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Investigation of static features for improved APT malware identification

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Abstract

Questa tesi parla di me.

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Chapter 1

Introduction

Chapter 2

Related works

This chapter presents the related works we started from to develop this work. Firstly we introduce a paper from Laurenza et al. that explain how to build a malware triage for APT classification. The second work, from Caliskan et al., shows how is it possible to de-anonymize different programmers even with a compiled executable. The last work of Dubyk propose an approach for malware similarities based on the Rich Header.

2.1 Malware Triage Based on Static Features and Public APT Reports

Laurenza et al. show that it is possible to help an analyst lightening the number of samples to analyze. They proposed an architecture for sample prioritization, which, based on a rank score, decides which sample has the priority to be further inspected by an analyst. In this way, it is possible to avoid wasting time analyzing samples that are not important.

They decide to rely only on static analysis instead of dynamic analysis to improve the speed of processing. In this architecture, the time elapsed for analyzing a classifying the samples is more important than the accuracy of the classification. Since it relies on static analysis, there is no need for sample execution, or to set up a complex virtualized environment. Every sample is processed, and some features are extracted from the header. The knowledge base created is used to classify new malware.

They proposed a malware triage architecture, based on the identification of malware similar to other malware known to be related to some APTs campaign. The idea is to collect public APT reports and their related samples. Then, extracting features from the samples and assigning them to the class of the APT they belong to. Those features vectors are used to train a classifier.

Figure 2.1 shows the architecture of both the training and testing phases. The APTs loading plugin frequently loads the information on APT crawled from public reports on the internet. The loading plugin feeds the system with new samples from different sources. The features extraction phase produces the features vectors from the malware, continuously updated by the previous loading plugin. In the classifier phase, a classifier is trained with features vector.

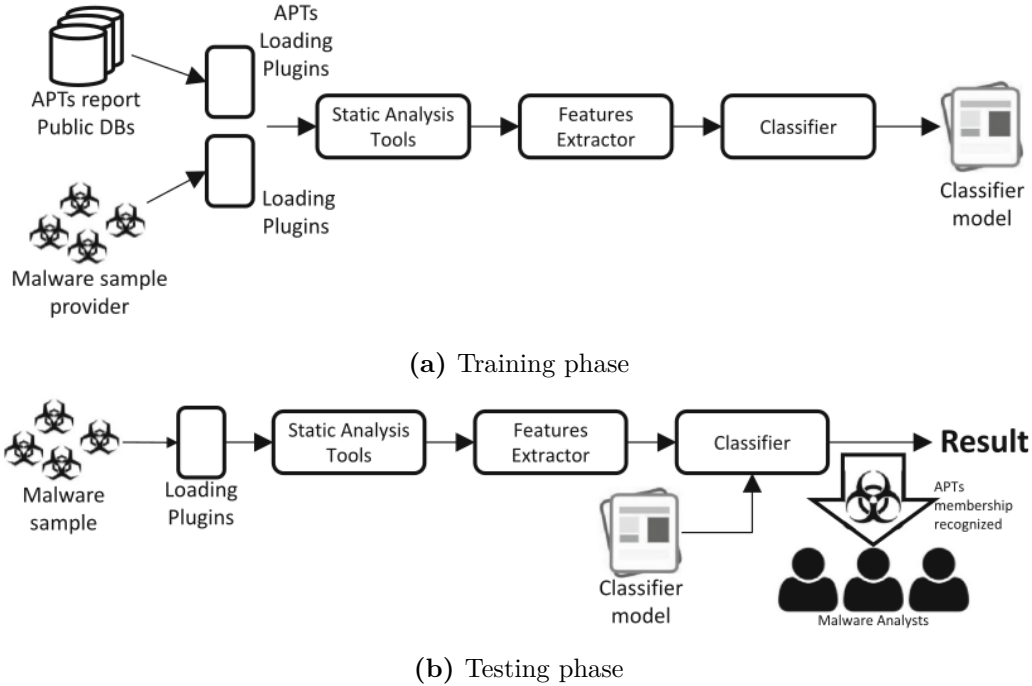


Figure 2.1. Malware triage flow.

In the analysis phase, novel samples follow the same pipeline; the features extraction stage extracts the features vector that is passed to the classifier. If the output of the classifier is positive, i.e., the sample is related a know APT, then the sample follows a different path, and is sent a human analyst for further inspection, otherwise it is discarded.

Unfortunately, this work has some drawbacks. First of all, it is possible to identify only samples correlated to a known APT campaign, if the sample belongs to a new never investigated APT, then it is impossible to detect it. Furthermore, even if the executable belongs to a known APT, there is no guarantee that the classifier detects it because it just relies on information present in the header of the file. The malware writer can hijack that information to mislead the model.

BOOOO

The idea in our work is to boost up Laurenza's et al. work, introducing different features without slowing down the entire flow. As written in their future works, they wanted to extend the architecture to new kind of features, based on code analysis.

The dataset used by Laurenza et al. is **dAPTaset**, a public database that collects data related to APTs from existing public sources through a semi-automatic methodology and produces an exhaustive dataset. Unfortunately, the dataset is not big enough and is not perfectly balanced. It contains only 2086 samples because there are not many samples belonging to an APT campaign. Instead, the majority of public analyzed samples are just malware.

2.2 De-anonymizing Programmers from Executable Binaries

In this paper, Caliskan et al. presented their approach to de-anonymize different programmers from their compiled programs. They used a dataset of executables from Google Code Jam, and they show that even after compilation the author fingerprints persist in the code, and it is still possible to de-anonymize them.

Their approach was to extract distinct blocks of features with different tools and then analyze them to determine the best ones to describe the stylistic fingerprint of the authors precisely. Firstly, with a disassembler is possible to disassemble the binary and to obtain the low-level features in assembly code.

Then with a decompiler, they extracted the **Control Flow Graph** and the **Abstract Syntax Tree**. They determine the stylistics features from those four documents.

In particular, the tools used are **ndisasm radare2** disassembler for the disassembled code and the Control Flow Graph; **Hexray** decompiler for the pseudocode, which is passed as input to **Joern**, a C fuzzy parser, to produce the **Abstract Syntax Tree**.

They used different types of features selection techniques to reduce the number of features to only 53. They trained a RandomForest Classifier with the dataset created to de-anonymize the authors correctly.

This paper is an entry point for our work, and we tried to apply the same approach to the apt triage problem. However, the tools used by Caliskan et al. are outdated and no more maintained, so we decided to use the novel open-source tool ghidra to write the script and extract the information we want. In this way, we significantly reduced the amount of time for feature extraction.

2.3 Rich Header

The work of Maksim Dubyk [1] shows how the rich header produces a robust series of data points that can be exploited in static PE-based malware detection. The Rich Header is an undocumented section of *Portable Executable* (**PE**) header and provides a view of the environment where the executable was built. Firstly, Dubik shows the location of the Rich Header, how to understand and decrypt it, and how to extract it. Then, he shows different techniques to leverage the header for PE-based malware classification. The Rich Header is part of our features vector.

When building a PE, there are two distinct phases. The first one is the *compilation phase*, where the high-level instructions from programming language are compiled into machine code, executable by the computer. The second one is the *linking phase*, a combination of those different machine code objects into a single executable. The act of combining different objects creates the Rich Header. However, only executables compiled with Microsoft Linker contain the rich header, other compilers, such as gcc or .Net, do not have it.

Analyzing an executable with a hexdump, the Rich Header starts from location

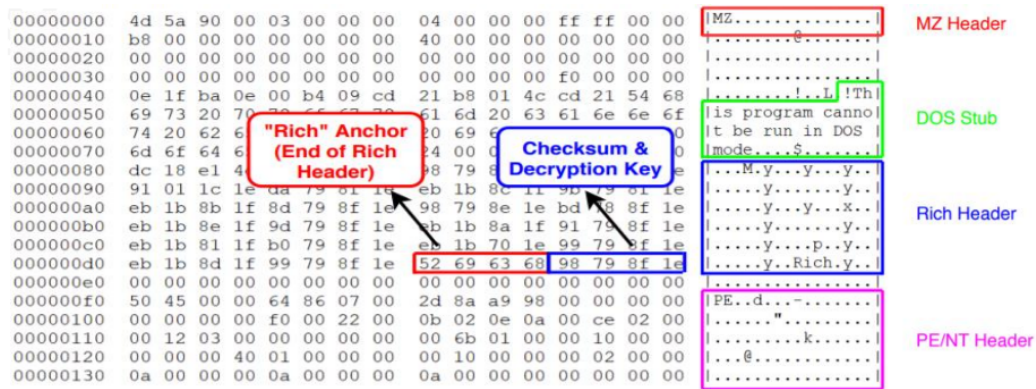


Figure 2.2. Hexview of cmd.exe

0x80 until the bytes sequence 0x52696368, which means "Rich" in ASCII. Figure 2.2 shows the location of Rich header and the ending string "Rich". The content of the rich header is encrypted, and the corresponding decryption key and checksum are located right after the "Rich" string.

The algorithm that computes the decryption key takes advantage of two checksum algorithms. The first checksum is generated from the bytes that make the DOS header, but with the `e_lfanew` field zeroed out[2]. The second checksum is the combination of each value in the array generated. The outputs of the checksum algorithms are summed together and then masked with the bytes 0xFFFFFFFF, the key generated is then used to encrypt the rich header section using the XOR.

It is straightforward to decrypt the rich header section. The key found after the "Rich" string is XORed backward with the chunks of the section until the end string "DanS" is found.

The decrypted rich header is an array that stores metadata related to each phase of the linking process. Each array's element is an 8-byte structure that contains three fields: *product identification* (**pID**), *product version* (**pV**), and a *product count* (**pC**). Those numbers identify the Microsoft product used in that linking phase. However, since the Rich Header is an undocumented section, there is no official mapping of pID with Microsoft products. Nevertheless, some researches partially mapped out some pID with known compilers [3].

To calculate the rich header of each sample, we used the python script provided in [1].

2.4 Advanced Persistent Threat

APT stands for Advanced Persistent Threat, a kind of sophisticated attack which requires an advanced level of expertise and aims to remain persistent on the attacked infrastructure.

The term APT can refer to a persistent attack with a specific target, or it can refer to the group that organized the attack, sometimes the group is affiliated with some sovereign state.

To understand better what is an APT, we need to decompose the word:

Advanced: the people behind the attack have an advanced level of expertise, resources, and money. They usually do not use known malware, but they write their malware specific to the target they want. Moreover, they can gather information on the target from the intelligence of their country of origin.

Persistent: The adversary does not aim to gain access in the most number of system, but rather to have persistent access to the infrastructure. The more time they remain undiscovered in the organization's network infrastructure, the higher are the chances of lateral movement, the greater are the information they can gather. Persistent access is the key to every APT.

Threat: As said before, this is an organized threat, with a strategical vision of what to achieve. It is not an automatic tool that attacks everything trying to gather something. It is a meticulously planned attack that aims to obtain certain information from a given organization. [4]

In general, APTs aim to higher-value targets like other nations or some big corporations. However, any individual can be a target. FireEye publish a report each year about the new APT campaign, the diagram below states which industry is the most attacked in the last year.

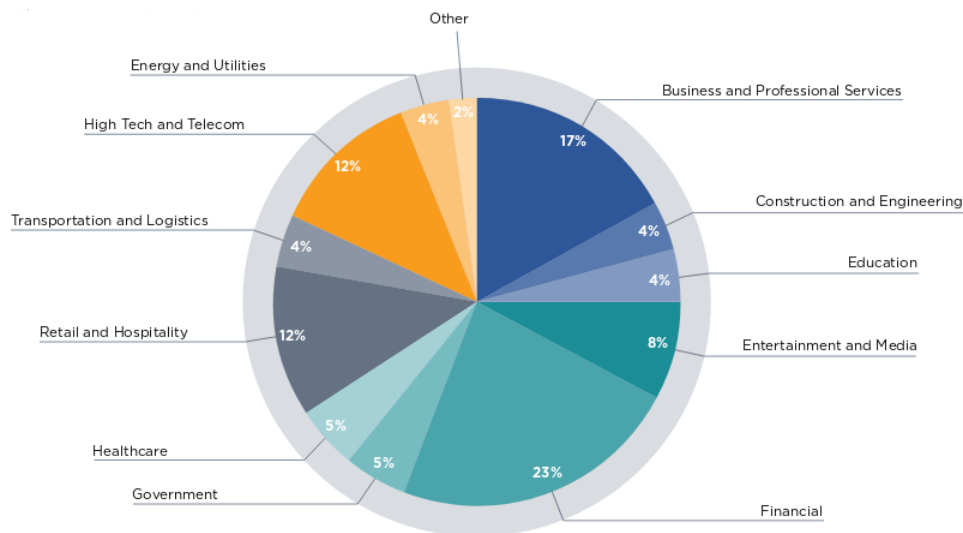


Figure 2.3. Diagram of industry target

A point of particular concern is the retargeting, in the Americas, 63% of the companies attacked by an APT, are attacked again last year by the same or similar group. In the Asian and Pacific areas, this is even worse, 78% of the industries are hacked again. [5]

Advanced persistent threats, contrary to regular malware, are composed of different phases, each of which has an important role.

The attack is decomposed into smaller steps, for example, if a group of hackers wants to attack a CEO of a given company, they will not send directly to the CEO a phishing email, because it's likely that he has a complex system of security and

Region	2017	2018
Americas	44%	63%
EMEA	47%	57%
APAC	91%	78%
Global	56%	64%

Figure 2.4. Retargeting divided by regions

they would be detected instantly.

Instead, the first step would hack a person in the same company with lower permissions that can have minor defense mechanisms. Once they got the first computer, they can explore the network infrastructure of the organization, and then decide which action is the best. They could cover their track from the log system, or locate the data they need or send a phishing email to the CEO from the owned user.

So how does an APT work? Fireeye described their behavior in six steps. [6]

1. The adversary gains access into the network infrastructure, installing a malware sent through a phishing email or by exploiting some vulnerability.
2. Once they comprised the network, the malware scans all the infrastructure looking for other entry points or weaknesses. It can communicate with a Command & Control server (C&C) to receive new instructions or to send information.
3. The malware typically establishes additional points of compromise to ensure that the attack can continue even if a position is closed.
4. Once the attackers have a reliable connection to the network, they start dumping data such as usernames and passwords, to gain credentials.
5. The malware sends the data to a server where the attackers can receive the information. Now the network is breached.
6. The malware tries to cover its tracks cleaning the log system, but the network is still compromised so the adversary can enter again if they are not detected.

Chapter 3

Preliminaries

forse da ampliare disassembler e decompiler

This chapter talks about the information needed to understand the work we did and the choice we made. We firstly introduce the reverse engineering problem, with all its components. Then we present the state-of-the-art in reverse engineering tools, why we choose Ghidra, and its features. Lastly, we discuss scikit-learn and Jupyter notebook, both used in machine learning tasks.

3.1 Reverse Engineering

Reverse engineering is the process of decomposing a human-made object to understand the underlying architecture, how it works, or to extract some information from it. This process can be applied in various fields, such as computer science, electronic, mechanical, or chemical [7].

We focus on reverse engineering applied to computer science.

The Institute of Electrical and Electronics Engineers (**IEEE**) states that reverse engineering is *"The process of analyzing a subject system to identify the system's components and their interrelationships, and to create representations of the system in another form or at a higher level of abstraction."*, where the *"subject system"* is referred to the software development [8].

When somebody writes a software, he writes it with a language that is understandable by a human, for example, C or Java. But the computer can not read it, so the programmer needs to compile the source code to let the computer understand what the software should do.

The compiling process is the process of translating the source code into a language understandable by a computer. But once the program is compiled, a human can no more read it, unless it has the corresponding source code.

If we want to understand a binary executable, but its source code is not available, we need to reverse it. There are different techniques of reversing for binary executable: disassembling the binary using a disassembler, decompiling the binary with a decompiler, or analyzing the information exchanged with a bus sniffer or a packet sniffer.

3.1.1 Disassembly code

Assembly language is a low-level programming language that has a substantial correspondence with the architecture's machine code. The program used to convert the assembly instruction to machine code instruction is called assembler. Since the assembly depends on the machine code, there is an assembly language, with its assembler, for each architecture.

With a disassembler, it is possible to revert the actions made by the assembler, so it's possible to translate machine code instruction to assembly language. The output code is formatted for human readability.

3.1.2 Decompiler?

The decompiler is a program that takes as input a binary executable and produces as output a high-level representation of the source code of the program. It is the opposite of a compiler, which, given a source code, generates an executable. The output of the decompiler can be recompiled, and the executable will have the same behavior as the first one.

Unfortunately, the decompiler is not able to revert correctly the executable, and often it produces obfuscated code. The obfuscated code behaves in the same way, but it is harder for an analyst to understand it.

3.1.3 Control Flow Graph

The control flow graph is a representation, in graph format, of the execution flow of a program or application. Frances E. Allen developed it in [9].

The Control Flow Graph is a directed graph, and it is process-oriented. Each node represents a basic block, a sequence of instructions that are executed consecutively without any jump. The edges of the graph represent the path of the execution. The graph represents all the possible paths that the program can take.

There are two types of blocks: *entry blocks* and *exit blocks*. The *entry blocks* are the one where the flow starts; the *exit blocks* the one where the flow ends. Figure 3.1 represents some examples of Control Flow Graph of different statements and loop.

The CFG is useful in code analysis, to determine if some portion of the code is inaccessible.

3.1.4 Cyclomatic Complexity

Cyclomatic complexity is a software metric to determine the complexity of a single function, a module, a method, some classes, or the entire program.

It is measured starting from a control flow graph of the program and indicates the number of linearly independent paths of it.

The formula to calculate the complexity is:

$$M = E - N + 2P,$$

where E indicates the number of *edges*, N specifies the number of *nodes*, and P indicates the number of *connected components*.

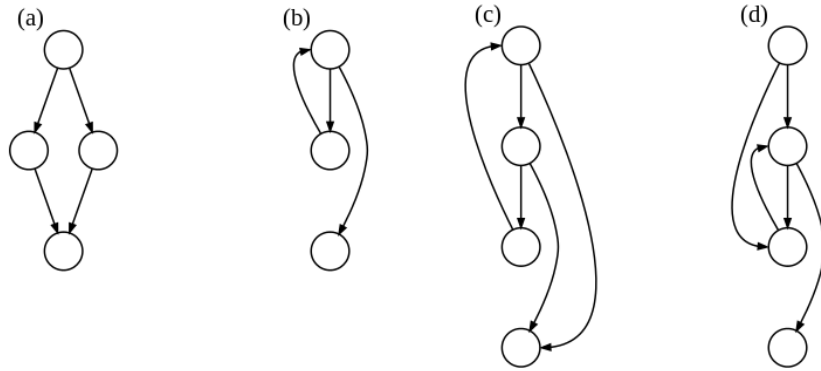


Figure 3.1. CFG of different statements and loops.

- (a) if-then-else
- (b) while loop
- (c) natural loop with two exit points
- (d) loop with two entry points

If the entry point and exit point are connected, we have a strongly connected graph, and the formula for complexity is slightly different:

$$M = E - N + P$$

Algorithm 1 Example of function with different loops and statements

```

1: while not EOF do
2:   Read record
2:   if field1 = 0 then
3:     total  $\leftarrow$  total + field1
3:     counter  $\leftarrow$  counter + 1
4:   else
4:     if field2 = 0 then
5:       Print counter, total
5:       counter  $\leftarrow$  0
6:     else
6:       total  $\leftarrow$  total - field2
7:     end if
8:   end if
8:   Print End record
9: Print counter

```

Algorithm 1 shows an example of function with different loops and statements. In Figure 3.2 there is the corresponding Control Flow Graph. The numbers before the lines represent the id of the basic block to which they belong, i.e. the graph's nodes.

Being **node #1** the entry node, and **node #9** the exit code, we can calculate manually the number of independent path of the function:

- 1, 9

- 1, 2, 3, 8, 1, 9
- 1, 2, 4, 5, 7, 8, 1, 9
- 1, 2, 4, 6, 7, 8, 1, 9

Using the formula presented above is possible to calculate the complexity of the function that is equal to 4. $M = 11 - 9 + 2 \times 1 = 4$, where 11 is the *number of edges*, 9 the *number of nodes*, and 2×1 the *number of connected components*. The complexity calculated equals the number of independent path of the graph.

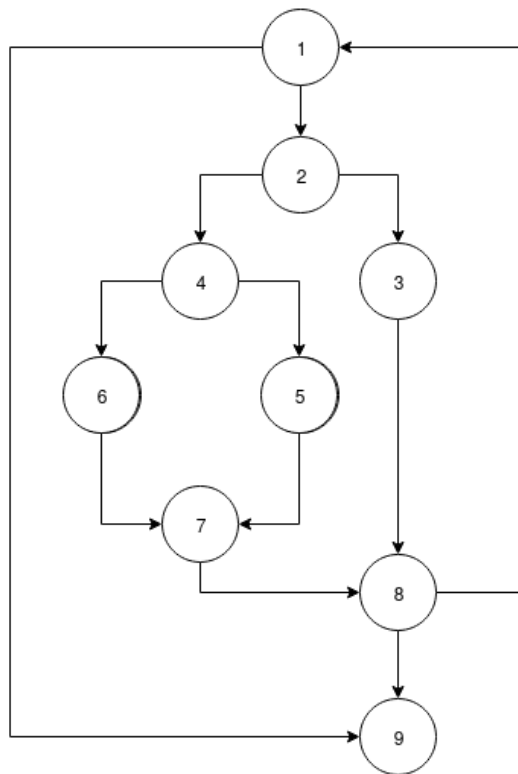


Figure 3.2. Control flow graph of function 1

3.2 Reverse Engineering tools

There are a lot of tools in the market that helps in reverse engineering. Some of them have tons of functionality, and others can do just a few things.

The most important is **IDA**, a reverse engineering software developed by Hex-Rey that can achieve different things. It comes in a free version and a pro version.

It is compatible with most of the executable from different OSes, such as PE, ELF, Mach-O, or even raw binaries. It has extensive support and compatibility with almost every family processors.

The free version contains all the features necessary for some basic reverse engineering; it has a disassembler and performs an automatic analysis of the sample, determining the API used, which parameters are passed to them, and other information.

The analyst can navigate the code and add some notation, rename functions, and variables, to better understand the behavior of the binary. However, most of the functionality works only with the PRO version, which costs 9000\$.

The main features of IDA PRO are the debugger that lets the analyst debug the executables, the possibility of writing scripts to run against the sample, and a disassembler to revert the binary into some source code. [10]

Another famous framework for RE is **radare2**. It is free and offers a decompiler and a disassembler. It is compatible with tons of processors, and executable types. It comes with a set of command-line utilities that can be used individually or together, but it also has a graphic interface to navigate the code and the possibility of running scripts. However, it is not user-friendly as other tools [11].



Ghidra is a novel open-source reverse engineering framework developed by the National Security Agency (NSA). It helps analyze malicious code and malware like viruses and can give cybersecurity professionals a better understanding of potential vulnerabilities in their networks and systems [12]. It is a direct competitor of IDA pro because it offers almost all the features that IDA has, but Ghidra is entirely free. It is possible to run a headless version

of Ghidra, and control it by remote. We installed it on a virtual machine on a server and use it to run headless scripts on the executables to extract information about the binary. Ghidra does not have a large community and support because it was released last year, but it is a valid and complete tool for RE.

We choose to run our tests on **Ghidra** for different reasons. First of all, it is entirely free and open-source.

Secondly, it has an headless version of the framework. The possibility of a headless version was perfect for our needs because we can let it run on a server, always powered on, without bothering about resource consuming.

Moreover, we wanted to simplify as much as possible the extraction of features, and we do not want merging results from different tools, so we decided to use only one software.

Last but not least, the scripting part of Ghidra was perfect for running analysis and extracting information from the samples.

The only inconvenient is that, since it was released less than a year ago, the documentation, the support, and the community are not well developed, so at first was hard understanding how the software works.

3.3 Ghidra

This section will cover the Ghidra's features regarding the disassembled code, de-compiler, control flow graph and complexity presented above.

3.3.1 Disassembled code

The extraction of disassembled code was an easy and fast task. The documentation provides all the information on how to correctly use the disassembler.

Ghidra does not have a functionality to extract all the disassembled code, like in the GUI. But it is possible, for each function, to iterate the instructions in a given address space range. The instruction object has a `toString()` method that returns the disassembled line, that will be used to create the features needed.

3.3.2 PCode

Pcode is a register transfer language developed by NSA for the reverse engineering framework Ghidra. The idea behind PCode is to create a language as general as possible, to let it adapt to as many different processors architecture. An intermediate language that can model the behavior of different processors is fundamental to develop a comprehensive reverse engineering framework.

The idea behind pcode is that each processor instruction can be expressed as a sequence of pcode. Developers translated each instruction into a sequence of pcode operation as input and output variables (**varnodes**).

The entire set of single pcode instruction comprises a set of arithmetic and logic instructions that almost all processors perform. The direct translation of the instructions into those operations is called raw-pcode, which can be used to emulate a single processor instruction directly. NSA developed the pcodes to facilitate the construction and the analysis of a data flow graph of disassembled instructions.

A p-code operation is the analog of a machine instruction. All pcode operations have the same format; they have one or mode varnode as input, and optionally they can have an output. Only the output varnode can be modified.

Address Space

The address space for p-code is a generalization of RAM. It represents an indexed sequence of bytes in memory that pcode can read and write into it. The address space has an identifying name, a size indicating the number of distinct indexes of memory, and an endianness that specify the encoding used to store integers and multi-byte values into the space address.

A regular processor has a ram space to model memory accessible via its data bus, a register space to model the processor's registers, and usually a constant space to store all the constants used by pcodes. All the data that pcodes handle must be stored into an address space. Pcode generally uses a temporary address space to store intermediate values when modeling the processor's instructions. The implementation of a processor can have as many address spaces as it is needed.

Varnode

A varnode is a generalization of a register or memory location and has the functionality of handle the data manipulated by pcodes. It is composed of an address space, an offset into the address space, and a size. A varnode is a sequence of contiguous bytes that can be treated as a single value. The address and the size identify the varnode. Even if they have no type, some pcode operations can cast them into three types: integer, boolean, or floating-point.

In the case of integer values, the pcode operation represents the varnode using the endianness linked with the address space. In the case of floating-point, the operation uses the encoding of the varnodes that depends on its size. In the case of boolean values, the varnode has a single byte that can be 0 for false, 1 for true.

If the varnode's address space is in the constant space, the varnode is a constant or an immediate value. In this case the size of the varnode is the size or the precision available for the encoding of the constant.

3.3.3 Control Flow Graph

We rely on Ghidra's Pcode representation to build our dataset for *Control Flow Graph*. Ghidra contains three different scripts for analyzing the flow of the program, and we studied those scripts to understand how Ghidra manages the Pcode and their flow. The script iterates all the functions of the given sample and generates a .json file with the extracted data.

Ghidra offers a `DecompileInterface`, a class that can decompile a function, and that returns an object `DecompiledResult` with all the information needed. It is also possible to pass different options to the `DecompileInterface` using the `DecompileOption` class. The resulting object contains an instance of `HighFunction`, a high-level abstraction associated with a low-level function made up of assembly instructions. The `HighFunction` object offers the possibility to iterate over the `BasicBlocks` of the corresponding function so we can analyze all the blocks and create our graph.

The graph is composed of an array of basic blocks, each of which has an index, a list of pcodes, and two lists, one containing the indexes of the previous basic blocks and the other one the indexes where the basic block points, i.e., the flow of our function. The pcodes have a field with the associated pcode operation, a list of input varnodes, and a possible output varnode.

The main problem encountered running the script, is the decompilation time. Some functions were intricate, and when it comes to decompile, Ghidra can take a very long time, even 25 minutes per sample. Furthermore, the `DecompileOption` has a field indicating the maximum dimension of the payload of the decompiled function. The default value is 50MB, but for some specific functions, it is still low, and we needed to increase it to 500MB correctly decompile all the functions.

3.3.4 Cyclomatic Complexity

Ghidra offers a class to compute the complexity of a function, `CyclomaticComplexity`. This class has a method to calculate the cyclomatic complexity of a function by decomposing it into a flow graph using a `BasicBlockModel`. During the decompilation, we calculate the complexity of each function and stores it into the .json file.

3.4 Scikit-learn

Scikit-learn is a Python module integrating a wide range of state-of-the-art machine learning algorithms for medium-scale supervised and unsupervised problems.

It is open-source, commercially usable, and contains many modern machine learning algorithms for classification, regression, clustering, feature extraction, and optimization. For this reason, Scikit-Learn is often the first tool in a Data Scientists toolkit for machine learning of incoming data sets. [13]

We choose Scikit as a machine learning library because it is the most used in literature, and it has a great community and support. Moreover, it offers all the models and methods required by our work.

3.5 Jupyter Notebook

"The Jupyter Notebook is an open-source web application that allows you to create and share documents that contain live code, equations, visualizations and narrative text. Uses include: data cleaning and transformation, numerical simulation, statistical modeling, data visualization, machine learning, and much more" [14].

We choose Jupyter because it excellently fits our need for remote running. In the same server, where we installed Ghidra, we installed Jupyter, and we enabled it to run remotely, with the proper precautions! This setup allows us to work remotely without any problem.

Machine learning tasks are often time and computationally expensive, so running them on a personal computer would be slower due to limited computer resources, and it would keep busy the workstation.

Chapter 4

Features Creation

When we decided which features could be the most representative for our model, we choose to use only static features. We are looking for a framework fast and efficient, that can analyze lots of sample without being resource expensive.

At first, we tried to replicate the work done by Caliskan et al., but we found that most of the tools used depend on software no more maintained. Some of those tools do not work as expected, and others were slow in processing files. To simplify as much as possible the process of analyzing executables, we decided to use only Ghidra as software for extracting features.

Ghidra comes with a headless analyzer, which analyzes and runs scripts on the given sample. The headless version can run in any server, even without a desktop environment. So we built up a virtual machine in the Sapienza network and installed Ghidra there. Unfortunately, Ghidra's documentation is not exhaustive since it was released less than a year ago. The hardest part was understanding Ghidra's APIs and how to exploit them for our purpose. The already made scripts were useful for our task because they contain many approaches for extracting data.

4.1 Disassemble features

The extraction of disassembled code was an easy and fast task. The documentation provides all the information on how to correctly use the disassembler. We wrote a script that extracts the disassembled code for each function and stores it into a .dis file. The script creates a folder for each sample and stores inside the disassembled code.

From the disassembled code, we extracted 5 kinds of various features:

- Entire line unigrams
- Disassemble unigrams
- Disassemble bigrams
- Instruction only unigrams

- Instruction only bigrams

First of all, we stripped out all the hexadecimal and numbers, replacing the regex '+' with the word 'number', and '0[xX][0-9a-fA-F]+' with the word hexadecimal. Stripping the numbers and hexadecimal reduced the possibility of overfitting because some numbers may be unique, and that would create a useless feature.

Furthermore, we create a .csv file for each sample, containing all the features calculated, the md5, used as an identifier of the executable, and the apt name. Then all the files are merged into a big .h5 with all the samples. In the first approach, we stored all the features into a .csv file, but the more features we extract, the more significant were the dimensionality of our dataset. When it comes to reading into python, pandas was very slow in both reading and processing the files. A valid alternative to pandas is Dask, a flexible parallel computing library for analytics, that integrates with pandas, numpy, and scikit. However, the dask-ml package lacks some functionalities for the cross-validation and random forest model. Furthermore, It was still slow in reading bigger files, so we decided to find another solution to speed up the process. In the end, we decided to store our dataset into a Hierarchical Data Format (HDF5) designed to store and organize large amounts of data. This format comes with a cost, the files are much bigger, but we drastically improved the speed of reading and processing the dataset.

4.1.1 Entire line unigram

The first block of features is the whole line unigram, we split the disassembled code of each function on the new-line character and then count all the occurrences of different line instructions. We stripped out all the commas because, in the beginning, we saved the dataset to .csv with comma as a separator. For example, the features of the following disassembled function would be:

Table 4.1. Code for function f

push ebx
mov eax, 1
cmp ebx, eax
jle 0xDEADBEEF
add eax, 1
cmp ebx, eax
jle 0xBACADDAC
mov eax, 0x400231BC
call eax
ret

Table 4.2. Entire line unigrams

Feature	Value
push ebx	1
mov eax,number	1
cmp ebx,eax	2
add ebx, number	2
jle hex	2
mov eax, hexadecimal	1
call eax	1
ret	1
apt	PatchWork
md5	1234dc...eb121

4.1.2 Disassemble unigrams and bigrams

For this block of features, we split the entire line in instruction, eventual registers, or numbers. We first divided on the first space, and then if the second half of the string

still contains data, we split for all the commas to get the single registers/number. the line "mov eax, 0x12" would be split in the following array: ["mov", "eax", "hexadecimal"] . As before, we counted the occurrences of every word in the file.

For the unigram files, we only considered as a feature every word we would obtain after splitting the string. For the bigram files, instead, we considered as a feature the pair of words in the file.

Furthermore, we added a start token ("`<s>`") at the beginning of the function file, and an end token ("`</s>`") at the end of the file. We concatenate the first and second element of the bigram with the the string "=>" The features generated from the same disassembled code would be the following:

Table 4.3. Disassemble unigrams

Feature	Value
push	1
ebx	3
mov	2
eax	6
number	2
cmp	2
jle	2
hex	3
add	1
call	1
ret	1
apt	PatchWork
md5	1234dc...eb121

Table 4.4. Disassemble bigrams

Feature	Value
<code><s>=>push</code>	1
<code>push=>ebx</code>	1
<code>ebx=>mov</code>	1
<code>mov=>eax</code>	2
<code>eax=>num</code>	2
<code>num=>cmp</code>	2
<code>cmp=>ebx</code>	2
<code>ebx=>eax</code>	2
<code>eax=>jle</code>	2
<code>jle=>hex</code>	2
<code>hex=>add</code>	1
<code>add=>eax</code>	1
<code>hex=>mov</code>	1
<code>eax=>hex</code>	1
<code>hex=>call</code>	1
<code>call=>hex</code>	1
<code>hex=>ret</code>	1
<code>ret=></s></code>	1
apt	PatchWork
md5	1234dc...eb121

4.1.3 Instruction only unigrams and bigrams

For the last block of features, we decided to study only the frequency of the different instructions in the code, without considering the registry. As before in the bigrams, we added a start and an end token to avoid linking two instructions from different functions. The features from the previous example would be:

4.2 Control Flow Graph features

From the CFG files, we extracted 3 kinds of features:

Table 4.5. Instruction only unigrams

Feature	Value
push	1
mov	2
cmp	2
jle	2
add	1
call	1
ret	1
apt	PatchWork
md5	1234dc...eb121

Table 4.6. Instruction only bigrams

Feature	Value
<s>=>push	1
push=>mov	1
mov=>cmp	1
cmp=>jle	2
jle=>add	1
add=>cmp	1
jle=>mov	1
mov=>call	1
call=>ret	1
ret=></s>	1
apt	PatchWork
md5	1234dc...eb121

- Control Flow Graph unigrams complete
- Control Flow Graph unigrams Pcode only
- Control Flow Graph bigrams Pcode only

4.2.1 Control Floe Graph unigrams complete

This first set of features contains the unigrams of the complete Pcode representation. The key for each feature is the concatenation of the Pcode, the input and output nodes. In particular, we construct the key as follow: `PCODE_nodeoutput#nodeinput*count` of nodes So this .json file is converted to:

```
"pcodes": [ { "code": "CALL", "varnode_in": [ "ram", "const" ], "count": 2 } ] key = call_ram#const*2 **Sistemare qua**
```

We counted the occurrences of each key and build our dataset.

4.2.2 Control Flow Graph Pcode only unigrams and bigrams

These two sets of features contain the unigrams and bigrams of the pcode only. We built the key using only the pcode operator, and then counted the occurrences. For the bigrams, we concatenated as before the key with the string `=>`.

4.2.3 Cyclomatic Complexity

4.2.4 Standard Library

One primary task of reverse engineering binary code is to identify library code. Since what the library code does is often known, it is of no interest to an analyst. Hex-Rays has developed the IDA FLIRT signatures to tackle the problem. Function ID is Ghidra's function signature system. Unfortunately, Ghidra has very few Function ID datasets. There is only function identification for the Visual Studio supplied libraries. Ghidra's Function ID allows identifying functions based on hashing the

masked function bytes automatically.[15]

We exploit this functionality to determine which of the functions belongs to a standard library. Then we calculate the number of standard functions in the given sample and use it as a feature.

4.3 Rich Header features

We used the script in the paper to calculate the rich hash and pv for each of the samples. Sadly, as pointed out in the paper, not every binary is compiled with the rich header; in fact, only 10 samples out of 100 have it. The script extracts the `Product_ID`, the `Product_Version`, and `Product_Count`, we concatenate those numbers with a dash "-" to create a key and set 1 if the sample contains the previous key, 0 otherwise.

Chapter 5

Classification and evaluation

This chapter presents the classification model used in our task, the validation techniques and the features selection algorithm applied to our data.

5.1 Random Forest

Random forest is an ensemble learning method for classification, regression, and other tasks that operates by constructing multiple decision trees at training time and outputting the class that is the mode of the classes (classification) or mean prediction (regression) of the individual trees. [16]

5.1.1 Decision tree

A decision tree is a method used in different machine learning tasks. It uses a tree-like model of decisions and their possible consequences, including chance event outcomes, resource costs, and utility. It is one way to display an algorithm that only contains conditional control statements. [17]

Each graph's nodes represent a test on a different feature, every branch represents the outcome of the previous test, and each leaf represents the decision after analyzing all the features, i.e., the class label.

Unfortunately, the deeper is the graph, the higher are the chances of overfitting the training test. Random forest is a method to average multiple decision trees, trained on different chunks of the training set, to reduce the variance of the output. However, this comes with a cost, an increase of the bias, and a decrease in results interpretability. [18]

5.1.2 Bagging

Bagging, also known as **Bootstrap Aggregating**, is a machine learning meta-algorithm used to improve the accuracy of a model, reducing the model's variance and the likelihood of overfitting.

The noise in the training set affects the prediction of a single tree, but it does not affect multiple trees, as long as they are not correlated to each other. Training multiple decision trees on the same training set would produce trees highly correlated

to each other. Instead, with the bootstrap aggregation technique, we can de-correlate the trees by training them on different parts of the training set. [19]

Given a training set $X = x_1, \dots, x_n$ and the corresponding labels $Y = y_1, \dots, y_n$, the bagging algorithm repeats for B times the following process:

1. The algorithm selects a random sample with replacement of the training set X_b, Y_b
2. The model f_b is then trained on the X_b, Y_b sets.

The predictions for unseen samples x' are calculated by taking the primary vote of each model f_b . The parameter B is free, and it can go from a few hundred to several thousand, depending on the training set size. The optimal value can be found via cross-validation, or by examining the out-of-bag-error. [20]

5.1.3 Bagging in Random Forest

In a random forest, the bagging algorithm slightly differs from the one presented above. The algorithm selects a random subset of features, a process also known as "features bagging".

The reason of this change is the correlation of trees in an ordinary bootstrap sample. If few features are a powerful predictor for the output, then most of the B trees select those features, causing the trees to be correlated. Ho gives an analysis of how bagging and random subspace projection contribute to the accuracy of the model. [21]

Commonly, in a classification problem with p features, the model uses \sqrt{p} features at each split. Those parameters depend on the problem, and they should be treated as tuning parameters. [18]

5.1.4 Features importance

Random forest ranks the features based on their importance to the model. Breiman describes this technique in his paper. [22]

The first step is to fit the model to the data. During this process, the model calculates the out-of-bag-error for each feature and records it. The model determines the importance of the i^{th} feature by permutating the value of the i^{th} feature against the training set, and then it calculates the out-of-bag-error again.

The average of the difference in out-of-bag-error before and after the permutations, normalized by the standard deviation of these differences, represents the feature's importance score.

The higher is the score, the more important is the feature for the model.

However, this method does not work correctly with categorical variables. If these features have different levels, the model is more likely to bias the one with more levels. Using partial permutations and growing unbiased trees, it is possible to reduce these problems. [23]

5.2 XGBoost

XGBoost stands for **eXtreme Gradient Boosting**. It is an open-source optimized distributed gradient boosting library designed to be highly efficient, flexible and portable. It implements machine learning algorithms under the Gradient Boosting framework.

XGBoost provides a parallel tree boosting (also known as GBDT, GBM) that solve many data science problems in a fast and accurate way. The same code runs on major distributed environment (Hadoop, SGE, MPI) and can solve problems beyond billions of examples. [24]

The XGBoost model supports three different forms of gradient boosting: [25]

- **Gradient Boosting** with learning rate
- **Stochastic Gradient Boosting** with sub-sampling at the row, column and column per split levels.
- **Regularized Gradient Boosting** with both L1 and L2 regularization

5.2.1 Gradient Boosting

Gradient boosting is a machine learning technique for regression and classification, which produces a prediction model in the form of an ensemble of weak prediction models.

Gradient Boosting is a modified version of the Boosting algorithm. Boosting is an ensemble method that converts weak learners into strong ones. It adds new models to compensate the shortcomings of by existing models until the error can not be reduced anymore. [26]

Gradient Boosting is a boosting algorithm that uses a *gradient descent algorithm* to minimize the error when adding new models.

Suppose we want to train a model F to predict some values $y = F(x)$. At each step m we have a weak model F_m . To improve the model F_m , the gradient descent algorithm creates a new model F_{m+1} by adding to the previous model an estimator h such that $F_{m+1}(x) = F_m(x) + h(x)$. [27]

To find h the gradient descent algorithm starts from the perfect solution where $F_{m+1}(x) = F_m(x) + h(x) = y$, i.e. $h(x) = y - F_m(x)$. Consequently gradient boosting will fit h to the residual $y - F_m(x)$.

5.3 Cross-validation

Validation is a fundamental technique in machine learning because it allows us evaluating the stability of a model. It limits the problem of overfitting or underfitting, i.e. it makes sure that the model has low bias and variance.

Cross-validation is a model validation technique for assessing how the results of statistical analysis (model) will generalize to an independent data set.

The main idea is to split the dataset \mathcal{D} into a train set \mathcal{T} and a test set \mathcal{R} where the union of this subset is the entire dataset and their intersection is an empty set. [28]

$$\mathcal{T} \cup \mathcal{R} = \mathcal{D}$$

$$\mathcal{T} \cap \mathcal{R} = \emptyset$$

The model is trained on the training subset \mathcal{T} , and then it is evaluated on the validation subset \mathcal{R} that contains unseen data. This process can be repeated many times, using different partitions of the dataset, and then we can calculate the average of the results.

The goal of cross-validation is to test the effectiveness of the model in predicting new data, never seen in the training phase.

We have different kind of cross-validation, leave-p-out cross-validation, k-fold cross-validation, holdout. We are going to analyze the k-fold, the one used in our tests.

5.3.1 KFold

Algorithm 2 K-Fold cross-validation

```

1: for  $k$  from 1 to  $K$  do
2:    $\mathcal{R} \leftarrow$  Partition  $k$  from  $\mathcal{D}$ 
3:    $\mathcal{T} = \mathcal{D} \setminus \mathcal{R}$ 
4:   Train the model with  $\mathcal{T}$ 
5:    $Err_k \leftarrow$  Test the model on  $\mathcal{R}$ 
6:  $Err \leftarrow \frac{1}{K} \sum_{k=1}^K Err_k$ 

```

In K-Fold cross-validation the dataset \mathcal{D} is randomly split in K sets of approximately equals size, such that: [28] [29]

$$|\mathcal{D}_1| \approx |\mathcal{D}_2| \approx \dots \approx |\mathcal{D}_K|$$

$$\bigcup_{k=1}^K \mathcal{D}_k = \mathcal{D}$$

$$\mathcal{D}_i \cap \mathcal{D}_j = \emptyset, \forall i, j \in \{1, \dots, K\}, i \neq j$$

For every k , the model is trained with all the samples, except for the one in \mathcal{D}_k , called first fold. After that the model is tested against the first fold set to estimate its performance. This process, described in Algorithm 2, is repeated for each \mathcal{D}_k , at each stage the error of the predictions is calculated. The estimation of total error of the model is the average of the error in the single execution.

There is no formal rule in the choice of k , usually it is 5 or 10. All you need to know is that as k gets larger, the difference in size between the training set and the resampled set gets smaller; the bias, the difference between the expected and the predicted value, too decreases as k gets larger.

Another fundamental aspect in resampling is the variance or uncertainty. An unbiased method can guess correctly but with the drawback of high uncertainty. Repeating the resampling many times is possible in a big difference between performances. However, this difference decreases as the number of resampling increases.

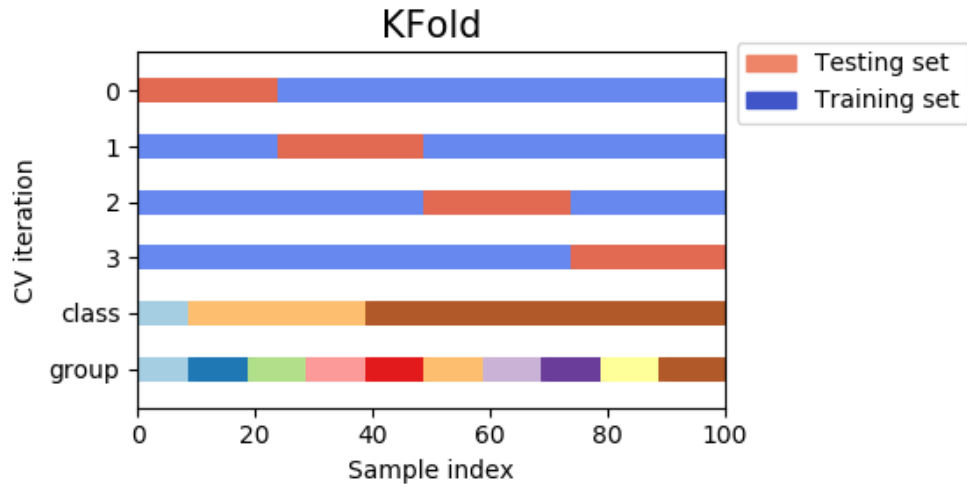


Figure 5.1. Example of 4-Fold cross-validation

The example in Figure 5.1 represents a 4-Fold cross-validation execution. For each iteration the model is trained with a different partition of the dataset, and then the average of the three execution represents the performance of the model.

Stratified KFold

When the dataset's class are not equally balanced, it possible to have some folds without samples of a certain class. The stratification cross-validation ensures that each fold contains roughly the same proportions of classes of the entire dataset. Kohavi in [30] states that normally stratification is better in terms of bias and variance, when compared to cross-validation.

In Figure 5.2 is depicted an execution of stratified k-fold. As illustrated in the figure, a small portion of each class is taken as testing set at each fold.

5.4 Features Selection

Features selection is a growing trend in machine learning problems. As technology advances, there is an increase in the quantity of data we can extract; this means bigger datasets to analyze and a decrease in performance and an increase in execution time.

Features selection is the process of selecting a subset of features that are more relevant for the model and ignore the rest. The main goals of features selection are: [31]

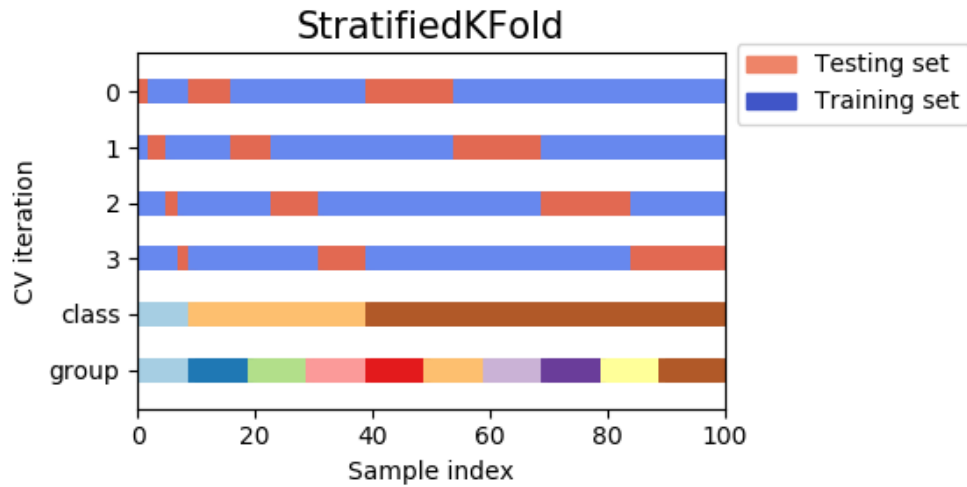


Figure 5.2. Example of stratified 4-Fold cross-validation

- Improve the performance of a classifier
- Reduce the time and cost of analysis
- Enhance data visualization and understanding

The idea behind feature selection is that if the dataset contains unnecessary or redundant features, those features can be removed without loss of information. [32]

However, there is a distinction between usefulness and relevance of a feature, a set of useful features can exclude some redundant features, that could be, instead, relevant to the problem.[33] **da riverere da kohavi**

Features selection techniques can be grouped into three categories based on the approach used: **Filter methods**, **Wrapper methods**, **Embedded methods**.

5.4.1 Filter methods

Filter methods are applied directly to the dataset, so they are independent of the model used in the prediction. Compared to methods dependent on the model, such as wrapper or embedded methods, they have a better generalization of the problem, and they are faster. [33]

However, they have less predictive performance. They rely only on the characteristics of the features in the training set and can show the relationship between variables. [34] Usually, the filter methods rely on variable ranking. Ranking functions assign a score to each variable, and then the analyst can set a threshold of features to keep.

Hastie et al. [18] state that filter methods may be preferable at first to other features selection techniques because they are computationally and statistically scalable. Computationally efficient because we only need to apply a function to n features in the dataset and statistically because they introduce bias, but they could have substantially less variance.

Scikit provides different functions for filter feature selection, such as Mutual information, chi-square, Pearson correlation, variance threshold. Those methods are explained in detail in the next chapter.

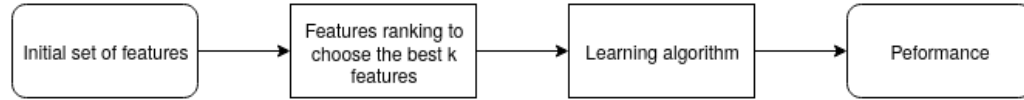


Figure 5.3. Filter method flow

5.4.2 Wrapper methods

Wrapper methods depend on the predictive model to choose a subset of features. The wrapper algorithm does not know the machine learning model used, and it is considered a black box [33].

The algorithm relies on the model to evaluate the performance of each subset of features. Each subset trains a model, and the model error rate establishes the score of the given subset. This procedure is repeated until an optimal subset of features is found.

The main drawbacks of this method are that it is very computationally expensive, Amaldi et al. [35] state that it is an NP-hard problem, and it can lead to overfitting if there are not enough data. Nevertheless, it usually gives the best result in predictive performance for the given model.

Efficient search algorithms are crucial to reducing the computational cost and time, and they are not always a synonym of decreasing in predictive performance. Greedy search algorithms are optimal for wrapper methods, and they are divided into two main categories: *forward selection* and *backward elimination*. [36].

In *forward selection*, the algorithm starts from an empty set, and at each iteration, it adds a new feature to the dataset. Instead, in *backward elimination*, the algorithm starts from the whole dataset, and it removes a feature at each iteration, until it finds the best subset.

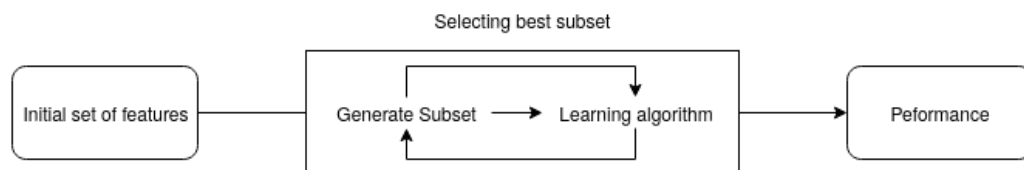


Figure 5.4. Wrapper method flow

5.4.3 Embedded methods

Embedded methods are a combination of the other two. They perform feature selection during the training process. [31] This technique allows the algorithms to be more efficient than wrapper methods. First of all, they do not need to split the dataset into training and testing sets. Secondly, they are faster because they do

avoid to retrain the model for every subset of features. The most common methods are *Lasso* and *Ridge regression* and *decision tree*.

Lasso and *Ridge regression* penalize the beta coefficient by a factor, to avoid that the model focuses on a particular set of features.

Decision tree algorithms select a feature at each recursive step, during the tree growing process, dividing the sample into smaller subsets. The more child node a tree has of the same class, the more important are the features.

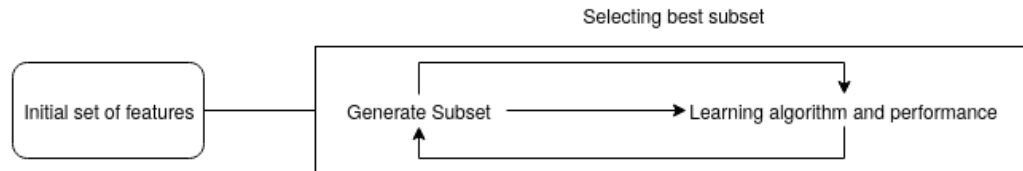


Figure 5.5. Embedded method flow

Chapter 6

Discussion

Chapter 7

Future works

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