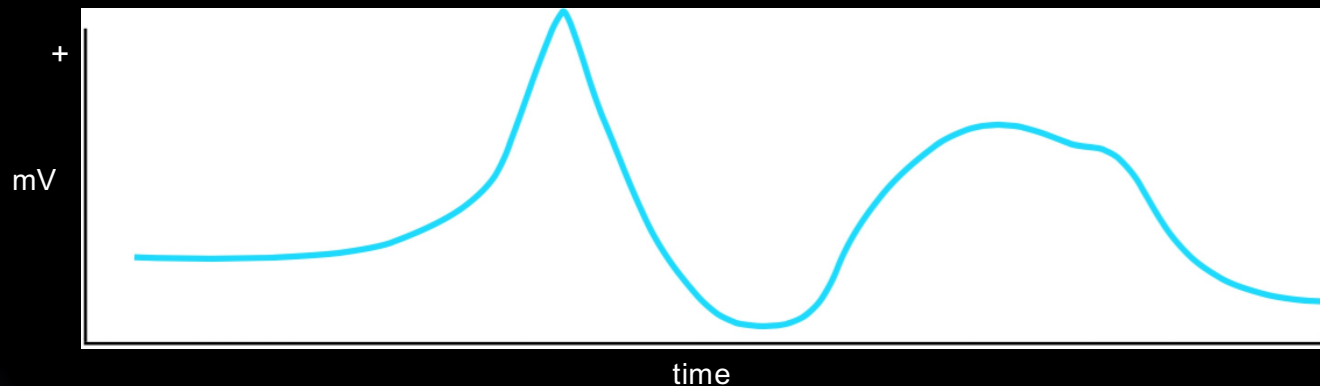
$$\pi_{ij}^2(f) = \frac{|A_{ij}(f)|^2}{\sum_{k=1}^M |A_{kj}(f)|^2}$$

(Baccalá and Sameshima, 2001)



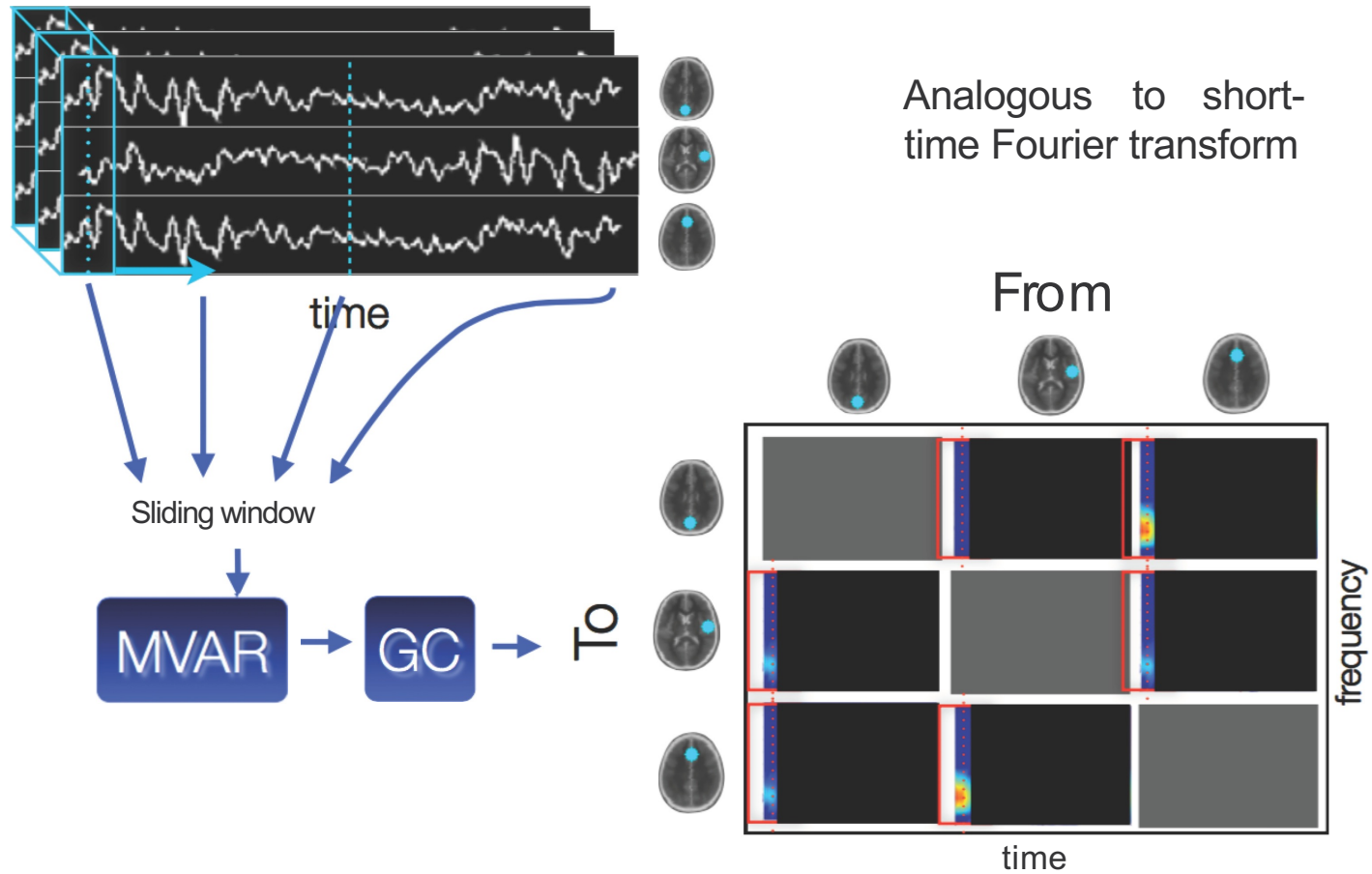
# Adapting to Non-Stationarity

- The brain is a **dynamic system** and measured brain activity and coupling can change rapidly with time (non-stationarity)
  - event-related perturbations (ERSP, ERP, etc)
  - structural changes due to learning/feedback
- How can we adapt to non-stationarity?



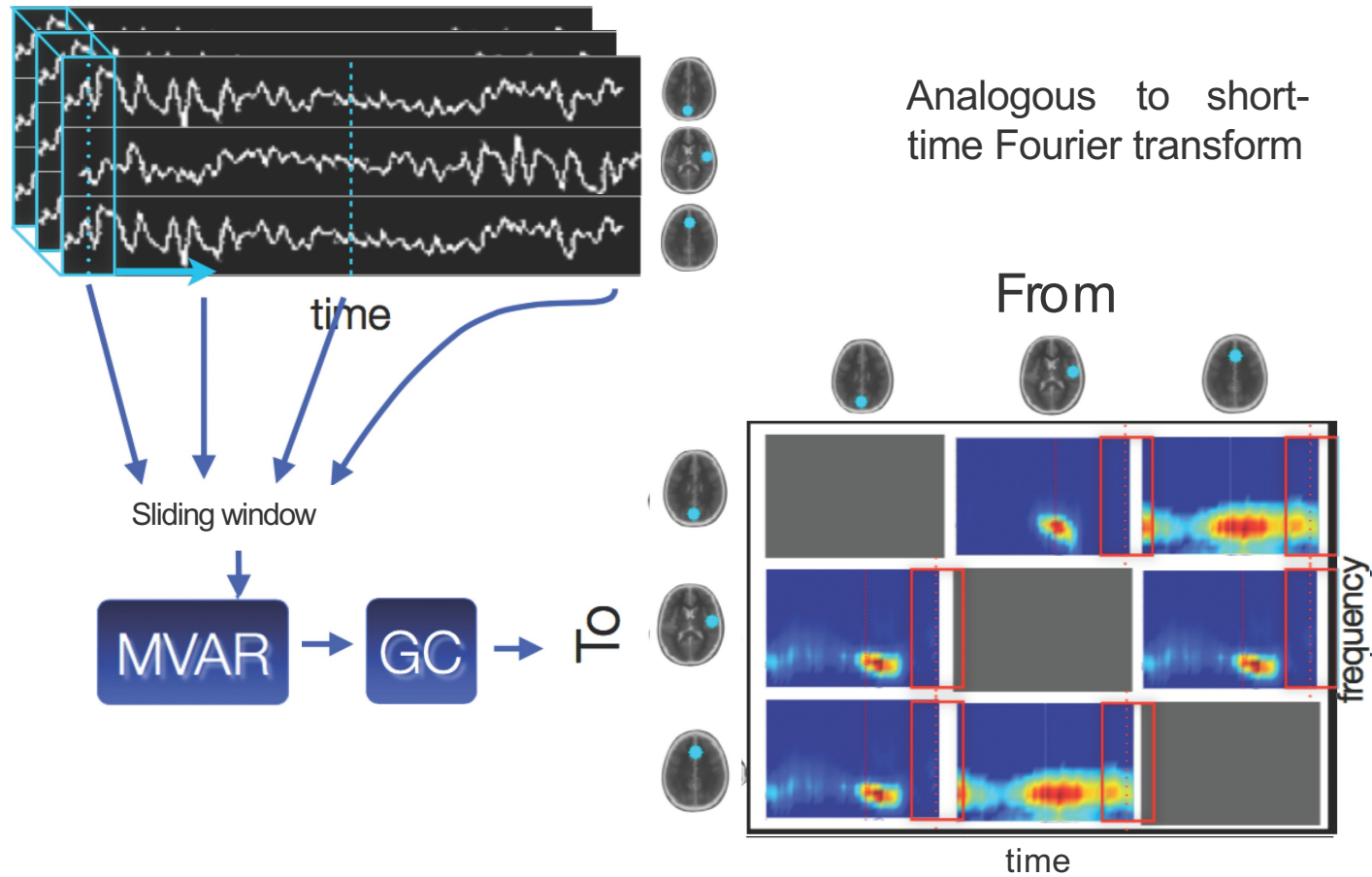
# Segmentation-based VAR

(Jansen et al., 1981; Florian and Pfurtscheller, 1995; Ding et al, 2000)



# Segmentation-based VAR

(Jansen et al., 1981; Florian and Pfurtscheller, 1995; Ding et al, 2000)

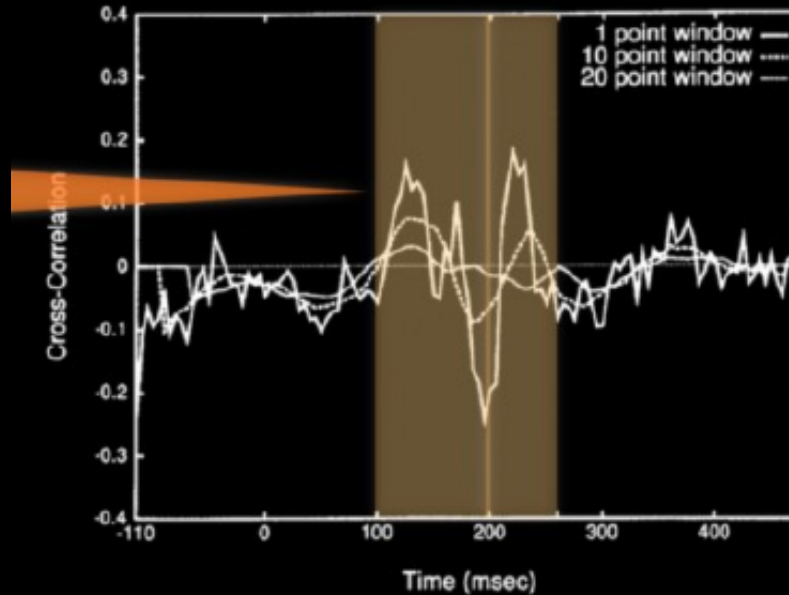


# Important Choices

- Model Order
  - Determines complexity of spectrum you can model
  - Larger orders need more data
- Window Length
  - Window must be long enough to contain sufficient data for your chosen model order
  - Must be long enough to encompass the time-scale of interactions
  - Yet not too long as to smear temporal dynamics or include non-stationary data
  - *If trials are present, can optimize AR model over trials*

# Consideration: Local Stationarity

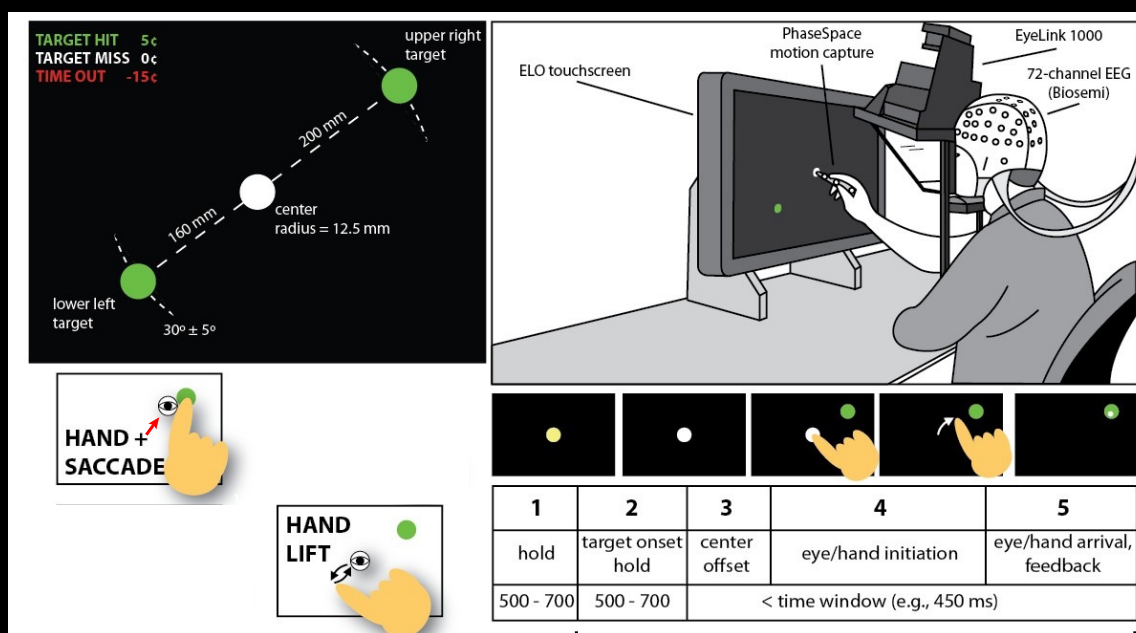
Too-large, windows may not be locally-stationary



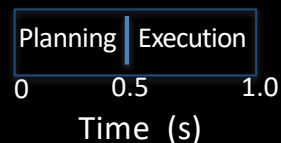


# How does brain plan visually guided movements?

- Pointing Task (Park, et al. 2014, *IEEE Trans Neural Syst Rehabil Eng*)



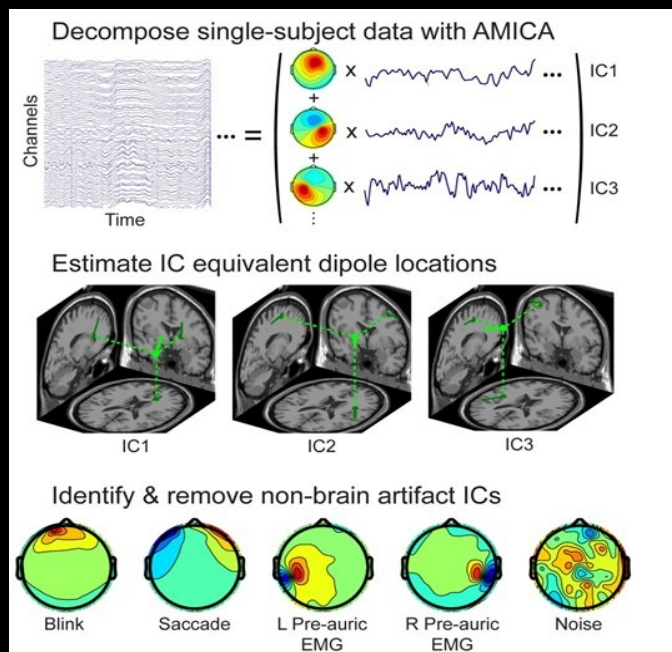
N=10 (right-handed, mean age=21) 70 channel EEG (Biosemi) 512 Hz; 128Hz for connectivity



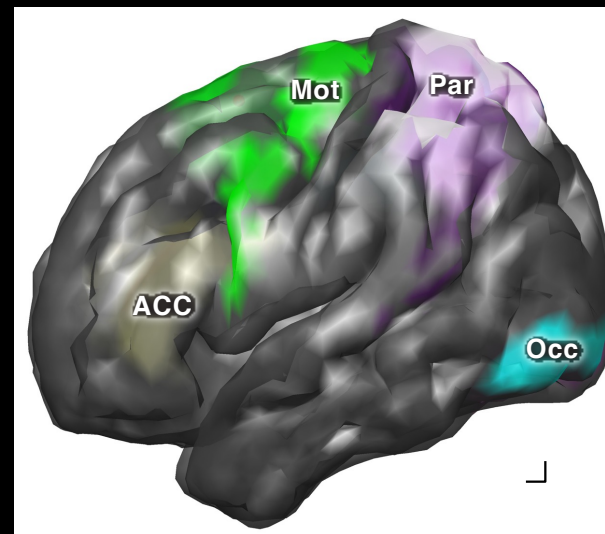
John R. Iversen, Alejandro Ojeda, Tim Mullen, Markus Plank, Joseph Snider, Gert Cauwenberghs, Howard Poizner (2014) EMBC

# ICA source space analysis

## Independent Component Analysis



## Cortical Regions of Interest



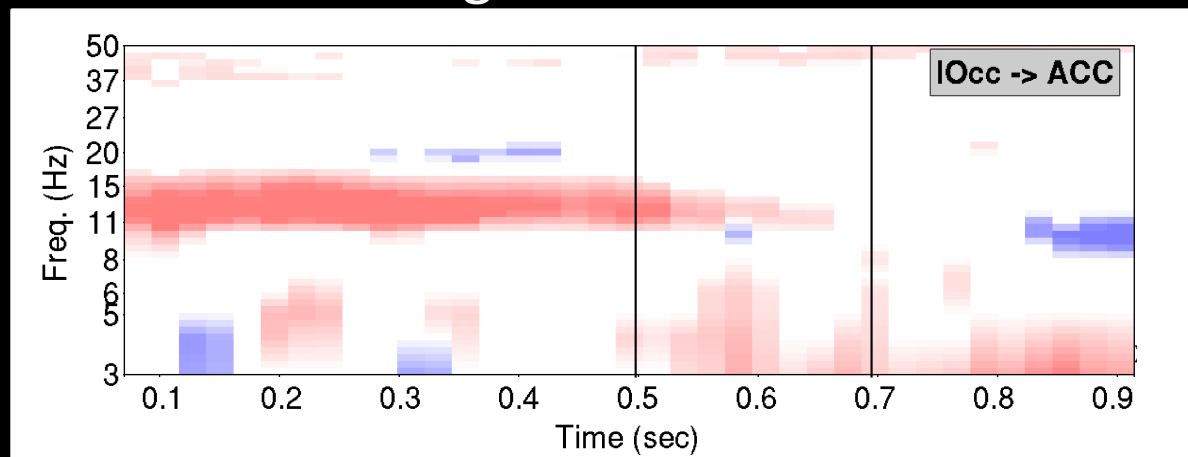
**Group SIFT:** Project ICs onto cortical surface using LORETA; extract ROI time series. Advantage: Same ROIs for all subjects enables statistical comparison. (Use *BCILAB srcpot*)



# Occipital -> ACC

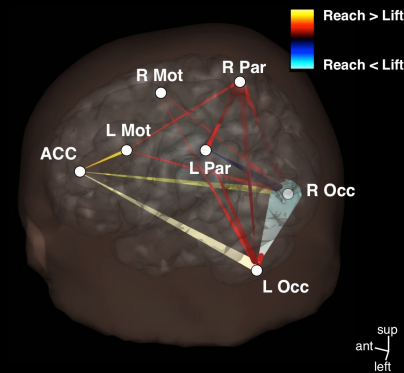
Planning

Execution

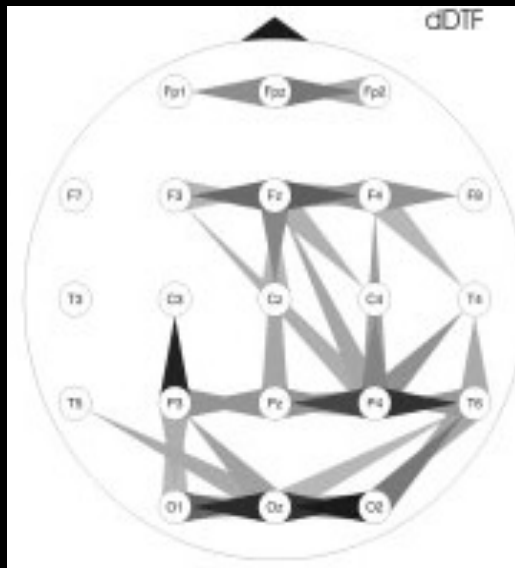


## Result discussion

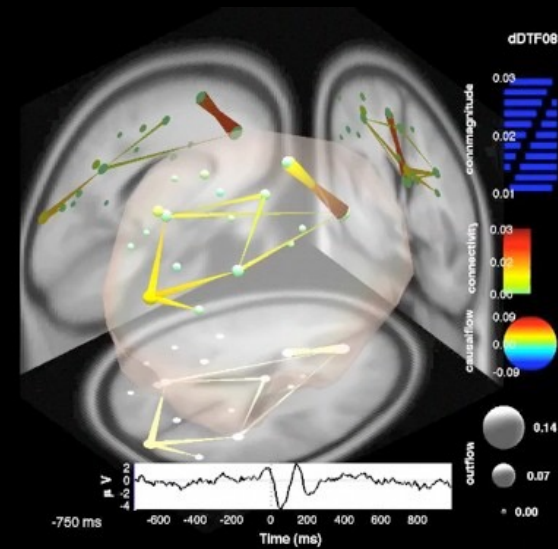
- SIFT is a capable toolkit for causal dynamical analysis at source level
- Parietal network expected for visually guided action (e.g. Heider, et al., 2010)
- ACC more strongly driven by Occipital Motor. Locus for translation of intention into action (Paus, 2001; Srinivasan, et al. 2013). ACC drives SMA (not shown).
- Causal network results depend on the number of nodes
  - E.g. Occipital " ACC could be mediated by region not included in model
  - There will always be a tradeoff between network size and amount of data needed to fit the model.
  - Regularization



# Scalp or Source?

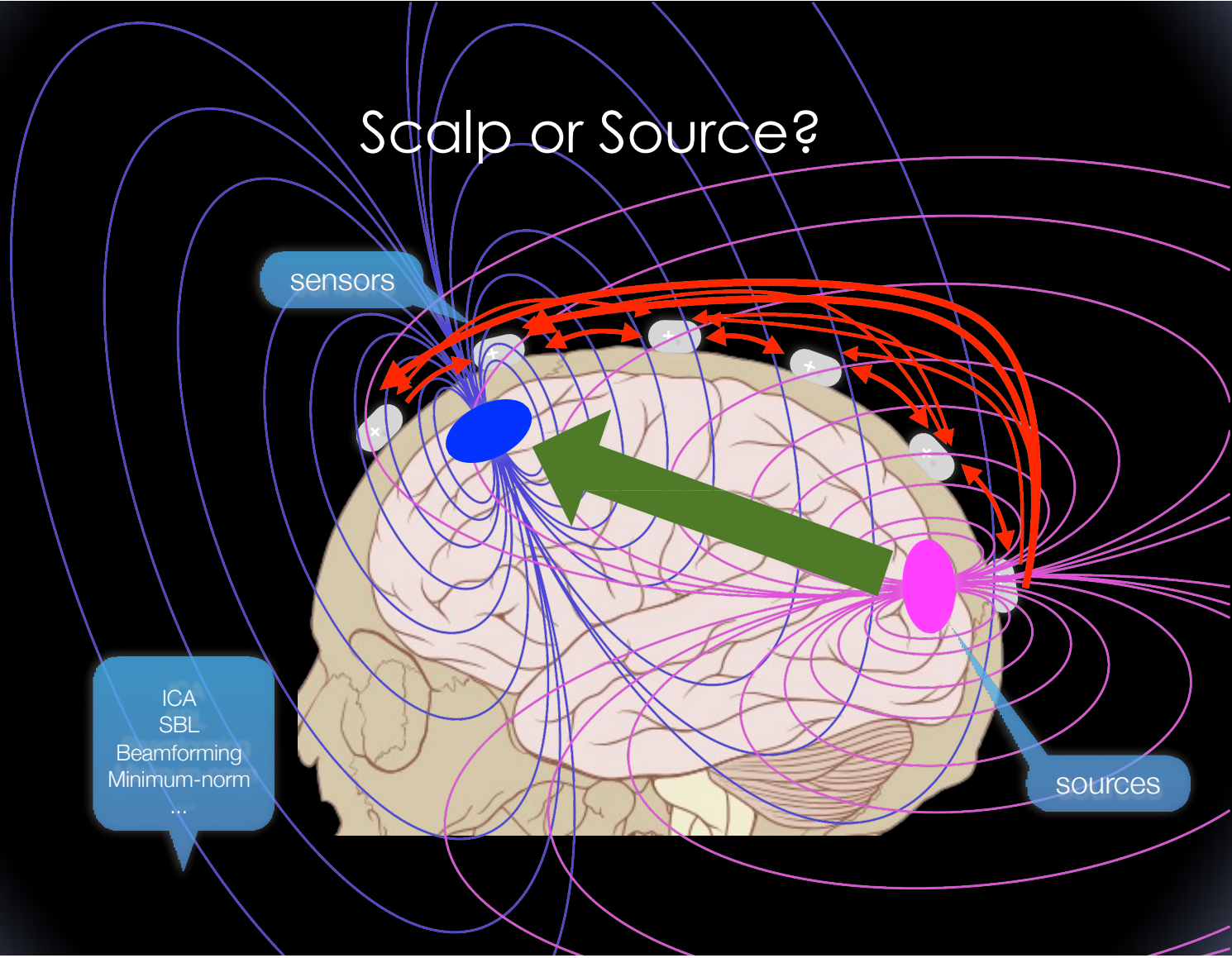


or





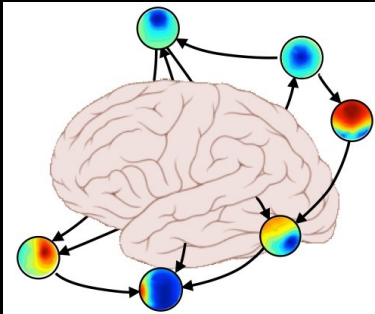
# Scalp or Source?



sensors

sources

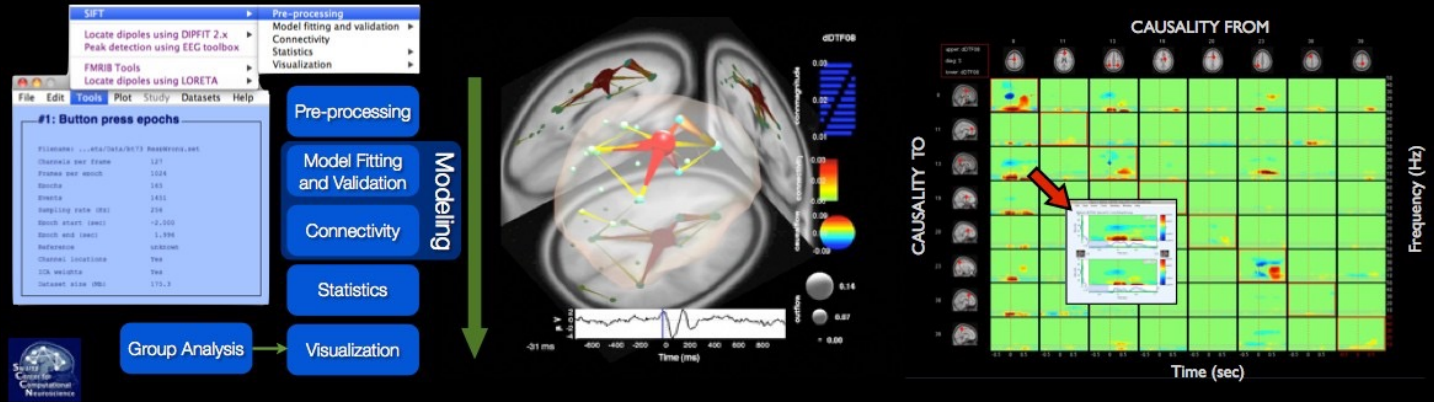
ICA  
SBL  
Beamforming  
Minimum-norm  
...



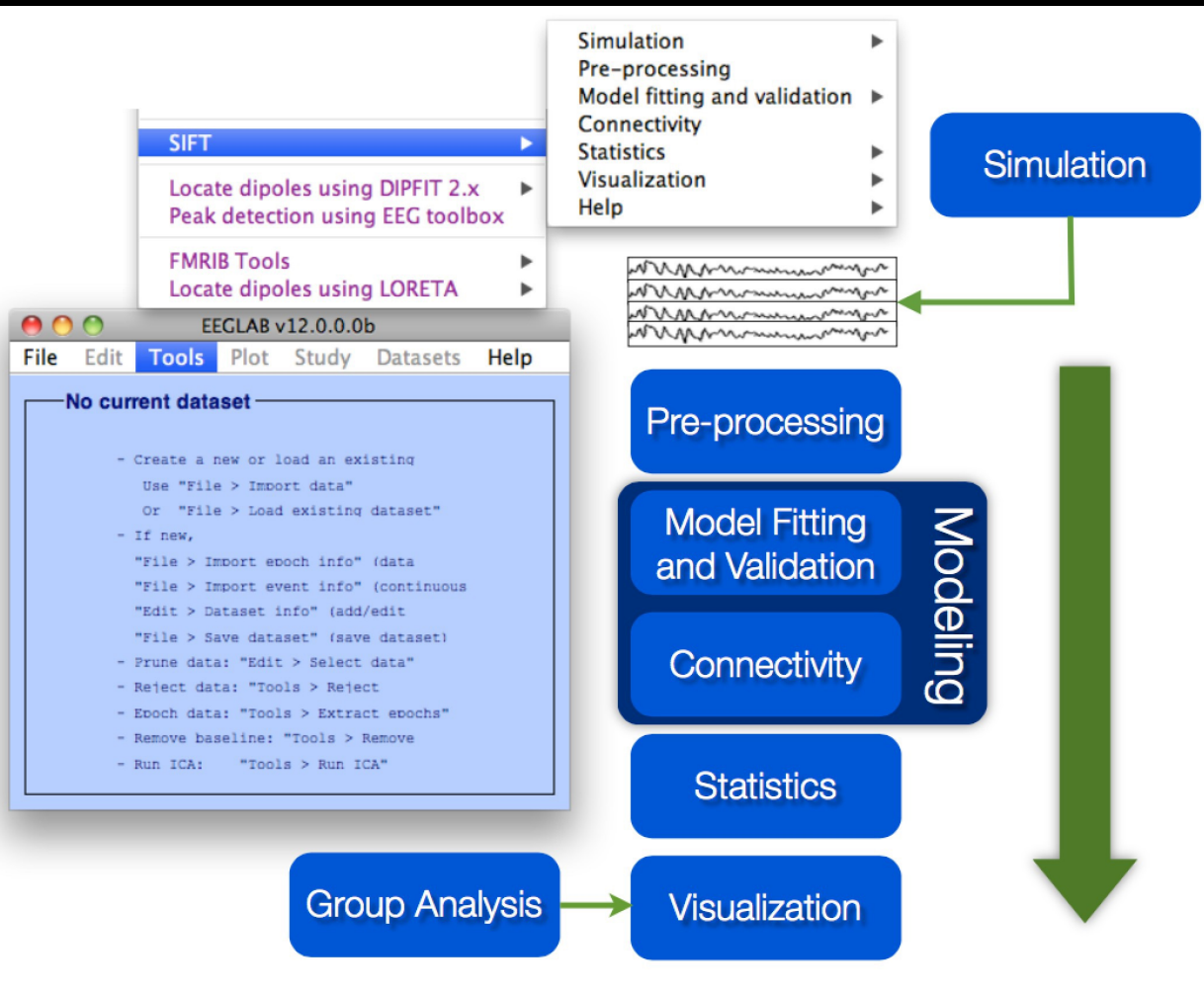
# SIFT

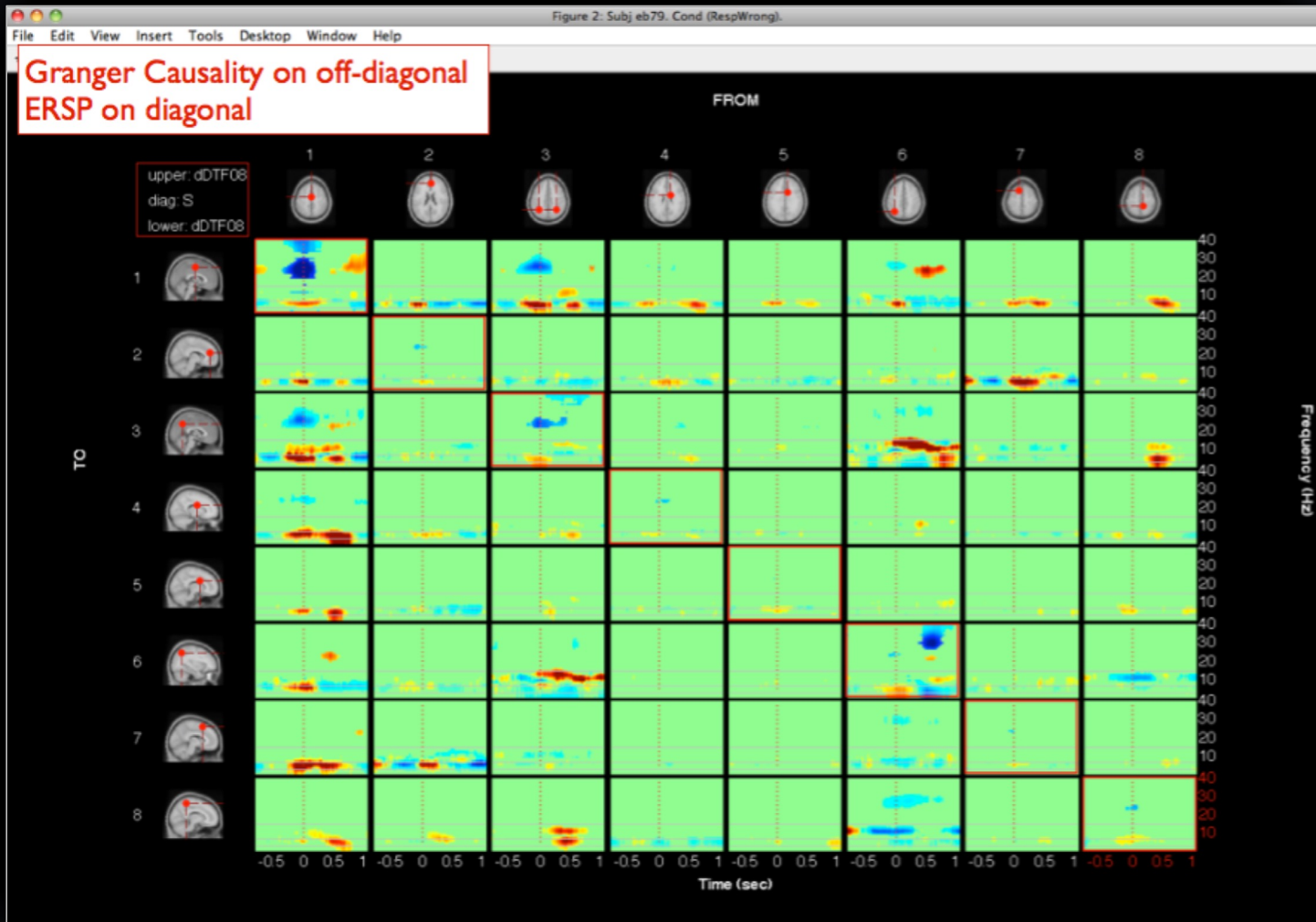
Source Information Flow Toolbox

<http://sccn.ucsd.edu/wiki/SIFT>  
 Mullen, et al, *Journal of Neuroscience Methods* (in prep, 2012)  
 Mullen, et al, *Society for Neuroscience*, 2010  
 Delorme, Mullen, Kothe et al, *Computational Intelligence and Neuroscience*, vol 12, 2011



- A toolbox for (source-space) electrophysiological information flow and causality analysis (single- or multi-subject) integrated into the EEGLAB software environment.
- Emphasis on vector autoregression and time-frequency domain approaches
- Standard and novel interactive visualization methods for exploratory analysis of connectivity across time, frequency, and spatial location

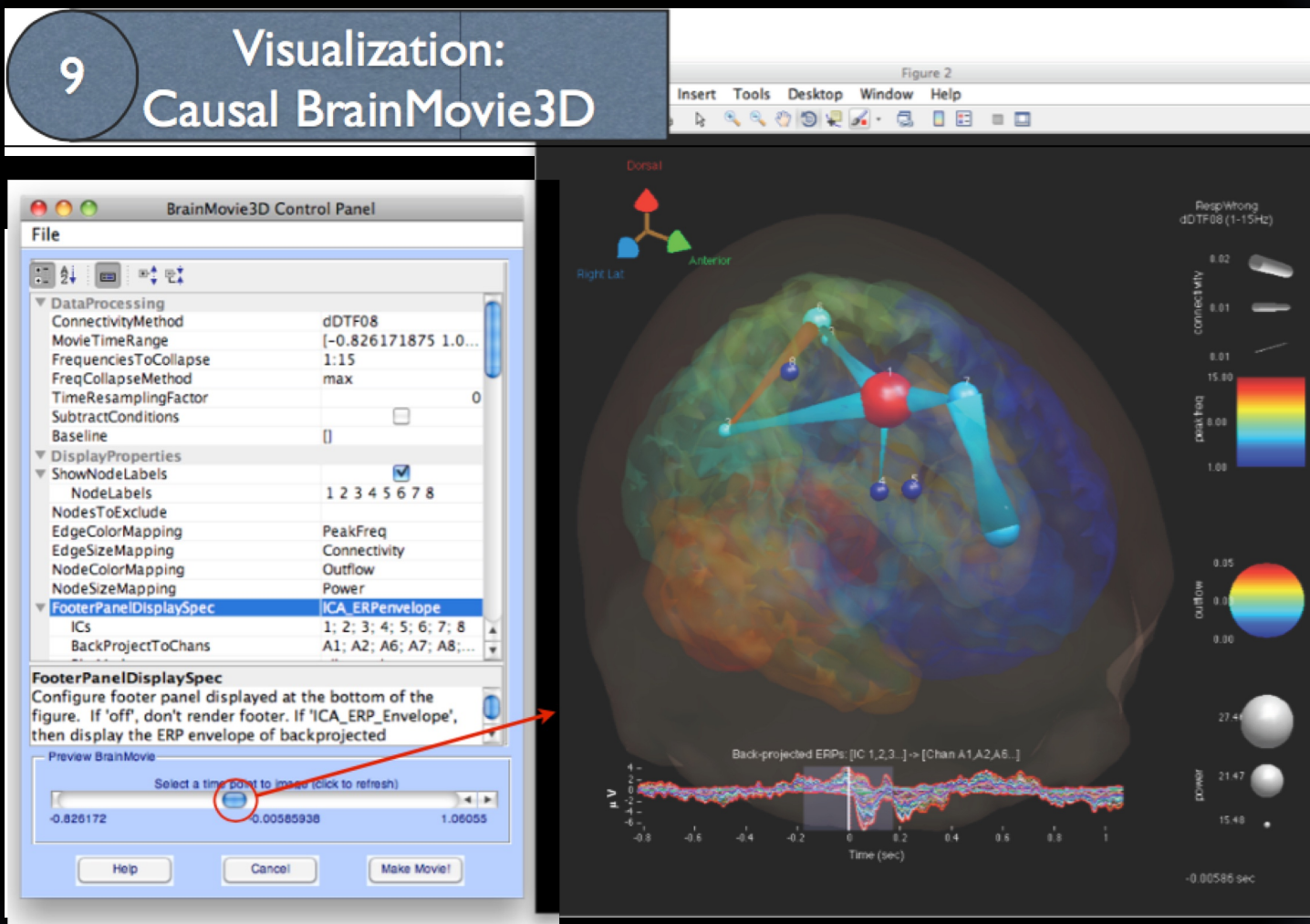






9

# Visualization: Causal BrainMovie3D



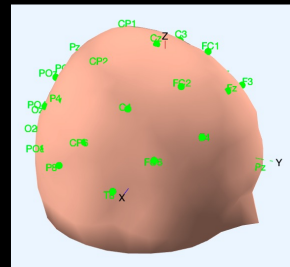
Time-Frequency Analysis of  
EEG Time series

**More Connectivity analysis**



# EEGLAB ROI connectivity plugin

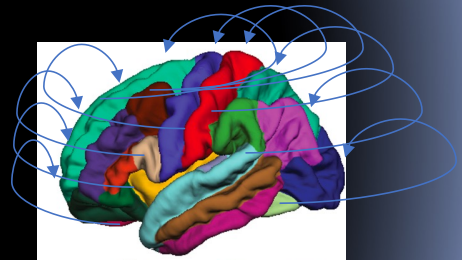
Align electrodes  
with scalp model



Distributed source  
modeling

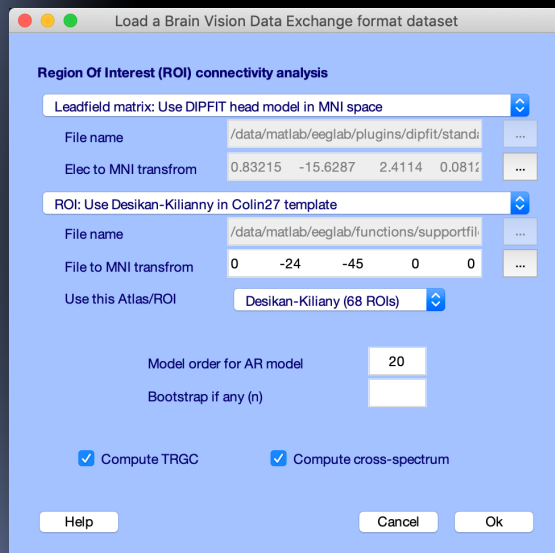
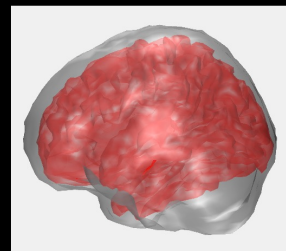


Group voxels in regions  
and compute connectivity



Measures **TRGC**, GC, TRPDC,  
PDC, TRDTF, DTF and **CS**

Align atlas with  
cortex model

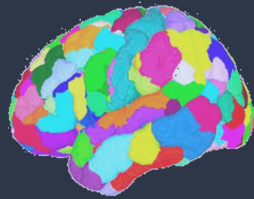


Haufe, S., Nikulin, V. V., Miller, K. R., & Nolte, G. (2013). A critical assessment of connectivity measures for EEG data: a simulation study. *Neuroimage*, 64, 120-133.

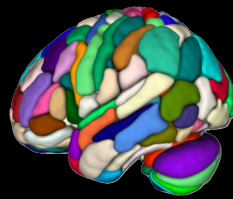
# Connectivity analysis using EEG

Volumetric  
atlases

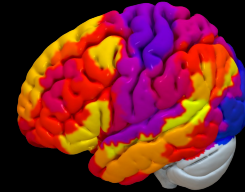
AFNI MNI



Brainnetome

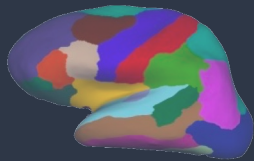


Schaefer 2018

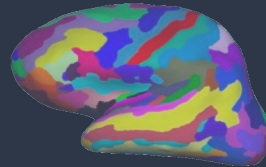


Surface  
atlases

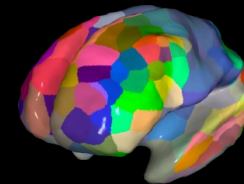
Desikan Kiliany



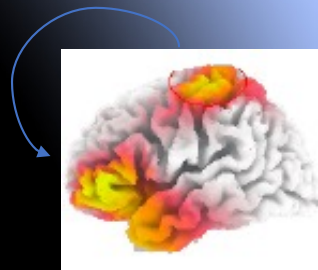
Destrieux



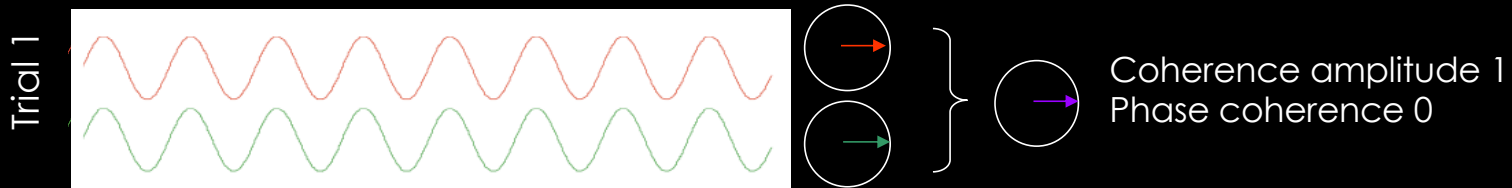
PrAGMATiC



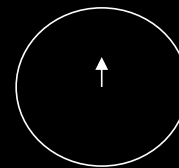
# Cross-coherence amplitude and phase



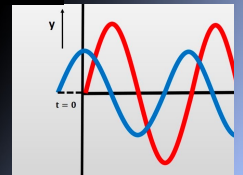
2 areas, comparison on the same trials



COHERENCE = mean(phase vector)

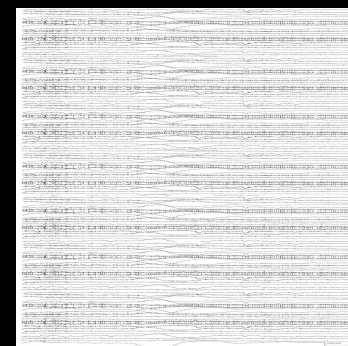
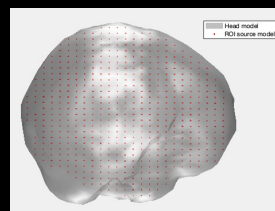
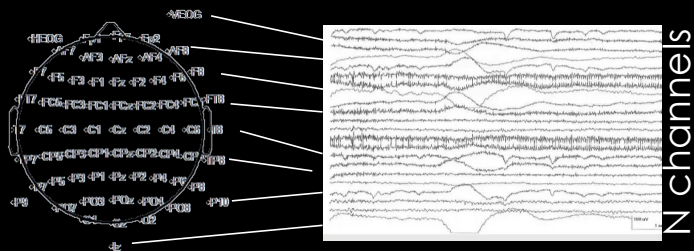


Norm 0.33  
Phase 90 degree



Channel space (~100 dim)

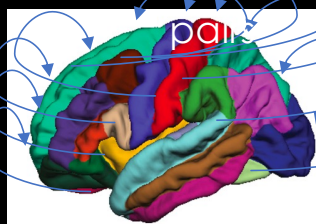
Source space (~10,000)



First ROI

Second ROI

Compute connectivity between all ROI



PCA

PCA

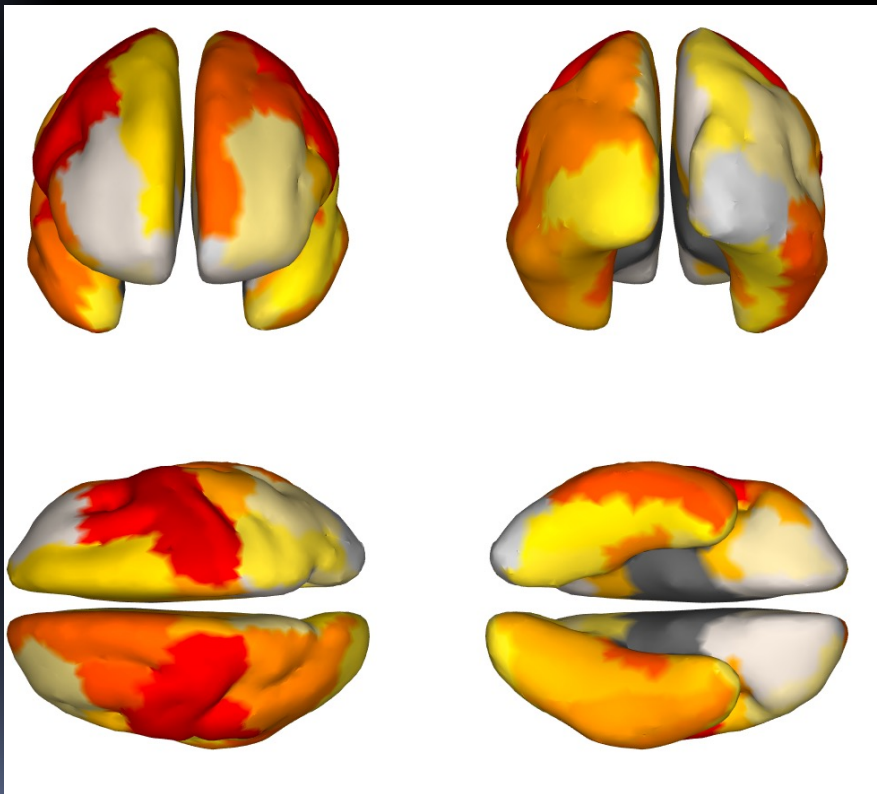
Dim ~ 2 to 4

Dim ~ 2 to 4

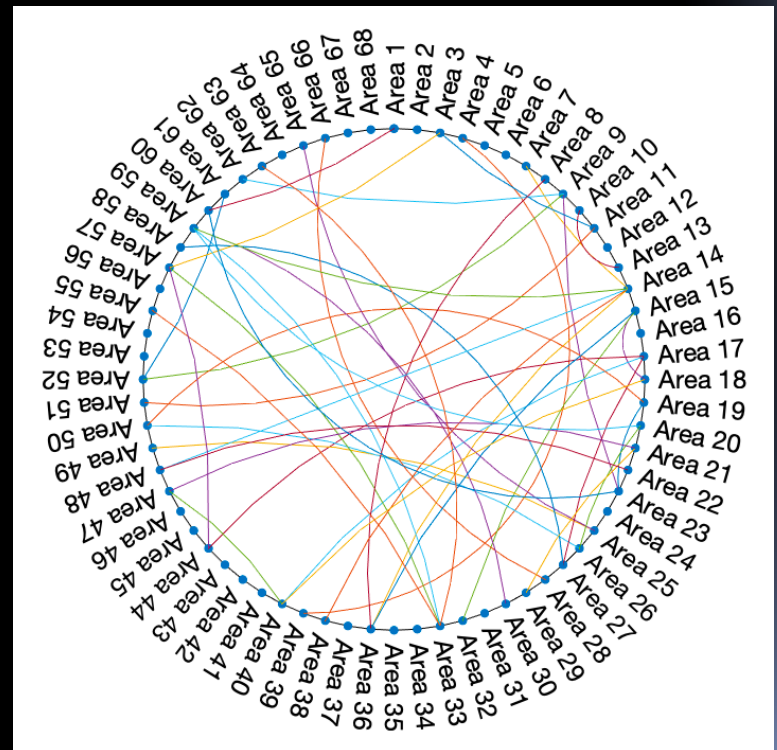


Pairwise connectivity  
TRGC, GC, TRPDC,  
PDC, TRDTF, DTF and CS

Red regions are highly interacting

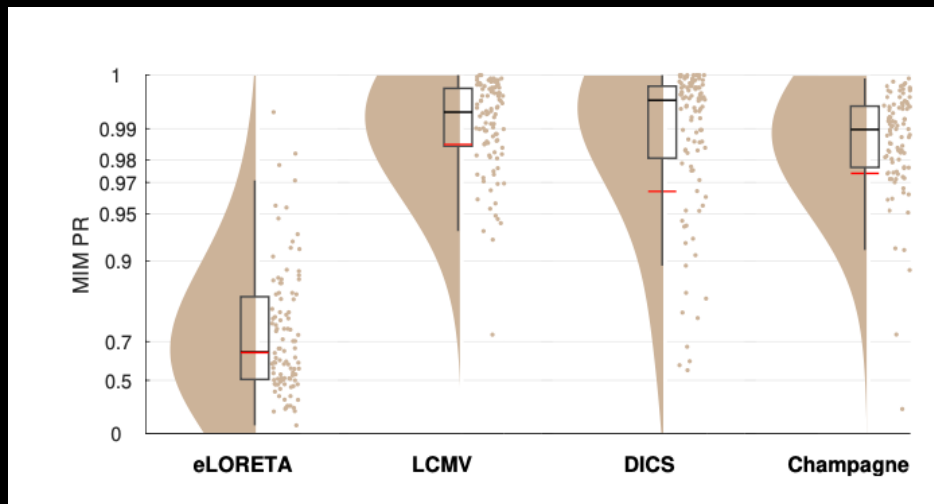


Connectivity matrix between 68 ROIs



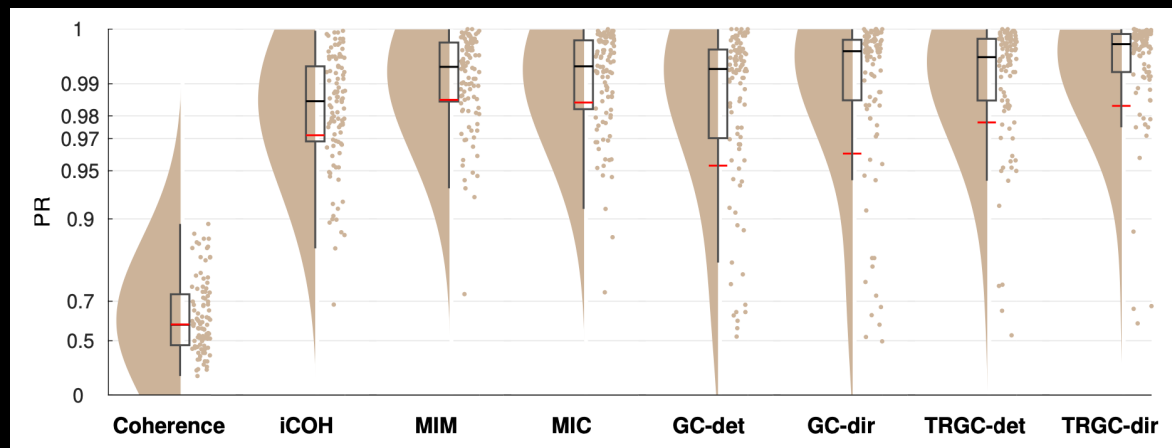


## Inverse method

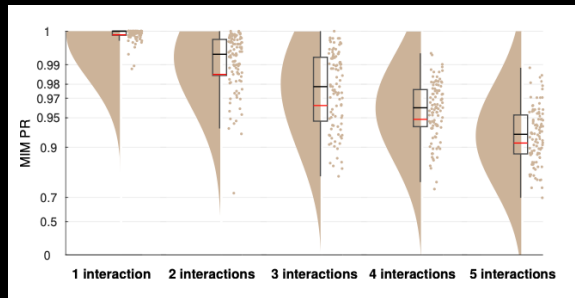




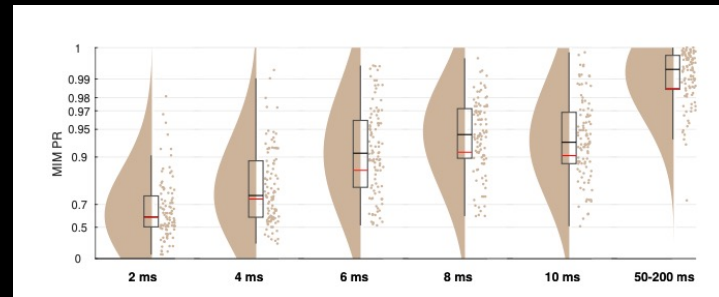
## Connectivity method



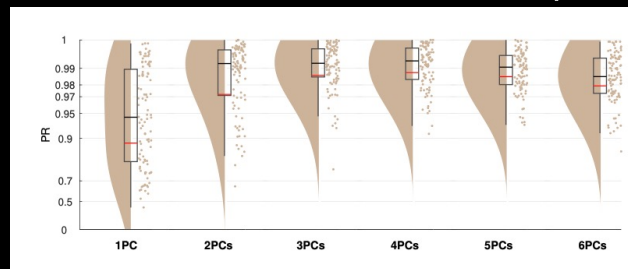
## Number of interactions



## Delay between sources



## Number of PCA comp.



## Data intake

- Stationary continuous data
- About 100 Hz
- 2 second data chunks (or epochs)
- Same length of data for each condition
- No dynamics – static image

# The end/La fin

