Random Initialization

Initializing all theta weights to zero does not work with neural networks. When we backpropagate, all nodes will update to the same value repeatedly. Instead we can randomly initialize our weights for our \Theta matrices using the following method:

Random initialization: Symmetry breaking

→ Initialize each $\Theta_{ij}^{(l)}$ to a random value in $[-\epsilon, \epsilon]$
(i.e. $-\epsilon \leq \Theta_{ij}^{(l)} \leq \epsilon$)

E.g.

random 10×11 matrix (betw. 0 and 1)

→ Theta1 = `rand(10,11)`*(2*INIT_EPSILON)
           - INIT_EPSILON; $[-\epsilon, \epsilon]$

→ Theta2 = `rand(1,11)`*(2*INIT_EPSILON)
           - INIT_EPSILON;

Hence, we initialize each \Theta^{(l)}_{ij} to a random value between [-\epsilon,\epsilon]. Using the above formula guarantees that we get the desired bound. The same procedure applies to all the \Theta's. Below is some working code you could use to experiment.

```
1   If the dimensions of Theta1 is 10x11, Theta2 is 10x11 and Theta3 is 1x11.
2
3   Theta1 = rand(10,11) * (2 * INIT_EPSILON) - INIT_EPSILON;
4   Theta2 = rand(10,11) * (2 * INIT_EPSILON) - INIT_EPSILON;
5   Theta3 = rand(1,11) * (2 * INIT_EPSILON) - INIT_EPSILON;
6
```

rand(x,y) is just a function in octave that will initialize a matrix of random real numbers between 0 and 1.

(Note: the epsilon used above is unrelated to the epsilon from Gradient Checking)