# Part02: Survey of machine learning models for CA hedata

In this chapter I survey a range of machine learning models, including ridge, support vector, random fore: boosting regression models. I am interested in finding a "best" model for predicting median\_house\_value

The g03 linear model from Part01 had a comparative rmse score of \$75,471; when predicting only for dis median\_house\_value < 500K, the error score drops to \$55,832. Most of the ML algorithms surveyed belt to beat these scores.

#### Load training and test sets created in Part01

1662

-121.94

37.93

```
In [4]: train = pd.read_csv('/home/greg/Documents/stat/Geron_ML/datasets/housing/trai
                                index_col=0)
          test = pd.read_csv('/home/greg/Documents/stat/Geron_ML/datasets/housing/test_
                               index col=0)
          print(train.shape)
          print(test.shape)
          (16482, 16)
          (4121, 16)
In [17]: train.head()
Out[17]:
                longitude latitude housing_median_age total_rooms total_bedrooms population households I
            334
                  -122.17
                           37.74
                                             43.0
                                                        818
                                                                      193
                                                                               494
                                                                                          179
```

3421

427

1341

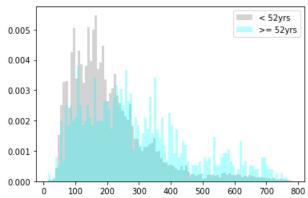
428

1 of 31 7/18/21, 10:01

16.0

```
'population', 'households', 'median_income',
                           'ocean_proximity','rooms_per_hh', bdrms_per_room',
                           'pop_per_hh','HHdens_ln','long_transf','latitude']].copy()
         print(y_train.shape)
         print(X_train.shape)
         (16482,)
         (16482, 13)
In [19]: y_train.__class__
Out[19]: pandas.core.series.Series
In [20]: # Recall that we removed the 'ISLAND' records since there
         # were only 5 in the entire 20.64K dataset.
         pd.value_counts(X_train['ocean_proximity'])
Out[20]: OCEAN
                        7338
         INLAND
                        5187
         NEAR OCEAN
                        2137
         NEAR BAY
                        1820
         Name: ocean_proximity, dtype: int64
 In [6]: y_test = test['median_house_value'].copy()
         y test.name = 'median house value'
         X_test = test[['housing_median_age','total_rooms','total_bedrooms',
                           'population', 'households', 'median_income',
                           'ocean_proximity','rooms_per_hh','bdrms_per_room',
                           'pop_per_hh', 'HHdens_ln', 'long_transf', 'latitude']].copy()
         print(y_test.shape)
         print(X_test.shape)
         (4121,)
         (4121, 13)
In [23]: # The training set and test data have median house values > 500K.
         # In other words, we are working with about 4.8% imputed data
         # for this variable.
         round(y_test.describe())
Out[23]: count
                     4121.0
                   210578.0
         mean
         std
                   130124.0
         min
                   22500.0
         25%
                   118200.0
         50%
                   178800.0
         75%
                   262300.0
         max
                   777151.0
         Name: median_house_value, dtype: float64
         Plot of age vs median_house_value
In [58]: | df_GE52 = train[train.housing_median_age >= 52]
         print(df GE52.shape)
```

Median: 176500.0 Mean: 207439



#### Load some of the functions we will need

```
In [7]:
    from sklearn.compose import ColumnTransformer
    from sklearn.pipeline import Pipeline, make_pipeline
    from sklearn.preprocessing import StandardScaler, MinMaxScaler, RobustScaler
    from sklearn.preprocessing import PolynomialFeatures, OneHotEncoder
    from sklearn.model_selection import cross_val_score, GridSearchCV
    from sklearn.metrics import mean_squared_error
```

```
In [8]: # Distinguish between the numerical and categorical features.
# We will use this distinction in some of the pipelines below.

num_attribs = list(X_train.drop(["ocean_proximity"], axis=1).columns)
cat_attribs = ["ocean_proximity"]
print(num_attribs)

# There are 13 attributes altogether, excluding the response variable.

# Population and households have a very high positive correlation.
# Both are highly correlated with total_rooms and total_bedrooms.
```

['housing\_median\_age', 'total\_rooms', 'total\_bedrooms', 'population', 'housel n\_income', 'rooms\_per\_hh', 'bdrms\_per\_room', 'pop\_per\_hh', 'HHdens\_ln', 'long titude']

In [8]: # This function is useful for displaying scores from cross val score.

In [ ]:

## Section 1: ML linear models: OLS, ridge, and lasso

For most of the linear models that follow, I use only the 6 predictors used in the g03 model of Part01. The Part01 shows that we are likely to get better linear models using only median\_income, long\_transf, latituc housing\_median\_age, and HHdens\_In.

#### **OLS model**

```
In [10]: X_train_6preds = X_train[['median_income','long_transf','latitude',
                                    'pop_per_hh','HHdens_ln','housing_median_age']].cop
         X_test_6preds = X_test[['median_income','long_transf','latitude',
                                   'pop per hh', 'HHdens ln', 'housing median age']].cor
In [15]: from sklearn.linear model import LinearRegression, Ridge, Lasso, ElasticNet
In [46]: # A simple regression with the 6 predictors.
         lin_reg_cv_scores = cross_val_score(LinearRegression(), X_train_6preds, y_tra
                                             scoring="neg_mean_squared_error",
                                             cv=10, n_jobs=10)
         lin reg scores = np.sqrt(-lin reg cv scores)
         display_scores(lin_reg_scores)
         Mean: 79297.0
         StdDev: 2650.0
In [47]: # Here I apply the scaler AFTER the polynomial transformations.
         # The order matters for the scaler that is chosen in the grid
         # search. (Typically I apply the scaler first.)
```

```
In [48]: # A parameter grid for LinearRegression().
         param_grid = {'poly__degree': [1,2,3],
                        scaler': [StandardScaler(), MinMaxScaler(),
                                  None, RobustScaler()]}
In [49]: grid = GridSearchCV(pipe, param_grid, cv=10, scoring='neg_mean_squared_error'
         grid.fit(X_train_6preds, y_train)
         grid.best_params_
         # {'poly__degree': 3, 'scaler': None}
Out[49]: {'poly__degree': 3, 'scaler': None}
In [50]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_6preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best score))
         print("Test-set score: {:.0f}".format(test score))
         # Best cross-validation score: 68,141
         # Test-set score: 66,259
         # These scores are much better than what we saw for the g03 model in Part01.
         # This model is much more complex though, with 84 terms (g03 has 15 terms).
         Best cross-validation score: 68141
         Test-set score: 66259
 In [ ]: ### COMMENTS:
         # In this instance the grid search returns the same values
         # if we apply the scaler prior to the polynomial transformation.
```

#### Get comparative score for the OLS model

For consistency, I apply a procedure similar to what I used at the end of Part01. I take 500 1000-record s testset data and compute an rmse score for each. I then take the average of these 500 scores.

```
In [78]: # The following is a score for all test districts.

testdat = X_test_6preds.join(y_test)

seed_choices = np.arange(start=1000, stop=21000, dtype=int)
np.random.seed(4321)
smp = np.random.choice(seed_choices, size=500, replace=False)

OLS_rmse = get_rmse(smp, testdat)

print("Comparative rmse score for ML OLS model: " + '$' +
    f'{OLS_rmse:,.0f}')
```

```
OLS_rmse = get_rmse(smp, testdat2)
print("Comparative rmse score for ML OLS model when median house value < 500F
    f'{OLS_rmse:,.0f}')
# $57,448
# For the g03 model in Part01, this score was 55.8K.</pre>
```

Comparative rmse score for ML OLS model when median house value < 500K: \$57

```
In [82]: # The difference between the 2 testsets is about 200 records.
print(testdat2.shape)
print(testdat.shape)

(3924, 7)
(4121, 7)
```

#### **OLS Comments**

The score on 500 samples from the test set data is much lower than what we saw with the g03 model of score was 75.5K. The delta is about 14.4K.

But if we limit the test districts to those with a median house value < 500K, the g03 model out-performs tl by 1.6K.

OLS best score on test set: 61,151

#### Ridge model

```
In [86]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_6preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best_score))
         print("Test-set score: {:.0f}".format(test_score))
         # Best cross-validation score: 66.5K
         # Test-set score: 64.5K
         Best cross-validation score: 66522
         Test-set score: 64453
In [33]: # Have the scaler follow the polynomial transformations.
         pipe = Pipeline([('poly', PolynomialFeatures()),
                           ('scaler', MinMaxScaler()),
                           ('model', Ridge())])
In [88]:
         param_grid = {'poly__degree': [1,2,3,4], 'scaler': [StandardScaler(), MinMaxs
                                                             RobustScaler()],
                       'model alpha': list((0.01, 0.02, 0.04, 0.06, 0.08, 0.1, 1.0, 1
         start_time = datetime.now()
         grid = GridSearchCV(pipe, param_grid, cv=10, scoring='neg_mean_squared_error'
         grid.fit(X_train_6preds, y_train)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 0.1 minutes
         grid.best_params_
         # {'model_alpha': 0.01, 'poly_degree': 4, 'scaler': MinMaxScaler()}
         Time difference of 0.1 minutes
Out[88]: {'model__alpha': 0.01, 'poly__degree': 4, 'scaler': MinMaxScaler()}
In [89]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_6preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best_score))
         print("Test-set score: {:.0f}".format(test_score))
         # Best cross-validation score: 66.5K
         # Test-set score: 64.4K
         Best cross-validation score: 66522
         Test-set score: 64453
In [731: nine = Pineline([('scaler', MinMaxScaler()).
```

```
start_time = datetime.now()
         grid = GridSearchCV(pipe, param_grid, cv=10, scoring='neg_mean_squared_error'
         grid.fit(X_train_6preds, y_train)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 0.1 minutes
         grid.best_params_
         # {'model__alpha': 0.01, 'poly__degree': 4, 'scaler': MinMaxScaler()}
         Time difference of 0.1 minutes
Out[90]: {'model__alpha': 0.01, 'poly__degree': 4, 'scaler': MinMaxScaler()}
In [91]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_6preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best_score))
         print("Test-set score: {:.0f}".format(test_score))
         # Best cross-validation score: 66.5K
         # Test-set score: 64.5K
         Best cross-validation score: 66522
         Test-set score: 64453
```

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#### Get comparative score for the Ridge model

```
In [93]: # The following is a score for all test districts.

testdat = X_test_6preds.join(y_test)

seed_choices = np.arange(start=1000, stop=21000, dtype=int)
np.random.seed(4321)
smp = np.random.choice(seed_choices, size=500, replace=False)

rmse_score = get_rmse(smp, testdat)

print("Comparative rmse score for the Ridge model: " + '$' +
    f'{rmse_score:,.0f}')

# $59,851

# For the g03 model of Part01, this score was 75.5K.

# The ML OLS model's score was: $61,151
```

Comparative rmse score for the Ridge model: \$59,851

```
In [94]: # The following is a score for districts with a median_house_value < 500K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()</pre>
```

Comparative rmse score for the Ridge model when median house value < 500K: 5

#### Comments on Ridge model using only the 6 predictors of the g03 model

Thus far, our best predictive model is the ridge regression.

Ridge model tentative best score on test set: 59.9K

```
In [ ]:
```

## Add more predictors to the Ridge model

We can improve the ridge model somewhat by adding predictors total rooms and rooms per hh.

From what I am seeing, the categorical variable, ocean\_proximity, does not help us get a better predictive because there are a number of combinations with ocean\_proximity that I do not test in what follows.)

Out[104]:

```
total_rooms total_bedrooms population rooms_per_hh bdrms_per_room pop_per_hh
                     1.000000
                                      0.926511
                                                  0.858527
                                                                 0.189991
                                                                                                 -0.110973
    total_rooms
                                                                                   -0.197630
 total_bedrooms
                     0.926511
                                      1.000000
                                                  0.874802
                                                                 0.002857
                                                                                    0.084066
                                                                                                 -0.146140
      population
                     0.858527
                                      0.874802
                                                  1.000000
                                                                 -0.074324
                                                                                    0.020928
                                                                                                 0.177688
                     0.189991
                                      0.002857
                                                                                   -0.564184
                                                                                                 -0.056187
  rooms_per_hh
                                                 -0.074324
                                                                 1.000000
bdrms_per_room
                    -0.197630
                                      0.084066
                                                 0.020928
                                                                 -0.564184
                                                                                    1.000000
                                                                                                 0.007697
                    -0.110973
                                     -0.146140
                                                 0.177688
                                                                 -0.056187
                                                                                    0.007697
                                                                                                 1.000000
    pop_per_hh
```

```
("cat", OneHotEncoder(sparse=False), cat_attribs_raw),
          ])
In [110]: pipe = Pipeline([("prep dat", preproc),
                           ('poly', PolynomialFeatures()),
                           ('model', Ridge())])
In [113]: # On my machine Ridge struggles when we test poly_degree=5.
          param_grid = {'poly__degree': [3,4],
                         'model alpha': [0.01, 0.03, 0.05]}
          start_time = datetime.now()
          grid = GridSearchCV(pipe, param_grid, cv=5, scoring='neg_mean_squared_error',
          grid.fit(X_train_raw, y_train)
          stop_time = datetime.now()
          delta = stop_time - start_time
          timeval = round(delta.seconds/60, 2)
          print("Time difference of " + str(timeval) + " minutes")
          # Time difference of 0.28 minutes.
          grid.best_params_
          # {'model__alpha': 0.03, 'poly__degree': 4}
          Time difference of 0.28 minutes
Out[113]: {'model__alpha': 0.03, 'poly__degree': 4}
In [114]: # Get scores from the best model.
          best_score = np.power(-grid.best_score_, 0.5)
          test_score = grid.score(X_test_raw, y_test)
          test_score = np.power(-test_score, 0.5)
          print("Best cross-validation score: {:.0f}".format(best_score))
          print("Test-set score: {:.0f}".format(test score))
          # Best cross-validation score: 63.7K
          # Test-set score: 63.0K
          Best cross-validation score: 63737
          Test-set score: 63037
```

Get comparative score for the Ridge model that uses more predictors

```
In [116]: # The following is a score for districts with a median_house_value < 500K.
           testdat2 = testdat[testdat.median house value < 500000].copy()</pre>
           rmse score = get rmse(smp, testdat2)
           print("Comparative rmse score for 2nd Ridge model when median house value < 5</pre>
                 f'{rmse_score:,.0f}')
           # $52,511
           # For the simpler ridge model this score was 55.3K.
           Comparative rmse score for 2nd Ridge model when median house value < 500K: 5
           Remove ocean proximity and bdrms per room
In [12]: X_train_raw = train[['housing_median_age','total_rooms',
                                      'population', 'median_income', 'HHdens_ln',
                                      'rooms_per_hh','pop_per_hh',
'long_transf','latitude']].copy()
           print(X_train_raw.shape)
           (16482, 9)
 In [13]: X_test_raw = test[['housing_median_age','total_rooms',
                                      'population','median_income','HHdens_ln',
                                      'rooms_per_hh','pop_per_hh',
'long_transf','latitude']].copy()
           print(X test raw.shape)
           (4121, 9)
In [120]: pipe = Pipeline([('scaler', MinMaxScaler()),
                             ('poly', PolynomialFeatures()),
('model', Ridge())])
In [121]: param_grid = {'poly__degree': [3,4],
                          'model__alpha': [0.01, 0.03, 0.05]}
           start time = datetime.now()
           grid = GridSearchCV(pipe, param_grid, cv=5, scoring='neg_mean_squared_error',
           grid.fit(X_train_raw, y_train)
           stop_time = datetime.now()
           delta = stop_time - start_time
           timeval = round(delta.seconds/60, 2)
           print("Time difference of " + str(timeval) + " minutes")
           # Time difference of 0.03 minutes.
```

Time difference of 0.03 minutes

Out[121]: {'model alpha': 0.01. 'polv degree': 4}

# {'model\_\_alpha': 0.01, 'poly\_\_degree': 4}

grid.best params

```
# Test-set score: 63.3K

Best cross-validation score: 66264
Test-set score: 63263
```

#### Get comparative score for this new ridge model

Comparative rmse score for the 3rd Ridge model: \$59,492

```
In [124]: # The following is a score for districts with a median_house_value < 500K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()

rmse_score = get_rmse(smp, testdat2)

print("Comparative rmse score for 3rd Ridge model when median house value < !
    f'{rmse_score:,.0f}')

# $53,843

# For the simpler ridge model this score was 55.3K.</pre>
```

Comparative rmse score for 3rd Ridge model when median house value < 500K: 5

#### Ridge model best score on test set: 59.5K

The corresponding OLS regression score is 61.2K. The g03 model had a score of 75.5K. The Ridge moc complex than either of these 2 models.

```
In []:
```

## Lasso model with 6 predictors

```
In [143]: pipe = Pipeline([('scaler', MinMaxScaler()),
                            ('poly', PolynomialFeatures()),
('model', Lasso(max_iter=10000, tol=0.001))])
In [145]: # Parameter grid for Lasso():
          param_grid = {'poly__degree': [3,4,5],
                         'model__alpha': [15, 20, 25]}
          start_time = datetime.now()
          grid = GridSearchCV(pipe, param_grid, cv=10, scoring='neg_mean_squared_error'
          grid.fit(X_train_6preds, y_train)
          stop_time = datetime.now()
          delta = stop_time - start_time
          timeval = round(delta.seconds/60, 2)
          print("Time difference of " + str(timeval) + " minutes")
          # Time difference of 1.77 minutes
          grid.best_params_
          # {'model__alpha': 15, 'poly__degree': 5}
          Time difference of 1.77 minutes
Out[145]: {'model__alpha': 15, 'poly__degree': 5}
In [146]: # Get scores from the best model.
          best_score = np.power(-grid.best_score_, 0.5)
          test_score = grid.score(X_test_6preds, y_test)
          test_score = np.power(-test_score, 0.5)
          print("Best cross-validation score: {:.0f}".format(best_score))
          print("Test-set score: {:.0f}".format(test_score))
          # Best cross-validation score: 69.3K
          # Test-set score: 67.3K
          Best cross-validation score: 69305
          Test-set score: 67282
```

#### Get comparative score for the lasso model

```
In [148]: # The following is a score for all test districts.
testdat = X train 6preds.ioin(v test)
```

```
# $64,014

# The best ridge model has a score of 59.5K.
Comparative rmse score for the lasso model: $64,014

In [150]: # The following is a score for districts with a median_house_value < 500K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()

rmse_score = get_rmse(smp, testdat2)

print("Comparative rmse score for the lasso when median house value < 500K:
    f'{rmse_score:,.0f}')

# $56,892

# The best ridge model has a score of 53.8K.</pre>
```

Comparative rmse score for the lasso when median house value < 500K: \$56,892

#### Comments on Lasso model

For this dataset and the number of predictors I am working with, and for the basic parameter settings I ar and ridge, ridge is proving to be much better to work with. Lasso requires more computing time than ridge orders of magnitude. This makes experimentation and tuning of the model much more difficult.

Lasso model best score on test set, using 9 predictors: 64K

```
In [ ]:
```

### **Section 1 Final Comments**

Of the linear models surveyed above, Ridge has the best score on the testset data. This holds true even restricted to the 6 predictors of model g03.

Ridge has the added virtue of still being relatively fast. This is not so with lasso (nor with elastic net). Bec not work well with this dataset, I will not review any elastic net models. The elastic net models I have look the same way that lasso does.

```
In [ ]:
```

## Section 2: A Support Vector Machine regression mo

Here, too, I restrict the models to the 6 predictors used in the g03 model.

```
'model__gamma': [0.2, 0.3],
                        'scaler' : [StandardScaler(), RobustScaler(), MinMaxScaler()]
         start time = datetime.now()
         grid = GridSearchCV(pipe, param_grid, cv=5, scoring='neg_mean_squared_error',
         grid.fit(X_train_6preds, y_train)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 2.6 minutes
         grid.best params
         # {'model C': 200000, 'model gamma': 0.3, 'scaler': StandardScaler()}
         Time difference of 2.6 minutes
Out[16]: {'model__C': 200000, 'model__gamma': 0.3, 'scaler': StandardScaler()}
In [17]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_6preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best score))
         print("Test-set score: {:.0f}".format(test_score))
         # Best cross-validation score: 62.4K
         # Test-set score: 60K
         Best cross-validation score: 62426
         Test-set score: 60040
In [18]: # Add StandardScaler to the pipe.
         pipe = Pipeline([('scaler', StandardScaler()),
                          ('model', SVR(kernel="rbf"))])
In [19]: # Search for best parameters, Round 2:
         param_grid = [{'model__C': [200000, 250000],
                         'model gamma': [0.4, 0.5],
                        }]
         start_time = datetime.now()
         grid = GridSearchCV(pipe, param_grid, cv=5, scoring='neg_mean_squared_error',
         grid.fit(X_train_6preds, y_train)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 2.07 minutes
         grid.best params
         # {'model C': 250000, 'model gamma': 0.4}
```

```
print("Best cross-validation score: {:.0f}".format(best_score))
print("Test-set score: {:.0f}".format(test_score))
# Best cross-validation score: 62.3K
# Test-set score: 60.1K

Best cross-validation score: 62259
Test-set score: 60148
```

#### Get comparative score for the SVR model

```
In [21]: # The following is a score for all test districts.

testdat = X_train_6preds.join(y_test)

seed_choices = np.arange(start=1000, stop=21000, dtype=int)
np.random.seed(4321)
smp = np.random.choice(seed_choices, size=500, replace=False)

# The runtime is much longer than any of the previous models.
rmse_score = get_rmse(smp, testdat)

print("Comparative rmse score for the SVR model: " + '$' +
    f'{rmse_score:,.0f}')

# $57,683

# The best ridge model has a score of 59.5K.
```

Comparative rmse score for the SVR model: \$57,683

```
In [22]: # The following is a score for districts with a median_house_value < 500K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()

start_time = datetime.now()

rmse_score = get_rmse(smp, testdat2)
stop_time = datetime.now()
delta = stop_time - start_time
timeval = round(delta.seconds/60, 2)
print("Time difference of " + str(timeval) + " minutes")
# Time difference of 1.6 minutes

print("")
print("Comparative rmse score for the SVR model when median house value < 500
    f'{rmse_score:,.0f}')

# $49,388

# The best ridge model has a score of 53.8K.</pre>
```

Time difference of 1.6 minutes

Comparative rmse score for the SVR model when median house value < 500K: \$49

## Final comments on SVM regression model

```
In [ ]:
```

## **Section 3: Random forest models**

I start by using X\_train\_9preds. Previous work has shown that ocean\_proximity and pop\_per\_hh are imp for the random forest model.

```
In [12]: from sklearn.ensemble import RandomForestRegressor
In [20]: X_train_9preds = X_train[['median_income','long_transf','latitude',
                                   'pop_per_hh','HHdens_ln','housing_median_age',
                                   'total_rooms','bdrms_per_room','ocean_proximity']].
         X_test_9preds = X_test[['median_income','long_transf','latitude',
                                 'pop_per_hh','HHdens_ln','housing_median_age',
                                 'total_rooms','bdrms_per_room','ocean_proximity']].cc
In [21]: num_attribs = list(X_train_9preds.drop(["ocean_proximity"], axis=1).columns)
         cat_attribs = ["ocean_proximity"]
In [15]: # We need to convert the levels of ocean_proximity to dummy variables.
         # The scaling is not required.
         preproc = ColumnTransformer([
             ("num", StandardScaler(), num_attribs),
             ("cat", OneHotEncoder(sparse=False), cat_attribs),
         pipe = Pipeline([("prep_dat", preproc),
                          ('model', RandomForestRegressor(bootstrap=False, random_stat
In [27]: param_grid = [{'model__bootstrap': [True, False],
                        'model__n_estimators' : [300, 400, 500],
                        'model__max_features': [3, 4, 5, 6]
                        }]
         start time = datetime.now()
         grid = GridSearchCV(pipe, param_grid, cv=7, scoring='neg_mean_squared_error',
         grid.fit(X_train_9preds, y_train)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 8.97 minutes
         grid.best_params_
         # {'model__bootstrap': False,'model__max_features': 3,'model__n_estimators':
         Time difference of 8.97 minutes
```

```
# Test-set score: 53.2K

Best cross-validation score: 56105
Test-set score: 53188
```

#### Get comparative score for the random forest model

```
In [29]: # The following is a score for all test districts.
    testdat = X_test_9preds.join(y_test)
    seed_choices = np.arange(start=1000, stop=21000, dtype=int)
    np.random.seed(4321)
    smp = np.random.choice(seed_choices, size=500, replace=False)

# The runtime is much longer than any of the previous models.
    rmse_score = get_rmse(smp, testdat)

print("Comparative rmse score for the random forest model: " + '$' +
    f'{rmse_score:,.0f}')

# $50,477

# The previous best model, the SVR, has a score of 57.7K.
```

Comparative rmse score for the random forest model: \$50,477

```
In [30]: # The following is a score for districts with a median_house_value < 5000K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()

start_time = datetime.now()
    rmse_score = get_rmse(smp, testdat2)
    stop_time = datetime.now()
    delta = stop_time - start_time
    timeval = round(delta.seconds/60, 2)
    print("Time difference of " + str(timeval) + " minutes")
# Time difference of 1.42 minutes

print("")
    print("Comparative rmse score for the random forest model when median house \( \)
    f'{rmse_score:,.0f}')

# $45,267

# The previous best model, the SVR, has a score of 49.4K.</pre>
```

Time difference of 1.42 minutes

Comparative rmse score for the random forest model when median house value < 7

#### Feature importances for the random forest model

To get a readable print-out of the feature importances, some preliminary work is required.

```
grid.fit(X_train_9preds, y_train)
          stop time = datetime.now()
          delta = stop_time - start_time
          timeval = round(delta.seconds/60, 2)
          print("Time difference of " + str(timeval) + " minutes")
          # Time difference of 0.75 minutes
          grid.best_params_
          Time difference of 0.75 minutes
Out[16]: {'model_bootstrap': False,
           'model__max_features': 3,
           'model__n_estimators': 500}
In [17]: print("Best estimator:\n{}".format(grid.best_estimator_))
          Best estimator:
          Pipeline(steps=[('prep dat',
                             ColumnTransformer(transformers=[('num', StandardScaler(),
                                                                 ['median_income',
                                                                  'long_transf', 'latitude'
'pop_per_hh', 'HHdens_ln'
                                                                  'housing_median_age',
                                                                  'total_rooms',
                                                                  'bdrms_per_room']),
                                                                ('cat',
                                                                OneHotEncoder(sparse=False)
                                                                 ['ocean proximity'])])),
                            ('model',
                             RandomForestRegressor(bootstrap=False, max_features=3,
                                                    n_estimators=500, random_state=42))])
In [18]: best current model = grid.best estimator .named steps["model"]
          feature_importances = best_current_model.feature_importances_.round(4)
          processed_dat = grid.best_estimator_.named_steps['prep_dat']
print("processed_dat:\n{}".format(processed_dat))
          processed dat:
          ColumnTransformer(transformers=[('num', StandardScaler(),
                                              ['median_income', 'long_transf', 'latitude'
    'pop_per_hh', 'HHdens_ln',
                                               'housing_median_age', 'total_rooms',
                                               'bdrms_per_room']),
                                             ('cat', OneHotEncoder(sparse=False),
                                              ['ocean_proximity'])])
In [19]: cat_encoder = processed_dat.named_transformers_['cat']
          cat_one_hot_attribs = list(cat_encoder.categories_[0])
          print(cat_one_hot_attribs)
          ['INLAND', 'NEAR BAY', 'NEAR OCEAN', 'OCEAN']
In [20]: # Feature importances of our best current random forest model.
          attributes = num attribs + cat one hot attribs
```

```
[(0.3153, 'median_income'),
    (0.1658, 'long_transf'),
    (0.1212, 'bdrms_per_room'),
    (0.101 'box box bb')

In []: ### COMMENTS:

# If we construct a model with longitude rather than long_transf,
# INLAND is second only to median_income in terms of importance.
# So, as expected, the transformation applied to longitude creates
# a predictor which negates a great deal of the importance of
# ocean_proximity.

# The above output suggests that ocean_proximity is negating some
# of the importance of HHdens_ln, the urbanacity metric.
```

#### Final comments on the random forest model

The random forest model beats the SVR by \$7,200 and runs a bit faster. It makes very good use of the band pop\_per\_hh predictors. Note that in the current model I have neither population nor households. Bot correlated with total\_rooms.

The score of 50.5K is extraordinary considering that the corresponding score for g03 is 75.5K. Our ridge 59.5K. Ridge is much faster than random forest on this dataset, and g03 is another order of magnitude fathe better predictions are at a cost.

Random forest best score on the test set: 50.5K

```
In []:
```

## Section 4: Gradient boosting regression

Start by using X\_train\_9preds, the same predictors as were used for our random forest model.

```
print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 15.15 minutes
         grid.best_params_
         # {'model_learning_rate': 0.04,
         # 'model__max_depth': 5,
         # 'model n estimators': 1500}
In [25]: # Get scores from the best model.
         best_score = np.power(-grid.best_score_, 0.5)
         test_score = grid.score(X_test_9preds, y_test)
         test_score = np.power(-test_score, 0.5)
         print("Best cross-validation score: {:.0f}".format(best_score))
         print("Test-set score: {:.0f}".format(test_score))
         # Best cross-validation score: 56.8K
         # Test-set score: 51.9K
         Best cross-validation score: 56808
         Test-set score: 51882
In [26]: # Run more cross-folds to get a better measure of the
         # "actual" score and its variability.
         ct = ColumnTransformer([
             ("num", 'passthrough', num_attribs),
             ("cat", OneHotEncoder(sparse=False), cat attribs),
         X_train_prepared = ct.fit_transform(X_train_9preds)
In [27]: # The parameters used in the model are those which produced the best
         # cv score for X_train_9preds above.
         start time = datetime.now()
         gbrt_cv_scores = cross_val_score(GradientBoostingRegressor(random_state=42,
                                                                     max depth=5,
                                                                     n_estimators=1500,
                                                                     learning_rate=0.04
                                          X_train_prepared, y_train,
                                          scoring="neg_mean_squared_error",
                                          cv=20, n jobs=10)
         stop_time = datetime.now()
         delta = stop_time - start_time
         timeval = round(delta.seconds/60, 2)
         print("Time difference of " + str(timeval) + " minutes")
         # Time difference of 4.07 minutes
         gbrt_scores = np.sqrt(-gbrt_cv_scores)
         display_scores(gbrt_scores)
         # Mean: 55,823.0
         # StdDev: 3202.0
         Time difference of 4.07 minutes
```

Mean: 55823.0 StdDev: 3202.0

```
Best cross-validation score: 56808
Test-set score: 51882
```

#### Get comparative score for the gradient boosting model

```
In [31]: # The following is a score for all test districts.

testdat = X_test_9preds.join(y_test)

seed_choices = np.arange(start=1000, stop=21000, dtype=int)
np.random.seed(4321)
smp = np.random.choice(seed_choices, size=500, replace=False)

rmse_score = get_rmse(smp, testdat)

print("Comparative rmse score for the gradient boosting model: " + '$' +
    f'{rmse_score:,.0f}')

# $48,382

# The random forest model has a score of 50.5K.
```

Comparative rmse score for the gradient boosting model: \$48,382

Time difference of 0.17 minutes

Comparative rmse score for the gradient boosting model when median house value, 6,266

## Try xgboost package

Try first without ocean\_proximity.

```
In [331: immort xahoost as xah
```

```
In [36]: # Testing shows that the gamma parameter is not being used here.
          params = {'booster': 'gbtree', 'max_depth': 6, 'learning_rate': 0.3,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse',
                      'gamma': 1}
In [38]: | dtrain = xgb.DMatrix(X_train_8preds, label= y_train)
          dtest = xgb.DMatrix(X_test_8preds, label= y_test)
In [53]: bst = xgb.cv(params, dtrain, num boost round=40, nfold=10,
                        metrics= ['rmse'], early_stopping_rounds= 3)
In [54]: bst.tail().round()
Out[54]:
              train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
           35
                     42308.0
                                   443.0
                                                           2396.0
                                               57942.0
           36
                     42005.0
                                   391.0
                                               57962.0
                                                           2363.0
                                   342.0
                                                           2386.0
           37
                     41743.0
                                               57908.0
           38
                     41466.0
                                   361.0
                                               57892.0
                                                           2404.0
                     41175.0
                                   480.0
                                                           2376.0
           39
                                               57881.0
In [56]: # Change the parameters.
          params = {'booster': 'gbtree', 'max_depth': 6, 'learning_rate': 0.25,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                        metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[56]:
              train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
                                                           2195.0
           35
                     43680.0
                                   301.0
                                               57868.0
           36
                     43425.0
                                   272.0
                                               57854.0
                                                           2200.0
           37
                     43193.0
                                   283.0
                                               57870.0
                                                           2197.0
           38
                     42956.0
                                   267.0
                                               57839.0
                                                           2164.0
                     42707.0
                                   257.0
           39
                                               57809.0
                                                           2114.0
In [58]: # Change the parameters.
          params = {'booster': 'gbtree', 'max_depth': 6, 'learning_rate': 0.20,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                        metrics= ['rmse'], early stopping rounds= 3)
          bst.tail().round()
```

37

32640.0

376.0

```
In [67]: # Change the parameters.
          params = {'booster': 'gbtree', 'max_depth': 5, 'learning_rate': 0.28,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                         metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[67]:
               train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
                                                             2050.0
           35
                                    590.0
                                                58370.0
                      48536.0
                                    576.0
                                                58302.0
                                                             2042.0
           36
                      48319.0
           37
                      48059.0
                                    558.0
                                                58243.0
                                                             2015.0
           38
                      47823.0
                                    574 0
                                                58185.0
                                                             1986.0
                      47639.0
                                    567.0
                                                58139.0
                                                             2003.0
           39
In [68]: # Change the parameters.
          params = {'booster': 'gbtree', 'max depth': 7, 'learning rate': 0.20,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                         metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[68]:
               train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
                                                56842.0
           35
                      39423.0
                                    343.0
                                                             2111.0
           36
                      39210.0
                                    351.0
                                                56819.0
                                                             2094 0
           37
                      38866.0
                                    349.0
                                                56778.0
                                                             2133.0
           38
                      38592.0
                                    369.0
                                                56744.0
                                                             2183.0
                      38341.0
                                    337.0
                                                56675.0
                                                             2148.0
           39
In [69]: # Change the parameters.
          params = {'booster': 'gbtree', 'max_depth': 8, 'learning_rate': 0.20,
                      'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                         metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[69]:
               train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
           35
                      33252.0
                                                             2168.0
                                    396.0
                                                56509.0
           36
                      32964.0
                                    418.0
                                                56498.0
                                                             2184.0
```

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56446.0

2202.0

56

57

31219.0

31045.0

460.0

476.0

```
bst.tail().round()
Out[70]:
              train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
                                                          2259.0
          35
                    36054.0
                                  273.0
                                              56535.0
          36
                    35755.0
                                  249.0
                                              56506.0
                                                          2233.0
                                  285.0
                                              56471.0
                                                          2252.0
          37
                    35538.0
          38
                    35249.0
                                  419.0
                                              56425.0
                                                          2299.0
                    35024.0
                                  390.0
                                              56387.0
                                                          2263.0
          39
In [71]: # Change the parameters.
          params = {'booster': 'gbtree', 'max_depth': 9, 'learning_rate': 0.15,
                     'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.cv(params, dtrain, num_boost_round=40, nfold=10,
                        metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[71]:
              train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
                                                          2107.0
          35
                    30189.0
                                  366.0
                                              56769.0
          36
                    29867.0
                                  408.0
                                              56739.0
                                                          2082.0
          37
                    29581.0
                                  447.0
                                              56706.0
                                                          2098.0
          38
                    29367.0
                                  483.0
                                              56673.0
                                                          2077.0
          39
                    29062.0
                                  468.0
                                              56666.0
                                                          2038.0
 In [ ]: ### COMMENTS:
          # Best parameters thus far: max_depth = 8; eta = 0.15.
          # And from the following cell, it looks like we can use 60 rounds.
In [73]: # Try with 60 rounds.
          # Change the parameters.
          bst = xgb.cv(params, dtrain, num_boost_round=60, nfold=10,
                        metrics= ['rmse'], early_stopping_rounds= 3)
          bst.tail().round()
Out[73]:
              train-rmse-mean train-rmse-std test-rmse-mean test-rmse-std
          55
                    31401.0
                                                          2358.0
                                  475.0
                                              55963.0
```

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55929.0

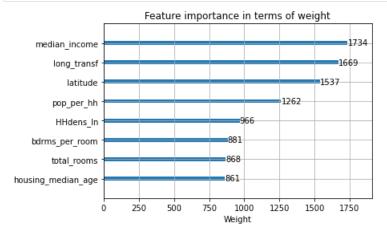
55927.0

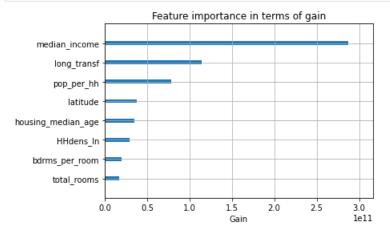
2363.0 2372.0

```
bst = xgb.train(params, dtrain, num_boost_round=60)
preds = bst.predict(dtest)
```

In [83]: bst\_rmse = round(np.power(sum(np.power(preds - np.array(y\_test), 2))/len(y\_test), print(bst\_rmse)
# 52,696

52696





```
In [84]: # Function to obtain comparative rmse scores for our xgb model.

def get_xgb_rmse(seedv, dat):
    # dat needs to also have median_house_value as a column.
```

vout[i] = round(np.power(sum(np.power(df preds - np.array(y df), 2))/

Comparative rmse score for the xgb model: \$49,090

# it makes use of the ocean\_proximity predictor.

df\_preds = bst.predict(df\_test)

```
In [86]: # The following is a score for districts with a median_house_value < 500K.

testdat2 = testdat[testdat.median_house_value < 500000].copy()

start_time = datetime.now()
    rmse_score = get_xgb_rmse(smp, testdat2)
    stop_time = datetime.now()
    delta = stop_time - start_time
    timeval = round(delta.seconds/60, 2)
    print("Time difference of " + str(timeval) + " minutes")

# Time difference of 0.02 minutes

print("")
    print("Comparative rmse score for the xgb model when median house value < 506
        f'{rmse_score:,.0f}')

# $45,432

# The previous gradient boosting model has a score of 46.3K.</pre>
```

Time difference of 0.02 minutes

Comparative rmse score for the xgb model when median house value < 500K: \$4!

## Try xgboost with the ocean\_proximity predictor

As we see in what follows, the xgboost algorithm gives us a better model when we do not include ocean\_

```
In [98]: X_train_9preds.columns
```

```
In [101]: # We need to pass an ndarray object to xgb.DMatrix. So the
          # categorical variable needs to be converted to dummy variables.
          dumvars_train = pd.get_dummies(X_train_9preds['ocean_proximity'])
          dumvars train.head()
Out[101]:
                INLAND NEAR BAY NEAR OCEAN OCEAN
            334
            1662
                     1
                                                0
            8781
            9392
                              1
                                                0
           10706
                                                1
In [102]: X train xgb = X train 9preds.join(dumvars train)
          X_train_xgb.drop(['ocean_proximity'], axis=1, inplace=True)
          X_train_xgb.shape
Out[102]: (16482, 12)
In [119]: # Do the same for the test set.
          dumvars_test = pd.get_dummies(X_test_9preds['ocean_proximity'])
          X_test_xgb = X_test_9preds.join(dumvars_test)
          X_test_xgb.drop(['ocean_proximity'], axis=1, inplace=True)
          X_test_xgb.shape
Out[119]: (4121, 12)
In [104]: dtrain = xgb.DMatrix(X train xgb, label= y train)
          dtest = xgb.DMatrix(X_test_xgb, label= y_test)
```

#### Find optimal parameters

38340.0

Out [106] .

74

out[100].		train-rmse-mean	train-rmse-std	test-rmse-mean	test-rmse-std
	70	38883.0	424.0	56769.0	1839.0
	71	38725.0	417.0	56775.0	1854.0
	72	38589.0	410.0	56768.0	1872.0
	73	38474.0	411.0	56755.0	1864.0

439.0

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56754.0

1892.0

	train-rmse-mean	train-rmse-std	test-rmse-mean	test-rmse-std
55	35815.0	459.0	56673.0	2423.0
56	35619.0	445.0	56637.0	2422.0
57	35462.0	439.0	56631.0	2425.0
58	35277.0	485.0	56627.0	2431.0

#### Out[112]:

		train-rmse-mean	train-rmse-std	test-rmse-mean	test-rmse-std
-	13	33683.0	559.0	56431.0	2286.0
4	14	33404.0	549.0	56416.0	2248.0
4	15	33177.0	569.0	56398.0	2194.0
4	16	32921.0	534.0	56350.0	2170.0
4	17	32608.0	600.0	56315.0	2190.0

#### Construct xgb model for predictions

```
In [113]:
    params = {'booster': 'gbtree', 'max_depth': 8, 'learning_rate': 0.15,
        'objective': 'reg:squarederror', 'eval_metric': 'rmse'}

    bst = xgb.train(params, dtrain, num_boost_round=48)

    preds = bst.predict(dtest)
    bst_rmse = round(np.power(sum(np.power(preds - np.array(y_test), 2))/len(y_teprint(bst_rmse))
# 52,770

# The score was a bit lower (52,696) without ocean_proximity.
```

52770

```
In [121]: # The following is a score for all test districts.

testdat = X_test_xgb.join(y_test)

seed_choices = np.arange(start=1000, stop=21000, dtype=int)
np.random.seed(4321)
smp = np.random.choice(seed_choices, size=500, replace=False)

rmse_score = get_xgb_rmse(smp, testdat)

print("Comparative rmse score for the xgb model that includes ocean_proximit)
    f'{rmse_score:,.0f}')
```

```
start_time = datetime.now()
rmse_score = get_xgb_rmse(smp, testdat2)
stop_time = datetime.now()
delta = stop_time - start_time
timeval = round(delta.seconds/60, 2)
print("Time difference of " + str(timeval) + " minutes")
# Time difference of 0.02 minutes
print("")
print("Comparative rmse score for the xgb model when median house value < 500
      f'{rmse_score:,.0f}')
# $46,181
# The previous gradient boosting model has a score of 45.4K.
```

Time difference of 0.02 minutes

Comparative rmse score for the xgb model when median house value < 500K: \$40

#### Run better model with more rounds

```
In [123]: | dtrain = xgb.DMatrix(X_train_8preds, label= y_train)
          dtest = xgb.DMatrix(X_test_8preds, label= y_test)
In [132]: params = {'booster': 'gbtree', 'max_depth': 8, 'learning_rate': 0.15,
                     'objective': 'reg:squarederror', 'eval_metric': 'rmse'}
          bst = xgb.train(params, dtrain, num boost round=80)
          preds = bst.predict(dtest)
          bst_rmse = round(np.power(sum(np.power(preds - np.array(y_test), 2))/len(y_te
          print(bst_rmse)
          # 52,366
          # This same model at 60 rounds had a score of 52,696
          52366
In [133]: # The following is a score for all test districts.
          testdat = X_test_8preds.join(y_test)
          seed_choices = np.arange(start=1000, stop=21000, dtype=int)
          np.random.seed(4321)
          smp = np.random.choice(seed_choices, size=500, replace=False)
          rmse_score = get_xgb_rmse(smp, testdat)
          print("Comparative rmse score for the xgb model with 80 rounds: " + '$' +
                f'{rmse_score:,.0f}')
          # $48,548
          # The gradient boosting model that included ocean proximity has a
```

```
stop_time = datetime.now()
delta = stop_time - start_time
timeval = round(delta.seconds/60, 2)
print("Time difference of " + str(timeval) + " minutes")
# Time difference of 0.02 minutes

print("")
print("Comparative rmse score for the xgb model with 80 rounds when median hc f'{rmse_score:,.0f}')

# $45,139

# The gradient boosting model that included ocean_proximity
# has a score of 46.3K.
```

Time difference of 0.02 minutes

Comparative rmse score for the xgb model with 80 rounds when median house va $^{-1}$  \$45,139

In [ ]:

## Final comments on gradient boosting

Two of the gradient boosting models have near equal performance. One uses ocean\_proximity; the other the model with fewer predictors. Its rmse score is about \$150 more than the gradient boosting model that ocean\_proximity. But if we predict only for districts with a median house value < 500K, then the xgb mode cousin by \$1,200. Also, the xgboost model is quite a bit faster.

There may be other xgboost models that are even better. I only scratched the surface here.

Gradient boosted regression best score: 48.5K

In [ ]:

#### Final comments for Part02

From the models surveyed, we obtain the best set of predictions, on average, from an xgboost model. Remodel from Part01 has an rmse score of 75.5K. By contrast, the xgboost model has a score of 48.5K. The reduction in the score.

The work involved in producing the g03 model made life significantly easier when surveying the above ra learning models, for it provided me with a core set of predictors to focus on. In the end, I went from using using 8 of the original 13. Also, because g03 is a parametric model that can be tuned without relying on a could use it in the Gibbs sampler to impute values for the records with a censored median house value.

In [ ]: