Exercise 3.16

In [104…
```
import numpy as np
from numpy.linalg import matrix_power
from scipy.linalg import orth

def find_fist_singular_vector(a):
    B = np.transpose(a)@a
    x = np.random.rand(B.shape[0],1)
    threshold = 0.002
    difference = 1
    k=1
    new_x=x
    while difference > threshold:
        new_x = (matrix_power(B,k)@x)
        scalar = np.amin(new_x)
        scalar = 1/scalar
        new_x = scalar*new_x
        difference = np.linalg.norm(new_x-x, ord=2)
        x = new_x
        k = k+1
        if(k == 50):
            print("Had to break")
            break

    return new_x/np.linalg.norm(new_x)

def find_singular_vectors(k,a):
    B = np.transpose(a)@a
    x = np.random.rand(B.shape[0],k)
    x = orth(x)
    new_x = x
    i = 1
    difference = 1
    threshold = 0.002
    while difference > threshold:
        new_x = (matrix_power(B,i)@x)
        new_x = orth(new_x)
        difference = np.linalg.norm(new_x-x,ord=2)
        x = new_x
        i = i+1
        if(i == 100):
            print("Had to break")
            break
    return new_x
```

In [99]:
```
A = np.matrix([[1,2,3,4,5,6,7,8,9,10],
               [2,3,4,5,6,7,8,9,10,0],
               [3,4,5,6,7,8,9,10,0,0],
               [4,5,6,7,8,9,10,0,0,0],
               [5,6,7,8,9,10,0,0,0,0],
               [6,7,8,9,10,0,0,0,0,0],
               [7,8,9,10,0,0,0,0,0,0],
               [8,9,10,0,0,0,0,0,0,0],
               [9,10,0,0,0,0,0,0,0,0],
               [10,0,0,0,0,0,0,0,0,0]])
```

1).

In [100…
```
print(find_fist_singular_vector(A))
```

```
[[0.31975061]
 [0.36962503]
 [0.39811309]
 [0.4039189 ]
 [0.38728043]
 [0.34995869]
 [0.29512625]
 [0.22716237]
 [0.15136863]
 [0.07362362]]
```

2).

In [105…
```
print(find_singular_vectors(4,A))
```

```
[[-0.3197506   0.45784552 -0.42415456  0.39364456]
 [-0.36962502  0.3936509  -0.24288284  0.02848698]
 [-0.39811309  0.25497036  0.07043602 -0.36153369]
 [-0.4039189   0.06980555  0.33936334 -0.38322689]
 [-0.38728043 -0.12450888  0.41233765 -0.01439342]
 [-0.3499587  -0.2887672   0.24775341  0.37382728]
 [-0.29512626 -0.38972804 -0.06268814  0.39082214]
 [-0.22716239 -0.40675711 -0.34546459  0.01996826]
 [-0.15136864 -0.33594883 -0.44265159 -0.36463231]
 [-0.07362363 -0.19090282 -0.30058613 -0.37498211]]
```

In [ ]:

In [ ]: