## Modeling with k-means, Part 1

The overall aim of this project is to understand the extent to which the k-means algorithm can help us build better classification models than what we can already construct using various supervised learning approaches. Here I am employing k-means as a supervised learning algorithm, giving it information about the labels indirectly in two distinct ways: (1) through input from one or more supervised learning algorithms in the form of an additional variable, or probability column; and (2) through the addition of weights in the dissimilarity measure, the weights arrived at through cross-validation scores that rely on the labels, or response variable.

Even when k-means is used for unsupervised learning, there are a number of ways we guide, or constrain, the algorithm. For example, (a) we tell it the number of clusters to find; (b) we select the variables we want the algorithm to work with; and (c) we choose the transformations to apply to those variables. Variable selection and variable transformations greatly affect the results we see when applying k-means. The less appropriate the inputs to the algorithm are, the less useful the results will be.

A fourth way we can guide the algorithm is by applying weights to the variables. While this is a variant of (c), it deserves its own category because the weights I refer to appear in our object dissimilarity measure and are used to regulate a variable's relative influence "in determining the overall dissimilarity between objects [i.e., observations]" (p.505 of *The Elements of Statistical Learning, Second Edition*, by Hastie, Tibshirani, and Friedman; see Equation (14.24)). In the modeling that follows, the weight given to a variable depends on the role the variable has, in the presence of the other variables, in partitioning the data into the subgroups that are of interest to us. Those variables assigned a greater weight are, we might say, more important for correctly identifying these subgroups, while the variables assigned a smaller weight are less important. In any case, it is very likely we will not know what weights to assign unless we have data to work with in which the subgroups of interest are already identified, or labeled. When k-means is used in an unsupervised learning setting, this information is not available to us.

Sometimes, however, we do have the data we need in order to assign meaningful and relevant weights. These are the scenarios that are of interest to me in this project. Preliminary results have shown that a k-means classification model can rival, or even outperform, other classification models. This is what we see in Parts 1 and 2 of this project, where I work with data on "downer cows". In Part 3 I again take up the California housing dataset. Optimal weights are much harder to establish for the variables in that dataset since the number of predictors more than doubles and the amount of training data is 33X greater. Preliminary results with the CA dataset show that k-means can provide us with a model whose performance is on par with the best random forest model I was able to find.

In Part 5 I continue to work with the CA dataset, but this time trying to identify 3 subgroups rather than just 2. In Part 4 I work with the Italian wine dataset used by Kabacoff (*R in Action*, p.370); there are 3 varieties to identify.

\* \* \* \* \*

The downer cow data for Part 1 are introduced on p.266 of Sanford Weisberg's Applied Linear Regression, 3rd Edition:

"For unknown reasons, dairy cows sometimes become recumbent---they lay down. Called *downers*, these cows may have a serious illness that may lead to death of the cow. These data are from a study of blood samples of over 400 downer cows studied at the Ruakura New Zealand Animal Health Laboratory during 1983-1984. A variety of blood tests were performed, and for many of the animals, the outcome (survived, died, or animal was killed) was determined. The goal is to see if survival can be predicted from the blood measurements. The variables in the data file *downer.txt* are described [below]. These data were collected from veterinary records, and not all variables were recorded for all cows."

\* \* \* \* \*

## Section 1: Initial look at the cow data

In this section I look at some of the relationships between the variables in the dataset and choose a subset of these variables for model construction.

In [ ]: require(car)
require(repr)

```
require(ggplot2)
        require(stringr)
        require(faraway)
        require(parallel)
        require(randomForest)
        require(gbm)
        require(plyr)
        require(e1071)
In [2]: options(digits= 5, show.signif.stars= FALSE)
In [3]: | df <- read.table("/home/greg/Documents/stat/alr3data/downer.txt", header= TRUE)</pre>
        dim(df)
        colnames(df)
        435 9
        'Calving' 'Daysrec' 'CK' 'AST' 'Urea' 'PCV' 'Inflamat' 'Myopathy' 'Outcome'
In [ ]: # Description of the variables in the dataset:
        # Outcome : = 1 if the cow survived; 0 if it died or was killed
        ### Categorical variables:
        # Calving : = 0 if measurements were taken before calving; = 1 if taken after.
        # Inflamat : Is inflammation present? 0 = no; 1 = yes.
        # Myopathy : Is muscle disorder present? 0 = no; 1 = yes.
        ### Continuous variables:
        # Daysrec : days recumbent when measurements were taken.
        # CK : serum creatine phosphokinase (in U/l at 30C)
        # AST : serum asparate amino transferase (in U/l at 30C)
        # Urea : serum ureas (in mmol/l)
        # PCV : packed cell volume (hematocrit), percent
In [4]: # For the categorical variables, we should note the
        # degree to which the data is imbalanced. The
        # following output shows that 38% of the 435 cows
        # survived.
        table(df$Outcome)
        round(mean(df$0utcome, na.rm=TRUE), 4)
        269 166
        0.3816
In [4]: table(df$Inflamat, useNA= "ifany")
                1 <NA>
          38
               98 299
```

```
In [5]: table(df$Calving, useNA= "ifany")
            0
                 1 <NA>
          107 324
 In [6]: table(df$Myopathy, useNA= "ifany")
                 1 <NA>
          127
                95 213
 In [7]: summary(df$Daysrec)
                                                              NA's
            Min. 1st Qu.
                          Median
                                     Mean 3rd Qu.
                                                      Max.
           0.000
                   0.000
                                    1.947 3.000 20.000
                            1.000
 In [3]: # Percent of cows recumbent < 1 day.</pre>
         val <- dim(df[which(df$Daysrec < 1),])[1]</pre>
         round(val/nrow(df), 3)
         0.308
 In [8]: summary(df$CK)
            Min. 1st Qu.
                          Median
                                     Mean 3rd Qu.
                                                      Max.
                                                              NA's
              13
                      560
                             1760
                                     5352
                                             5467
                                                     71000
                                                                22
 In [9]: summary(df$AST)
                                                              NA's
            Min. 1st Qu.
                           Median
                                     Mean 3rd Qu.
                                                      Max.
            33.0
                  123.0
                            240.0
                                    398.4 492.0 2533.0
                                                                 6
In [10]: summary(df$Urea)
                                     Mean 3rd Qu.
                                                              NA's
            Min. 1st Qu.
                           Median
                                                     Max.
           1.000
                   5.625
                            7.600
                                    9.803 10.975 50.000
                                                               169
In [11]: summary(df$PCV)
            Min. 1st Qu.
                                     Mean 3rd Qu.
                                                              NA's
                           Median
                                                     Max.
                  32.00
                            35.00
                                    35.56
                                           40.00
                                                               260
           13.00
                                                    61.00
In [15]: # To what degree does Calving "explain" Outcome?
         fit_calv <- glm(Outcome ~ Calving, data=df, family= binomial())</pre>
         summary(fit_calv)
```

```
Call:
         glm(formula = Outcome ~ Calving, family = binomial(), data = df)
         Deviance Residuals:
                     10 Madian
            M: ~
                                      ^{2}
                                             M-..
In [16]: # To what degree does Inflamat explain Outcome?
         fit infla <- glm(Outcome ~ Inflamat, data=df, family= binomial())</pre>
         summary(fit_infla)
         Call:
         glm(formula = Outcome ~ Inflamat, family = binomial(), data = df)
         Deviance Residuals:
                                      30
            Min
                     10 Median
                                             Max
          -1.089
                 -0.855
                         -0.855
                                  1.268
                                           1.539
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                      -0.211
                                    0.326
                                          -0.65
                                                      0.52
         Inflamat
                       -0.607
                                    0.393
                                            -1.54
                                                      0.12
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 175.35 on 135 degrees of freedom
         Residual deviance: 172.99 on 134 degrees of freedom
           (299 observations deleted due to missingness)
         AIC: 177
         Number of Fisher Scoring iterations: 4
In [17]: # Look at Calving and Inflamat together.
         fit calv infla <- glm(Outcome ~ Calving*Inflamat, data=df, family= binomial())</pre>
         summary(fit calv infla)
         Call:
         glm(formula = Outcome ~ Calving * Inflamat, family = binomial(),
             data = df)
         Deviance Residuals:
            Min
                     1Q Median
                                     30
                                             Max
         -1.096 -0.914 -0.914 1.261
                                           2.265
         Coefficients:
                          Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                            -0.2877
                                        0.7638
                                                -0.38
                                                          0.706
                                                          0.912
         Calving
                            0.0935
                                        0.8447
                                                  0.11
                                                          0.089
         Inflamat
                            -2.1972
                                        1.2910
                                                 -1.70
         Calving:Inflamat 1.7333
                                        1.3599
                                                  1.27
                                                          0.202
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 175.35 on 135 degrees of freedom
         Residual deviance: 168.40 on 132 degrees of freedom
           (299 observations deleted due to missingness)
         AIC: 176.4
         Number of Fisher Scoring iterations: 5
In [26]: # To what degree does Myopathy explain Outcome?
         fit myop <- glm(Outcome ~ Myopathy, data=df, family= binomial())</pre>
         summary(fit_myop)
```

```
Call:
         glm(formula = Outcome ~ Myopathy, family = binomial(), data = df)
         Deviance Residuals:
            Min 1Q Median
                                              Max
         -0.987 -0.987 -0.361 -0.361
         Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                        -0.465
                                    0.182 -2.55
         Myopathy
                        -2.232
                                     0.459
                                             -4.86 1.2e-06
         (Dispersion parameter for binomial family taken to be 1)
         Null deviance: 248.57 on 221 degrees of freedom Residual deviance: 214.14 on 220 degrees of freedom
            (213 observations deleted due to missingness)
         AIC: 218.1
         Number of Fisher Scoring iterations: 5
 In [3]: # Function for computing the probability that the response
         # variable is 1 given the value of the predictor, its
         # logistic regression coefficient (link = logit), and
         # the coefficient of the intercept.
         get_prob <- function(x, coeffs) {</pre>
             b0 <- as.numeric(coeffs[1])</pre>
             b1 <- as.numeric(coeffs[2])</pre>
             prob <- (\exp(b0 + b1*x)/(1 + \exp(b0 + b1*x)))
             return(round(prob, 3))
In [30]: # Probability of the "average" sick cow surviving if
         # muscle disorder is not present.
         get_prob(0, fit_myop$coeff)
         0.386
In [31]: # Probability of the "average" sick cow surviving if
         # muscle disorder IS present.
         get_prob(1, fit_myop$coeff)
         0.063
 In [ ]: ### COMMENTS:
         # Myopathy, as we would expect, is an important predictor.
         # However, this variable is missing for nearly half of the
         # observations in the dataset.
         # The negative coefficient in the above regression model is
         # another way to see that when myopathy is present, the
         # likelihood of the cow surviving decreases.
In [20]: # Is Calving important, controlling for Myopathy? (The
         # interaction term has a non-significant p-value and,
         # thus, is not used in the following model.)
         fit_calv_myop <- glm(Outcome ~ Calving + Myopathy,</pre>
                               data=df, family= binomial)
         summary(fit_calv_myop)
```

```
Call:
         glm(formula = Outcome ~ Calving + Myopathy, family = binomial(),
             data = df
         Deviance Residuals:
             Min
                       1Q
                          Median
         -1.0536 -0.9703 -0.3543
                                   0.0609
                                              2.3663
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                      -0.298
                                   0.365 -0.82
         (Intercept)
                                                     0.41
         Calving
                       -0.210
                                   0.401
                                           -0.53
                                                     0.60
         Myopathy
                       -2.228
                                   0.462
                                          -4.82 1.4e-06
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 247.43 on 219 degrees of freedom
         Residual deviance: 213.60 on 217 degrees of freedom
           (215 observations deleted due to missingness)
         AIC: 219.6
         Number of Fisher Scaring iterations: 5
In [32]: # Is Daysrec a predictor of Outcome?
         fit_daysre <- glm(Outcome ~ Daysrec, data=df, family= binomial())</pre>
         summary(fit_daysre)
         Call:
         glm(formula = Outcome ~ Daysrec, family = binomial(), data = df)
         Deviance Residuals:
            Min
                    1Q Median
                                     30
                                            Max
         -1.103 -1.034 -0.842
                                1.254
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                          -1.36 0.17311
         (Intercept) -0.1782
                                 0.1308
                                  0.0512
                                          -3.30 0.00097
         Daysrec
                      -0.1689
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 574.57 on 431 degrees of freedom
         Residual deviance: 561.62 on 430 degrees of freedom
           (3 observations deleted due to missingness)
         AIC: 565.6
         Number of Fisher Scoring iterations: 4
In [33]: # The 3rd quartile for Daysrec is 3.0. Here is the probability
         # of the average downer cow surviving if it has been recumbent
         # for 3 days.
         get_prob(3.0, fit_daysre$coeff)
         0.335
In [34]: # The probability that the average cow survives increases as
         # the number of days recumbent decreases.
         get_prob(0, fit_daysre$coeff)
         0.456
 In [ ]: ### COMMENT:
         # Since Daysrec is predictive of the outcome, we perhaps
```

```
# ought to control for this variable when regressing
         # Outcome on the blood measurements.
         # Further downstream I regress CK and AST on Daysrec.
         # The results tell us that we should control for
         # Daysrec.
In [31]: # Is Calving predictive when we control for Daysrec?
         fit_daysre_calv <- glm(Outcome ~ Daysrec + Calving, data=df,</pre>
                                family= binomial())
         summary(fit daysre calv)
         glm(formula = Outcome ~ Daysrec + Calving, family = binomial(),
             data = df
         Deviance Residuals:
            Min
                 1Q Median
                                     30
                                            Max
         -1.146 -1.026 -0.834
                                 1.230
                                          2.468
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                      -0.3682
                                  0.2268
                                           -1.62 0.10447
         Daysrec
                      -0.1877
                                  0.0537
                                            -3.49 0.00048
                                  0.2398
                                            1.22 0.22158
         Calving
                       0.2931
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 569.75 on 427 degrees of freedom
         Residual deviance: 553.09 on 425 degrees of freedom
           (7 observations deleted due to missingness)
         AIC: 559.1
         Number of Fisher Scoring iterations: 4
In [32]: # Is Inflamat predictive when we control for Daysrec?
         fit daysre infla <- glm(Outcome ~ Daysrec + Inflamat, data=df,
                                family= binomial())
         summary(fit_daysre_infla)
         glm(formula = Outcome ~ Daysrec + Inflamat, family = binomial(),
             data = df
         Deviance Residuals:
                    1Q Median
                                     3Q
                                            Max
         -1.197 -0.984 -0.736
                                1.347
                                          1.813
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                  0.3499
         (Intercept)
                      0.0459
                                            0.13
                                                    0.896
         Daysrec
                      -0.2594
                                  0.1228
                                           -2.11
                                                    0.035
         Inflamat
                      -0.4360
                                  0.4035
                                           -1.08
                                                    0.280
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 175.35 on 135 degrees of freedom
         Residual deviance: 167.83 on 133 degrees of freedom
           (299 observations deleted due to missingness)
         AIC: 173.8
         Number of Fisher Scoring iterations: 4
In [33]: # Is Myopathy still predictive when we control for Daysrec?
```

```
fit daysre myop <- glm(Outcome ~ Daysrec + Myopathy, data=df,
                                family= binomial())
         summary(fit_daysre_myop)
         Call:
         glm(formula = Outcome ~ Daysrec + Myopathy, family = binomial(),
             data = df
         Deviance Residuals:
                    1Q Median
                                     30
            Min
                                            Max
         -1.013 -0.977 -0.370 -0.310
                                          2.367
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                     -0.3700
                                  0.3484
                                           -1.06
         (Intercept)
                                                     0.29
                      -0.0305
                                  0.0955
                                            -0.32
                                                     0.75
         Daysrec
         Myopathy
                      -2.2469
                                  0.4626
                                           -4.86 1.2e-06
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 248.57 on 221 degrees of freedom
         Residual deviance: 214.03 on 219 degrees of freedom
           (213 observations deleted due to missingness)
         AIC: 220
         Number of Fisher Scoring iterations: 5
 In [ ]: ### COMMENT:
         # Daysrec and Myopathy are doing some of the same work.
         # The p-value on Daysrec in the above model says we do
         # not need this variable when we have Myopathy in the
         # model.
         # An increase in the value of either variable means that
         # a cow's chances of surviving go down.
In [23]: # To what extent does Daysrec predict Myopathy?
         tmpdat <- na.omit(df[, c("Myopathy", "Daysrec")])</pre>
         mod_daysre_myop <- glm(Myopathy ~ I(Daysrec^0.5), data=tmpdat,</pre>
                                family= binomial)
         summary(mod daysre myop)
         glm(formula = Myopathy ~ I(Daysrec^0.5), family = binomial, data = tmpdat)
         Deviance Residuals:
            Min
                    1Q Median
                                     30
                                            Max
         -1.230 -1.105 -0.876
                                  1.251
                                          1.990
         Coefficients:
                        Estimate Std. Error z value Pr(>|z|)
                                      0.392
                                               2.13 0.0328
         (Intercept)
                           0.837
                                                      0.0023
         I(Daysrec^0.5)
                                      0.234
                                              -3.05
                          -0.713
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 303.13 on 221 degrees of freedom
         Residual deviance: 293.01 on 220 degrees of freedom
         AIC: 297
         Number of Fisher Scoring iterations: 4
In [44]: # The following table is another way of seeing the
         # negative correlation between Daysrec and Myopathy.
```

```
aggregate(Daysrec ~ Myopathy, data=tmpdat, FUN= mean)
         A data.frame: 2 × 2
          Myopathy Daysrec
              <int>
                     <dbl>
                    3.1260
                    2.7053
In [49]: # Sample correlation between Myopathy and Daysrec.
          round(cor(tmpdat$Myopathy, sqrt(tmpdat$Daysrec)), 3)
         -0.211
 In [6]: # Function for computing "proportion of deviance explained", an
         # R-sqrd statistic for link= logit. See p.41 of Julian Faraway's # "Extending the Linear Model with R" (2006: Chapman & Hall).
         # This statistic is due to N. Nagelkerke (1991; see Faraway's
         # bibliography).
         get_RsqrdDev <- function(modl) {</pre>
              n obs <- length(modl$fitted.values)</pre>
              ans <- (1-exp((modl$deviance - modl$null.deviance)/n_obs))/(1-exp(-modl$null.deviance/n</pre>
              return(round(ans, 4))
In [45]: # In ordinary least squares regression (OLS), R-sqrd is the
         # square of the sample correlation between the predictor
         # and the response. What follows is a pseudo-correlation
         # based on the R-sqrd metric for logistic regression
         # computed by get_RsqrdDev.
         ans <- get_RsqrdDev(mod_daysre_myop)</pre>
         print(paste("Approximate correlation betw. Myopathy and Daysrec: ",
                     as.character(round(-sqrt(ans), 3)), sep=""))
          [1] "Approximate correlation betw. Myopathy and Daysrec: -0.245"
In [19]: # The negative correlation between Daysrec and Myopathy is a bit
         # surprising. However, since it is unlikely that the missing
         # Myopathy data is missing at random, there is reason to be skeptical
         # regarding this negative correlation. Or, the explanation for the
         # negative correlation might be as follows: if muscle disorder is
         # present, fewer days of recumbency are needed before one thinks
         # the cow is sick enough for blood samples to be drawn.
         # We get a sense of the rate of change in the table that follows.
         newdat \leftarrow c(0, 1, 4, 9, 16)
         dim(newdat) \leftarrow c(5, 1)
         newdat <- as.data.frame(newdat)</pre>
         colnames(newdat) <- c("Daysrec")</pre>
         # Find the probability that Myopathy = 1 as Daysrec varies.
         newdat$Prob <- round(predict(mod_daysre_myop, newdata=newdat, type="response"), 2)</pre>
         print(head(newdat))
```

Daysrec Proh

#### The blood measurement variables

```
In [7]: # Variable CK:
         fit ck <- glm(Outcome ~ I(log(CK)), data= df, family= binomial())</pre>
         summary(fit ck)
         Call:
         glm(formula = Outcome \sim I(log(CK)), family = binomial(), data = df)
         Deviance Residuals:
           Min 1Q Median
                                     30
                                            Max
         -2.134 -0.881 -0.561 1.059
                                          1.994
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                           6.89 5.7e-12
         (Intercept)
                     4.0006
                                  0.5809
                                           -7.71 1.2e-14
         I(log(CK))
                     -0.6117
                                  0.0793
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 550.49 on 412 degrees of freedom
         Residual deviance: 475.18 on 411 degrees of freedom
           (22 observations deleted due to missingness)
         AIC: 479.2
         Number of Fisher Scoring iterations: 3
In [38]: # Variable CK, controlling for Daysrec:
         fit_ck_days <- glm(Outcome ~ I(log(CK)) + Daysrec,</pre>
                            data= df, family= binomial())
         summary(fit_ck_days)
         Call:
         glm(formula = Outcome \sim I(log(CK)) + Daysrec, family = binomial(),
             data = df
         Deviance Residuals:
                   10 Median
                                     30
                                            Max
         -2.195 -0.885 -0.559 1.039
                                          2.072
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
         (Intercept) 4.0929 0.5887
                                         6.95 3.6e-12
         I(log(CK)) -0.5939
                                  0.0805
                                           -7.38 1.6e-13
         Daysrec
                      -0.1330
                                  0.0643
                                           -2.07
                                                    0.039
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 546.64 on 409 degrees of freedom
         Residual deviance: 465.95 on 407 degrees of freedom
           (25 observations deleted due to missingness)
         AIC: 471.9
         Number of Fisher Scoring iterations: 3
In [25]:
         # Regress CK on Daysrec to see whether the time when the
         # blood measurement was taken matters.
         resp_var_pwr <- -0.2
         ck_days <- lm(I(CK^resp_var_pwr) ~ Daysrec, data= df)</pre>
         summary(ck_days)
```

```
Call:
         lm(formula = I(CK^resp_var_pwr) ~ Daysrec, data = df)
         Residuals:
             Min
                      1Q Median
                                      30
         -0.1441 -0.0554 -0.0129 0.0452 0.3475
         Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
                               0.00529 47.51
         (Intercept) 0.25117
                                                 <2e-16
                                          -3.96
                     -0.00847
                                 0.00214
                                                   9e-05
         Daysrec
         Residual standard error: 0.0784 on 408 degrees of freedom
           (25 observations deleted due to missingness)
         Multiple R-squared: 0.0369,
                                      Adjusted R-squared: 0.0346
         F-statistic: 15.7 on 1 and 408 DF, p-value: 8.97e-05
 In [ ]: ### COMMENT:
         # Daysrec explains only 3.5% of the variation in CK.
In [35]: # Variable AST:
         fit_ast <- glm(Outcome ~ I(log(AST)), data= df, family= binomial())</pre>
         summary(fit_ast)
         Call:
         glm(formula = Outcome ~ I(log(AST)), family = binomial(), data = df)
         Deviance Residuals:
                 1Q Median
                                     30
            Min
                                            Max
         -1.889 -0.906 -0.535 1.020
                                          2.357
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                           7.33 2.4e-13
         (Intercept)
                        5.407
                                   0.738
         I(log(AST))
                       -1.089
                                   0.137
                                           -7.93 2.3e-15
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 569.75 on 428 degrees of freedom
         Residual deviance: 489.08 on 427 degrees of freedom
           (6 observations deleted due to missingness)
         AIC: 493.1
         Number of Fisher Scoring iterations: 4
In [39]: # Variable AST, controlling for Daysrec:
         fit_ast_days <- glm(Outcome ~ I(log(AST)) + Daysrec,</pre>
                             data= df, family= binomial())
         summary(fit_ast_days)
```

```
Call:
         glm(formula = Outcome \sim I(log(AST)) + Daysrec, family = binomial(),
             data = df
         Deviance Residuals:
                     10 Median
                                      30
                                             Max
         -1.905 -0.896 -0.539 1.005
                                           2.329
         Coefficients:
                      Fetimate Std Frrom 7 value Pr(>171)
 In [ ]: | ### COMMENTS:
         # We see from the above model that Daysrec and AST
         # are doing some of the same work in terms of
         # explaining the variance in the response variable.
         # The output suggests that we remove Daysrec
         # from the model. As already mentioned, I will keep
# Daysrec in the final model to control for the
         # effects of this variable on the measurements of
         # both CK and AST.
         # Also, having a third dimension is likely to help
         # the k-means algorithm and give a boost to the tree
         # models examined further downstream.
In [35]: # Regress AST on Daysrec to see whether the time when the
         # blood measurement was taken matters.
         resp_var_pwr <- -0.2
         ast_days <- lm(I(AST^resp_var_pwr) ~ Daysrec, data= df)</pre>
         summary(ast days)
         lm(formula = I(AST^resp_var_pwr) ~ Daysrec, data = df)
         Residuals:
              Min
                         1Q Median
                                           30
         -0.13600 -0.04345 -0.00063 0.04520 0.16391
         Coefficients:
                     Estimate Std. Error t value Pr(>|t|)
         (Intercept) 0.35054 0.00374 93.83 < 2e-16
                      -0.00719
                                  0.00119
                                           -6.04 3.4e-09
         Residual standard error: 0.06 on 424 degrees of freedom
           (9 observations deleted due to missingness)
         Multiple R-squared: 0.0792, Adjusted R-squared: 0.077
         F-statistic: 36.4 on 1 and 424 DF, p-value: 3.43e-09
 In [ ]: ### COMMENT:
         # Daysrec explains around 8% of the variation in AST.
In [36]: # Variable Urea:
         fit urea <- glm(Outcome ~ Urea, data= df, family= binomial())</pre>
         summary(fit urea)
```

```
Call:
         glm(formula = Outcome ~ Urea, family = binomial(), data = df)
         Deviance Residuals:
                                     30
           Min 1Q Median
                                            Max
         -1.388 -1.050 -0.703
                                1.230
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                   0.284
         (Intercept)
                        0.604
                                         2.13
         Urea
                       -0.121
                                   0.031
                                          -3.91 9.4e-05
         (Dispersion parameter for binomial family taken to be 1)
In [40]: # Variable Urea, controlling for Daysrec:
         fit urea days <- glm(Outcome ~ Urea + Daysrec, data= df,
                              family= binomial())
         summary(fit_urea_days)
         glm(formula = Outcome ~ Urea + Daysrec, family = binomial(),
             data = df)
         Deviance Residuals:
           Min 1Q Median
                                    30
                                           Max
         -1.584 -0.968 -0.551 1.077
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                 0.3668
         (Intercept)
                     1.3929
                                          3.80 0.00015
                      -0.1577
                                  0.0365
         Urea
                                           -4.32 1.6e-05
                      -0.3651
                                  0.0936
                                          -3.90 9.6e-05
         Daysrec
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 352.25 on 264 degrees of freedom
         Residual deviance: 309.69 on 262 degrees of freedom
           (170 observations deleted due to missingness)
         AIC: 315.7
         Number of Fisher Scoring iterations: 5
In [37]: # Variable PCV:
         fit pcv <- glm(Outcome ~ PCV, data= df, family= binomial())</pre>
         summary(fit pcv)
```

```
Call:
                                                hinamia1/\ da+a
In [41]: # Variable PCV, controlling for Daysrec:
         fit_pcv_days <- glm(Outcome ~ PCV + Daysrec, data= df,</pre>
                             family= binomial())
         summary(fit_pcv_days)
         glm(formula = Outcome ~ PCV + Daysrec, family = binomial(), data = df)
         Deviance Residuals:
            Min
                    1Q Median
                                     30
                                             Max
         -1.180 -0.960 -0.734
                                  1.277
         Coefficients:
                     Estimate Std. Error z value Pr(>|z|)
                                                    0.7445
         (Intercept)
                      0.2860
                                 0.8778
                                           0.33
         PCV
                                  0.0238
                                            -0.62
                      -0.0148
                                                    0.5345
         Daysrec
                      -0.3195
                                  0.1144
                                           -2.79
                                                    0.0052
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 223.69 on 174 degrees of freedom
         Residual deviance: 213.76 on 172 degrees of freedom
           (260 observations deleted due to missingness)
         AIC: 219.8
         Number of Fisher Scoring iterations: 4
In [36]: # Because Urea and PCV have quite a few missing values, I
         # drop these terms relatively quickly in the modeling that
         # follows.
         dfb <- df[, c("Outcome", "Daysrec", "CK", "AST", "Urea", "PCV")]</pre>
         435
```

### Find best logistic regression model for predicting Outcome

```
Call:
         glm(formula = Outcome \sim Daysrec + I(log(CK)) + I(log(AST)) +
             I(scale(Urea)) + I(scale(PCV)), family = binomial(), data = dfb)
         Deviance Residuals:
                  10 Median
                                     30
                                            Max
In [42]: # Remove PCV from the model because it has so many NAs. For
         # the f02 model we have 256 observations.
         f02 <- glm(Outcome ~ Daysrec + I(log(CK)) + I(log(AST)) +
                     I(scale(Urea)),
                     data= dfb, family= binomial())
         summary(f02)
         Call:
         glm(formula = Outcome \sim Daysrec + I(log(CK)) + I(log(AST)) +
             I(scale(Urea)), family = binomial(), data = dfb)
         Deviance Residuals:
                     10 Median
                                     30
         -2.160 -0.839 -0.349
                                  0.887
                                          3.239
         Coefficients:
                        Estimate Std. Error z value Pr(>|z|)
                                      1.093
                                               4.95 7.6e-07
         (Intercept)
                           5.404
         Daysrec
                          -0.209
                                      0.105
                                              -1.99 0.04653
         I(log(CK))
                          -0.302
                                      0.159
                                              -1.89 0.05824
                                              -2.32 0.02031
         I(log(AST))
                          -0.687
                                      0.296
                                      0.295
         I(scale(Urea))
                          -1.027
                                              -3.48 0.00049
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 341.64 on 255 degrees of freedom
         Residual deviance: 262.71 on 251 degrees of freedom
           (179 observations deleted due to missingness)
         AIC: 272.7
         Number of Fisher Scoring iterations: 5
In [43]: # Model without Urea; it, too, has many NAs. The f03
         # model has 408 observations.
         f03 <- glm(Outcome ~ Daysrec + I(log(CK)) + I(log(AST)),</pre>
                     data= dfb, family= binomial())
         summary(f03)
```

```
Call:
         glm(formula = Outcome \sim Daysrec + I(log(CK)) + I(log(AST)), family = binomial(),
 In [ ]: ### COMMENTS:
         # Each of Daysrec, CK, and AST are highly predictive of the
         # outcome. AST and Daysrec do some of the same work in terms
         # of predicting Outcome. Even so, it is important to control
         # for this variable since CK and AST are blood measurements
         # observed at different times for each cow. In this case,
         # time is measured by Daysrec. Also, as we saw above, Daysrec
         # explains around 3.5% of the variation in CK and around 8% of
         # the variation in AST.
In [50]: dfb <- df[, c("Outcome", "Daysrec", "CK", "AST")]</pre>
         nrow(dfb)
         435
In [51]: # Remove observations with missing values.
         dfb <- na.omit(dfb)</pre>
         dim(dfb)
         408 4
In [48]: # It often helps to model with time squared. However,
         # adding a quadratic, or the quadratic and cubic of
         # Daysrec, to our model does not help.
         Call:
         glm(formula = Outcome ~ Daysrec + I(Daysrec^2) + I(Daysrec^3) +
             I(log(CK)) + I(log(AST)), family = binomial(), data = dfb)
         Deviance Residuals:
            Min
                     10 Median
                                     30
                                             Max
         -2.175 -0.888
                        -0.520
                                  0.997
         Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
                      5.16501
                                  0.76990
         (Intercept)
                                             6.71
                                                      2e-11
         Daysrec
                       0.13925
                                  0.36068
                                             0.39
                                                     0.6994
         I(Daysrec^2) -0.09002
                                  0.15492
                                             -0.58
                                                     0.5612
         I(Daysrec^3) 0.00849
                                  0.01645
                                             0.52
                                                     0.6058
         I(log(CK))
                      -0.40182
                                  0.12602
                                                     0.0014
                                             -3.19
         I(log(AST)) -0.48462
                                  0.22086
                                             -2.19
                                                     0.0282
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 543.76 on 407 degrees of freedom
         Residual deviance: 457.09 on 402 degrees of freedom
         AIC: 469.1
         Number of Fisher Scoring iterations: 4
```

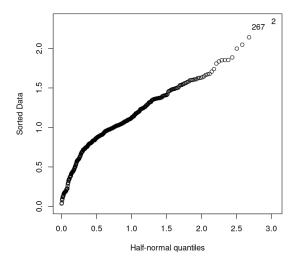
#### f03 model diagnostics

#### Check f03 for overdispersion

```
In [63]: # If we have overdispersion, the standard errors for the
# model coefficients will be too small.
```

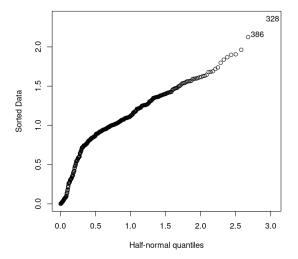
```
# We want the following value to NOT be considerably larger
         # than 1. If it is, then we have to use family= quasibinomial
         # in our modeling. (See p.311 of Kabacoff's "R in Action".)
         phi <- deviance(f03)/df.residual(f03)</pre>
         print(round(phi, 3))
         [1] 1.132
In [62]: # For a more accurate test, we need to also fit using family =
         # quasibinomial.
         f03_od <- glm(Outcome ~ Daysrec + I(log(CK)) + I(log(AST)),</pre>
                     data= dfb, family= quasibinomial)
In [64]: # See p.311 of Kabacoff's "R in Action". The null hypothesis
         # is that the dispersion (phi) = 1. The alternative hypothesis
         # is that phi != 1. If the following p-value is small (e.g.,
         \# < 0.05), we have good evidence for rejecting the null
         # hypothesis.
         ans <- pchisq(summary(f03 od)$dispersion * f03$df.residual,
                        f03$df.residual, lower= FALSE)
         round(ans, 4)
         0.5695
 In [ ]: ### COMMENT:
         # There is no evidence of overdispersion with the f03 model.
In [57]: length(f03$fitted.values)
         408
In [61]: # get RsqrdDev is defined above. It computes the "proportion
         # of deviance explained", an R-sqrd statistic for link= logit.
         f03_Rsqrd <- get_RsqrdDev(f03)</pre>
         print(f03_Rsqrd)
         # [1] 0.2588
         [1] 0.2588
In [43]: # Try different power transformations on the predictors to
         # see if we can boost the Rsqrd.
         f03_b <- glm(Outcome ~
                      I(Daysrec^1.5) +
                      I(CK^0.6) +
                      I(AST^{-0.33}),
                     data= dfb, family= binomial())
         summary(f03_b)
         print(get_RsqrdDev(f03_b))
         # [1] 0.2821
```

```
Call:
         glm(formula = Outcome \sim I(Daysrec^1.5) + I(CK^0.6) + I(AST^-0.33),
             family = binomial(), data = dfb)
         Deviance Residuals:
                     10 Median
         -1.836
                 -0.934 -0.419
                                  0.985
                                           2.345
         Coefficients:
                        Estimate Std. Error z value Pr(>|z|)
                        -0.56651
                                    0.81313
                                               -0.70
                                                        0.486
         (Intercept)
         I(Daysrec^1.5) -0.04411
                                    0.02874
                                               -1.53
                                                        0.125
         I(CK^0.6)
                        -0.00851
                                     0.00214
                                               -3.97
                                                      7.1e-05
         I(AST^-0.33)
                         6.65170
                                     3.49487
                                                1.90
                                                        0.057
         [1] 0.2821
In [44]: # Plot the residuals. Julian Faraway's half-normal plot can
         # be used to check for outliers. See p.46 of Faraway's
         # "Extending the Linear Model with R". The residuals plotted
         # here are the deviance residuals.
         options(repr.plot.width= 6, repr.plot.height= 6)
         # Function halfnorm is from package faraway.
         halfnorm(residuals(f03_b))
```



 $I(AST^{-0.3}),$ 

```
data= tmpdat, family= binomial())
         summary(f03 b2)
         print(get_RsqrdDev(f03_b2))
         Call:
         glm(formula = Outcome \sim I(Daysrec^1.3) + I(CK^1) + I(AST^-0.3),
             family = binomial(), data = tmpdat)
         Deviance Residuals:
            Min
                     10 Median
                                     30
                                            Max
         -1.798
                -0.954 -0.315
                                  0.979
                                          2.360
         Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
                        -1.22e+00
                                    7.88e-01 -1.55 0.12026
         (Intercept)
         I(Daysrec^1.3) -6.53e-02
                                    4.15e-02
                                               -1.57 0.11544
                                    5.71e-05
         I(CK^1)
                        -2.11e-04
                                               -3.71 0.00021
         I(AST^-0.3)
                         7.49e+00
                                    3.15e+00
                                                2.38 0.01734
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 539.92 on 405 degrees of freedom
         Residual deviance: 436.59 on 402 degrees of freedom
         AIC: 444.6
         Number of Fisher Scoring iterations: 6
         [1] 0.3055
In [54]: options(repr.plot.width= 6, repr.plot.height= 6)
         halfnorm(residuals(f03_b2))
```



```
I(Daysrec^1.3) +
I(CK^1) +
I(AST^-0.3),
```

```
data= tmpdat, family= binomial())
         summary(f03_b3)
         print(get_RsqrdDev(f03_b3))
         Call:
         glm(formula = Outcome \sim I(Daysrec^1.3) + I(CK^1) + I(AST^-0.3),
             family = binomial(), data = tmpdat)
         Deviance Residuals:
                  10 Median
                                     30
            Min
                                            Max
                                          2.243
         -1.817 -0.945 -0.264
                                  0.968
         Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
         (Intercept)
                        -1.184216
                                    0.811590
                                              -1.46 0.14453
         I(Daysrec^1.3) -0.063026
                                    0.041829
                                              -1.51 0.13187
                                    0.000064
         I(CK^1)
                        -0.000247
                                              -3.86 0.00011
         I(AST^-0.3)
                        7.495533
                                    3.221989
                                                2.33 0.02000
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 536.05 on 403 degrees of freedom
         Residual deviance: 425.80 on 400 degrees of freedom
         AIC: 433.8
         Number of Fisher Scoring iterations: 7
         [1] 0.3251
In [68]: # Tweak the power transformations.
         f03_b4 <- glm(Outcome ~
                      I(Daysrec^1.5) +
                      I(CK^1.25) +
                      I(AST^{-0.1}),
                     data= tmpdat, family= binomial())
         summary(f03 b4)
         print(get_RsqrdDev(f03_b4))
         Call:
         glm(formula = Outcome \sim I(Daysrec^1.5) + I(CK^1.25) + I(AST^-0.1),
             family = binomial(), data = tmpdat)
         Deviance Residuals:
            Min
                     10 Median
                                     30
                                            Max
         -1.746 -0.959 -0.233
                                  0.970
                                          2.274
         Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
                                   2.09e+00 -2.46 0.01392
         (Intercept)
                        -5.13e+00
         I(Daysrec^1.5) -4.16e-02
                                    2.93e-02
                                             -1.42 0.15546
         I(CK^1.25)
                        -2.41e-05
                                    6.91e-06 -3.49 0.00049
         I(AST^-0.1)
                        9.10e+00
                                    3.35e+00
                                               2.71 0.00671
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 536.05 on 403 degrees of freedom
         Residual deviance: 425.55 on 400 degrees of freedom
         AIC: 433.6
         Number of Fisher Scoring iterations: 7
         [1] 0.3257
```

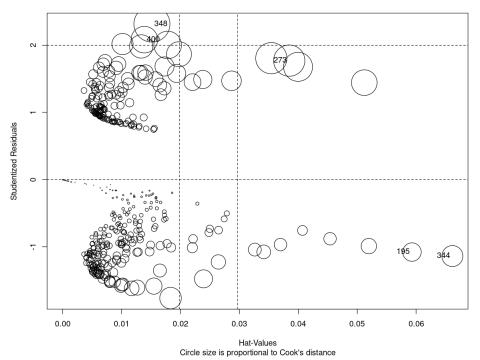
```
In [ ]: ### COMMENT:

# We started out with an Rsqrd of about 26%. With the
# power transformations and the removal of 4 outliers,
# we now have a model with an Rsqrd close to 32.6%.
```

#### A data.frame: 5 × 3

	StudRes	Hat	CookD
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
195	-1.0799	0.059290	0.012557
273	1.7705	0.038456	0.036109
344	-1.1393	0.066158	0.016244
348	2.3148	0.015148	0.047872
400	2.0827	0.013865	0.026058

#### Influence Plot for f03\_b4



```
In [70]: # Remove obs. 348 from tmpdat. Here the point is identified
# by its rowname.

tmpdat02 <- tmpdat[which(!(rownames(tmpdat) %in% c(348))),]</pre>
```

```
summary(f03_b5)
         print(get_RsqrdDev(f03_b5))
         Call:
         glm(formula = Outcome \sim I(Daysrec^1.5) + I(CK^1.2) + I(AST^-0.1),
             family = binomial, data = tmpdat02)
         Deviance Residuals:
            Min
                    1Q Median
                                     30
                                            Max
         -1.743
                -0.955
                         -0.207
                                  0.963
                                          2.127
         Coefficients:
                         Estimate Std. Error z value Pr(>|z|)
                        -4.75e+00
                                    2.13e+00
         (Intercept)
                                               -2.23 0.02544
                                    2.94e-02
         I(Daysrec^1.5) -4.29e-02
                                               -1.46 0.14515
         I(CK^1.2)
                        -4.28e-05
                                    1.17e-05
                                               -3.66 0.00025
         I(AST^-0.1)
                         8.55e+00
                                    3.41e+00
                                                2.51 0.01220
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 534.11 on 402 degrees of freedom
         Residual deviance: 420.23 on 399 degrees of freedom
         AIC: 428.2
         Number of Fisher Scoring iterations: 7
         [1] 0.3352
In [74]: # Adjust the power transformations.
         f03 b6 <- glm(Outcome ~
                      Daysrec +
                      I(CK^1.2) +
                      I(AST^{-0.1}),
                     data= tmpdat02, family= binomial)
         summary(f03 b6)
         print(get_RsqrdDev(f03_b6))
         glm(formula = Outcome \sim Daysrec + I(CK^1.2) + I(AST^-0.1), family = binomial,
             data = tmpdat02)
         Deviance Residuals:
                    1Q Median
            Min
                                     30
                                            Max
         -1.752 -0.960 -0.208
                                  0.959
                                          2.139
         Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
         (Intercept) -4.60e+00
                                 2.16e+00
                                            -2.13 0.03306
                     -1.06e-01
         Daysrec
                                 7.10e-02
                                             -1.50 0.13403
         I(CK^1.2)
                     -4.25e-05
                                 1.16e-05
                                             -3.66 0.00025
         I(AST^-0.1) 8.37e+00
                                 3.45e+00
                                             2.43 0.01519
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 534.11 on 402 degrees of freedom
         Residual deviance: 420.14 on 399 degrees of freedom
         AIC: 428.1
         Number of Fisher Scoring iterations: 7
         [1] 0.3355
In [75]: nrow(tmpdat02)
         403
```

```
In [76]: # Update our working dataframe.
         dfb <- tmpdat02
In [77]: # Save the file.
         write.csv(dfb, file="/home/greg/Documents/stat/github_repos/cows/downer.csv",
                  row.names= TRUE)
In [78]: # Re-construct the model with the dfb dataframe.
         f03_b6 <- glm(Outcome ~
                      Daysrec +
                      I(CK^1.2) +
                      I(AST^{-0.1}),
                     data= dfb, family= binomial())
         summary(f03_b6)
         print(get_RsqrdDev(f03_b6))
         # [1] 0.3355
         Call:
         glm(formula = Outcome \sim Daysrec + I(CK^1.2) + I(AST^-0.1), family = binomial(),
             data = dfb
         Deviance Residuals:
                     1Q Median
                                          2.139
         -1.752 -0.960 -0.208 0.959
         Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
         (Intercept) -4.60e+00 2.16e+00
                                           -2.13 0.03306
                    -1.06e-01
                                 7.10e-02
                                            -1.50 0.13403
         Daysrec
                   -4.25e-05
         I(CK^1.2)
                                 1.16e-05
                                            -3.66 0.00025
                                3.45e+00
         I(AST^-0.1) 8.37e+00
                                             2.43 0.01519
         (Dispersion parameter for binomial family taken to be 1)
             Null deviance: 534.11 on 402 degrees of freedom
         Residual deviance: 420.14 on 399 degrees of freedom
         AIC: 428.1
         Number of Fisher Scoring iterations: 7
         [1] 0.3355
In [79]: # If we do not lower the power transformation on CK, the
         # anova on the model generates a warning message
         # (probability of 0 or 1 in glm.fit). I find later
         # that even this is not enough to prevent the anova
         # function from issuing a warning. I am not sure what
         # the source of the problem is, especially given that
         # no such warning is generated by glm itself. (It may
         # be that the anova function uses different default
         # settings for glm.fit.)
         f03_b7 <- glm(Outcome ~
                      Daysrec +
                      CK +
                      I(log(AST)),
                     data= dfb, family= binomial())
         summary(f03 b7)
         print(get_RsqrdDev(f03_b7))
```

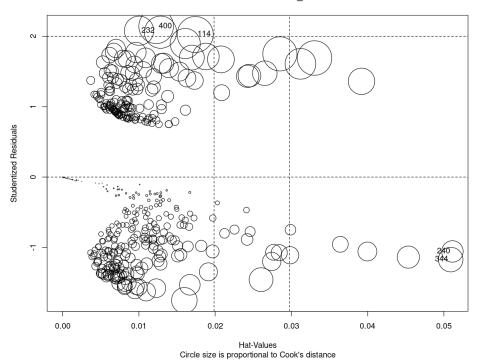
```
# [1] 0.3345
```

```
glm(formula = Outcome ~ Daysrec + CK + I(log(AST)), family = binomial(),
   data = dfb)
Deviance Residuals:
           1Q Median
                           30
                                  Max
-1.735 -0.955 -0.240
                        0.961
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) 2.862181
                       0.990384
                                   2.89 0.00385
Daysrec
           -0.108535
                       0.071057
                                  -1.53 0.12665
            -0.000264
                       0.000069
                                  -3.83 0.00013
I(log(AST)) -0.458373
                       0.209175
                                  -2.19 0.02843
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 534.11 on 402 degrees of freedom
Residual deviance: 420.53 on 399 degrees of freedom
AIC: 428.5
Number of Fisher Scoring iterations: 7
[1] 0.3345
```

A data.frame:  $5 \times 3$ 

	StudRes	Hat	CookD
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
114	2.0255	0.017385	0.028599
232	2.0792	0.010017	0.018825
240	-1.0569	0.051118	0.010145
344	-1.1725	0.050894	0.013265
400	2.1425	0.012260	0.026451

#### Influence Plot for f03\_b7



```
In [82]: options(repr.plot.width= 6, repr.plot.height= 6)
halfnorm(residuals(f03_b7), labs=rownames(dfb))
```

```
In [83]: # If we remove the last 3 influential points that are also
# outliers, our dataset will have been trimmed from 408
# records down to 400, a reduction of nearly 2%.
# Let's see what kind of difference this makes for our
# linear model.

tmpdat <- dfb[which(!(rownames(dfb) %in% c(400, 232, 114))),]
nrow(tmpdat)</pre>
400
```

```
Call:
         glm(formula = Outcome \sim Daysrec + CK + I(log(AST)), family = binomial,
             data = tmpdat)
         [1] 0.3565
In [85]: # Update our working dataframe.
         dfb <- tmpdat
In [86]: # Save the file. dfb has 400 records in it.
         write.csv(dfb, file="/home/greg/Documents/stat/github repos/cows/downer.csv",
                  row.names= TRUE)
```

#### Check model f03\_b8 for overdispersion

```
In [87]: # If the following value is close to 1, the dispersion is
         # close to what our model assumes it to be. Thus, no
         # need to correct for overdispersion.
         phi <- deviance(f03_b8)/df.residual(f03_b8)</pre>
         print(round(phi, 3))
```

[1] 1.028

```
In [89]: # See p.311 of Kabacoff's "R in Action". The null hypothesis
         # is that the dispersion (phi) = 1. The alternative hypothesis
         # is that phi != 1. If the following p-value is small (e.g.,
         \# < 0.05), we have good evidence for rejecting the null
         # hypothesis.
         f03b8_od <- glm(Outcome ~ Daysrec + CK + I(log(AST)),
                     data= dfb, family= quasibinomial)
         ans <- pchisq(summary(f03b8_od)$dispersion * f03_b8$df.residual,</pre>
                       f03_b8$df.residual, lower= FALSE)
         round(ans, 4)
         # 0.9884 (p-value)
```

0.9884

#### Using anova output, compute the importance of the f03 predictors

Here the importances of the predictors in the f03\_b8 model are determined by their anova contributions. Since there are 3 terms in the model and the order of the terms matters, I need to use 6 different models and average over each term's anova contribution for each model.

This section is included because I am curious to see whether the weights we arrive at for our base k-means model (with only AST, CK, and Daysrec as predictors) are at all like these anova weights.

\* \* \* \* \*

```
In [90]: # f03 b8 is our base model. It is built on all 400 remaining records.
         f03 anova <- anova(f03 b8)
         print(f03 anova)
```

```
Analysis of Deviance Table
           Model: binomial, link: logit
           Response: Outcome
           Terms added sequentially (first to last)
                        Df Deviance Resid. Df Resid. Dev
           NULL
                                            399
In [91]: | names(f03_anova)
           'Df' 'Deviance' 'Resid. Df' 'Resid. Dev'
In [136]: rownames(f03_anova)
           'NULL' 'Daysrec' 'CK' 'I(log(AST))'
In [92]: ss01 <- f03 anova$'Deviance'</pre>
           names(ss01) <- c("null", "Daysrec", "CK", "AST")</pre>
           ss01tot <- sum(as.numeric(ss01[2:4]))</pre>
           print(round(ss01tot, 4))
           [1] 121.17
 In [93]: dayrec percent <- round(ss01["Daysrec"]/ss01tot, 4)</pre>
           ck_percent <- round(ss01["CK"]/ss01tot, 4)</pre>
           ast_percent <- round(ss01["AST"]/ss01tot, 4)</pre>
           ss01_contribs <- c(dayrec_percent, ck_percent, ast_percent)</pre>
           print(ss01_contribs)
           Daysrec
                         CK
                                 AST
            0.1152 0.8474 0.0374
In [161]: # Function for gauging the importance of the predictors
           # in a model based on each predictor's anova contribution.
           # As currently written, this function will not work if our
           # model contains interaction terms. This function is
           # specific to the f03 series of models.
           get_f03contribs <- function(dat) {</pre>
               # NOTE: the columns in dat must have the power
               # transformations used in the model. The first
               # column of dat must be the model response variable.
               preds <- colnames(dat)[-1]</pre>
               resp <- colnames(dat)[1]</pre>
               # get all permutations of the predictors;
               n <- length(preds)</pre>
               perm_matrix <- gtools::permutations(n, n, preds)</pre>
               # create result vector for predictor contributions
               result \leftarrow rep(0, n)
               names(result) <- preds</pre>
               for(i in 1:nrow(perm_matrix)) {
                   pred_str <- paste(perm_matrix[i,], collapse= "+")</pre>
                   form <- as.formula(paste(as.character(resp), " ~ ", pred_str, sep=""))</pre>
```

```
modl <- glm(form, family= binomial, data= dat)</pre>
                   # The anova function calls glm.fit in a way that it sometimes
                   # produces warnings: "glm.fit: fitted probabilities numerically 0 or 1 occurred"
                   modl_anova <- suppressWarnings(anova(modl))</pre>
                   ss <- modl anova$'Deviance'</pre>
                   names(ss) <- rownames(modl_anova)</pre>
                   ss_total <- round(sum(as.numeric(ss[-1])), 2)</pre>
                   percents <- round(ss[-1]/ss_total, 6)</pre>
                   names(percents) <- names(ss)[-1]</pre>
                   # accumulate results
                   for(name in names(result)) {
                        result[name] <- as.numeric(result[name]) + as.numeric(percents[name])
                   }
               } # end of for-loop
               return(round(result/nrow(perm_matrix), 4))
In [139]: # Create the dataframe for use with get_f03contribs.
          tmpdat <- dfb
          tmpdat$AST <- log(tmpdat$AST)</pre>
          dim(tmpdat)
          colnames(tmpdat)
           400 4
          'Outcome' 'Daysrec' 'CK' 'AST'
In [162]: # The following weights are obtained using all 400 records.
          # These weights will be tested in Section 2 to see if they
          # can improve upon the basic k-means model, i.e., one without
          # weights.
          ans <- get_f03contribs(tmpdat)</pre>
          print(ans)
          # Daysrec
                           CK
              0.0528 0.5646 0.3827
          print(sum(ans))
          # [1] 1.0001
          Daysrec
                        CK
                                AST
            0.0528 0.5646 0.3827
           [1] 1.0001
```

#### Comments on anova weights

The anova weights are significantly different from the best weights for the k-means model of this Part 1 and from the best weights for the k-means model of the Part2 notebook that follows. (Part 2 also works with the cow data.)

```
The Part 1 k-means weights are: AST= 0.54; CK= 0.28; Daysrec=0.18
```

The Part 2 k-means weights are: AST= 0.59; CK= 0.27; Daysrec= 0.14

We see further downstream how these weights are obtained.

### Create training and test sets (320 rcds/ 80 rcds)

```
In [ ]: # For Part 1 of this project, I want the ratio
          # of surviving to non-surviving cows to be the
          # same in each of the two sets. In Part 2 of
          # this project, this constraint is removed.
          # Since the test set provides us with only a single
          # data point for model comparison, in Part 2 of this
          # project I no longer use a test set and simply
          # rely on cross-validation scores taken over a very
          # large number of folds (5000 in this case).
In [22]: dfb <- rbind(traindat, testdat)</pre>
          dim(dfb)
          colnames(dfb)
          400 4
          'Outcome' 'Daysrec' 'CK' 'AST'
In [29]: # We keep only Outcome, Daysrec, CK, and AST. 80% of the
          # records are assigned to the training set.
          set.seed(5491)
          # shuffle dfb
          smp <- sample(rownames(dfb), dim(dfb)[1], replace= FALSE)
dfb <- dfb[smp, c("Outcome", "AST", "CK", "Daysrec")]</pre>
          # Get ratio of surviving to non-surviving cows.
          dfb_surv <- dfb[which(dfb$0utcome==1),]</pre>
          dfb_nonSurv <- dfb[which(dfb$0utcome==0),]</pre>
          surv_ratio <- nrow(dfb_surv)/nrow(dfb)</pre>
          segmentsv <- c(320, 80)
          row_list <- vector("list", length=2)</pre>
          used_surv <- used_nonSurv <- c()</pre>
          for(k in 1:2) {
              surv_count <- round(surv_ratio * segmentsv[k])</pre>
              nonSurv\_count <- \ segmentsv[k] \ - \ surv\_count
              avail_survRows <- rownames(dfb_surv)[which(!(rownames(dfb_surv)) %in% used surv))]</pre>
              avail_nonSurvRows <- rownames(dfb_nonSurv)[which(!(rownames(dfb_nonSurv) %in% used_nonS
              if(k < 2) {
                   smp01 <- sample(avail_survRows, surv_count, replace=FALSE)</pre>
                   smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                   smp01 <- avail_survRows</pre>
                   smp02 <- avail_nonSurvRows</pre>
                   stopifnot(length(c(smp01, smp02)) == segmentsv[k])
              used_surv <- c(used_surv, smp01)</pre>
              used_nonSurv <- c(used_nonSurv, smp02)</pre>
              row_list[[k]] <- c(smp01, smp02)
          } # end of for-loop, index k
          testdat <- dfb[row_list[[2]],]</pre>
          traindat <- dfb[which(!(rownames(dfb) %in% rownames(testdat))),]</pre>
          dim(traindat)
          dim(testdat)
          320 4
```

80 4

### Section 2: Four different classification models

### Logistic regression: final model (g03)

When observations with missing values are removed from the original 435 record dataset, we are left with 408 records. Above I then constructed a linear model on these 408 records and found 8 of them to be outliers (relative to my model), some of which were also influential. These 8 records were removed from the dataset. In this section I now construct a model on a subset of the 400 remaining records.

This is not the normal approach to working with data. The removal of the model-based outliers may favor the logistic regression model over the other models looked at when comparing performance scores on the testset data However, since there is often an overlap between variable-relative outliers and model-based outliers, all models should do better on this subset of 400 remaining records, particularly the k-means model.

Also, much of the model comparison that follows will be done using cross-validation scores on folds of the training set. This is how we would do model selection in practice. Applying the models to the testset data is not all that helpful for comparing model performance because the amount of data we have to work with is so small. The cross-validation scores obtained below provide a much better measure of model generalizability.

```
Outcome AST
                             CK Daysrec
                  1 183
        331
                            325
                  1 117
        201
                           3300
                                       1
                  0 1133 39000
                                       3
        161
                                       0
        283
                  0
                      73
                            130
                       60
        404
                   0
                            482
        121
                   0 130
                            230
                                       2
In [7]: # I am satisfied with the current power transformations.
        g03 <- glm(Outcome ~ Daysrec + CK + I(log(AST)),
                    data= traindat, family= binomial)
        summary(g03)
        print(get RsgrdDev(g03))
        # [1] 0.3585
        glm(formula = Outcome ~ Daysrec + CK + I(log(AST)), family = binomial,
            data = traindat)
        Deviance Residuals:
           Min 1Q Median
                                     30
                                             Max
        -1.748 -0.912 -0.179 0.945
                                           2.127
        Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
        (Intercept) 2.82e+00
                                 1.11e+00
                                              2.53
                                                     0.0115
        Daysrec
                     -9.74e-02
                                 8.01e-02
                                             -1.22
                                                     0.2237
                     -3.10e-04
                                 8.57e-05
                                             -3.62
                                                     0.0003
                                 2.34e-01
        I(log(AST)) - 4.37e - 01
                                            -1.87
                                                     0.0615
        (Dispersion parameter for binomial family taken to be 1)
            Null deviance: 422.37 on 319 degrees of freedom
        Residual deviance: 324.84 on 316 degrees of freedom
        AIC: 332.8
        Number of Fisher Scoring iterations: 7
        [1] 0.3585
In [ ]: #&* Bookmark
In [8]: # Function to compute f-score for a 2x2 confusion matrix.
        get_fscore <- function(mat) {</pre>
            FN <- as.numeric(mat[2,1])</pre>
            TP \leftarrow as.numeric(mat[2,2])
            FP <- as.numeric(mat[1,2])</pre>
            recall <- TP/(TP + FN)
            precision <- TP/(TP + FP)</pre>
            f_score <- 2* (recall*precision)/(recall + precision)</pre>
            return(round(f_score, 4))
        }
In [9]: # Function to output a confusion matrix and the f-score
        # for that matrix (if it is 2x2).
        get_confusion <- function(preds, df_actual) {</pre>
            # df_actual is a one-column dataframe;
            # preds is a named vector of predictions;
            # preds is of type factor; it is assumed there
            # are at least 2 factor levels
            levs <- levels(preds)</pre>
            n_levs <- length(levs)</pre>
```

```
if(n_levs== 1) { levs <- c('0', '1') }</pre>
              n_levs <- max(n_levs, 2)</pre>
              actual <- as.vector(df_actual[, 1])</pre>
              names(actual) <- rownames(df_actual)</pre>
              datout <- rep(0, n_levs * (n_levs + 1))</pre>
              dim(datout) \leftarrow c(n levs, n levs + 1)
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c(levs, "class.error")</pre>
              rownames(datout) <- levs</pre>
              result <- vector("list", length= 2)</pre>
              names(result) <- c("matrix","f_score")</pre>
              # for each factor level, identify the rcd names
              # which should be classed as such
              for(rowlev in levs) {
                  actlev_names <- names(actual[actual == rowlev])</pre>
                  # columns are for the predicted values:
                  for(collev in levs) {
                       predlev_names <- names(preds[preds == collev])</pre>
                       if(length(predlev names > 0)) {
                           datout[rowlev, collev] <- sum(predlev_names %in% actlev_names)</pre>
                       }
                  }
                  nonrow_cols <- levs[!(levs %in% rowlev)]</pre>
                  datout[rowlev, "class.error"] <- round(sum(as.vector(datout[rowlev, nonrow_cols]))/</pre>
                                                             sum(as.vector(datout[rowlev, levs])), 4)
              }
              result$matrix <- datout
              if(n_levs == 2) {
                  result[[2]] <- get_fscore(as.matrix(datout))</pre>
              } else {
                  result$f_score <- NA
              return(result)
In [40]: preds <- predict(g03, newdata= traindat, type="response")</pre>
          print(round(head(preds), 3))
                 201 161 283 404
          0.439 0.405 0.000 0.711 0.706 0.604
In [41]: | preds_transf <- preds</pre>
          preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
          preds_transf[which(preds_transf < 0.5)] <- 0</pre>
          table(as.factor(preds_transf))
            0
                1
          201 119
In [42]: print(head(preds_transf))
          print(tail(preds_transf))
          331 201 161 283 404 121
                    0 1 1
           60 39 120 363 63 208
                   1 \quad 1 \quad 0
In [43]: preds_transf <- as.factor(preds_transf)</pre>
          ans <- get_confusion(preds_transf, traindat[, "Outcome", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for model g03, trainset (320 rcds): ", as.character(ans[[2]]), sep="")
```

```
# 0.6387
         # Accuracy = 73.125%
         # NOTE the even split between false positives and false negatives.
         # Type 2 is 0.6757
              0 1 class.error
         0 158 43
                       0.2139
         1 43 76
                        0.3613
          [1] "f-score for model g03, training set: 0.6387"
In [44]: # Get g03's scores on the testset of 80 records.
         preds <- predict(g03, newdata= testdat, type="response")</pre>
         preds transf <- preds</pre>
         preds transf[which(preds transf >= 0.5)] <- 1</pre>
         preds_transf[which(preds_transf < 0.5)] <- 0</pre>
         preds_transf <- as.factor(preds_transf)</pre>
         ans <- get_confusion(preds_transf, testdat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for model g03, testset (80 rcds): ", as.character(ans[[2]]), sep=""))
         # 0.6129
         \# Accuracy = 0.70
         # Type2 = 0.6477
         # Again note the near-even split betw. FPs and FNs.
             0 1 class.error
         0 37 13
                       0.2600
         1 11 19
                       0.3667
          [1] "f-score for model g03, testset (80 rcds): 0.6129"
```

## Random forest classifier (first look)

```
Call:
         [1] 0.6043
In [46]: preds <- predict(rfclf, newdata= testdat, type="response")</pre>
         print(head(preds))
         357 148 305 105 358 214
          1 0 1 0 1 1
         Levels: 0 1
In [47]: # f-score on the test set data:
         ans <- get_confusion(preds, testdat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for model rfclf, test set (80 rcds): ",
                     as.character(ans[[2]]), sep=""))
         # 0.5672
         # Accuracy: 63.75%
         # Type2 score: 0.5953
            0 1 class.error
         0 32 18
                  0.3600
                      0.3667
         1 11 19
         [1] "f-score for model rfclf, test set (80 rcds): 0.5672"
```

# **Gradient boosting classifier (first look)**

```
In [36]: # The output of this model is also dependent on the initial
         # seed value.
         options(repr.plot.width= 6, repr.plot.height= 4)
         set.seed(123)
         gbclf <- gbm(Outcome ~ ., data= traindat, n.trees= 100,</pre>
                      distribution= "bernoulli", shrinkage= 0.1)
         summary(gbclf)
         A data.frame: 3 x 2
                        rel.inf
                   var
                        <dbl>
                  <chr>
            AST
                   AST 45.7640
             CK
                    CK 45.1344
          Daysrec Daysrec 9.1016
            AST
            쏫
            Daysrec
               0
                      10
                             20
                                    30
                                            40
                           Relative influence
In [49]: print(head(gbclf$fit))
         In [50]: print(head(exp(gbclf$fit))/(1 + exp(gbclf$fit))))
         [1] 0.37298 0.50364 0.04309 0.72114 0.66185 0.60985
In [51]:
```

```
preds <- suppressMessages(predict(gbclf, newdata= traindat, type="response"))</pre>
          print(head(preds))
          [1] 0.37298 0.50364 0.04309 0.72114 0.66185 0.60985
In [52]: preds_transf <- preds</pre>
          names(preds_transf) <- rownames(traindat)</pre>
          preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
          preds_transf[which(preds_transf < 0.5)] <- 0</pre>
          table(as.factor(preds_transf))
            0
                1
          210 110
In [53]: preds_transf <- as.factor(preds_transf)</pre>
          print(head(preds_transf))
```

331 201 161 283 404 121

1 1

0 1 0

Levels: 0 1

```
In [54]: ans <- get_confusion(preds_transf, traindat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for gbclf, training set (320 rcds): ", as.character(ans[[2]]), sep="")
         # 0.6725
         # Note the uneven split between false positives and false negatives.
              0 1 class.error
         0 168 33
                        0.1642
         1 42 77
                        0.3529
          [1] "f-score for gbclf, training set (320 rcds): 0.6725"
In [55]: # Increase the number of trees in the model and increase the shrinkage.
         # (This model is likely too complex.)
         set.seed(123)
         gbclf <- gbm(Outcome ~ ., data= traindat, n.trees= 1000,</pre>
                       distribution= "bernoulli", shrinkage= 0.3)
         preds <- suppressMessages(predict(gbclf, newdata= traindat, type="response"))</pre>
         preds transf <- preds</pre>
         names(preds_transf) <- rownames(traindat)</pre>
         preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
         preds_transf[which(preds_transf < 0.5)] <- 0</pre>
         preds_transf <- as.factor(preds_transf)</pre>
         ans <- get_confusion(preds_transf, traindat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for model gbclf, training set: ", as.character(ans[[2]]), sep=""))
         # 0.8548
              0 1 class.error
         0 182 19
                        0.0945
                         0.1345
         1 16 103
          [1] "f-score for model gbclf, training set: 0.8548"
```

# Optimize the rf and gbrt models using cross-validation scores

```
gbmod <- suppressMessages(gbm(Outcome ~ ., data= traindat, n.trees= ntrees,</pre>
                                      distribution= "bernoulli", shrinkage= shrinkage))
    preds <- suppressMessages(predict(gbmod, newdata= testdat, type="response"))</pre>
    preds_transf <- preds</pre>
    names(preds transf) <- rownames(testdat)</pre>
    preds transf[which(preds transf >= 0.5)] <- 1</pre>
    preds_transf[which(preds_transf < 0.5)] <- 0</pre>
    preds transf <- as.factor(preds transf)</pre>
    ans <- get_confusion(preds_transf, testdat[, "Outcome", drop=FALSE])</pre>
}
# Type2 score is a weighted average of accuracy and
# the f-score.
mat <- as.matrix(ans[[1]])</pre>
percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
result \leftarrow round((0.4 * percent correct + 0.6 * ans[[2]]), 4)
return(result)
```

```
In [136]: # Function to obtain a cross-validation score, averaging the
           # Type2 scores of the folds. Valid values for the classifier
           # argument are: 'randomforest' and 'gradientboost'.
           get_cvScore <- function(seed, dat, classifier, ntrees,</pre>
                                     folds= 5, shrinkage= 0.1) {
               ###############################
               # Partition the data into folds, making sure
               # the ratio of survivors to non-survivors is
               # about the same for each traindat/valdat pair.
               # divide dat by the number of folds
               segment_size <- round(dim(dat)[1]/folds)</pre>
               diff <- nrow(dat) - folds * segment_size</pre>
               last_seg_size <- segment_size + diff</pre>
               segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
               stopifnot(sum(segmentsv) == nrow(dat))
               # shuffle dat
               set.seed(seed * 17)
               smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
               dat <- dat[smp,]</pre>
               # Get ratio of surviving to non-surviving cows.
               dat_surv <- dat[which(dat$0utcome==1),]</pre>
               dat nonSurv <- dat[which(dat$Outcome==0),]</pre>
               surv_ratio <- round(nrow(dat_surv)/nrow(dat), 4)</pre>
               row_list <- vector("list", length=folds)</pre>
               used_surv <- used_nonSurv <- c()</pre>
               for(k in 1:folds) {
                   surv_count <- round(surv_ratio * segmentsv[k])</pre>
                   nonSurv_count <- segmentsv[k] - surv_count</pre>
                   avail_survRows <- rownames(dat_surv)[which(!(rownames(dat_surv)) %in% used_surv))]</pre>
                   avail_nonSurvRows <- rownames(dat_nonSurv)[which(!(rownames(dat_nonSurv) %in% used_
                   if(k < folds) {</pre>
                        smp01 <- sample(avail survRows, surv count, replace=FALSE)</pre>
                        smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                        smp01 <- avail_survRows</pre>
                        smp02 <- avail_nonSurvRows</pre>
                        stopifnot(length(c(smp01, smp02)) == segmentsv[k])
                   used surv <- c(used surv, smp01)
                   used_nonSurv <- c(used_nonSurv, smp02)</pre>
                    row_list[[k]] <- c(smp01, smp02)</pre>
               } # end of for-loop, index k
```

```
In [137]: # Since the seed value is having such a big effect on the results,
           # I take the average over a number of seeds.
           avg_seed_scores <- function(seed_vector, traindat, classifier,</pre>
                                         n_trees, shrinkage= 0.01, folds= 5) {
               seed len <- length(seed vector)</pre>
               outv <- rep(NA, seed_len)</pre>
               for(i in 1:seed len) {
                   seed <- seed_vector[i]</pre>
                   if(classifier== 'randomforest') {
                        outv[i] <- get_cvScore(seed, traindat, classifier,</pre>
                                                n_trees, folds= folds)
                   if(classifier== 'gradientboost') {
                        outv[i] <- get cvScore(seed, traindat, classifier, n trees,</pre>
                                                folds=folds, shrinkage=shrinkage)
                   }
               return(round(mean(outv), 5))
           }
```

```
In [138]: # This grid search takes a vector of seeds as an argument.
           # It is only for the random forest and gradient boosting
           # models.
           gridSearch02 <- function(seed vector, traindat, classifier, ntree vector,</pre>
                                      shrinkage_vector= c(0.1), folds=5) {
               tree_len <- length(ntree_vector)</pre>
               shrink_len <- length(shrinkage_vector)</pre>
               # We need to capture the gridSearch parameters as well as
               # the cross-val scores.
               datout <- rep(NA, 2 * tree_len * shrink_len)</pre>
               dim(datout) <- c((tree_len * shrink_len), 2)</pre>
               datout <- as.data.frame(datout)</pre>
               colnames(datout) <- c("params", "Type2")</pre>
               datout$params <- ""
               index <- 0
               for(i in 1:tree_len) {
                   n_trees <- ntree_vector[i]</pre>
                   if(classifier== 'gradientboost') {
                        for(j in 1:shrink_len) {
                            index <- index + 1
                            shrinkage <- shrinkage vector[j]</pre>
                            param_string <- paste(as.character(n_trees),</pre>
```

```
as.character(shrinkage), sep= "--")
                           datout$params[index] <- param_string</pre>
                           datout$Type2[index] <- avg_seed_scores(seed_vector, traindat, classifier, n</pre>
                                                                       folds=folds, shrinkage=shrinkage)
                       }
                   if(classifier== 'randomforest') {
                       index <- index + 1
                       datout$params[index] <- as.character(n trees)</pre>
                       datout$Type2[index] <- avg_seed_scores(seed_vector, traindat, classifier,</pre>
                                                                  n_trees, folds= folds)
                  }
              return(datout)
In [60]:
          # Run grid search to get better parameters for the
          # random forest model. Test with 90 seeds.
          set.seed(7543)
          seed_smp <- sample(1:9999, 90, replace=FALSE)</pre>
          tree_vector <- c(50, 80, 100, 120, 130, 150, 200)
          ans <- gridSearch02(seed smp, traindat, 'randomforest', tree vector)</pre>
          # NOTE: this best_param output is not that stable, even with
          # 90 seeds.
          (best_params <- ans[which(ans$Type2 == max(ans$Type2)),]$params)</pre>
          (best rf Type2 <- round(ans[which(ans$Type2 == max(ans$Type2)),]$Type2, 4))</pre>
          # 0.6436
          '120'
          0.6436
In [61]: # Test with 120 seeds.
          set.seed(7543)
          seed_smp <- sample(1:9999, 120, replace=FALSE)</pre>
          tree_vector <- c(80, 100, 120, 130, 150, 200)
          ans <- gridSearch02(seed_smp, traindat, 'randomforest', tree_vector)</pre>
          (best_params <- ans[which(ans$Type2 == max(ans$Type2)),]$params)</pre>
          # '120'
          (best rf Type2 <- round(ans[which(ans$Type2 == max(ans$Type2)),]$Type2, 4))</pre>
          # 0.6428
          '120'
          0.6428
In [62]:
          # Using 120 seed output here.
          ans
          A data.frame: 6 × 2
          params
                   Type2
            <chr>
                   <dbl>
              80 0.63954
              100 0.64064
              120 0.64276
```

## Best random forest classifier: rfclf\_best

```
In [63]: # We are interested in the feature importances based on the
         # training data.
         set.seed(123)
         rfclf_best <- randomForest(I(as.factor(Outcome)) ~ ., data= traindat,</pre>
                                     ntree= 120, mtry= 1, nodesize= 1,
                                     importance= TRUE)
         print(rfclf_best)
         print(get_fscore(as.matrix(rfclf_best$confusion)))
         \# [1] 0.5983 (f-score on traindat)
         # Accuracy is 0.70625 (training set)
         # Type2 is 0.6415
         Call:
          randomForest(formula = I(as.factor(Outcome)) ~ ., data = traindat,
                                                                                    ntree = 120, mtry
         = 1, nodesize = 1, importance = TRUE)
                        Type of random forest: classification
                               Number of trees: 120
         No. of variables tried at each split: 1
                 00B estimate of error rate: 29.38%
         Confusion matrix:
             0 1 class.error
         0 156 45
                      0.22388
         1 49 70
                      0.41176
         [1] 0.5983
In [64]: # Get f-score on the testset (80 rcds) using this model.
         preds <- predict(rfclf_best, newdata= testdat, type="response")</pre>
         ans <- get_confusion(preds, testdat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for rfclf_best, test set (80 rcds): ",
                     as.character(ans[[2]]), sep=""))
         # 0.5758
         \# Accuracy = 0.65
         # Type2 = 0.6055
         ### NOTE: the above scores are seed-dependent.
            0 1 class.error
         0 33 17
                      0.3400
         1 11 19
                      0.3667
         [1] "f-score for rfclf_best, test set (80 rcds): 0.5758"
 In [ ]: ### COMMENTS:
         # We can see from the following plot why there might be
```

```
# Outcome in the test data set. (Compare this plot with
# the other 3 plots that follow.) The two levels might
# be easier to separate after we introduce the Daysrec
# dimension.

In [11]: # Plot the test data to get a sense of the degree of
# separation between the two levels of testdat$Outcome.

# Transform data for plotting.
dat_plot <- testdat
dat_plot$AST <- log(dat_plot$AST)
dat_plot$CK <- log(dat_plot$CK)

options(repr.plot.width= 12, repr.plot.height= 9)

p <- ggplot(dat_plot, aes(AST, CK, color= factor(Outcome))) +

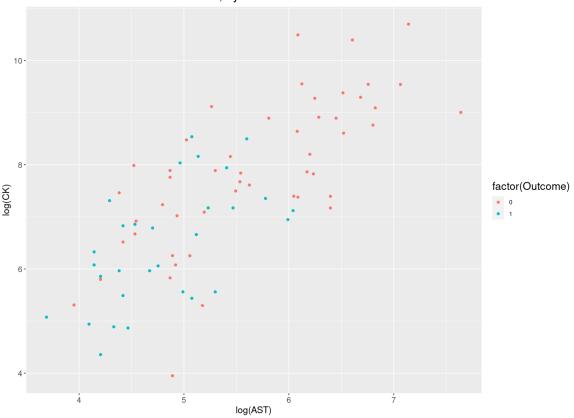
geom_point(alpha= 1.0) +
xlab("log(AST)") + ylab("log(CK)") +
ggtitle("Differences in testdat CK and AST, by Outcome level") +
theme(axis.text= element_text(size = 12)) +</pre>
```

## Differences in testdat CK and AST, by Outcome level

theme(axis.title= element\_text(size= 14)) +

theme(title= element text(size= 16))

# some difficulty distinguishing between the 2 levels of



```
In []: ### COMMENT:

# The above plot is only one perspective on the degree
# of separation between the levels of Outcome. We still
# have another dimension to work with: Daysrec.
```

## Best logistic regression model: test set score

```
In [66]: # Compare the random forest f-score on the test set with that
         # from our logistic regression model.
         preds <- preds_transf <- predict(g03, newdata= testdat, type="response")</pre>
         preds transf[which(preds transf >= 0.5)] <- 1</pre>
         preds_transf[which(preds_transf < 0.5)] <- 0</pre>
         preds_transf <- as.factor(preds_transf)</pre>
         ans <- get_confusion(preds_transf, testdat[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for model g03, test set (80 rcds): ", as.character(ans[[2]]), sep=""))
         # 0.6129
         # Accuracy is 0.70
         # Type2 is 0.6477
         ### The current test set favors the logistic regression model.
            0 1 class.error
         0 37 13
                   0.2600
         1 11 19
                      0.3667
         [1] "f-score for model q03, test set (80 rcds): 0.6129"
 In [ ]: ### COMMENT:
         # If we rely only on this one test set, the
         # logistic regression model is significantly
         # outperforming the random forest model. It may
         # be that the logistic regression model has an
         # advantage because the 8 outliers that were
         # removed were outliers from the perspective
         # of logistic regression modeling.
         # This difference in performance remains between
         # the 2 models even after we average scores for
         # the best random forest model over 300 seeds.
         # See below. Average scores over 1000 seeds are
         # also shown at the end of this notebook.
In [67]: print(round(rfclf best$importance, 3))
                           1 MeanDecreaseAccuracy MeanDecreaseGini
         AST
                  0.043 0.112
                                              0.068
                                                              50.986
                  0.028 0.083
                                              0.047
                                                              49.026
         CK
         Daysrec -0.009 0.058
                                              0.015
                                                              15.443
 In [ ]: # We can compute "feature importances" based on the Gini
         # measure. I want the weights to sum to 1. So we have:
         # Daysrec = 14%; CK = 42%; AST = 44%
```

## Best gradient boosting classifier: gbclf\_best

```
In [139]: # Run grid search to get better parameters for the
# gradient boosting model. This test is with 200 seeds.

set.seed(7543)
seed_smp <- sample(1:9999, 200, replace=FALSE)
tree_vector <- c(60, 80, 100, 120, 130)
shrinkage_vector <- c(0.01, 0.02, 0.03, 0.04, 0.05)</pre>
```

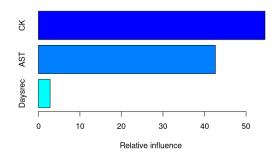
Time difference of 2.81 mins

'130--0.02'

0.66051

```
A data.frame: 3 x 2
```

	var	rel.inf	
	<chr></chr>	<dbl></dbl>	
СК	CK	54.5614	
AST	AST	42.6191	
Daysrec	Daysrec	2 8195	



```
In [141]: # Get f-score on the training set for gbclf_best.

preds <- suppressMessages(predict(gbclf_best, newdata= traindat, type="response"))
preds_transf <- preds
names(preds_transf) <- rownames(traindat)
preds_transf[which(preds_transf >= 0.5)] <- 1
preds_transf[which(preds_transf < 0.5)] <- 0
preds_transf <- as.factor(preds_transf)
ans <- get_confusion(preds_transf, traindat[, "Outcome", drop=FALSE])
print(ans$matrix)
""
print(paste("f-score for gbclf_best, trainset (320 rcds): ", as.character(ans[[2]]), sep="" # 0.6372

# Accuracy is 0.74375</pre>
```

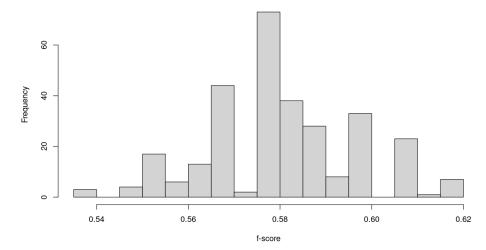
```
# Type2 is 0.6798
               0 1 class.error
          0 166 35
                         0.1741
          1 47 72
                         0.3950
           [1] "f-score for gbclf_best, trainset (320 rcds): 0.6372"
In [142]: # Get f-score on the test set for gbclf_best.
          preds <- suppressMessages(predict(gbclf_best, newdata= testdat, type="response"))</pre>
          preds transf <- preds</pre>
          names(preds transf) <- rownames(testdat)</pre>
          preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
          preds_transf[which(preds_transf < 0.5)] <- 0</pre>
          preds_transf <- as.factor(preds_transf)</pre>
          ans <- get_confusion(preds_transf, testdat[, "Outcome", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for gbclf best, test set (80 rcds): ", as.character(ans[[2]]), sep="")
          # 0.5938
          # Accuracy is 0.675
          # Type2 is 0.6263
              0 1 class.error
          0 35 15
                        0.3000
          1 11 19
                        0.3667
           [1] "f-score for gbclf_best, test set (80 rcds): 0.5938"
```

# More stable scores for rfclf\_best and gbclf\_best

```
In [ ]: ### COMMENT:
          # In order to get more stable scores for the random forest
          # and gradient boost models, I need to average scores for
          # the best models over many different seeds. This is done
          # in the following cells. (Here each individual score is
          # a score on the test set. The point is to get a more
          # accurate comparison to the g03 logistic model; for the
          # moment, this comparison is made using only the testset
          # data.)
In [143]: dim(traindat)
          summary(traindat[, -1])
          320 4
                                CK
                AST
                                             Daysrec
           Min. : 33
                         Min.
                                    13
                                         Min. :0.00
                               :
           1st Qu.: 124
                          1st Qu.: 585
                                          1st Qu.:0.00
                         Median : 1800
           Median : 244
                                         Median :1.00
                : 408
                               : 5595
                                         Mean :1.69
                         Mean
           3rd Qu.: 490
                          3rd Qu.: 5254
                                          3rd Qu.:3.00
                                :71000
           Max.
                  :2533
                         Max.
                                         Max.
                                                :7.00
In [150]: # Get more stable scores on the testset data for the best
          # random forest model.
```

```
set.seed(1433)
seed smp <- sample(1:9999, 300, replace=FALSE)</pre>
datout <- rep(NA, 6 * length(seed smp))</pre>
dim(datout) <- c(length(seed_smp), 6)</pre>
datout <- as.data.frame(datout)</pre>
colnames(datout) <- c("seed", "fscore", "Acc", "Type2", "FN", "FP")</pre>
datout$seed <- seed smp
for(i in 1:length(seed_smp)) {
    set.seed(seed smp[i])
    rfmod <- randomForest(I(as.factor(Outcome)) ~ .,</pre>
                                 data= traindat, ntree=120,
                                 mtry= 1, nodesize= 1)
    preds <- predict(rfmod, newdata= testdat, type="response")</pre>
    ans <- get confusion(preds, testdat[, "Outcome", drop=FALSE])</pre>
    mat <- as.matrix(ans[[1]])</pre>
    percent correct <- sum(diag(mat))/floor(sum(mat))</pre>
    datout[i, c("Acc")] <- round(percent correct, 4)</pre>
    datout[i, c("fscore")] <- round(ans[[2]], 4)</pre>
    datout[i, c("Type2")] <- round(0.4*percent_correct + 0.6*as.numeric(ans[[2]]), 4)</pre>
    datout[i, c("FN")] <- as.numeric(mat[2,1])</pre>
    datout[i, c("FP")] <- as.numeric(mat[1,2])</pre>
}
options(repr.plot.width= 10, repr.plot.height= 6)
hist(datout$fscore, breaks=12, xlab="f-score"
     main="Distribution of f-scores for rfclf_best on testset")
```

## Distribution of f-scores for rfclf\_best

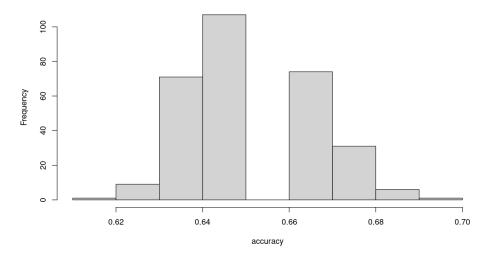


0.5802 0.6527 10.803333333333 16.9766666666667

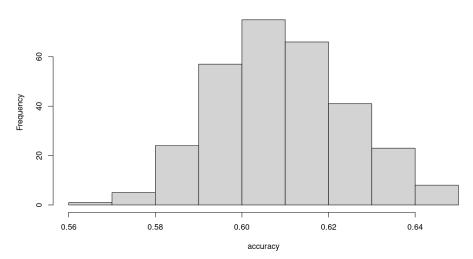
```
In [152]: options(repr.plot.width= 10, repr.plot.height= 6)
hist(datout$Acc, breaks=8, xlab="accuracy",
```

main="Distribution of accuracy scores for rfclf\_best on testset")

#### Distribution of accuracy scores for rfclf\_best



### Distribution of Type2 scores for rfclf\_best



```
In [154]: # Find out the seed that generates the best Type2
# score.

tmpdat <- datout[which(datout$Type2 > 0.642),]
tmpdat[, -1]
```

A data.frame: 7 × 5

	fscore	Acc	Type2	FN	FP
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
33	0.6154	0.6875	0.6442	10	15
37	0.6154	0.6875	0.6442	10	15
59	0.6154	0.6875	0.6442	10	15
75	0.6154	0.6875	0.6442	10	15
153	0.6129	0.7000	0.6477	11	13

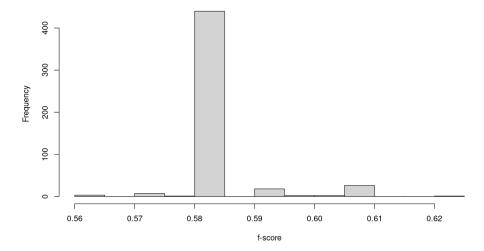
```
        fscore
        Acc
        Type2
        FN
        FP

        <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
```

```
In []: # If we use seed = 153 we get the highest accuracy
# score and the best balance between false positives
# and false negatives. (This is good considering
# that the base k-means model has an imbalance: 3X
# as many false positives as false negatives.)
```

```
In [144]: # Get more stable scores on the testset data for the
           # best gradient boosting model.
           set.seed(1433)
           seed smp <- sample(1:9999, 500, replace=FALSE)</pre>
           datout <- rep(NA, 5 * length(seed_smp))</pre>
           dim(datout) <- c(length(seed_smp), 5)</pre>
           datout <- as.data.frame(datout)</pre>
           colnames(datout) <- c("seed", "fscore", "Acc", "FN", "FP")</pre>
           datout$seed <- seed_smp</pre>
           for(i in 1:length(seed_smp)) {
               set.seed(seed_smp[i])
               gbmod <- gbm(Outcome ~ ., data= traindat, n.trees= 130,</pre>
                               distribution= "bernoulli", shrinkage= 0.02)
               preds <- suppressMessages(predict(gbmod, newdata= testdat, type="response"))</pre>
               preds_transf <- preds</pre>
               names(preds_transf) <- rownames(testdat)</pre>
               preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
               preds_transf[which(preds_transf < 0.5)] <- 0</pre>
               preds transf <- as.factor(preds transf)</pre>
               ans <- get confusion(preds transf, testdat[, "Outcome", drop=FALSE])</pre>
               mat <- as.matrix(ans[[1]])</pre>
               percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
               datout[i, c("Acc")] <- round(percent_correct, 4)</pre>
               datout[i, c("fscore")] <- round(ans[[2]], 4)</pre>
               datout[i, c("FN")] <- as.numeric(mat[2,1])</pre>
               datout[i, c("FP")] <- as.numeric(mat[1,2])</pre>
           options(repr.plot.width= 10, repr.plot.height= 6)
           hist(datout$fscore, breaks=10, xlab="f-score",
                main="Distribution of f-scores for gbclf_best on testset")
```

#### Distribution of f-scores for gbclf\_best on testset



```
# false negatives: 10.97
# false positives: 15.94

# The gradient boosting model, like the base k-means model,
# tends to have more FPs than FNs.

0.5859 0.6637 10.966 15.936

In []: ### COMMENT:

# Notice that the gradient boosting model is somewhat
# stronger than the random forest classifier. On the
# testset data, we get much better performance from
# the g03 logistic regression model.
```

## **SVM** classifier

A support vector machine classifier using a radial basis function as the kernel.

```
In [41]: # For SVM modeling, we need to scale the data.
          # NOTE: we get a better svm model if we do not apply
          # any prior transformations to the variables (such as
          # taking the log or sqrt).
          svmtrain <- traindat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
          svm_scaled <- scale(svmtrain[, -1])</pre>
          svm_centers <- attr(svm_scaled, "scaled:center")
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
          svm_scaled <- as.data.frame(cbind(svmtrain$0utcome, svm_scaled),</pre>
                                         row.names=rownames(svmtrain))
          colnames(svm scaled) <- colnames(svmtrain)</pre>
In [42]: # Scale the testset data.
          svmtest <- testdat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
          svmtest_scaled <- scale(svmtest[, -1], center=svm_centers,</pre>
                                     scale=svm_scales)
          svmtest_scaled <- as.data.frame(cbind(svmtest$Outcome, svmtest_scaled),</pre>
                                              row.names=rownames(svmtest))
          colnames(svmtest_scaled) <- colnames(svmtest)</pre>
In [32]: # Test out a support vector machine. I am interested in
          # using the radial basis function as the kernel.
          svm01 <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
                        gamma= 2.5, cost= 700, scale=FALSE)
          pred <- fitted(svm01)</pre>
          (ans <- table(pred, as.factor(svm_scaled$Outcome)))</pre>
          get_fscore(as.matrix(ans))
          pred
                0
                     1
             0 166 19
             1 35 100
          0.7874
In [33]: # See how the svm performs on the test data.
```

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preds <- predict(svm01, newdata=svmtest\_scaled)</pre>

```
(ans <- table(preds, as.factor(symtest_scaled$Outcome)))</pre>
          get fscore(as.matrix(ans))
          preds 0 1
               0 36 11
               1 14 19
          0.6032
In [29]: levels(preds[1])
          '0' '1'
 In [ ]: #&* Bookmark
 In [7]: # Function to compute a Type2 score for an svm cv-fold.
          get Type2 svm <- function(traindat, valdat, gamma, cost) {</pre>
              # traindat and valdat need to be scaled
              train scaled <- scale(traindat[, -1])</pre>
              train_centers <- attr(train_scaled, "scaled:center")
train_scales <- attr(train_scaled, "scaled:scale")</pre>
              train_scaled <- as.data.frame(cbind(traindat$Outcome, train_scaled),</pre>
                                                 row.names=rownames(traindat))
              colnames(train scaled) <- colnames(traindat)</pre>
              svmmod <- svm(I(as.factor(Outcome)) ~ ., data= train_scaled, gamma=gamma,</pre>
                                 cost=cost, scale=FALSE, kernel="radial")
               # Scale valdat.
              test scaled <- scale(valdat[, -1], center=train_centers,</pre>
                                      scale=train scales)
              test scaled <- as.data.frame(cbind(valdat$Outcome, test scaled),</pre>
                                               row.names=rownames(valdat))
              colnames(test_scaled) <- colnames(valdat)</pre>
              preds <- predict(svmmod, newdata= test scaled)</pre>
               ans <- table(preds, as.factor(valdat$Outcome))</pre>
              mat <- as.matrix(ans)</pre>
              percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
               result <- round((0.4 * percent_correct + 0.6 * get_fscore(mat)), 4)
               return(result)
 In [8]: # This grid search searches for the best parameters for svm
          # modeling of the data.
          # Because our training set is so small---only 320 records---it
          # is better to run the grid search over many seeds.
          gridSearch_svm <- function(seedv, dat, gammav, costv, folds=5) {</pre>
              gamma_len <- length(gammav)</pre>
              cost len <- length(costv)</pre>
               # We need to capture the gridSearch parameters as well as
              # the cross-val scores.
              datout <- rep(NA, 2 * gamma_len * cost_len)</pre>
              dim(datout) <- c((gamma len * cost len), 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("params", "Type2")
datout$params <- ""</pre>
               # Get ratio of surviving to non-surviving cows.
              dat_surv <- dat[which(dat$0utcome==1),]</pre>
              dat_nonSurv <- dat[which(dat$0utcome==0),]</pre>
              surv_ratio <- round(nrow(dat_surv)/nrow(dat), 4)</pre>
```

```
# Divide dat by the number of folds to get a
# size for each fold.
segment_size <- round(nrow(dat)/folds)</pre>
diff <- nrow(dat) - folds * segment_size</pre>
last_seg_size <- segment_size + diff</pre>
segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
stopifnot(sum(segmentsv) == nrow(dat))
index <- 0
for(i in 1:gamma_len) {
    gamma <- gammav[i]</pre>
    for(j in 1:cost_len) {
        index <- index + 1
        cost <- costv[j]</pre>
        param_string <- paste(as.character(gamma),</pre>
                                as.character(cost), sep= "--")
        datout$params[index] <- param string</pre>
        # Each set of parameters gets tested over many folds.
        # The different folds are created using different seeds.
        # Create a vector to store the Type2 score for each seed.
        seedv len <- length(seedv)</pre>
        seed_scores <- rep(NA, seedv_len)</pre>
        for(h in 1:seedv_len) {
             # shuffle dat
             cur_seed <- seedv[h]</pre>
             set.seed(cur seed)
             smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
             dat <- dat[smp,]</pre>
             # Each element of row_list will be the rows we pick
             # out for one of the folds. E.g., the first element
             # of row list will contain the rows we want for the
             # first fold, the second element of row list will
             # contain the rows we want for the second fold, and
             # so forth.
             row_list <- vector("list", length=folds)</pre>
             used_surv <- used_nonSurv <- c()</pre>
             # Make sure that the ratio of survivors to non-survivors
             # is about the same for each traindat/valdat pair.
             for(k in 1:folds) {
                 surv_count <- round(surv_ratio * segmentsv[k])</pre>
                 nonSurv_count <- segmentsv[k] - surv_count</pre>
                 avail_survRows <- rownames(dat_surv)[which(!(rownames(dat_surv) %in% us
                 avail_nonSurvRows <- rownames(dat_nonSurv)[which(!(rownames(dat_nonSurv
                 if(k < folds) {</pre>
                      smp01 <- sample(avail survRows, surv count, replace=FALSE)</pre>
                      smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                 } else {
                      smp01 <- avail_survRows</pre>
                      smp02 <- avail_nonSurvRows</pre>
                      stopifnot(length(c(smp01, smp02)) == segmentsv[k])
                 used_surv <- c(used_surv, smp01)</pre>
                 used_nonSurv <- c(used_nonSurv, smp02)</pre>
                 row_list[[k]] <- c(smp01, smp02)
             } # end of for-loop, index k
             train_list <- test_list <- vector("list", length= folds)</pre>
             for(k in 1:folds) {
                 testdat <- dat[row_list[[k]],]</pre>
                 traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                 stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == n
                 test_list[[k]] <- testdat</pre>
                 train_list[[k]] <- traindat</pre>
             }
```

```
# When there are only 5 folds, only 5 cores get used.
                           scores <- mcmapply(get_Type2_svm, train_list, test_list,</pre>
                                                MoreArgs= list(gamma=gamma, cost=cost),
                                                SIMPLIFY= TRUE, mc.cores=5)
                           # For the current seed, store the average of the Type2
                           # scores, the average taken over the folds.
                           seed scores[h] <- round(mean(scores), 5)</pre>
                       } ## end of for-loop, index h
                       # Here I am taking an average of average scores. This
                       # could be improved by simply taking a single average.
                       datout$Type2[index] <- round(mean(seed_scores), 5)</pre>
                  } ## end of for-loop, index j
              } ## end of for-loop, index i
              return(datout)
In [10]: # Run grid search to get better parameters for the
          # svm classifier.
          set.seed(7543)
          seed_vector <- sample(1:9999, 200, replace=FALSE)</pre>
          gamma v \leftarrow seq(0.1, 0.5, by=0.05)
          cost_v \leftarrow seq(100, 500, by=50)
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          ans <- gridSearch_svm(seed_vector, traindat, gamma_v, cost_v)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 11.12 mins
          (best params <- ans[which(ans$Type2 == max(ans$Type2)),]$params)</pre>
          # '0.1--100'
          (best_Type2 <- ans[which(ans$Type2 == max(ans$Type2)),]$Type2)</pre>
          # 0.6538
          'Start time: 2021-04-05 21:52:27'
          Time difference of 11.12 mins
          '0.1--100'
          0.6538
In [11]: # Refine the grid search.
          set.seed(7543)
          seed_vector <- sample(1:9999, 200, replace=FALSE)</pre>
          gamma_v \leftarrow seq(0.05, 0.15, by=0.01)
          cost_v \leftarrow seq(1, 200, by=20)
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          ans <- gridSearch_svm(seed_vector, traindat, gamma_v, cost_v)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 14 mins
          (best_params <- ans[which(ans$Type2 == max(ans$Type2)),]$params)</pre>
          # '0.05 - - 20'
          (best_Type2 <- ans[which(ans$Type2 == max(ans$Type2)),]$Type2)</pre>
          # 0.6575
```

```
'Start time: 2021-04-05 22:06:32'
          Time difference of 13.99 mins
          '0.05--21'
          0.65748
In [15]: # Again, refine the search.
          set.seed(7543)
          seed_vector <- sample(1:9999, 200, replace=FALSE)</pre>
          gamma_v \leftarrow seq(0.01, 0.05, by=0.01)
          cost v \leftarrow seq(10, 60, by=10)
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          ans <- gridSearch_svm(seed_vector, traindat, gamma_v, cost_v)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 3.75 mins
          (best_params <- ans[which(ans$Type2 == max(ans$Type2)),]$params)</pre>
          # '0.01--20'
           (best Type2 <- ans[which(ans$Type2 == max(ans$Type2)),]$Type2)</pre>
          # 0.66377
          'Start time: 2021-04-05 22:31:26'
          Time difference of 3.75 mins
          '0.01--20'
          0.66377
```

#### Get scores for best svm (svm02) on trainset and testset

```
In [43]: # Construct an svm with the identified parameters.
         # We need to get probability estimates from the output.
         # So we set probability=TRUE.
         svm02 <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
                       gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
         pred <- fitted(svm02)</pre>
         (ans <- table(pred, as.factor(svm scaled$Outcome)))</pre>
         print(paste("f-score for 'best' sym classifier, trainset (320 rcds): ",
                      as.character(get_fscore(as.matrix(ans))), sep=""))
         # 0.652
         # Accuracy is 0.7531
         # Type2 is 0.6924
         pred
                0
                     1
            0 151 36
          [1] "f-score for 'best' svm classifier, trainset (320 rcds): 0.6587"
In [44]: # Check performance of the svm on the test set.
         preds <- predict(svm02, newdata=svmtest_scaled)</pre>
         (ans <- table(preds, as.factor(symtest$Outcome)))</pre>
```

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print(paste("f-score for 'svm02, testset (80 rcds): ",

```
as.character(get_fscore(as.matrix(ans))), sep=""))
# 0.6471

# Accuracy is 0.70

# Type2 is 0.6683
```

```
preds 0 1
    0 34 8
    1 16 22

[1] "f-score for 'svm02, testset (80 rcds): 0.6471"
```

## **Final Comments for Section 1**

With the survivor to non-survivor ratio preserved between trainset and testset, we are seeing that the logistic regression model---on the testset data---outperforms the random forest and gradient boosting models. The logistic regression model has, for the 80 record testset, 11 false negatives; both the random forest and gradient boosting models average 10.8 false negatives. The logistic regression model has 13 false positives. The random forest averages 17 false positives, and the gradient boosting averages 16 false positives.

The Type2 score for the logistic regression model is about 0.65. The random forest model averages about 0.61. And the gradient boosting model averages about 0.62.

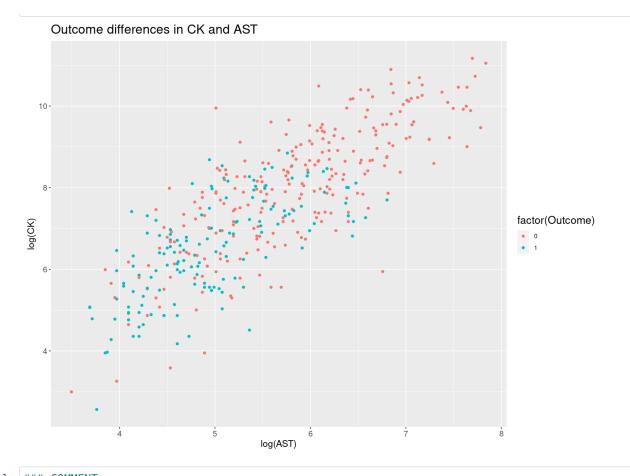
The logistic regression model's performance on the 80 record testset is not quite as good as that of the svm model, svm02. They both have an accuracy score of 70%. Unlike g03, svm02 was constructed through a rigorous cross-validation process (using the training set, of course). svm02 also has a higher Type2 score than g03 on the testset (0.67 vs 0.65).

\* \* \* \* \*

## Section 3: A k-means base model

How does the k-means algorithm cluster the 400 observations for AST, CK, and Daysrec?

```
In [12]: dat <- rbind(traindat, testdat)</pre>
         dim(dat)
         400 4
In [13]: # Transform data for plotting.
         dat plot <- dat
         dat_plot$AST <- log(dat_plot$AST)</pre>
         dat_plot$CK <- log(dat_plot$CK)</pre>
In [14]: # Plot data to see the degree of separation between
         # records with Outcome = 1 and those with Outcome = 0
         # (again, leaving out the Daysrec dimension).
         options(repr.plot.width= 12, repr.plot.height= 9)
         p <- ggplot(dat_plot, aes(AST, CK, color= factor(Outcome))) +</pre>
           geom_point(alpha=1.0) +
           xlab("log(AST)") + ylab("log(CK)") +
           ggtitle("Outcome differences in CK and AST") +
           theme(axis.text= element_text(size = 12)) +
           theme(axis.title= element_text(size= 14)) +
           theme(title= element_text(size= 16))
```



```
In []: ### COMMENT:
    # We see in the above plot that there is a degree of
    # separation in Outcome levels based on the AST and
    # CK blood measurements. These are the 2 most important
    # dimensions we have for predicting Outcome.

In [57]: ### COMMENT:

# Can Daysrec increase the separation between levels of
# Outcome? As this variable increases, Outcome tends to
# 0. Also, as Daysrec increases, both CK and AST tend to
# increase. The next plot suggests that Daysrec can help
# us distinguish between the survivors and the cows that
# did not survive.
```

```
In [58]: # Transform data for plotting.

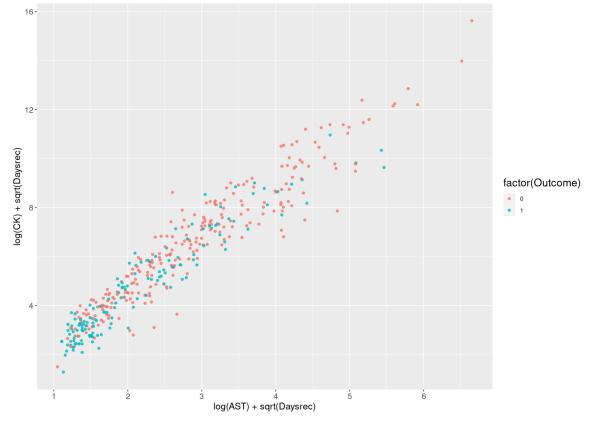
dat_plot <- dat
    dat_plot$AST <- log(dat_plot$AST) * 0.3 * sqrt(1 + dat_plot$Daysrec)
    dat_plot$CK <- log(dat_plot$CK) * 0.5 * sqrt(1 + dat_plot$Daysrec)

options(repr.plot.width= 12, repr.plot.height= 9)

p <- ggplot(dat_plot, aes(AST, CK, color= factor(Outcome))) +

    geom_point(alpha= 0.8) +
    xlab("log(AST) + sqrt(Daysrec)") + ylab("log(CK) + sqrt(Daysrec)") +
    ggtitle("Outcome differences in CK and AST") +
    theme(axis.text= element_text(size= 12)) +
    theme(axis.title= element_text(size= 14)) +
    theme(title= element_text(size= 16))
p</pre>
```

#### Outcome differences in CK and AST



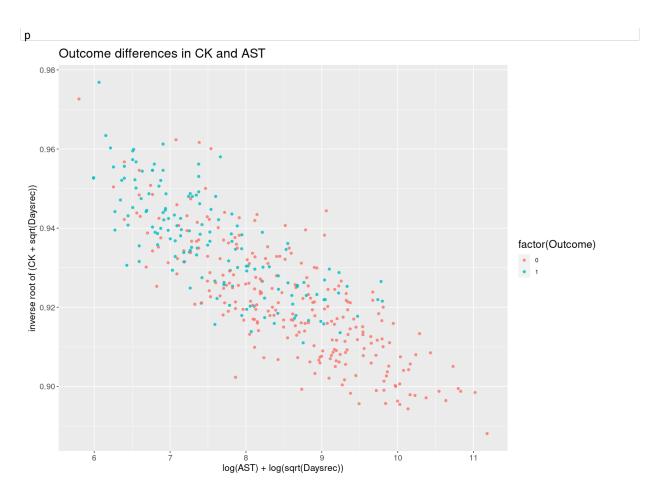
```
In [59]: # Try a different transformation.

dat_plot <- dat
    dat_plot$AST <- log(dat_plot$AST * 10 * sqrt(1 + dat_plot$Daysrec))
    dat_plot$CK <- (dat_plot$CK * (0.8 * sqrt(1 + dat_plot$Daysrec)))^-0.01</pre>
```

```
In [60]: options(repr.plot.width= 12, repr.plot.height= 9)

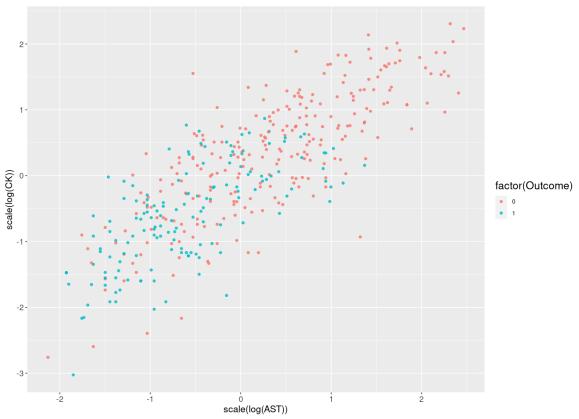
p <- ggplot(dat_plot, aes(AST, CK, color= factor(Outcome))) +

geom_point(alpha= 0.8) +
    xlab("log(AST) + log(sqrt(Daysrec))") + ylab("inverse root of (CK + sqrt(Daysrec))") +
    ggtitle("Outcome differences in CK and AST") +
    theme(axis.text= element_text(size = 12)) +
    theme(axis.title= element_text(size= 14)) +
    theme(title= element_text(size= 16))</pre>
```



```
In [20]: # Transform the data as it will be transformed
         # for k-means. HTF in The Elements of Statistical Learning
         # point out that there are times when scaling makes it MORE
         # difficult for clustering algorithms to separate the data
         # as we would like, or expect. See Figure 14.5 on p.506.
         dat_plot <- dat</pre>
         dat_plot$AST <- log(dat_plot$AST)</pre>
         dat_plot$CK <- log(dat_plot$CK)</pre>
         dat plot$AST <- scale(dat plot$AST)</pre>
         dat_plot$CK <- scale(dat_plot$CK)</pre>
         options(repr.plot.width= 12, repr.plot.height= 9)
         p <- ggplot(dat_plot, aes(AST, CK, color= factor(Outcome))) +</pre>
           geom_point(alpha= 0.8) +
           xlab("scale(log(AST))") + ylab("scale(log(CK))") +
            ggtitle("Outcome differences in CK and AST") +
           theme(axis.text= element_text(size = 12)) +
           theme(axis.title= element_text(size= 14)) +
           theme(title= element_text(size= 16))
```

#### Outcome differences in CK and AST



```
In [15]: rm(dat)
```

## Get scores for base k-means model: trainset and testset

```
In [16]: # Scale the data before running k-means clustering. I have
    # transformations on each of the 3 variables prior to
    # scaling so that the resultant ranges given in the
    # summaries below are much more alike.
```

```
# train = df
train <- traindat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
train$AST <- log(train$AST)</pre>
train$CK <- log(train$CK)</pre>
train$Daysrec <- sqrt(train$Daysrec)</pre>
train_scaled <- scale(train[, -1])
centers <- attr(train_scaled, "scaled:center")</pre>
scales <- attr(train_scaled, "scaled:scale")</pre>
train_scaled <- as.data.frame(cbind(traindat$Outcome, train_scaled),</pre>
                                  row.names=rownames(traindat))
colnames(train_scaled) <- colnames(train)</pre>
summary(train_scaled)
    Outcome
                        AST
                                               CK
                                                                Daysrec
 Min. :0.000
                   Min. :-2.1490
                                              :-2.9832
                                                            Min. :-1.2944
                                        Min.
 1st Qu.:0.000
                   1st Qu.:-0.7651
                                        1st Qu.:-0.6691
                                                             1st Qu.:-1.2944
```

```
Median :0.000
              Median :-0.0542
                               Median : 0.0142
                                                Median :-0.0372
              Mean : 0.0000
                               Mean : 0.0000
                                                Mean : 0.0000
Mean :0.372
              3rd Qu.: 0.6769
3rd Qu.:1.000
                               3rd Qu.: 0.6654
                                                3rd Qu.: 0.8832
Max. :1.000
              Max. : 2.3959
                               Max. : 2.2483
                                                Max. : 2.0320
```

```
In [17]: # Run k-means algorithm with number of clusters set to 2.
set.seed(1233)
fit_km <- kmeans(train_scaled, 2, iter.max = 50, nstart = 30)
print(fit_km$size)
# [1] 175 145</pre>
```

[1] 175 145

```
In [18]: print(head(fit_km$cluster))
```

331 201 161 283 404 121 1 2 1 2 2 2

```
In [19]: datout <- as.data.frame(cbind(train_scaled$Outcome, fit_km$cluster))
    colnames(datout) <- c("Outcome", "cluster")
    rownames(datout) <- rownames(train_scaled)
    head(datout)</pre>
```

A data.frame: 6 × 2

#### Outcome cluster

	<dbl></dbl>	<dbl></dbl>
331	1	1
201	1	2
161	0	1
283	0	2
404	0	2
121	0	2

```
In [26]: # max_vals identifies the Outcome level we would expect
# each cluster to map to.

(mat <- as.matrix(table(datout$Outcome, as.factor(datout$cluster))))
    (max_vals <- apply(mat, MARGIN=2, which.max))</pre>
```

```
1
         2
         2
In [ ]: ### COMMENTS:
         # From the above table we see that the first cluster
         # is associated with Outcome level 0, the cows that did not
         # survive.
         # If we say that all cows in the first cluster are non-survivors
         # and all cows in the second cluster are survivors, we can get
In [ ]: #&* Bookmark
In [33]: # Function returning mapping between clusters and
         # Outcome levels. We choose the mapping that yields
         # the best accuracy score. (Keep in mind that the
         # mapping is based on the trainset data; it is then
         # applied to the validation and/or test set data.)
         c1_toLevel_1 <- function(dat) {</pre>
             # Returns TRUE if cluster 1 maps to Outcome= 1 (survivors)
             # dat is a dataframe with 2 columns, c("Outcome", "cluster");
             # nrow(dat) = number of predictions from the model;
             # dat$Outcome = traindat$Outcome (from the calling function)
             # We find the "correct" mapping between cluster number and
             # Outcome level by computing accuracy scores for the different
             # valid mappings. We choose the mapping with the best
             # accuracy score.
             tbl <- as.matrix(table(dat$Outcome, as.factor(dat$cluster)))</pre>
             # The colnames of tbl refer to the names of the clusters.
             # With only 2 levels for Outcome, we need only 2 scores.
             scores <- rep(NA, 2)</pre>
             # First possibility: cluster 1 maps to non-survivors
             tmpdat <- dat
             tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 0</pre>
             tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 1</pre>
             preds <- as.factor(tmpdat$0utcome)</pre>
             names(preds) <- rownames(tmpdat)</pre>
             ans <- get_confusion(preds, dat[, "Outcome", drop=FALSE])</pre>
             scores[1] <- ans[[2]]
             # Alternative mapping: cluster 1 maps to survivors
             tmpdat <- dat
             tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 1</pre>
             tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 0</pre>
             preds <- as.factor(tmpdat$0utcome)</pre>
             names(preds) <- rownames(tmpdat)</pre>
             ans <- get_confusion(preds, dat[, "Outcome", drop=FALSE])</pre>
             scores[2] <- ans[[2]]
             return(scores[1] <= scores[2])</pre>
         }
```

```
In [34]: |c1_to_Outcome1 <- c1_toLevel_1(datout)</pre>
          paste("Map cluster 1 to Outcome level 1? : ", c1_to_Outcome1, sep="")
          'Map cluster 1 to Outcome level 1?: FALSE'
In [35]: tmpdat <- datout</pre>
          tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 0</pre>
          tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 1</pre>
          dim(tmpdat)
          320 2
In [36]: | sum(rownames(tmpdat) == rownames(train_scaled)) == nrow(train_scaled)
          TRUE
In [37]: table(as.factor(tmpdat$Outcome))
          175 145
In [38]: # Generate confusion matrix for the k-means clusters.
          # Output f-score for this confusion matrix.
          preds <- as.factor(tmpdat$0utcome)</pre>
          names(preds) <- rownames(tmpdat)</pre>
          ans <- get_confusion(preds, train_scaled[, "Outcome", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for k-means, trainset (320 rcds): ", as.character(ans[[2]]), sep=""))
          # 0.6515
          # Accuracy is 0.7125
          # Type2 is 0.6759
              0 1 class.error
          0 142 59
                        0.2935
          1 33 86
                         0.2773
          [1] "f-score for k-means, trainset (320 rcds): 0.6515"
In [89]: # Get confusion matrix for k-means on the test data.
          # This allows us to compare the clustering with our
          # models above. We have to first scale the testset
          # data using the centers and scales from the training
          # set data.
          # Prepare the test data.
          test <- testdat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
          test$AST <- log(test$AST)</pre>
          test$CK <- log(test$CK)</pre>
          test$Daysrec <- sqrt(test$Daysrec)</pre>
          test_scaled <- scale(test[, -1], center=centers, scale=scales)</pre>
          test_scaled <- as.data.frame(cbind(test$Outcome, test_scaled),</pre>
                                                row.names=rownames(test))
          colnames(test_scaled) <- colnames(test)</pre>
In [67]: # Function for identifying which cluster each record
```

```
# belongs to. This function later gets replaced by
         # getCluster.
         get_cluster <- function(df, centers) {</pre>
              # Create a $cluster column for the result
              df$cluster <- NA
              for(i in 1:nrow(df)) {
                  rcd <- df[i, colnames(centers)]</pre>
                  dists <- rep(NA, dim(centers)[1])</pre>
                  names(dists) <- rownames(centers)</pre>
                  for(class in rownames(centers)) {
                      dists[class] <- as.numeric(dist(rbind(rcd, centers[class,]),</pre>
                                                        method= "euclidean",
                                                        upper= FALSE))
                  nearest_center <- dists[dists== min(dists)][1]</pre>
                  df[i, c("cluster")] <- as.numeric(names(nearest_center))</pre>
              return(df)
In [68]: # Find the cluster which is "predicted" for each
         # record in the testset.
         dat_result <- get_cluster(test_scaled, fit_km$centers)</pre>
         table(as.factor(dat result$cluster))
          1 2
         38 42
In [69]: # Use the mapping that we used for the trainset data.
         dat_result$pred_Outcome <- NA</pre>
         dat result[which(dat_result$cluster==2),]$pred_Outcome <- 1</pre>
         dat result[which(dat result$cluster==1),]$pred Outcome <- 0</pre>
In [70]: # Generate confusion matrix for the k-means clusters and
         # the corresponding f-score.
         preds <- as.factor(dat_result$pred_Outcome)</pre>
         names(preds) <- rownames(dat_result)</pre>
         ans <- get_confusion(preds, dat_result[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for k-means on testset (80 rcds): ",
                      as.character(ans[[2]]), sep=""))
         # 0.6667
         # Accuracy is 0.70
         # Type2 score is 0.6800
             0 1 class.error
         0 32 18
                         0.36
         1 6 24
                         0.20
          [1] "f-score for k-means on testset (80 rcds): 0.6667"
 In [ ]: ### COMMENTS:
         # The k-means algorithm, without any enhancements such as
         # weights or an added probability column, does a better
         # job classifying the records in the testset than any of
```

```
# our previous models (logistic regression, random forest,
# gradient boosting, and svm). The accuracy score for the
# k-means model is the same as that for the logistic and
# svm models (0.70), but k-means has a better f-score.
# This, in turn, gives it the highest Type2 score on the
# test set.

# It is interesting that the parameters for the best random
# forest, gradient boosting, and svm models were established
# through cross-validation---meaning they were optimized for
# generalizability to unseen data. The k-means model did not
# have this advantage.

# We have to be cautious regarding the above comparison. It
# is only one data point. It remains to be seen how k-means
# compares with the SL classifiers in terms of a cross-validation
# score. This is done below.
```

# Section 4: k-means hybrid model

Add a predicted Outcome column (called "prob01") to the dataframe that k-means is applied to. See if this additional column improves the clustering solution. This approach is one where we leverage supervised learning to improve upon, or boost, the unsupervised k-means algorithm. It remains to be seen whether we can improve upon the current k-means model (what I will refer to as the *base model*) with information from one or more models which appear to be no better than the base k-means model when applied to new data. It would seem that in order for the prob01 column to boost the performance of the k-means model, it will need to not only (a) bring in new information; but also (b) add to, rather than subtract from the information already found in the other variables. In other words, the new information will need to complement, rather than conflict with, that found in the other variables.

The model used to generate \$prob01 is constructed from training set data and chosen for its generalizability to unseen data. In this next section I use the sym02 model from above because its parameters were chosen through cross-validation and, of the three models arrived at in this way, it is the best. Choosing the model with the best performance would seem to increase the chances that the performance of the hybrid model will be better than the base k-means model. Ideally, we would like the performance of the hybrid model to exceed that of all previous models surveyed.

Another reason for choosing svm02 to generate the prob01 columne: on the testset data, the base k-means model has 3X as many false positives as false negatives, whereas svm02 has 2X as many false negatives as false positives. I want to see whether the probabilities from svm02 help to correct this imbalance in the k-means output.

Since the base k-means model already performs quite well, it might be difficult to boost its performance with this added probability column. Let's see what happens.

```
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
         svm scaled <- as.data.frame(cbind(svmtrain$Outcome, svm scaled),</pre>
                                       row.names=rownames(svmtrain))
         colnames(svm_scaled) <- colnames(svmtrain)</pre>
         train <- traindat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
         # Transformations used in the k-means modeling.
         train$AST <- log(train$AST)</pre>
         train$CK <- log(train$CK)</pre>
         train$Daysrec <- sqrt(train$Daysrec)</pre>
         preds01 <- predict(svm02, newdata=svm_scaled, scale=FALSE, probability=TRUE)</pre>
         train$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])</pre>
         # Previous testing shows that we want to also scale the
         # prob01 column.
         train_scaled <- scale(train[, -1])</pre>
         centers <- attr(train_scaled, "scaled:center")</pre>
         scales <- attr(train_scaled, "scaled:scale")</pre>
         train scaled <- as.data.frame(cbind(traindat$Outcome, train scaled),
                                          row.names=rownames(traindat))
         colnames(train_scaled) <- colnames(train)</pre>
         summary(train_scaled[, -1])
                                                                        prob01
                AST
                                    CK
                                                    Daysrec
                             Min. :-2.9832
          Min. :-2.1490
                                                 Min. :-1.2944
                                                                    Min. :-1.5153
           1st Qu.:-0.7651
                             1st Qu.:-0.6691
                                                 1st Qu.:-1.2944
                                                                    1st Qu.:-0.9596
          Median :-0.0542
                             Median : 0.0142
                                                 Median :-0.0372
                                                                    Median :-0.0893
           Mean : 0.0000
                              Mean : 0.0000
                                                 Mean : 0.0000
                                                                    Mean : 0.0000
           3rd Qu.: 0.6769
                              3rd Qu.: 0.6654
                                                 3rd Qu.: 0.8832
                                                                    3rd Qu.: 0.8324
           Max.
                 : 2.3959
                              Max.
                                    : 2.2483
                                                 Max. : 2.0320
                                                                    Max. : 1.6274
In [46]: print(head(train*prob01))
         summary(train*prob01)
          [1] 0.75595 0.53371 0.99876 0.32724 0.33377 0.47183
            Min. 1st Qu. Median
                                      Mean 3rd Qu.
                                                       Max.
                   0.427
                                     0.639
                            0.619
                                             0.823
                                                      1.000
In [48]: # Construct model with the new prob01 column.
         set.seed(1233)
         kmod <- kmeans(train scaled[, -1], 2, iter.max = 50, nstart = 25)</pre>
In [49]: # See how the clusters are associated with Outcome.
         dfout <- as.data.frame(cbind(as.numeric(train_scaled$Outcome),</pre>
                                        kmod$cluster), row.names=rownames(train_scaled))
         colnames(dfout) <- c("Outcome", "cluster")</pre>
         c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
         tmpdat <- dfout
         if(c1_to_Outcome1) {
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 1</pre>
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 0</pre>
         } else {
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 0</pre>
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 1</pre>
```

```
# Generate confusion matrix for the k-means clusters and
# the corresponding f-score.
preds <- as.factor(tmpdat$0utcome)</pre>
names(preds) <- rownames(tmpdat)</pre>
ans <- get confusion(preds, train scaled[, "Outcome", drop=FALSE])</pre>
print(ans$matrix)
print(paste("f-score for kmeans (w/ p1), trainset (320 rcds): ", as.character(ans[[2]]), se
# [1] "f-score for kmeans (w/ p1), trainset (320 rcds): 0.6255"
mat <- as.matrix(ans[[1]])</pre>
percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
result \leftarrow round((0.4 * percent correct + 0.6 * ans[[2]]), 4)
print(paste("Type2 score for kmeans (w/ p1), trainset (320 rcds): ", as.character(result),
# [1] "Type2 score for kmeans (w/ p1), trainset (320 rcds): 0.6466"
print(paste("Accuracy: ", as.character(round(percent_correct,4)), sep=""))
# [1] "Accuracy: 0.6781"
    0 1 class.error
0 131 70
             0.3483
1 33 86
              0.2773
[1] "f-score for kmeans (w/ p1), trainset (320 rcds): 0.6255"
[1] "Type2 score for kmeans (w/p1), trainset (320 rcds): 0.6466"
[1] "Accuracy: 0.6781"
```

## Testset scores for k-means with p1

```
In [50]: # Prepare testset data.
          svmtest <- testdat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
          svmtest_scaled <- scale(svmtest[, -1], center=svm_centers, scale=svm_scales)</pre>
          svmtest_scaled <- as.data.frame(cbind(svmtest$Outcome, svmtest_scaled),</pre>
                                         row.names=rownames(svmtest))
          colnames(symtest scaled) <- colnames(symtest)</pre>
          test <- testdat[, c("Outcome", "AST", "CK", "Daysrec"), drop=FALSE]</pre>
          # Transformations used in the k-means modeling.
          test$AST <- log(test$AST)</pre>
          test$CK <- log(test$CK)</pre>
          test$Daysrec <- sqrt(test$Daysrec)</pre>
          preds01 <- predict(svm02, newdata=svmtest_scaled, scale= FALSE, probability=TRUE)</pre>
          test$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])</pre>
          test_scaled <- scale(test[, -1], center=centers, scale=scales)</pre>
          test_scaled <- as.data.frame(cbind(testdat$Outcome, test_scaled),</pre>
                                           row.names=rownames(testdat))
          colnames(test scaled) <- colnames(test)</pre>
          summary(test_scaled[, -1])
```

```
AST
                                   CK
                                                  Daysrec
                                                                      prob01
                 :-1.948
                                   :-2.1405
                                               Min. :-1.2944
          Min.
                            Min.
                                                                  Min. :-1.477
          1st Qu.:-0.951
                            1st Qu.:-0.7674
                                               1st Qu.:-1.2944
                                                                  1st Qu.:-1.091
          Median :-0.382
                            Median :-0.0647
                                               Median :-0.0372
                                                                  Median :-0.332
                                                                  Mean :-0.170
          Mean :-0.208
                                  :-0.0774
                                                     :-0.0945
                            Mean
                                               Mean
In [51]: # Get k-means predictions on the testset data.
         # Each element of the following list is a row of testdat.
         testScaled_asList <- split(test_scaled[, colnames(kmod$centers)],</pre>
                                      seq(nrow(test_scaled)))
         # Create a second list of the same length, each
         # element being the centers from the k-means model.
         apply.n.times <- function(n, x) {</pre>
             if (n == 1) list(x) else c(list(x), Recall(n - 1, x))
         ctr_list <- apply.n.times(nrow(test_scaled), kmod$centers)</pre>
         # Get the predictions for the validation set.
         preds <- mapply(getCluster, testScaled_asList, ctr_list,</pre>
                              SIMPLIFY=TRUE)
         test_scaled$cluster <- as.numeric(preds)</pre>
In [52]: table(as.factor(test_scaled$cluster))
         c1_to_Outcome1
          1 2
         34 46
         FALSE
In [53]: # Create a predicted Outcome column for dat result.
         dat result <- test scaled
         dat_result$pred_Outcome <- NA</pre>
         dat_result[which(dat_result$cluster==2),]$pred_Outcome <- 1</pre>
         dat_result[which(dat_result$cluster==1),]$pred_Outcome <- 0</pre>
In [54]: # Test set scores: k-means with prob01
         preds <- as.factor(dat result$pred Outcome)</pre>
         names(preds) <- rownames(dat_result)</pre>
         ans <- get_confusion(preds, dat_result[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for k-means (w/ p1) on testset (80 rcds): ",
                      as.character(ans[[2]]), sep=""))
         # [1] "f-score for k-means (w/ p1) on testset (80 rcds): 0.6579"
            0 1 class.error
         0 29 21
                       0.4200
         1 5 25
                       0.1667
         [1] "f-score for k-means (w/ p1) on testset (80 rcds): 0.6579"
In [55]: # Type2 score for k-means (w/ p1) when applied to the test set.
         mat <- as.matrix(ans[[1]])</pre>
         percent correct <- sum(diag(mat))/floor(sum(mat))</pre>
         result \leftarrow round((0.4 * percent_correct + 0.6 * ans[[2]]), 4)
         print(paste("Type2 score for k-means (w/ p1) on testset (80 rcds): ",
                      as.character(result), sep=""))
         \# [1] "Type2 score for k-means (w/ p1) on testset (80 rcds): 0.6647"
```

```
""
print(paste("Accuracy: ", as.character(round(percent_correct,4)), sep=""))
# [1] "Accuracy: 0.675"

[1] "Type2 score for k-means (w/ pl) on testset (80 rcds): 0.6647"

"

[1] "Accuracy: 0.675"

In []: ### COMMENTS:

# On the testset data, the hybrid model does not perform
# quite as well as the base k-means model. The FPs
# increased by 3, while the FNs decreased by only 1.
# On the testset data, the hybrid model does not perform
# quite as well as svm02.

# Further downstream, the models are compared in terms of
# their cross-validation scores. That will be the more
# informative test.
```

## Add weights to the hybrid k-means model

We should be able to improve the hybrid model by adding weights to it.

```
In [ ]: #&* Bookmark
In [71]: # Function to generate combination of parameters for gridSearch;
         # each combination must add to a number ~1. Returns a dataframe,
         # each row of which is a valid combination.
         # I re-factored this ftn using R's expand.grid ftn. expand.grid
         # actually takes more time to run. This is probably due to
         # type-checking. It appears that we also run out of memory more
         # quickly when using expand.grid. So at the moment I am
         # reverting to the deprecated section.
         generate_combs <- function(arglist, tol=0.0001) {</pre>
             # arglist is a named list; each name is a column
             # name of the dataframe which goes to k-means
             # this next section is an alternative to expand.grid
             # if(FALSE) {
             n_args <- length(arglist)</pre>
             param_vlens <- rep(NA, n_args)</pre>
             for(i in 1:n_args) {
                 param_vlens[i] <- length(arglist[[i]])</pre>
             n_rows <- prod(param_vlens)</pre>
             datout <- rep(NA, n_args*n_rows)</pre>
             dim(datout) <- c(n_rows, n_args)</pre>
             datout <- as.data.frame(datout)</pre>
             colnames(datout) <- names(arglist)</pre>
             cprod <- 1
             for(j in 1:n args) {
                 vect <- arglist[[j]]</pre>
                 val <- rep(vect, rep(cprod, length(vect)))</pre>
                 datout[, j] <- rep(val, n_rows/length(val))</pre>
                 cprod <- cprod*length(vect)</pre>
```

```
}
              # } ## end of 'if(FALSE)'
              # datout <- expand.grid(arglist, KEEP.OUT.ATTRS= FALSE)</pre>
              # colnames(datout) <- names(arglist)</pre>
              row sums <- round(rowSums(datout), 4)</pre>
              names(row_sums) <- rownames(datout)</pre>
              tol <- tol
              row_sums <- row_sums[which((as.numeric(row_sums) <= (1 + tol)) & (as.numeric(row_sums)</pre>
              datout <- datout[names(row_sums),]</pre>
              return(datout)
In [85]: # Function for obtaining average of confusion matrix
          # f-score and percent correctly answered. This function
         # is called from gridSearch06.
         get cvScore kmp1 <- function(traindat, valdat, seed, wghts) {</pre>
              # wghts is a named vector of weights to apply. The names, and
              # order of the weights, correspond to the colnames of traindat
              # below. (Here the names are: AST, CK, Daysrec, and prob01.)
              # Scale traindat for purpose of an svm model.
              svm scaled <- scale(traindat[, -1])</pre>
              svm_centers <- attr(svm_scaled, "scaled:center")</pre>
              svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
              svm_scaled <- as.data.frame(cbind(traindat$Outcome, svm_scaled),</pre>
                                            row.names=rownames(traindat))
              colnames(svm scaled) <- colnames(traindat)</pre>
              # This is our current best svm model for the trainset data
              svmod <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
                            gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
              preds01 <- predict(svmod, newdata=svm_scaled, probability=TRUE)</pre>
              traindat$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])
              ###############################
              # Transform and scale training set data for the
              # k-means model.
              traindat$AST <- log(traindat$AST)</pre>
              traindat$CK <- log(traindat$CK)</pre>
              traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
              traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
              centers <- attr(traindat_scaled, "scaled:center")
scales <- attr(traindat_scaled, "scaled:scale")</pre>
              ##################################
              # Apply weights to traindat. The sqrt should have
              # been taken in the calling function.
              cols <- names(wghts)</pre>
              df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              traindat wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
              colnames(traindat_wghts) <- cols</pre>
              ###############################
              # Prepare valdat for svm modeling.
              svmval_scaled <- scale(valdat[, -1], center=svm_centers, scale=svm_scales)</pre>
              svmval scaled <- as.data.frame(svmval scaled,</pre>
                                               row.names=rownames(valdat))
```

```
# Compute the prob01 column.
preds01 b <- predict(symod, newdata=symval scaled, probability=TRUE)</pre>
valdat$prob01 <- as.numeric(attr(preds01_b, "probabilities")[, 2])</pre>
# Transform and scale valdat.
valdat$AST <- log(valdat$AST)</pre>
valdat$CK <- log(valdat$CK)</pre>
valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
valdat_scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
# Apply weights to valdat. (We want valdat to look exactly like
# traindat. The weights act as a transformation of the data.)
df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
colnames(valdat wghts) <- cols</pre>
##################################
# Construct k-means model.
set.seed(seed)
kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
# See how the clusters are associated with Outcome.
dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                        row.names=rownames(traindat))
colnames(dfout) <- c("Outcome", "cluster")</pre>
c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
###############################
# Apply the k-means model to valdat wghts.
# Each element of the following list is a row of valdat wghts.
valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                         seq(nrow(valdat_wghts)))
ctr_list <- vector("list", length= nrow(valdat))</pre>
for(i in 1:nrow(valdat)) {
    ctr list[[i]] <- kmod$centers</pre>
names(ctr_list) <- rownames(valdat_wghts)</pre>
# Get the predictions for the validation set.
cluster assgns <- mcmapply(getCluster, valdat asList, ctr list,</pre>
                   SIMPLIFY=TRUE, mc.cores=6)
valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
valdat_wghts$pred_Outcome <- NA</pre>
if(c1_to_Outcome1) {
    valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
    valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 0</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
}
# Generate confusion matrix for the k-means clusters and
# the corresponding f-score.
preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
names(preds) <- rownames(valdat)</pre>
ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
# The result returned is a Type2 score (which is a mixture
# of accuracy and f-score).
```

```
mat <- as.matrix(ans[[1]])</pre>
              percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
              result <- round((0.4 * percent_correct + 0.6 * ans[[2]]), 6)
              return(result)
In [86]: # This grid search searches for the best set of weights to use
         # in our k-means clustering model. The best weights are those
         # which generalize best to the validation set. So we look for
         # the best cross-validation score.
         # Because our training set is so small---only 320 records---we
         # need to run the gridSearch over several seeds. Otherwise, we
         # will not get very stable results. (Of course, the more seeds
         # we use, the more time the grid search takes.)
         gridSearch06 <- function(seed_vector, dat, df_params, folds=5) {</pre>
              datout <- rep(NA, 2*nrow(df_params))</pre>
              dim(datout) <- c(nrow(df params), 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("row", "Type2")</pre>
              datout$row <- rownames(df_params)</pre>
              # We want the sqrt of the weights.
              df_params <- df_params^0.5</pre>
              params_rows <- rownames(df_params)</pre>
              ###############################
              # Partition the data into folds, making sure
              # the ratio of survivors to non-survivors is
              # about the same for each traindat/valdat pair.
              # divide dat by the number of folds
              segment size <- round(nrow(dat)/folds)</pre>
              diff <- nrow(dat) - folds * segment size
              last seg size <- segment size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              stopifnot(sum(segmentsv) == nrow(dat))
              # Create a dataframe, each row for a distinct seed.
              # Each column of the dataframe is for a distinct set
              # of weights. The entries in the cells are Type2
              seedv len <- length(seed vector)</pre>
              df_scores <- rep(NA, seedv_len*nrow(df_params))</pre>
              dim(df_scores) <- c(seedv_len, nrow(df_params))</pre>
              df_scores <- as.data.frame(df_scores, row.names=as.character(seed_vector))</pre>
              colnames(df_scores) <- rownames(df_params)</pre>
              for(h in 1:seedv len) {
                  # shuffle dat
                  cur_seed <- seed_vector[h]</pre>
                  set.seed(cur_seed)
                  smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
                  dat <- dat[smp,]</pre>
                  # Get ratio of surviving to non-surviving cows.
                  dat surv <- dat[which(dat$0utcome==1),]</pre>
                  dat_nonSurv <- dat[which(dat$0utcome==0),]</pre>
                  surv_ratio <- round(nrow(dat_surv)/nrow(dat), 4)</pre>
                  # Each element of row_list will be the rows we pick
                  # out for one of the folds. E.g., the first element
                  # of row list will contain the rows we want for the
                  # first fold, the second element of row_list will
                  # contain the rows we want for the second fold, and
                  # so forth.
                  row_list <- vector("list", length=folds)</pre>
                  used_surv <- used_nonSurv <- c()</pre>
                  for(k in 1:folds) {
```

```
surv_count <- round(surv_ratio * segmentsv[k])</pre>
             nonSurv_count <- segmentsv[k] - surv_count</pre>
             avail_survRows <- rownames(dat_surv)[which(!(rownames(dat_surv) %in% used_surv)
             avail_nonSurvRows <- rownames(dat_nonSurv)[which(!(rownames(dat_nonSurv) %in% u
             if(k < folds) {</pre>
                 smp01 <- sample(avail survRows, surv count, replace=FALSE)</pre>
                 smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                 smp01 <- avail_survRows</pre>
                 smp02 <- avail_nonSurvRows</pre>
                 stopifnot(length(c(smp01, smp02)) == segmentsv[k])
             used surv <- c(used surv, smp01)
             used_nonSurv <- c(used_nonSurv, smp02)</pre>
             row_list[[k]] <- c(smp01, smp02)
        } # end of for-loop, index k
        ################################
        for(i in 1:nrow(df_params)) {
             cur_row <- params_rows[i]</pre>
             wghts <- as.numeric(df_params[i,])</pre>
             names(wghts) <- colnames(df_params)</pre>
             train_list <- test_list <- vector("list", length= folds)</pre>
             for(j in 1:folds) {
                 testdat <- dat[row list[[j]],]</pre>
                 traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                 stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == dim(d
                 test_list[[j]] <- testdat</pre>
                 train_list[[j]] <- traindat</pre>
             }
             # When there are only 5 folds, only 5 cores get used.
             scores <- mcmapply(get cvScore kmp1, train list, test list,</pre>
                                 MoreArgs= list(seed=cur seed, wghts=wghts),
                                 SIMPLIFY= TRUE, mc.cores=5)
             # For the current seed, store the average of the Type2
             # scores, the average taken over the folds.
             df_scores[as.character(cur_seed), cur_row] <- round(mean(scores), 5)</pre>
        } # end of for-loop, index i
    } ## end of for-loop, index h
    # Compute the average over the seeds of the Type2 scores
    # obtained for each set of parameters in df_params.
    datout$Type2 <- round(apply(df scores, MARGIN=2, mean), 5)</pre>
    return(datout)
}
```

## Search for the best set of weights for the hybrid model

```
In [103]: # There are 4 parameter lists to work with. The best
# approach, perhaps, is to start by exploring the
# region around the space where all parameters have an
# equal weight---in this case, a weight of 0.25.

lst <- vector("list", length= 4)
names(lst) <- c("AST", "CK", "Daysrec", "prob01")

lst[[1]] <- lst[[2]] <- lst[[3]] <- lst[[4]] <- seq(0.13, 0.37, by=0.02)

start <- Sys.time()
dfc01 <- generate_combs(lst)
stop <- Sys.time()
# round(stop - start, 2)</pre>
```

```
dim(dfc01)
           # 1469
           1469 4
In [104]: # Test on a sample of 10.
           set.seed(42)
           smp <- sample(rownames(dfc01), 10, replace=FALSE)</pre>
           tst params <- dfc01[smp,]
           head(tst_params)
           A data.frame: 6 × 4
                   AST
                          CK Daysrec prob01
                  <dbl> <dbl>
                                <dbl>
                                      <dbl>
            11425
                                 0.17
                                        0.23
                   0.33
                         0.27
             7201
                   0.35
                         0.27
                                 0.19
                                        0.19
            22165
                   0.37
                         0.15
                                 0.15
                                       0.33
            20509
                   0.27
                         0.21
                                 0.21
                                        0.31
            23329
                                 0.29
                                        0.33
                   0.25
                        0.13
            22057
                   0.29
                        0.25
                                 0.13
                                       0.33
  In [ ]: # Find the best weights of those in tst_params.
           set.seed(1233)
           seed_vector <- sample(1:9999, 10, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           dat_result <- gridSearch06(seed_vector, traindat, tst_params)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 20 secs (for 10 rows)
  In [ ]: # Find the best parameters among those searched over.
           best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
           length(best_params)
           best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
  In [ ]: dfc01[best_params,]
           best_Type2
In [108]: # Find the best weights of those in dfc01 (1469 rows,
           # 21 seeds, 5 folds).
           set.seed(1233)
           seed vector <- sample(1:9999, 21, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           dat_result <- gridSearch06(seed_vector, traindat, dfc01)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 1.92 hours
           'Start time: 2021-04-06 14:08:42'
```

Time difference of 1.92 hours

```
In [109]: # Find the best parameters among those searched over.
           best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
           length(best_params)
           best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat result$Type2, na.rm=TRUE)),]$Type2
In [110]: dfc01[best_params,]
                     AST
                               CK
                                      Daysrec
                                                    prob01
           # 3985 0.25
                             0.27
                                         0.33
                                                      0.15
           best_Type2
           # 0.65817
           A data.frame: 1 × 4
                  AST
                         CK Daysrec prob01
                 <dbl> <dbl>
                               <dbl>
                                      <dbl>
            3985
                 0.25
                        0.27
                                0.33
                                       0.15
           0.65817
In [112]: # Refine the search.
           lst <- vector("list", length= 4)</pre>
           names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
           lst[[1]] \leftarrow seq(0.21, 0.29, by= 0.01)
           lst[[2]] \leftarrow seq(0.23, 0.31, by= 0.01)

lst[[3]] \leftarrow seq(0.31, 0.35, by= 0.01)
           lst[[4]] \leftarrow seq(0.13, 0.17, by=0.01)
           start <- Sys.time()</pre>
           dfc02 <- generate_combs(lst)</pre>
           stop <- Sys.time()</pre>
           # round(stop - start, 2)
           dim(dfc02)
           # 185
           185 4
In [113]: # Add no weights to the combinations. This will
           # tell us whether using weights is better than not
           # using weights. (Setting each of the weight
           # coefficients to 1 is essentially equivalent to
           # setting each of the 4 weights to 0.25, although
           # small differences can appear in the resulting
           # score.)
           # NOTE: the result we get from this test is much
           # better than testing against the test set, since
           # this test is the equivalent of 100 such tests.
           dfc02 \leftarrow rbind(dfc02, rep(1,4))
```

```
In [114]: # Find the best weights of those in dfc02 (186 rows,
          # 21 seeds, 5 folds).
          set.seed(1233)
          seed vector <- sample(1:9999, 21, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc02)</pre>
          stop <- Sys.time()</pre>
           round(stop - start, 2)
          # Time difference of 14.36 mins
           'Start time: 2021-04-06 16:07:54'
          Time difference of 14.36 mins
In [115]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                             max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best Type2 <- dat result[which(dat result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
In [116]: dfc02[best_params,]
                        AST
                                  CK
                                        Daysrec
                                                     prob01
                       0.23
          # 1029
                                0.29
                                           0.33
                                                       0.15
          best_Type2
          # 0.6582
           A data.frame: 1 x 4
                 AST
                        CK Daysrec prob01
                <dbl> <dbl>
                             <dbl>
                                    <dbl>
                              0.33
                                     0.15
           1029
                0.23
                       0.29
          0.6582
  In [ ]: ### COMMENTS:
          # Notice that the best cross-validation score does
          # not occur when all coefficients, or weights, are
          # set to 1. Thus, the weights are an improvement over
          # no weights.
          # In order to compare the k-means model that includes
          # prob01 with the base k-means model, we need to get
          # a similar cross-validation score for the base k-means
          # model. We can do this when we also add weights to it.
          # (This is done further downstream.)
```

With best weights, get scores for hybrid model on trainset and testset

```
In [56]: dim(train_scaled)
         summary(train_scaled[, -1])
         320 5
                AST
                                    CK
                                                    Daysrec
                                                                        prob01
                                    :-2.9832
          Min. :-2.1490
                                                 Min. :-1.2944
                                                                    Min. :-1.5153
                             Min.
           1st Qu.:-0.7651
                              1st Qu.:-0.6691
                                                 1st Qu.:-1.2944
                                                                    1st Qu.:-0.9596
           Median :-0.0542
                                                 Median :-0.0372
                             Median : 0.0142
                                                                    Median :-0.0893
          Mean : 0.0000
                             Mean : 0.0000
                                                 Mean : 0.0000
                                                                    Mean : 0.0000
           3rd Qu.: 0.6769
                              3rd Qu.: 0.6654
                                                 3rd Qu.: 0.8832
                                                                    3rd Qu.: 0.8324
           Max. : 2.3959
                             Max.
                                    : 2.2483
                                                Max. : 2.0320
                                                                    Max. : 1.6274
In [57]: # Apply weights to train_scaled. We need to take
         # the sqrt of the weights.
         wghts \leftarrow c(0.23, 0.29, 0.33, 0.15)^0.5
         cols <- colnames(train_scaled)[-1]</pre>
         names(wghts) <- cols</pre>
         df2 <- t(t(train_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
         train_wghts <- cbind(as.numeric(train_scaled$Outcome), df2)</pre>
         train_wghts <- as.data.frame(train_wghts)</pre>
         colnames(train wghts) <- c("Outcome", cols)</pre>
         rownames(train_wghts) <- rownames(train_scaled)</pre>
In [58]: # Run k-means algorithm with number of clusters set to 2.
         set.seed(1233)
         fit02_km < - kmeans(train_wghts[, -1], 2, iter.max = 50, nstart = 25)
         print(fit02_km$size)
          [1] 172 148
In [59]: # See how the clusters are associated with Outcome.
         dfout <- as.data.frame(cbind(as.numeric(train_wghts$Outcome),</pre>
                                        fit02_km$cluster))
         colnames(dfout) <- c("Outcome", "cluster")</pre>
         rownames(dfout) <- rownames(train_wghts)</pre>
         c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
         if(c1_to_Outcome1) {
              # cluster 1 is associated with the survivors
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 1</pre>
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 0</pre>
         } else {
              # cluster 2 is associated with the survivors
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 1</pre>
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 0</pre>
         }
         # Generate confusion matrix for the k-means clusters and
         # the corresponding f-score.
         preds <- as.factor(tmpdat$0utcome)</pre>
         names(preds) <- rownames(tmpdat)</pre>
         ans <- get_confusion(preds, train_wghts[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for kmeans (w/ p1, wghts) on trainset (320 rcds): ",
                      as.character(ans[[2]]), sep=""))
         mat <- as.matrix(ans[[1]])</pre>
         percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
         result <- round((0.4 * percent\_correct + 0.6 * ans[[2]]), 4)
```

```
print(paste("Type2 score for kmeans (w/ p1, wghts) on trainset (320 rcds): ", as.character(
         print(paste("Accuracy: ", as.character(round(percent_correct,4)), sep=""))
             0 1 class.error
         0 131 70
                       0.3483
         1 33 86
                       0.2773
         [1] "f-score for kmeans (w/ p1, wghts) on trainset (320 rcds): 0.6255"
         [1] "Type2 score for kmeans (w/ p1, wghts) on trainset (300 rcds): 0.6466"
         [1] "Accuracy: 0.6781"
         Test set scores: k-means with p1 & weights (hybrid model)
In [60]: test_scaled <- test_scaled[, 1:5]</pre>
In [61]: dim(test_scaled)
         summary(test scaled[, -1])
         80 5
               AST
                                 CK
                                               Daysrec
                                                                   prob01
          Min. :-1.948
                         Min. :-2.1405
                                             Min. :-1.2944 Min. :-1.477
          1st Qu.:-0.951
                          1st Qu.:-0.7674
                                             1st Qu.:-1.2944
                                                              1st Qu.:-1.091
          Median :-0.382
                         Median :-0.0647
                                             Median :-0.0372 Median :-0.332
          Mean :-0.208 Mean :-0.0774
                                             Mean :-0.0945 Mean :-0.170
          3rd Qu.: 0.563
                          3rd Qu.: 0.6136
                                             3rd Qu.: 0.4836 3rd Qu.: 0.766
          Max.
                : 2.190
                          Max. : 1.9609
                                             Max.
                                                  : 2.0320 Max. : 1.626
In [62]: # Apply weights to test scaled.
         df2 <- t(t(test_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
         test_wghts <- cbind(as.numeric(test_scaled$Outcome), df2)</pre>
         test_wghts <- as.data.frame(test_wghts)</pre>
         colnames(test_wghts) <- c("Outcome", cols)</pre>
```

rownames(test\_wghts) <- rownames(test\_scaled)</pre>

```
1 2
         40 40
In [64]: c1_to_Outcome1
         FALSE
In [65]: # Create a predicted Outcome column for dat result.
         dat_result$pred_Outcome <- NA</pre>
         dat_result[which(dat_result$cluster==2),]$pred_Outcome <- 1</pre>
         dat result[which(dat result$cluster==1),]$pred Outcome <- 0</pre>
In [66]: # Test set scores: k-means with prob01 & wghts
         preds <- as.factor(dat_result$pred_Outcome)</pre>
         names(preds) <- rownames(dat_result)</pre>
         ans <- get confusion(preds, dat result[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for k-means (w/ p1, wghts) on testset (80 rcds): ",
                      as.character(ans[[2]]), sep=""))
         # 0.6286
            0 1 class.error
         0 32 18
                       0.3600
         1 8 22
                       0.2667
         [1] "f-score for k-means (w/ p1, wghts) on testset (80 rcds): 0.6286"
In [67]: # Type2 score for k-means when applied to the test set.
         mat <- as.matrix(ans[[1]])</pre>
         percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
         result <- round((0.4 * percent_correct + 0.6 * ans[[2]]), 4)
         print(paste("Type2 score for k-means (w/ p1, wghts) on testset (80 rcds): ",
                      as.character(result), sep=""))
         # [1] "Type2 score for k-means (w/ p1, wghts) on testset (80 rcds): 0.6472"
         print(paste("Accuracy: ", as.character(round(percent_correct,4)), sep=""))
         # [1] "Accuracy: 0.675"
         [1] "Type2 score for k-means (w/ p1, wghts) on testset (80 rcds): 0.6472"
         [1] "Accuracy: 0.675"
 In [ ]: ### COMMENTS:
         # The scores for the hybrid model with weights, on the test
         # set, are slightly less good than without the weights; on
         # the test set the hybrid model with weights fares even worse
         # compared to the base k-means model (i.e., without
         # weights and without the prob01 column).
         # We saw above that we get a better average cross-validation
         # score (using the prob01 column) with weights than without
         # weights. This tells us something about the importance of
         # using weights and using more than one test set. The model
         # we are interested in is the one that does the best job
         # generalizing to new data; in other words, we are interested
```

```
# in the model with the best cross-validation score (and not
# the model that simply has the best score on the test set).

# Next I apply the same test to the base k-means model.
# But when running the test, we can also test the base model
# using weights. For it is highly likely that the base model
# will also have better cross-validation scores when we use
# weights.
```

#### Get cross-val scores for k-means base model; add in weights.

I will need to make slight changes to our functions used in this test. gridSearch06, above, has been changed to call get\_cvScore\_kmBase (below).

```
In [80]: # Function for obtaining average of confusion matrix
         # f-score and percent correctly answered. This function
         # is called from gridSearch06.
         get_cvScore_kmBase <- function(traindat, valdat, seed, wghts) {</pre>
              # wghts is a named vector of weights to apply. The names, and
              # order of the weights, correspond to the colnames of traindat
              # below. (Here the names are: AST, CK, and Daysrec.)
              #################################
              # Transform and scale training set data for the
              # k-means model.
              traindat$AST <- log(traindat$AST)</pre>
              traindat$CK <- log(traindat$CK)</pre>
              traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
              traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
              centers <- attr(traindat_scaled, "scaled:center")</pre>
              scales <- attr(traindat_scaled, "scaled:scale")</pre>
              ####################################
              # Apply weights to traindat. The sgrt should have
              # been taken in the calling function.
              cols <- names(wghts)</pre>
              df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              traindat_wghts <- as.data.frame(df2, row.names(traindat))</pre>
              colnames(traindat_wghts) <- cols</pre>
              #################################
              # Prepare valdat for svm modeling.
              # Transform and scale valdat.
              valdat$AST <- log(valdat$AST)</pre>
              valdat$CK <- log(valdat$CK)</pre>
              valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
              valdat_scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
              valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
              # Apply weights to valdat. (We want valdat to look exactly like
              # traindat. The weights act as a transformation of the data.)
              df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
              colnames(valdat_wghts) <- cols</pre>
              ###################################
              # Construct k-means model.
              set.seed(seed)
              # Outcome is the first column of traindat; we need to
              # remove this column prior to clustering.
```

```
kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
    # See how the clusters are associated with Outcome.
    dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                             row.names=rownames(traindat))
    colnames(dfout) <- c("Outcome", "cluster")</pre>
    c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
    #################################
    # Apply the k-means model to valdat wghts.
    # Each element of the following list is a row of valdat wghts.
    valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                             seq(nrow(valdat_wghts)))
    ctr_list <- vector("list", length= nrow(valdat))</pre>
    for(i in 1:nrow(valdat)) {
        ctr_list[[i]] <- kmod$centers</pre>
    names(ctr_list) <- rownames(valdat_wghts)</pre>
    # Get the predictions for the validation set.
    cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                        SIMPLIFY=TRUE, mc.cores=6)
    valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
    valdat_wghts$pred_Outcome <- NA</pre>
    if(c1_to_Outcome1) {
        valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
        valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
        valdat wghts[which(valdat wghts$cluster==1),]$pred Outcome <- 0</pre>
        valdat wghts[which(valdat wghts$cluster==2),]$pred Outcome <- 1</pre>
    }
    # Generate confusion matrix for the k-means clusters and
    # the corresponding f-score.
    preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
    names(preds) <- rownames(valdat)</pre>
    ans <- get confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
    # The result returned is a Type2 score (which is a mixture
    # of accuracy and f-score).
    mat <- as.matrix(ans[[1]])</pre>
    percent correct <- sum(diag(mat))/floor(sum(mat))</pre>
    result \leftarrow round((0.4 * percent correct + 0.6 * ans[[2]]), 6)
    return(result)
lst <- vector("list", length= 3)</pre>
```

```
In [65]: # There are 3 parameter lists to work with.

lst <- vector("list", length= 3)
    names(lst) <- c("AST", "CK", "Daysrec")

lst[[1]] <- lst[[2]] <- lst[[3]] <- seq(0.15, 0.55, by=0.01)

start <- Sys.time()
    dfc04 <- generate_combs(lst, tol=0.0001)
    stop <- Sys.time()
    # round(stop - start, 2)

dim(dfc04)</pre>
```

1236 3

```
In [66]: # Test on a sample of 10.
          set.seed(42)
          smp <- sample(rownames(dfc04), 10, replace=FALSE)</pre>
          tst params <- dfc04[smp,]
 In [ ]: # Find the best weights of those in tst_params.
          set.seed(1233)
          seed_vector <- sample(1:9999, 10, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          dat_result <- gridSearch06(seed_vector, traindat, tst_params)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 15 secs (for 10 rows)
 In [ ]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
 In [ ]: dfc04[best_params,]
          best Type2
In [70]: # Find the best weights of those in dfc01 (1236 rows,
          # 10 seeds, 5 folds).
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc04)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 32.57 mins
          'Start time: 2021-04-06 12:30:21'
          Time difference of 32.57 mins
In [71]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best Type2 <- dat result[which(dat result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
In [72]: dfc04[best_params,]
                   AST
                            CK
                                   Daysrec
          # 5616 0.54
                          0.28
                                      0.18
          best_Type2
          # 0.66497
```

```
A data.frame: 1 x 3
                 AST
                        CK Daysrec
                <dbl> <dbl>
                              <dbl>
          0.66497
In [72]: # See whether the above weights are better
          # than no weights.
          lst <- vector("list", length= 3)</pre>
          names(lst) <- c("AST","CK","Daysrec")</pre>
          lst[[1]] \leftarrow c(0.54)
          lst[[2]] \leftarrow c(0.28)
          lst[[3]] \leftarrow c(0.18)
          start <- Sys.time()</pre>
          dfc05 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          (dfc05 \leftarrow rbind(dfc05, rep(1, 3)))
          A data.frame: 2 × 3
            AST
                   CK Daysrec
           <dbl> <dbl>
                         <dbl>
            0.54
                          0.18
                  0.28
            1.00
                  1.00
                          1.00
In [82]: # Find the best weights of those in dfc05 ( rows,
          # 10 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 10, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc05)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 2.74 secs
          'Start time: 2021-05-23 16:03:04'
          Time difference of 2.74 secs
In [83]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
In [84]: dfc05[best_params,]
                                   CK
                        AST
                                          Daysrec
          # 1
                        0.54
                                 0.28
                                             0.18
```

<chr>

r> <dbl>
1 0.66199

```
best_Type2
        # 0.66497
        A data.frame: 1 x 3
            AST
                   CK Daysrec
           <dbl> <dbl>
                        <dbl>
            0.54
                  0.28
                         0.18
        0.66497
In [ ]: ### COMMENTS:
        # The base k-means model works best with weights.
        # With weights, we have a cross-validation Type2 score,
        # averaged over 50 folds, of 0.6650.
        # If we add a probability column to the base k-means
        # model, using svm02 for the probabilities, the
        # cross-val Type2 score decreases by half a percentage
        # point, to 0.6599.
```

## Cross-val score for base k-means with weights, 1000 seeds

For model comparison, it is best if we obtain scores using far more seeds. For each of the models of interest, I generate scores using 1000 seeds. The scores are summarized in tables below. (Search on '#&\* Bookmark'.)

```
In [77]: lst <- vector("list", length= 3)</pre>
           names(lst) <- c("AST", "CK", "Daysrec")</pre>
           lst[[1]] \leftarrow c(0.54)
           lst[[2]] \leftarrow c(0.28)
           lst[[3]] \leftarrow c(0.18)
           dfc05 <- generate_combs(lst)</pre>
In [78]: set.seed(42)
           seed vector <- sample(1:9999, 1000, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           dat_result <- gridSearch06(seed_vector, traindat, dfc05)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 2.58 mins
           'Start time: 2021-04-06 13:38:47'
           Time difference of 2.58 mins
In [79]: dat result
           # Type2 score of 0.6620
           A data.frame: 1 ×
             row
                   Type2
```

## Cross-val score for hybrid model with weights, 1000 seeds

```
In [87]: lst <- vector("list", length= 4)</pre>
         names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
         # The first set of weights below is from when I
         # used just 10 seeds. The second set is from
         # when I used 21 seeds.
         # wghts <- c(0.17, 0.34, 0.34, 0.15)
         # wghts <- c(0.23, 0.29, 0.33, 0.15)
         lst[[1]] \leftarrow c(0.23)
         lst[[2]] \leftarrow c(0.29)
         lst[[3]] \leftarrow c(0.33)
         lst[[4]] \leftarrow c(0.15)
         dfc06 <- generate_combs(lst)</pre>
In [88]: # gridSearch06 needs to call the other get_cvScore ftn.
         set.seed(42)
         seed_vector <- sample(1:9999, 1000, replace=FALSE)</pre>
         start <- Sys.time()</pre>
         paste("Start time: ", start, sep="")
         dat_result <- gridSearch06(seed_vector, traindat, dfc06)</pre>
         stop <- Sys.time()</pre>
         round(stop - start, 2)
         # Time difference of 2.89 mins
          'Start time: 2021-05-23 16:08:01'
         Time difference of 2.89 mins
In [89]: dat result
         # Type2 score of 0.6559
         A data.frame: 1 x
                 Type2
            row
                 <dbl>
          <chr>
             1 0.65587
 In [ ]: ### COMMENTS:
         # Averaging over 1000 seeds (or 5000 folds of traindat),
         # our k-means model has a slightly worse Type2 score
         # when we include the probabilities from svm02. The
         # drop in average cross-val score is by 0.6 percentage
         # point.
         # Including the prob01 column, k-means has an average
         # Type2 cross-validation score of 0.6559. Without the
         # prob01 column, the score is 0.6620. In this comparison,
         # weights are used for both models. This means that we
         # need to have the Outcome variable in our dataset in
         # order to construct both of these models.
```

# Get scores for base k-means model with weights on trainset and testset

Although the following scores are not that important overall, I include them for completeness, since this is what I have been

doing thus far for each of the models. Similar scores will not be found in Part 2.

```
In [84]: # Apply weights to traindat. We need to take
          # the sqrt of the weights.
          wghts <- c(0.54, 0.28, 0.18)^{\circ}0.5
          cols <- colnames(traindat)[-1]</pre>
          names(wghts) <- cols</pre>
          df2 <- t(t(train_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
          train_wghts <- cbind(as.numeric(train_scaled$0utcome), df2)</pre>
          train_wghts <- as.data.frame(train_wghts)</pre>
          colnames(train_wghts) <- c("Outcome", cols)</pre>
          rownames(train wghts) <- rownames(traindat)</pre>
In [85]: # Run k-means algorithm with number of clusters set to 2.
          set.seed(1233)
          start <- Sys.time()</pre>
          fit02_km <- kmeans(train_wghts[, -1], 2, iter.max = 50, nstart = 25)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 0.15 secs
          print(fit02 km$size)
          Time difference of 0 secs
          [1] 151 169
In [86]: # See how the clusters are associated with Outcome.
          dfout <- as.data.frame(cbind(as.numeric(train wghts$0utcome),</pre>
                                         fit02 km$cluster))
          colnames(dfout) <- c("Outcome", "cluster")</pre>
          rownames(dfout) <- rownames(train_wghts)</pre>
          tmpdat <- dfout
          c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
          if(c1 to Outcome1) {
              # cluster 1 is associated with the survivors
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 1</pre>
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 0</pre>
          } else {
              # cluster 2 is associated with the survivors
              tmpdat[which(tmpdat$cluster== 2),]$Outcome <- 1</pre>
              tmpdat[which(tmpdat$cluster== 1),]$Outcome <- 0</pre>
          # Generate confusion matrix for the k-means clusters and
          # the corresponding f-score.
          preds <- as.factor(tmpdat$0utcome)</pre>
          names(preds) <- rownames(tmpdat)</pre>
          ans <- get_confusion(preds, train_wghts[, "Outcome", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for kmeans (w/ wghts) on trainset (320 rcds): ", as.character(ans[[2]]
          mat <- as.matrix(ans[[1]])</pre>
          percent correct <- sum(diag(mat))/floor(sum(mat))</pre>
          result <- round((0.4 * percent\_correct + 0.6 * ans[[2]]), 4)
          print(paste("Type2 score for kmeans (w/ wghts) on trainset (320 rcds): ", as.character(resu
          print(paste("Accuracy: ", as.character(round(percent correct,4)), sep=""))
```

## Test set scores; base k-means model with weights

On the test set, k-means with weights does not score as well as k-means without weights. But we know from the above work that the better model is when we use weights.

```
In [90]: # Scale the testset data. Then apply the
         # weights.
         test <- testdat[, c("Outcome","AST","CK","Daysrec"), drop=FALSE]</pre>
         test$AST <- log(test$AST)</pre>
         test$CK <- log(test$CK)</pre>
         test$Daysrec <- sqrt(test$Daysrec)</pre>
         test_scaled <- scale(test[, -1], center=centers, scale=scales)</pre>
         test scaled <- as.data.frame(cbind(testdat$0utcome, test scaled),</pre>
                                       row.names=rownames(testdat))
         colnames(test scaled) <- colnames(test)</pre>
         summary(test scaled)
             Outcome
                               AST
                                                   CK
                                                                  Daysrec
          Min. :0.000 Min. :-1.948 Min. :-2.1405
                                                               Min. :-1.2944
          1st Qu.:0.000 1st Qu.:-0.951 1st Qu.:-0.7674
                                                               1st Qu.:-1.2944
          Median :0.000 Median :-0.382 Median :-0.0647
                                                               Median :-0.0372
                                                               Mean :-0.0945
          Mean :0.375
                          Mean :-0.208 Mean :-0.0774
                          3rd Qu.: 0.563
                                            3rd Qu.: 0.6136
          3rd Ou.:1.000
                                                               3rd Qu.: 0.4836
                 :1.000
                                                               Max. : 2.0320
          Max.
                          Max. : 2.190
                                            Max. : 1.9609
In [91]: # Apply the weights to the testset data.
         df2 <- t(t(test_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
         test wghts <- cbind(as.numeric(test scaled$Outcome), df2)</pre>
         test wghts <- as.data.frame(test wghts)</pre>
         colnames(test wghts) <- c("Outcome", cols)</pre>
         rownames(test_wghts) <- rownames(testdat)</pre>
In [92]: # Get k-means predictions on the testset data.
         # Each element of the following list is a row of newtestdat.
         testwghts_asList <- split(test_wghts[, colnames(fit02_km$centers)],</pre>
                                     seq(nrow(test_wghts)))
         # Create a second list of the same length, each
         # element being the centers from the k-means model.
         apply.n.times <- function(n, x) {</pre>
             if (n == 1) list(x) else c(list(x), Recall(n - 1, x))
```

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ctr\_list <- apply.n.times(nrow(test\_wghts), fit02\_km\$centers)</pre>

# Get the predictions for the validation set.

```
preds <- mapply(getCluster, testwghts_asList, ctr_list,</pre>
                              SIMPLIFY=TRUE)
         test_wghts$cluster <- as.numeric(preds)</pre>
In [93]: c1_to_Outcome1
          1 2
         32 48
         FALSE
In [94]: # Create a predicted Outcome column for dat_result.
         dat_result <- test_wghts</pre>
         dat result$pred Outcome <- NA
         dat_result[which(dat_result$cluster==2),]$pred_Outcome <- 1</pre>
         dat_result[which(dat_result$cluster==1),]$pred_Outcome <- 0</pre>
In [95]: # Test set scores: base k-means with best weights.
         preds <- as.factor(dat_result$pred_Outcome)</pre>
         names(preds) <- rownames(dat_result)</pre>
         ans <- get_confusion(preds, dat_result[, "Outcome", drop=FALSE])</pre>
         print(ans$matrix)
         print(paste("f-score for k-means (w/ wghts) on testset (80 rcds): ",
                      as.character(ans[[2]]), sep=""))
         # 0.6667
            0 1 class.error
         0 28 22
                      0.4400
         1 4 26
                       0.1333
         [1] "f-score for k-means (w/ wghts) on testset (80 rcds): 0.6667"
In [96]: # Type2 score for k-means when applied to the test set.
         mat <- as.matrix(ans[[1]])</pre>
         percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
         result <- round((0.4 * percent\_correct + 0.6 * ans[[2]]), 4)
         print(paste("Type2 score for k-means (w/ wghts) on testset (80 rcds): ",
                      as.character(result), sep=""))
         # [1] "Type2 score for k-means (w/ wghts) on testset: 0.67"
         print(paste("Accuracy: ", as.character(round(percent_correct,4)), sep=""))
         # [1] "Accuracy: 0.675"
         [1] "Type2 score for k-means (w/ wghts) on testset (80 rcds): 0.67"
         [1] "Accuracy: 0.675"
         Cross-val score for svm02 over 1000 seeds (5000 folds)
         # Function to compute a Type2 score with svm02 on a
```

```
In [100]: # Function to compute a Type2 score with svm02 on a
# cross-validation fold.

get_Type2_svm02 <- function(traindat, valdat) {

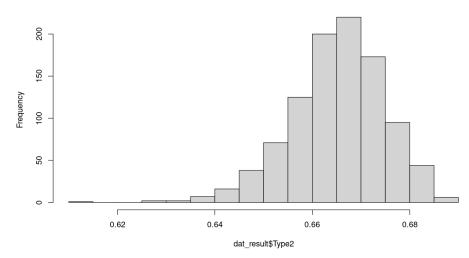
    # traindat and valdat need to be scaled
    train_scaled <- scale(traindat[, -1])</pre>
```

```
train_centers <- attr(train_scaled, "scaled:center")
train_scales <- attr(train_scaled, "scaled:scale")</pre>
    train_scaled <- as.data.frame(cbind(traindat$Outcome, train_scaled),</pre>
                                       row.names=rownames(traindat))
    colnames(train_scaled) <- colnames(traindat)</pre>
    svmmod <- svm(I(as.factor(Outcome)) ~ ., data=train scaled, kernel="radial",</pre>
                     gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
    # Scale valdat.
    test_scaled <- scale(valdat[, -1], center=train_centers,</pre>
                             scale=train_scales)
    test_scaled <- as.data.frame(cbind(valdat$Outcome, test_scaled),</pre>
                                      row.names=rownames(valdat))
    colnames(test_scaled) <- colnames(valdat)</pre>
    preds <- predict(svmmod, newdata= test scaled)</pre>
    ans <- table(preds, as.factor(valdat$Outcome))</pre>
    mat <- as.matrix(ans)</pre>
    percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
    result <- round((0.4 * percent correct + 0.6 * get fscore(mat)), 4)
    return(result)
}
```

```
In [98]:
          get_cvScore_svm02 <- function(seed_vector, dat, folds=5) {</pre>
              seedv_len <- length(seed_vector)</pre>
              datout <- rep(NA, 2*seedv_len)</pre>
              dim(datout) <- c(seedv_len, 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("seed", "Type2")</pre>
              datout$seed <- seed_vector</pre>
              ################################
              # Partition the data into folds, making sure
              # the ratio of survivors to non-survivors is
              # about the same for each traindat/valdat pair.
              # divide dat by the number of folds
              segment_size <- round(nrow(dat)/folds)</pre>
              diff <- nrow(dat) - folds * segment_size</pre>
              last_seg_size <- segment_size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              stopifnot(sum(segmentsv) == nrow(dat))
              for(h in 1:seedv_len) {
                   # shuffle dat
                   cur_seed <- seed_vector[h]</pre>
                   set.seed(cur_seed)
                   smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
                   dat <- dat[smp,]</pre>
                   # Get ratio of surviving to non-surviving cows.
                   dat_surv <- dat[which(dat$0utcome==1),]</pre>
                   dat_nonSurv <- dat[which(dat$0utcome==0),]</pre>
                   surv_ratio <- round(nrow(dat_surv)/nrow(dat), 4)</pre>
                   # Each element of row list will be the rows we pick
                   # out for one of the folds. E.g., the first element
                   # of row list will contain the rows we want for the
                   # first fold, the second element of row_list will
                   # contain the rows we want for the second fold, and
                   # so forth.
                   row_list <- vector("list", length=folds)</pre>
                   used_surv <- used_nonSurv <- c()</pre>
                   for(k in 1:folds) {
```

```
surv_count <- round(surv_ratio * segmentsv[k])</pre>
                        nonSurv_count <- segmentsv[k] - surv_count</pre>
                        avail_survRows <- rownames(dat_surv)[which(!(rownames(dat_surv) %in% used_surv)
                        avail_nonSurvRows <- rownames(dat_nonSurv)[which(!(rownames(dat_nonSurv) %in% u
                        if(k < folds) {</pre>
                            smp01 <- sample(avail survRows, surv count, replace=FALSE)</pre>
                            smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                            smp01 <- avail_survRows</pre>
                            smp02 <- avail_nonSurvRows</pre>
                            stopifnot(length(c(smp01, smp02)) == segmentsv[k])
                        used surv <- c(used surv, smp01)
                        used_nonSurv <- c(used_nonSurv, smp02)</pre>
                        row_list[[k]] <- c(smp01, smp02)</pre>
                   } # end of for-loop, index k
                   ###############################
                   train list <- test list <- vector("list", length= folds)
                   for(j in 1:folds) {
                        testdat <- dat[row_list[[j]],]</pre>
                        traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                        stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == nrow(dat)
                        test_list[[j]] <- testdat</pre>
                        train_list[[j]] <- traindat</pre>
                   }
                   scores <- mcmapply(get_Type2_svm02, train_list, test_list,</pre>
                                        SIMPLIFY= TRUE, mc.cores=5)
                   datout[h, c("Type2")] <- round(mean(scores), 5)</pre>
               } ## end of for-loop, index h
               return(datout)
In [146]: # Get Type2 scores for svm02 on 1000 seeds.
           set.seed(42)
           seed_vector <- sample(1:9999, 1000, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           dat_result <- get_cvScore_svm02(seed_vector, traindat)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 33 secs
           # The average we see here is over 5000 folds. Each seed
           # value is an average of 5 folds.
           summary(dat_result$Type2)
                                         Mean 3rd Qu.
                Min. 1st Qu. Median
                                                          Max.
                                                          0.687
                      0.659
                               0.666
                                         0.665 0.672
               0.615
           'Start time: 2021-04-06 19:00:26'
           Time difference of 33.57 secs
              Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                         Max.
             0.615
                     0.659
                              0.666
                                       0.665
                                               0.672
                                                        0.687
In [147]: round(mean(dat result$Type2), 4)
           # 0.6652
           0.6652
```

#### Distribution of cross-val Type2 scores for svm02



#### **Section Comments**

If we use cross-validation Type2 scores to identify the current best model, then our current best model is svm02 with an average cross-validation Type2 score over 5000 folds of 0.6652. The next best model is the base k-means model, with weights; its average cross-val Type2 score over 5K folds is 0.6620. The hybrid model's corresponding score is 0.6559.

The Type2 score is a weighted average of accuracy (40%) and f-score (60%). The f-score is the harmonic mean between recall and precision. The Type2 scores in this comparison are close enough that the three models might all have the same average accuracy over the 5K folds.

Applied to the test set, the svm02 model has 2X as many false negatives (FNs) as false positives (FPs), whereas the base k-means model, with weights, has 5.5X as many FPs as FNs. Perhaps with the hybrid model the probabilities from svm02 make it slightly more difficult for the k-means model to separate the survivors from the non-survivors due to the different directions in this lack of balance. In any case, it is worth seeing what the effect is of adding another set of probabilities, this time from our current best gradient boost model. The added dimension might help the k-means algorithm perform better.

\* \* \* \* \*

# Section 5: Hybrid model with 2 probability columns

Our next best model after svm02, constructed using cross-validation, is the gradient boosting model (gbclf\_best). So I will use this model to generate the probabilities for the prob02 column.

```
preds02 <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
# Scale traindat for purpose of an svm model.
svm_scaled <- scale(traindat[, -1])</pre>
svm_centers <- attr(svm_scaled, "scaled:center")
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
svm scaled <- as.data.frame(cbind(traindat$Outcome, svm scaled),</pre>
                                row.names=rownames(traindat))
colnames(svm scaled) <- colnames(traindat)</pre>
# This is our current best svm model for the trainset data
svmod <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
              gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
preds01 <- predict(svmod, newdata=svm_scaled, probability=TRUE)</pre>
traindat$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])</pre>
traindat$prob02 <- as.numeric(preds02)</pre>
###############################
# Transform and scale training set data for the
# k-means model.
traindat$AST <- log(traindat$AST)</pre>
traindat$CK <- log(traindat$CK)</pre>
traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
centers <- attr(traindat_scaled, "scaled:center")
scales <- attr(traindat_scaled, "scaled:scale")</pre>
#################################
# Apply weights to traindat. The sqrt should have
# been taken in the calling function.
cols <- names(wghts)</pre>
df2 <- t(t(traindat scaled[, cols]) * as.numeric(wghts[cols]))</pre>
traindat wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
colnames(traindat_wghts) <- cols</pre>
################################
# Prepare valdat for svm modeling.
svmval scaled <- scale(valdat[, -1], center=svm centers, scale=svm scales)</pre>
svmval_scaled <- as.data.frame(svmval_scaled,</pre>
                                   row.names=rownames(valdat))
# Compute prob01 and prob02.
preds01 b <- predict(symod, newdata=symval scaled, probability=TRUE)</pre>
preds02 b <- suppressMessages(predict(gbmod, newdata= valdat, type="response"))</pre>
valdat$prob01 <- as.numeric(attr(preds01 b, "probabilities")[, 2])</pre>
valdat$prob02 <- as.numeric(preds02_b)</pre>
# Transform and scale valdat.
valdat$AST <- log(valdat$AST)</pre>
valdat$CK <- log(valdat$CK)</pre>
valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
valdat_scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
# Apply weights to valdat. (We want valdat to look exactly like
# traindat. The weights act as a transformation of the data.)
df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
colnames(valdat_wghts) <- cols</pre>
##################################
# Construct k-means model.
```

```
set.seed(seed)
    kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
    # See how the clusters are associated with Outcome.
    dfout <- as.data.frame(cbind(traindat_wghts$Outcome, kmod$cluster),</pre>
                             row.names=rownames(traindat))
    colnames(dfout) <- c("Outcome", "cluster")</pre>
    c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
    ################################
    # Apply the k-means model to valdat wghts.
    # Each element of the following list is a row of valdat_wghts.
    valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                             seq(nrow(valdat wghts)))
    ctr_list <- vector("list", length= nrow(valdat))</pre>
    for(i in 1:nrow(valdat)) {
        ctr_list[[i]] <- kmod$centers</pre>
    names(ctr_list) <- rownames(valdat)</pre>
    # Get the predictions for the validation set.
    cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                        SIMPLIFY=TRUE, mc.cores=6)
    valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
    valdat_wghts$pred_Outcome <- NA</pre>
    if(c1_to_Outcome1) {
        valdat wghts[which(valdat wghts$cluster==1),]$pred Outcome <- 1</pre>
        valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
        valdat wghts[which(valdat wghts$cluster==1),]$pred Outcome <- 0</pre>
        valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
    }
    # Generate confusion matrix for the k-means clusters and
    # the corresponding f-score.
    preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
    names(preds) <- rownames(valdat)</pre>
    ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
    # The result returned is a Type2 score (which is a mixture
    # of accuracy and f-score).
    mat <- as.matrix(ans[[1]])</pre>
    percent correct <- sum(diag(mat))/floor(sum(mat))</pre>
    result \leftarrow round((0.4 * percent correct + 0.6 * ans[[2]]), 6)
    return(result)
}
```

#### Find best set of weights: hybrid model with prob01, prob02

```
In [19]: # There are 5 parameter lists to work with. Again, the
# best approach, perhaps, is to start by exploring the
# region around the space where all parameters have an
# equal weight---in this case, a weight of 0.20.

lst <- vector("list", length= 5)
names(lst) <- c("AST", "CK", "Daysrec", "prob01", "prob02")

lst[[1]] <- lst[[2]] <- lst[[3]] <- lst[[4]] <- lst[[5]] <- seq(0.14, 0.26, by=0.02)

start <- Sys.time()
dfc01 <- generate_combs(lst)
stop <- Sys.time()</pre>
```

```
# round(stop - start, 2)
         dim(dfc01)
         # 1451
          1451 5
 In []: # Test on a sample of 10.
         set.seed(42)
         smp <- sample(rownames(dfc01), 10, replace=FALSE)</pre>
         tst_params <- dfc01[smp,]</pre>
         head(tst params)
 In [ ]: # Find the best weights of those in tst_params.
         set.seed(1233)
         seed_vector <- sample(1:9999, 10, replace=FALSE)</pre>
         start <- Sys.time()</pre>
         dat_result <- gridSearch06(seed_vector, traindat, tst_params)</pre>
         stop <- Sys.time()</pre>
         round(stop - start, 2)
         # Time difference of 25.14 secs (for 10 rows)
 In [ ]: # Find the best parameters among those searched over.
         best params <- dat result[which(dat result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
         length(best_params)
         best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat result$Type2, na.rm=TRUE)),]$Type2
 In [ ]: dfc01[best_params,]
         best_Type2
In [30]: # Find the best weights of those in dfc01 (1451 rows,
         # 11 seeds, 5 folds).
         set.seed(1233)
         seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
         start <- Sys.time()</pre>
         paste("Start time: ", start, sep="")
         dat_result <- gridSearch06(seed_vector, traindat, dfc01)</pre>
         stop <- Sys.time()</pre>
         round(stop - start, 2)
         # Time difference of 1.14 hours
          'Start time: 2021-04-08 13:46:55'
         Time difference of 1.1 hours
In [31]: # Find the best parameters among those searched over.
         best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
         length(best_params)
         best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
```

```
In [32]: dfc01[best_params,]
                         AST
                                   CK
                                          Daysrec
                                                        prob01
                                                                      prob02
                        0.26
          # 14476
                                 0.18
                                              0.16
                                                           0.14
                                                                         0.26
          best_Type2
          # 0.64705
          A data.frame: 1 × 5
                  AST
                         CK Daysrec prob01 prob02
                  <dbl> <dbl>
                               <dbl>
                                      <dbl>
                                              <dbl>
           14476
                  0.26
                        0.18
                                 0.16
                                        0.14
                                               0.26
          0.64705
In [33]: # Refine the search.
          lst <- vector("list", length= 5)
names(lst) <- c("AST","CK","Daysrec","prob01","prob02")</pre>
          lst[[1]] \leftarrow seq(0.24, 0.32, by= 0.02)
          lst[[2]] \leftarrow seq(0.14, 0.22, by= 0.02)
          lst[[3]] \leftarrow seq(0.12, 0.18, by= 0.02)
          lst[[4]] \leftarrow seq(0.10, 0.16, by=0.02)
          lst[[5]] \leftarrow seq(0.24, 0.32, by=0.02)
          start <- Sys.time()</pre>
          dfc02 <- generate combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc02)
          # 251
          251 5
In [34]: # Add no weights to the combinations. This will
          # tell us whether using weights is better than not
          # using weights.
          dfc02 \leftarrow rbind(dfc02, rep(1,5))
In [35]: # Find the best weights of those in dfc02 (252 rows,
          # 11 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc02)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 12.26 mins
          'Start time: 2021-04-08 14:59:14'
          Time difference of 11.69 mins
In [36]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
```

```
length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
In [37]: dfc02[best_params,]
                         AST
                                   CK
                                          Daysrec
                                                        prob01
                                                                      prob02
          # 484
                        0.30
                                 0.16
                                              0.18
                                                           0.10
                                                                         0.26
          best_Type2
          # 0.65093
          A data.frame: 1 × 5
                 AST
                       CK Daysrec prob01 prob02
                                     <dbl>
                <dbl> <dbl>
                              <dbl>
                                            <dbl>
           484
                 0.3
                      0.16
                               0.18
                                       0.1
                                             0.26
          0.65093
In [38]: # Refine the search.
          lst <- vector("list", length= 5)
names(lst) <- c("AST","CK","Daysrec","prob01","prob02")</pre>
          lst[[1]] \leftarrow seq(0.28, 0.33, by= 0.01)
          lst[[2]] \leftarrow seq(0.13, 0.18, by= 0.01)
          lst[[3]] \leftarrow seq(0.15, 0.21, by= 0.01)
          lst[[4]] \leftarrow seq(0.05, 0.11, by=0.01)
          lst[[5]] \leftarrow seq(0.23, 0.30, by=0.01)
          start <- Sys.time()</pre>
          dfc03 <- generate combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc03)
          # 1183
          1183 5
In [39]: # Find the best weights of those in dfc02 (1183 rows,
          # 11 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat result <- gridSearch06(seed vector, traindat, dfc03)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 55 mins
          'Start time: 2021-04-08 15:18:18'
          Time difference of 54.93 mins
In [40]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
```

```
best Type2 <- dat result[which(dat result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$Type2
In [41]: dfc03[best_params,]
                                   CK
                                          Daysrec
                                                       prob01
                                                                     prob02
          # 4461
                        0.30
                                 0.18
                                             0.19
                                                                       0.25
                                                          0.08
          best Type2
          # 0.6518
          A data.frame: 1 x 5
                 AST
                        CK Daysrec prob01 prob02
                <dbl> <dbl>
                              <dbl>
                                     <dbl>
                                            <dbl>
           4461
                  0.3
                       0.18
                               0.19
                                      0.08
                                             0.25
          0.65184
In [43]: # Refine the search.
          lst <- vector("list", length= 5)</pre>
          names(lst) <- c("AST","CK","Daysrec","prob01","prob02")</pre>
          lst[[1]] \leftarrow seq(0.27, 0.31, by= 0.01)
          lst[[2]] \leftarrow seq(0.15, 0.19, by= 0.01)
          lst[[3]] \leftarrow seq(0.17, 0.21, by= 0.01)
          lst[[4]] \leftarrow seq(0.05, 0.10, by=0.01)
          lst[[5]] \leftarrow seq(0.23, 0.27, by=0.01)
          start <- Sys.time()</pre>
          dfc04 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc04)
          # 340
          340 5
In [44]:
          # Find the best weights of those in dfc02 (340 rows,
          # 11 seeds, 5 folds).
          set.seed(42)
          seed vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc04)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 16.28 mins
          'Start time: 2021-04-08 16:45:42'
          Time difference of 16.28 mins
In [45]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
```

```
best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
In [46]: dfc04[best_params,]
                         AST
                                    CK
                                          Daysrec
                                                        prob01
                                                                      prob02
          # 3234
                        0.30
                                 0.16
                                              0.21
                                                          0.06
                                                                        0.27
          best_Type2
          # 0.6467
          A data.frame: 1 × 5
                  AST
                        CK Daysrec prob01 prob02
                 <dbl> <dbl>
                               <dbl>
                                      <dbl>
                                             <dbl>
           3234
                  0.3
                       0.16
                               0.21
                                       0.06
                                              0.27
          0.6467
In [47]: # Refine the search.
          lst <- vector("list", length= 5)</pre>
          names(lst) <- c("AST","CK","Daysrec","prob01","prob02")</pre>
          lst[[1]] \leftarrow seq(0.28, 0.31, by= 0.01)
          lst[[2]] \leftarrow seq(0.14, 0.17, by= 0.01)
          lst[[3]] \leftarrow seq(0.20, 0.24, by= 0.01)
          lst[[4]] \leftarrow seq(0.04, 0.07, by=0.01)
          lst[[5]] \leftarrow seq(0.25, 0.28, by=0.01)
          start <- Sys.time()</pre>
          dfc05 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc05)
          # 175
          175 5
In [48]: # Find the best weights of those in dfc02 (175 rows,
          # 11 seeds, 5 folds).
          set.seed(1237)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()
paste("Start time: ", start, sep="")</pre>
          dat_result <- gridSearch06(seed_vector, traindat, dfc05)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 8.33 mins
          'Start time: 2021-04-08 17:07:27'
          Time difference of 8.33 mins
In [49]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
```

```
max(dat_result$Type2, na.rm=TRUE)),]$Type2
           1
In [50]: dfc05[best_params,]
                                      CK
                          AST
                                             Daysrec
                                                            prob01
                                                                           prob02
                          0.31
                                                                             0.25
           # 228
                                   0.14
                                                 0.24
                                                              0.06
           best_Type2
           # 0.6489
           A data.frame: 1 x 5
                  AST
                         CK Daysrec prob01 prob02
                 <dbl> <dbl>
                                <dbl>
                                       <dbl>
                                              <dbl>
                 0.31
                        0.14
                                                0.25
            228
                                0.24
                                        0.06
           0.64891
In [51]: # Refine the search.
           lst <- vector("list", length= 5)</pre>
           names(lst) <- c("AST","CK","Daysrec","prob01","prob02")</pre>
           lst[[1]] \leftarrow seq(0.29, 0.33, by= 0.01)
           lst[[3]] <- seq(0.12, 0.16, by= 0.01)
lst[[3]] <- seq(0.22, 0.26, by= 0.01)
lst[[4]] <- seq(0.04, 0.07, by=0.01)
           lst[[5]] \leftarrow seq(0.23, 0.27, by=0.01)
           start <- Sys.time()</pre>
           dfc06 <- generate_combs(lst)</pre>
           stop <- Sys.time()</pre>
           # round(stop - start, 2)
           dim(dfc06)
           # 313
           313 5
In [52]: # Find the best weights of those in dfc02 (313 rows,
           # 11 seeds, 5 folds).
           set.seed(1237)
           seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           dat_result <- gridSearch06(seed_vector, traindat, dfc06)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 15 mins
           'Start time: 2021-04-08 17:21:31'
```

Time difference of 14.96 mins

```
In [53]: # Find the best parameters among those searched over.
          best params <- dat result[which(dat result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
In [54]: dfc06[best_params,]
                                   CK
                                          Daysrec
                                                       prob01
                                                                     prob02
          # 1117
                        0.30
                                 0.15
                                             0.26
                                                          0.04
                                                                        0.25
          best_Type2
          # 0.6511
          A data.frame: 1 × 5
                 AST
                        CK Daysrec prob01 prob02
                 <dbl> <dbl>
                              <dbl>
                                     <dbl>
                                            <dbl>
           1117
                  0.3
                       0.15
                                      0.04
                                             0.25
          0.65112
In [55]: # Refine the search.
          lst <- vector("list", length= 5)</pre>
          names(lst) <- c("AST", "CK", "Daysrec", "prob01", "prob02")</pre>
          lst[[1]] \leftarrow seq(0.29, 0.31, by= 0.01)
          lst[[2]] \leftarrow seq(0.14, 0.16, by= 0.01)
          lst[[3]] \leftarrow seq(0.25, 0.28, by= 0.01)
          lst[[4]] \leftarrow seq(0.02, 0.05, by=0.01)
          lst[[5]] \leftarrow seq(0.23, 0.27, by=0.01)
          start <- Sys.time()</pre>
          dfc06 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc06)
          # 114
          114 5
In [56]: # Find the best weights of those in dfc02 (313 rows,
          # 11 seeds, 5 folds).
          set.seed(1237)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc06)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 5.36 mins
          'Start time: 2021-04-08 17:42:26'
          Time difference of 5.36 mins
```

```
In [57]: # Find the best parameters among those searched over.
          best params <- dat result[which(dat result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$Type2
In [58]: dfc06[best_params,]
                                  CK
                                         Daysrec
                                                      prob01
                                                                    prob02
                       0.29
          # 247
                                0.15
                                            0.28
                                                         0.04
                                                                      0.24
          best_Type2
          # 0.6529
          A data.frame: 1 × 5
                AST
                       CK Daysrec prob01 prob02
               <dbl> <dbl>
                             <dbl>
                                   <dbl>
                                          <dbl>
               0.29
                      0.15
                              0.28
                                    0.04
                                           0.24
          0.65287
 In [ ]: ### COMMENT:
          # It is interesting that the weight on prob02 is 6X the
          # weight on prob01. This looks to be more evidence that
          # the probabilities from the svm02 model are not
          # helping the k-means hybrid model.
          Cross-val score for hybrid model (p1 + p2), 1000 seeds
In [59]: lst <- vector("list", length= 5)</pre>
          names(lst) <- c("AST", "CK", "Daysrec", "prob01", "prob02")</pre>
          lst[[1]] \leftarrow c(0.29)
          lst[[2]] \leftarrow c(0.15)
          lst[[3]] \leftarrow c(0.28)
          lst[[4]] \leftarrow c(0.04)
          lst[[5]] \leftarrow c(0.24)
          dfc06 <- generate_combs(lst)</pre>
In [60]: # Make sure gridSearch06 calls get_cvScore_kmp1p2.
          set.seed(42)
          seed vector <- sample(1:9999, 1000, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc06)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
```

'Start time: 2021-04-08 17:51:20'

Time difference of 4.08 mins

# Time difference of 4.08 mins

```
In [61]: dat_result
# Type2 score of 0.6517

A data.frame: 1 ×
2

row Type2

<chr> <dbl>
1 0.65172
```

#### **Section Comments**

For the purpose of comparing model performance, the best scores we have thus far are those gotten when running against 1000 seeds; this equates to testing a model on 5000 folds, since for each seed we are computing an average cross-validation score over 5 folds (each fold having 64 records).

When we maintain the ratio between surviving cows and non-survivors across the folds, we are seeing that the best model is svm02, which has an average Type2 score over the 1000 seeds, or 5000 folds, of 0.6652.

The same score for the base k-means model with weights is 0.6620.

For the hybrid model with only prob01 (from svm02) and weights, this score is 0.6559.

And for the hybrid model with prob01 and prob02 and weights, this score is 0.6517.

In Part 2 of this project, we will make a similar comparison, but the folds will be ones in which the ratio between surviving cows and non-survivors is not maintained. In the real world, when applying our models to new data, we would not expect this ratio to be the same as what we see in our training set.

In Section 6 below, I collect even more accurate scores over the 1000 seeds. From this information we can then determine if the differences we are seeing are statistically significant.

# Section 6: Measures for comparing the different models

A table at the end of this section summarizes all of the data collected in this section.

## Get more information over a 1000 seeds for each model

```
In [11]: # This function is called by get_cvInfo. It returns a vector
          # of scores: f-score, accuracy, Type2, false negatives, and
          # false positives, in the stated order. The scores are for
          # the hybrid k-means model with both probability columns.
          get_cvScores_kmp1p2 <- function(traindat, valdat) {</pre>
              # wghts is a named vector of weights to apply. The names, and
              # order of the weights, correspond to the colnames of traindat
              # below. (Here the names are: AST, CK, Daysrec, and prob01.)
              set.seed(123)
              gbmod <- gbm(Outcome ~ ., data= traindat, n.trees= 130,</pre>
                              distribution= "bernoulli", shrinkage= 0.02)
              preds02 <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
              # Scale traindat for purpose of an svm model.
              svm_scaled <- scale(traindat[, -1])</pre>
              svm_centers <- attr(svm_scaled, "scaled:center")
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
              svm_scaled <- as.data.frame(cbind(traindat$Outcome, svm_scaled),</pre>
```

```
row.names=rownames(traindat))
colnames(svm_scaled) <- colnames(traindat)</pre>
# This is our current best svm model for the trainset data
svmod <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
              gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
preds01 <- predict(svmod, newdata=svm_scaled, probability=TRUE)</pre>
traindat$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])</pre>
traindat$prob02 <- as.numeric(preds02)</pre>
#################################
# Transform and scale training set data for the
# k-means model.
traindat$AST <- log(traindat$AST)</pre>
traindat$CK <- log(traindat$CK)</pre>
traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
centers <- attr(traindat scaled, "scaled:center")</pre>
scales <- attr(traindat scaled, "scaled:scale")</pre>
##################################
# Apply weights to traindat. (Take square root.)
wghts \leftarrow c(0.29, 0.15, 0.28, 0.04, 0.24)^{\circ}0.5
names(wghts) <- cols <- c("AST", "CK", "Daysrec", "prob01", "prob02")</pre>
df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
traindat_wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
colnames(traindat_wghts) <- cols</pre>
##################################
# Prepare valdat for svm modeling.
svmval_scaled <- scale(valdat[, -1], center=svm_centers, scale=svm_scales)</pre>
svmval_scaled <- as.data.frame(cbind(valdat$Outcome, svmval_scaled),</pre>
                                  row.names=rownames(valdat))
colnames(svmval_scaled) <- colnames(valdat)</pre>
# Compute prob01 and prob02.
preds01 b <- predict(symod, newdata=symval scaled, probability=TRUE)</pre>
preds02_b <- suppressMessages(predict(gbmod, newdata= valdat, type="response"))</pre>
valdat$prob01 <- as.numeric(attr(preds01_b, "probabilities")[, 2])</pre>
valdat$prob02 <- as.numeric(preds02_b)</pre>
# Transform and scale valdat.
valdat$AST <- log(valdat$AST)</pre>
valdat$CK <- log(valdat$CK)</pre>
valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
valdat_scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
# Apply weights to valdat. (We want valdat to look exactly like
# traindat. The weights act as a transformation of the data.)
df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
valdat_wghts <- cbind(as.numeric(valdat_scaled$Outcome), df2)</pre>
valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat_scaled))</pre>
colnames(valdat_wghts) <- cols</pre>
###############################
# Construct k-means model.
set.seed(123)
kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
```

```
# See how the clusters are associated with Outcome.
              dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                                        row.names=rownames(traindat))
              colnames(dfout) <- c("Outcome", "cluster")</pre>
              c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
              ###################################
              # Apply the k-means model to valdat wghts.
              # Each element of the following list is a row of valdat_wghts.
              valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                                        seq(nrow(valdat_wghts)))
              ctr_list <- vector("list", length= nrow(valdat))</pre>
              for(i in 1:nrow(valdat)) {
                   ctr_list[[i]] <- kmod$centers</pre>
              names(ctr_list) <- rownames(valdat)</pre>
              # Get the predictions for the validation set.
              cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                                            SIMPLIFY=TRUE, mc.cores=6)
              valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
              valdat_wghts$pred_Outcome <- NA</pre>
              if(c1 to Outcome1) {
                   valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
                   valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
              } else {
                   valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 0</pre>
                   valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
              }
              # Generate confusion matrix for the k-means clusters and
              # the corresponding f-score.
              preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
              names(preds) <- rownames(valdat)</pre>
              ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
              mat <- as.matrix(ans[[1]])</pre>
              fscore <- round(as.numeric(ans[[2]]), 4)</pre>
              acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
              type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
              FN <- as.numeric(mat[2,1])</pre>
              FP <- as.numeric(mat[1,2])</pre>
              return(c(fscore,acc,type2,FN,FP))
In [18]: # This function returns 5 cross-validation metrics for each
          # seed in the seed vector, seedv.
          get_cvInfo <- function(seedv, dat, folds=5) {</pre>
              seedv_len <- length(seedv)</pre>
              datout <- rep(NA, 5 * folds * seedv_len)</pre>
              dim(datout) <- c((seedv_len*folds), 5)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")</pre>
              # For each seed we record 5 sets of cross-val scores
              prefixes <- rep(as.character(seedv), rep(folds, seedv len))</pre>
              suffixes <- rep(paste(1:folds), seedv_len)</pre>
              seed_names <- paste(prefixes, suffixes, sep="--")</pre>
              rownames(datout) <- seed_names</pre>
              # Get ratio of surviving to non-surviving cows.
              dat_surv <- dat[which(dat$0utcome==1),]</pre>
              dat_nonSurv <- dat[which(dat$0utcome==0),]</pre>
              surv_ratio <- round(nrow(dat_surv)/nrow(dat), 4)</pre>
```

5/25/21, 07:01

```
# divide dat by the number of folds
              segment_size <- round(nrow(dat)/folds)</pre>
              diff <- nrow(dat) - folds * segment_size</pre>
              last_seg_size <- segment_size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              stopifnot(sum(segmentsv) == nrow(dat))
              for(h in 1:seedv len) {
                  # shuffle dat
                  cur_seed <- seedv[h]</pre>
                  set.seed(cur_seed)
                  smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
                  dat <- dat[smp,]</pre>
                  # Each element of row_list will be the rows we pick
                  # out for one of the folds. E.g., the first element
                  # of row_list will contain the rows we want for the
                  # first fold, the second element of row_list will
                  # contain the rows we want for the second fold, and
                   row list <- vector("list", length=folds)</pre>
                  used_surv <- used_nonSurv <- c()</pre>
                  # We want the ratio of survivors to non-survivors to be
                   # about the same in each fold.
                  for(k in 1:folds) {
                       surv_count <- round(surv_ratio * segmentsv[k])</pre>
                       nonSurv_count <- segmentsv[k] - surv_count</pre>
                       avail_survRows <- rownames(dat_surv)[which(!(rownames(dat_surv) %in% used_surv)</pre>
                       avail_nonSurvRows <- rownames(dat_nonSurv)[which(!(rownames(dat_nonSurv) %in% u</pre>
                       if(k < folds) {</pre>
                           smp01 <- sample(avail_survRows, surv_count, replace=FALSE)</pre>
                           smp02 <- sample(avail_nonSurvRows, nonSurv_count, replace=FALSE)</pre>
                           smp01 <- avail survRows</pre>
                           smp02 <- avail_nonSurvRows</pre>
                           stopifnot(length(c(smp01, smp02)) == segmentsv[k])
                       used_surv <- c(used_surv, smp01)</pre>
                       used_nonSurv <- c(used_nonSurv, smp02)</pre>
                       row_list[[k]] \leftarrow c(smp01, smp02)
                  } # end of for-loop, index k
                  train_list <- test_list <- vector("list", length= folds)</pre>
                   for(j in 1:folds) {
                       testdat <- dat[row_list[[j]],]</pre>
                       traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                       stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == dim(dat)[
                       test list[[j]] <- testdat</pre>
                       train_list[[j]] <- traindat</pre>
                  # When there are only 5 folds, only 5 cores get used.
                  scores <- mcmapply(get_cvScores_g03, train_list, test_list,</pre>
                                       SIMPLIFY= "array", mc.cores=5)
                   for(k in 1:folds) {
                       row_name <- paste(as.character(cur_seed), k, sep="--")</pre>
                       datout[row_name, 1:5] <- scores[, k]</pre>
                  }
              } ## end of for-loop, index h
              return(datout)
In [27]: # Get scores for the hybrid model with prob01 and prob02.
```

set.seed(1913)

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```
seed_vector <- sample(1:9999, 1000, replace=FALSE)
start <- Sys.time()
dat_result <- get_cvInfo(seed_vector, traindat)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 4.01 mins</pre>
```

Time difference of 4.01 mins

```
In [28]: dim(dat_result)
head(dat_result)
```

5000 5

A data.frame: 6 × 5

0.508

0.656

0.688

	fscore	Acc	Type2	FN	FP
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
47821	0.6415	0.7031	0.6661	7	12
47822	0.6522	0.7500	0.6913	9	7
47823	0.6984	0.7031	0.7003	2	17
47824	0.5714	0.6719	0.6116	10	11
47825	0.5556	0.6250	0.5834	8	16
92751	0.5517	0.5938	0.5685	8	18

## Summary info for hybrid model with prob01, prob02

```
In [29]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          # 0.6264
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0603
          summary(dat_result$fscore)
          'fscore mean: 0.6264'
          'fscore StdDev: 0.0603'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
            0.392 0.588
                             0.627
                                      0.626
                                              0.667
                                                       0.889
In [30]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          # 0.6887
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0521
          summary(dat_result$Acc)
          'accuracy mean: 0.6887'
          'accuracy StdDev: 0.0521'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
```

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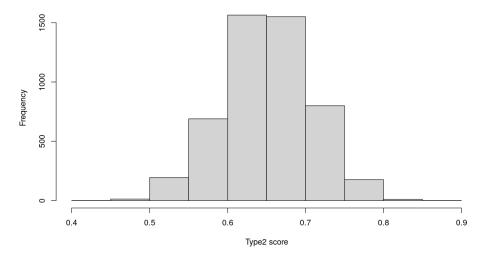
0.906

0.689 0.719

# 12.86

```
In [31]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
         Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
         paste0("Type2 mean: ", as.character(Type2_mean))
         # 0.6513
         paste0("Type2 StdDev: ", as.character(Type2_sd))
         # 0.0556
         summary(dat_result$Type2)
         'Type2 mean: 0.6513'
         'Type2 StdDev: 0.0556'
            Min. 1st Qu. Median
                                      Mean 3rd Qu.
                                                      Max.
            0.438
                    0.614
                            0.653
                                     0.651
                                             0.688
                                                      0.896
In [36]: # Histogram of the Type2 scores for the hybrid model
         options(repr.plot.width= 10, repr.plot.height= 6)
         hist(dat_result$Type2, breaks=10, xlab="Type2 score",
               main="Distribution of Type2 scores for hybrid model w/ p1 & p2")
```

#### Distribution of Type2 scores for hybrid model w/ p1 & p2



```
In [32]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
          FN_sd <- round(sd(dat_result$FN), 4)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          # 7.06
          paste0("FN StdDev: ", as.character(FN sd))
          # 2.13
          summary(dat_result$FN)
          'FN mean: 7.057'
          'FN StdDev: 2.1338'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                         Max.
             0.00
                      6.00
                               7.00
                                        7.06
                                                8.00
                                                        15.00
In [33]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
          FP_sd <- round(sd(dat_result$FP), 4)</pre>
          paste0("FP mean: ", as.character(FP_mean))
```

```
paste0("FP StdDev: ", as.character(FP_sd))
# 2.96
""
summary(dat_result$FP)
'FP mean: 12.8646'
'FP StdDev: 2.9614'
"

Min. 1st Qu. Median Mean 3rd Qu. Max.
4.0 11.0 13.0 12.9 15.0 24.0
```

# Summary info for base k-means model with weights

```
In [38]: # This function is called by get_cvInfo. It returns a vector
          # of scores: f-score, accuracy, Type2, false negatives, and
          # false positives, in the stated order. The scores are for
          # the base k-means model.
          get_cvScores_kmBase <- function(traindat, valdat) {</pre>
              # wghts is a named vector of weights to apply. The names, and
              # order of the weights, correspond to the colnames of traindat
              # below. (Here the names are: AST, CK, and Daysrec.)
              ###############################
              # Transform and scale training set data for the
              # k-means model.
              traindat$AST <- log(traindat$AST)</pre>
              traindat$CK <- log(traindat$CK)</pre>
              traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
              traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
              centers <- attr(traindat_scaled, "scaled:center")
scales <- attr(traindat_scaled, "scaled:scale")</pre>
              ###############################
              # Apply weights to traindat.
              wghts <- c(0.54, 0.28, 0.18)^{\circ}0.5
              names(wghts) <- cols <- c("AST", "CK", "Daysrec")</pre>
              df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              traindat wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
              colnames(traindat_wghts) <- cols</pre>
              ###############################
              # Prepare valdat for svm modeling.
              # Transform and scale valdat.
              valdat$AST <- log(valdat$AST)</pre>
              valdat$CK <- log(valdat$CK)</pre>
              valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
              valdat scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
              valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
              # Apply weights to valdat. (We want valdat to look exactly like
              # traindat. The weights act as a transformation of the data.)
              df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
              colnames(valdat_wghts) <- cols</pre>
              ##################################
              # Construct k-means model.
```

```
# See how the clusters are associated with Outcome.
dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                         row.names=rownames(traindat))
colnames(dfout) <- c("Outcome", "cluster")</pre>
c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
###############################
# Apply the k-means model to valdat_wghts.
# Each element of the following list is a row of valdat_wghts.
valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                         seq(nrow(valdat_wghts)))
ctr list <- vector("list", length= nrow(valdat))</pre>
for(i in 1:nrow(valdat)) {
    ctr_list[[i]] <- kmod$centers</pre>
names(ctr list) <- rownames(valdat)</pre>
# Get the predictions for the validation set.
cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                             SIMPLIFY=TRUE, mc.cores=6)
valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
valdat_wghts$pred_Outcome <- NA</pre>
if(c1_to_Outcome1) {
    valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
    valdat wghts[which(valdat wghts$cluster==1),]$pred Outcome <- 0</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
}
# Generate confusion matrix for the k-means clusters and
# the corresponding f-score.
preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
names(preds) <- rownames(valdat)</pre>
ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
mat <- as.matrix(ans[[1]])</pre>
fscore <- round(as.numeric(ans[[2]]), 4)</pre>
acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
FN <- as.numeric(mat[2,1])</pre>
FP <- as.numeric(mat[1,2])</pre>
return(c(fscore,acc,type2,FN,FP))
```

kmod <- suppressWarnings(kmeans(traindat\_wghts, 2, iter.max = 50, nstart=15))</pre>

```
In [40]: # Get scores for the base k-means model.

set.seed(1913)
seed_vector <- sample(1:9999, 1000, replace=FALSE)

start <- Sys.time()
dat_result <- get_cvInfo(seed_vector, traindat)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 2.91 mins</pre>
```

Time difference of 2.91 mins

```
In [41]: dim(dat_result)
          head(dat_result)
          5000 5
          A data.frame: 6 × 5
                                             FP
                                       FΝ
                  fscore
                          Acc Type2
                  <dbl> <dbl>
                               <dbl> <dbl>
                                          <dbl>
           4782--1 0.6557 0.6719 0.6622
                                             17
           4782--2 0.6667 0.7344 0.6938
                                         7
                                             10
           4782--3 0.7097 0.7188 0.7133
                                             16
           4782--4 0.6071 0.6562 0.6267
                                             15
           4782--5 0.6182 0.6719 0.6397
                                             15
           9275--1 0.6032 0.6094 0.6057
                                             20
In [42]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          # 0.6454
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0565
          summary(dat_result$fscore)
          'fscore mean: 0.6454'
          'fscore StdDev: 0.0565'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                         Max.
                    0.607
                                       0.645 0.679
                                                         0.836
            0.436
                              0.644
In [43]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          # 0.6861
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0533
          summary(dat_result$Acc)
          'accuracy mean: 0.6861'
          'accuracy StdDev: 0.0533'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
            0.500
                     0.656
                              0.688
                                       0.686 0.719
                                                         0.859
In [44]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          paste0("Type2 StdDev: ", as.character(Type2 sd))
          # 0.0542
          summary(dat_result$Type2)
          'Type2 mean: 0.6617'
          'Type2 StdDev: 0.0542'
```

```
Min. 1st Qu. Median
                        Mean 3rd Qu.
0.468
       0.627
               0.661
                       0.662
```

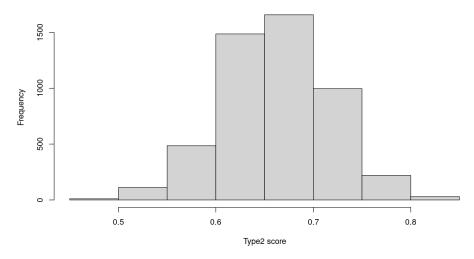
```
In [45]: # Histogram of the Type2 scores for the base k-means model.
         options(repr.plot.width= 10, repr.plot.height= 6)
         hist(dat_result$Type2, breaks=10, xlab="Type2 score",
              main="Distribution of Type2 scores for base k-means model")
```

Max.

0.846

#### Distribution of Type2 scores for base k-means model

0.700



```
In [46]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
          FN_sd <- round(sd(dat_result$FN), 4)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          paste0("FN StdDev: ", as.character(FN_sd))
          # 1.96
          summary(dat_result$FN)
          'FN mean: 5.5096'
          'FN StdDev: 1.9622'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                         Max.
             0.00
                      4.00
                               5.00
                                        5.51
                                                7.00
                                                        13.00
In [47]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
          FP_sd <- round(sd(dat_result$FP), 4)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          paste0("FP StdDev: ", as.character(FP_sd))
          # 2.91
          summary(dat_result$FP)
          'FP mean: 14.5824'
          'FP StdDev: 2.9105'
```

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Max.

26.0

Mean 3rd Qu.

14.6

17.0

Min. 1st Qu.

13.0

5.0

Median

15.0

### Summary info for hybrid model with prob01 generated from svm02

```
In [48]: # This function is called by get_cvInfo. It returns a vector
          # of scores: f-score, accuracy, Type2, false negatives, and
          # false positives, in the stated order. The scores are for
          # the hybrid k-means model with the prob01 column.
          get_cvScores_kmp1 <- function(traindat, valdat) {</pre>
              # Scale traindat for purpose of an svm model.
              svm_scaled <- scale(traindat[, -1])
svm_centers <- attr(svm_scaled, "scaled:center")
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
               svm_scaled <- as.data.frame(cbind(traindat$Outcome, svm_scaled),</pre>
                                               row.names=rownames(traindat))
              colnames(svm_scaled) <- colnames(traindat)</pre>
              # This is our current best svm model for the trainset data
              svmod <- svm(I(as.factor(Outcome)) ~ ., data=svm_scaled, kernel="radial",</pre>
                             gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
              preds01 <- predict(symod, newdata=sym scaled, probability=TRUE)</pre>
              traindat$prob01 <- as.numeric(attr(preds01, "probabilities")[, 2])</pre>
              ######################################
              # Transform and scale training set data for the
              # k-means model.
              traindat$AST <- log(traindat$AST)</pre>
               traindat$CK <- log(traindat$CK)</pre>
              traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
              traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
              centers <- attr(traindat_scaled, "scaled:center")</pre>
              scales <- attr(traindat_scaled, "scaled:scale")</pre>
              #################################
              # Apply weights to traindat.
              wghts \leftarrow c(0.23, 0.29, 0.33, 0.15)^0.5
              names(wghts) <- cols <- c("AST", "CK", "Daysrec", "prob01")</pre>
              df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              traindat_wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
              colnames(traindat_wghts) <- cols</pre>
              ###############################
               # Prepare valdat for svm modeling.
              svmval_scaled <- scale(valdat[, -1], center=svm_centers, scale=svm_scales)</pre>
              svmval_scaled <- as.data.frame(cbind(valdat$Outcome, svmval_scaled),</pre>
                                                  row.names=rownames(valdat))
              colnames(svmval_scaled) <- colnames(valdat)</pre>
              # Compute the prob01 column.
              preds01_b <- predict(svmod, newdata=svmval_scaled, probability=TRUE)</pre>
               valdat$prob01 <- as.numeric(attr(preds01_b, "probabilities")[, 2])</pre>
              # Transform and scale valdat.
              valdat$AST <- log(valdat$AST)</pre>
              valdat$CK <- log(valdat$CK)</pre>
              valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
              valdat_scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
              valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
```

```
# Apply weights to valdat. (We want valdat to look exactly like
              # traindat. The weights act as a transformation of the data.)
              df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
              colnames(valdat_wghts) <- cols</pre>
              ###############################
              # Construct k-means model.
              kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
              # See how the clusters are associated with Outcome.
              dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                                      row.names=rownames(traindat))
              colnames(dfout) <- c("Outcome", "cluster")</pre>
              c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
              ###################################
              # Apply the k-means model to valdat wghts.
              # Each element of the following list is a row of valdat_wghts.
              valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                                       seq(nrow(valdat_wghts)))
              ctr_list <- vector("list", length= nrow(valdat))</pre>
              for(i in 1:nrow(valdat)) {
                  ctr_list[[i]] <- kmod$centers</pre>
              names(ctr_list) <- rownames(valdat)</pre>
              # Get the predictions for the validation set.
              cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                                            SIMPLIFY=TRUE, mc.cores=6)
              valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
              valdat_wghts$pred_Outcome <- NA</pre>
              if(c1_to_Outcome1) {
                   valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
                   valdat wghts[which(valdat wghts$cluster==2),]$pred Outcome <- 0</pre>
              } else {
                  valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 0</pre>
                  valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
              # Generate confusion matrix for the k-means clusters and
              # the corresponding f-score.
              preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
              names(preds) <- rownames(valdat)</pre>
              ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
              mat <- as.matrix(ans[[1]])</pre>
              fscore <- round(as.numeric(ans[[2]]), 4)</pre>
              acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
              type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
              FN <- as.numeric(mat[2,1])</pre>
              FP <- as.numeric(mat[1,2])</pre>
              return(c(fscore,acc,type2,FN,FP))
In [50]: # Get scores for the hybrid model with prob01.
```

```
set.seed(1913)
seed_vector <- sample(1:9999, 1000, replace=FALSE)
start <- Sys.time()</pre>
```

```
dat_result <- get_cvInfo(seed_vector, traindat)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 3.56 mins
          Time difference of 3.56 mins
In [51]: dim(dat_result)
          head(dat_result)
          5000 5
          A data.frame: 6 × 5
                                       FN
                                             FP
                  fscore
                          Acc Type2
                  <dbl>
                         <dbl> <dbl> <dbl> <dbl> <dbl>
           4782--1 0.6538 0.7188 0.6798
                                         7
                                             11
           4782--2 0.6250 0.7188 0.6625
                                              9
                                         9
           4782--3 0.7333 0.7500 0.7400
                                         2
                                              14
           4782--4 0.5556 0.6250 0.5834
                                         9
                                              15
           4782--5 0.5556 0.6250 0.5834
                                         8
                                              16
           9275--1 0.5667 0.5938 0.5775
                                         7
                                              19
In [52]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0598
          summary(dat_result$fscore)
          'fscore mean: 0.632'
          'fscore StdDev: 0.0598'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
            0.377 0.593
                              0.632
                                       0.632 0.667
                                                         0.873
In [53]: Acc mean <- round(mean(dat result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc mean))
          # 0.6918
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0521
          summary(dat_result$Acc)
          'accuracy mean: 0.6918'
          'accuracy StdDev: 0.0521'
             Min. 1st Qu.
                             Median
                                        Mean 3rd Qu.
                                                          Max.
            0.477
                    0.656
                              0.688
                                       0.692 0.734
                                                         0.891
In [54]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          # 0.6559
          paste0("Type2 StdDev: ", as.character(Type2_sd))
```

```
# 0.0557
          summary(dat_result$Type2)
          'Type2 mean: 0.6559'
          'Type2 StdDev: 0.0557'
             Min. 1st Qu.
                             Median
                                         Mean 3rd Qu.
                                                           Max.
             0.417
                               0.656
                                                 0.694
                                                          0.880
                      0.618
                                        0.656
In [55]: # Histogram of the Type2 scores for the hybrid model with prob01.
          options(repr.plot.width= 10, repr.plot.height= 6)
          hist(dat_result$Type2, breaks=10, xlab="Type2 score",
                main="Distribution of Type2 scores for hybrid model w/ prob01")
                               Distribution of Type2 scores for hybrid model w/ prob01
              1500
              1000
           Frequency
              500
                   0.4
                                0.5
                                             0.6
                                                          0.7
                                                                        8.0
                                                                                     0.9
                                                 Type2 score
In [56]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
```

```
In [56]: FN_mean <- round(mean(dat_result$FN), 4)
FN_sd <- round(sd(dat_result$FN), 4)
paste0("FN mean: ", as.character(FN_mean))
# 6.83
paste0("FN StdDev: ", as.character(FN_sd))
# 1.99
""
summary(dat_result$FN)</pre>
```

'FN mean: 6.8334'

'FN StdDev: 1.9892'

"

Min. 1st Qu. Median Mean 3rd Qu. Max. 0.00 5.00 7.00 6.83 8.00 14.00

```
In [57]: FP_mean <- round(mean(dat_result$FP), 4)
    FP_sd <- round(sd(dat_result$FP), 4)
    paste0("FP mean: ", as.character(FP_mean))
# 12.89
    paste0("FP StdDev: ", as.character(FP_sd))
# 2.73
""
    summary(dat_result$FP)

'FP mean: 12.8926'

'FP StdDev: 2.728'
"

Min. 1st Qu. Median Mean 3rd Qu. Max.
    4.0 11.0 13.0 12.9 15.0 24.0</pre>
```

### Summary info for the svm02 model

```
In [58]: # This function is called by get_cvInfo. It returns a vector
          # of scores: f-score, accuracy, Type2, false negatives, and
          # false positives, in the stated order. The scores are for
          # the svm02 model.
          get_cvScores_svm02 <- function(traindat, valdat) {</pre>
               # traindat and valdat need to be scaled
               train_scaled <- scale(traindat[, -1])</pre>
              train_centers <- attr(train_scaled, "scaled:center")
train_scales <- attr(train_scaled, "scaled:scale")</pre>
               train_scaled <- as.data.frame(cbind(traindat$Outcome, train_scaled),</pre>
                                                 row.names=rownames(traindat))
               colnames(train_scaled) <- colnames(traindat)</pre>
               svmmod <- svm(I(as.factor(Outcome)) ~ ., data=train_scaled, kernel="radial",</pre>
                              gamma= 0.01, cost= 20, scale=FALSE, probability=TRUE)
               # Scale valdat.
               test_scaled <- scale(valdat[, -1], center=train_centers,</pre>
                                      scale=train_scales)
               test_scaled <- as.data.frame(cbind(valdat$Outcome, test_scaled),</pre>
                                                row.names=rownames(valdat))
               colnames(test_scaled) <- colnames(valdat)</pre>
               preds <- predict(svmmod, newdata= test scaled)</pre>
               ans <- table(preds, as.factor(valdat$Outcome))</pre>
               mat <- as.matrix(ans)</pre>
               fscore <- round(get_fscore(mat), 4)</pre>
               acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
               type2 <- round((0.4 * acc + 0.6 * fscore), 4)
               FN <- as.numeric(mat[2,1])</pre>
               FP <- as.numeric(mat[1,2])</pre>
               return(c(fscore,acc,type2,FN,FP))
          }
```

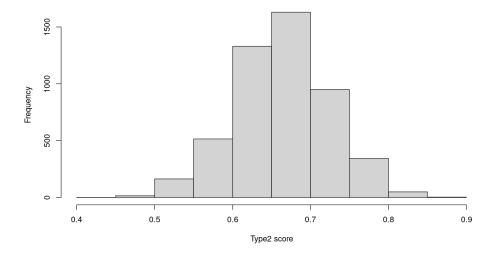
```
In [60]: # Get scores for the svm02 model.
set.seed(1913)
seed_vector <- sample(1:9999, 1000, replace=FALSE)

start <- Sys.time()
dat_result <- get_cvInfo(seed_vector, traindat)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 40.18 secs</pre>
```

```
Time difference of 40.18 secs
In [61]: dim(dat_result)
          head(dat_result)
          5000 5
          A data.frame: 6 × 5
                                             FP
                                       FN
                  fscore
                          Acc Type2
                               <dbl> <dbl>
                  <dbl> <dbl>
                                          <dbl>
           4782--1 0.6538 0.7188 0.6798
                                              7
                                        11
           4782--2 0.6512 0.7656 0.6970
                                        5
                                              10
           4782--3 0.7586 0.7812 0.7676
                                        12
                                              2
           4782--4 0.5714 0.6719 0.6116
                                        11
                                              10
           4782--5 0.5098 0.6094 0.5496
                                        15
                                              10
           9275--1 0.5818 0.6406 0.6053
                                        15
                                              8
In [62]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          # 0.6337
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0653
          summary(dat_result$fscore)
          'fscore mean: 0.6337'
          'fscore StdDev: 0.0653'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
            0.378
                     0.590
                              0.636
                                       0.634
                                               0.679
                                                         0.863
In [63]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0526
          summary(dat_result$Acc)
          'accuracy mean: 0.7104'
          'accuracy StdDev: 0.0526'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
                    0.672
                              0.719
                                       0.710
                                               0.750
                                                         0.891
```

```
In [64]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
         Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
         paste0("Type2 mean: ", as.character(Type2_mean))
         paste0("Type2 StdDev: ", as.character(Type2 sd))
         summary(dat_result$Type2)
         'Type2 mean: 0.6644'
         'Type2 StdDev: 0.059'
            Min. 1st Qu.
                           Median
                                      Mean 3rd Qu.
                                                       Max.
            0.442
                    0.625
                            0.666
                                     0.664
                                             0.701
                                                      0.874
In [65]: # Histogram of the Type2 scores for the svm02 model.
         options(repr.plot.width= 10, repr.plot.height= 6)
         hist(dat_result$Type2, breaks=10, xlab="Type2 score",
               main="Distribution of Type2 scores for the svm02 model")
```

#### Distribution of Type2 scores for the svm02 model



```
In [66]: FN mean <- round(mean(dat result$FN), 4)</pre>
          FN sd <- round(sd(dat result$FN), 4)
          paste0("FN mean: ", as.character(FN mean))
          # 10.82
          paste0("FN StdDev: ", as.character(FN_sd))
          # 2.82
          summary(dat result$FN)
          'FN mean: 10.817'
          'FN StdDev: 2.819'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                        Max.
              2.0
                       9.0
                              11.0
                                       10.8
                                               13.0
                                                        24.0
In [67]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
          FP_sd <- round(sd(dat_result$FP), 4)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          # 7.72
          paste0("FP StdDev: ", as.character(FP_sd))
```

```
# 2.16
        summary(dat_result$FP)
        'FP mean: 7.718'
        'FP StdDev: 2.155'
           Min. 1st Qu.
                          Median
                                     Mean 3rd Ou.
                                                      Max.
           1.00
                    6.00
                            8.00
                                     7.72
                                             9.00
                                                     17.00
In [1]: results <- read.csv("/home/greg/Documents/stat/github repos/cows/model results.csv",</pre>
                             header=TRUE, row.names=1)
        dim(results)
        4 10
In [ ]: #&* Bookmark
In [2]: # The following table is a summary of all the
        # Section 6 results from above. The Type2 score
        # is a weighted average of accuracy (40%) and
        # f-score (60%).
        results
```

A data.frame: 4 × 10

	fscore	fscore_sd	Type2	Type2_sd	accuracy	acc_sd	FN	FN_sd	FP	FP_sd
	<dbl></dbl>									
svm02	0.6337	0.0653	0.6644	0.0590	0.7104	0.0526	10.82	2.82	7.72	2.16
k-means	0.6454	0.0565	0.6617	0.0542	0.6861	0.0533	5.51	1.96	14.58	2.91
km_p1	0.6320	0.0598	0.6559	0.0557	0.6918	0.0521	6.83	1.99	12.89	2.73
km_p1p2	0.6264	0.0603	0.6513	0.0556	0.6887	0.0521	7.06	2.13	12.86	2.96

### **Section Comments**

The above table shows that the svm02 model outperforms the other models in terms of accuracy, with an average accuracy rate of 71%. The next best model in terms of accuracy is the k-means model with the prob01 column; it has an accuracy of 69.2%. The difference between these two mean scores is statistically significant: the Z-statistic (difference in means divided by pooled variance) is 17.765, giving us a two-tailed p-value of 1.32e-70. This means that there is also a statistically significant difference between the accuracy scores of svm02 and the base k-means model.

The Type2 score is a broader, or less-specialized, metric. Comparing the Type2 of the base k-means model with svm02, the Z-statistic is 2.38, giving us a two-tailed p-value of 0.017. So we have a statistically significant difference at the 0.05 level but not at the 0.01 level. Given how large n is (the measures are averages over 5000 folds, each fold having 64 records), I would want the significance level to be at 0.01 or smaller. Arguably, then, there is reason to think that there is not a true difference in Type2 scores between the two models.

The base k-means model has a better f-score than the svm02 model. This difference is statistically significant: the Z-statistic is 9.581, giving us a two-tailed p-value of 9.61e-22.

Overall, then, it appears that the svm02 and base k-means model are about equivalent in terms of performance. But if we want a low false-positive rate, the svm02 model will be preferable. If we want a low false negative rate, the base k-means model is preferable.

The above table shows us that the prob01 and prob02 columns do not help the k-means modeling by much. Some qualification is needed here because, although the Type2 score decreases with each added probability column, the

accuracy increases a bit. In Part 2 I will generate the very same table but for the scenario in which the ratio of the Outcome levels is not maintained between training and validation sets. It may be that a prob01 and/or prob02 column will make a more positive difference under such conditions

# Section 7: Hybrid model using gbclf\_best for prob01

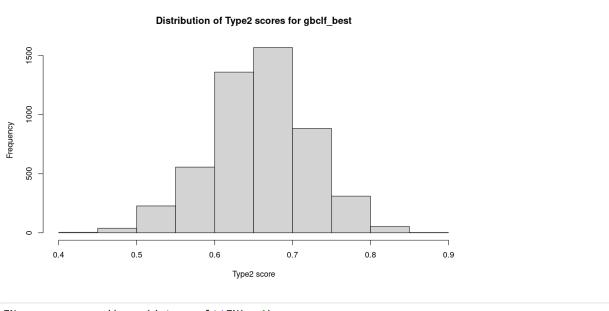
See whether we get a better hybrid model using the gradient boosting model to generate prob01 probabilities.

Before constructing the hybrid model, I get summary scores for the gbclf\_best model. We need these for the type of table we see immediately above.

# Summary info for gbclf\_best

```
In [10]: # This function is called by get_cvInfo. It returns a vector
          # of scores: f-score, accuracy, Type2, false negatives, and
          # false positives, in the stated order. The scores are for
          # the gbclf_best model.
          get_cvScores_gbclf <- function(traindat, valdat) {</pre>
              set.seed(123)
              gbmod <- gbm(Outcome ~ ., data= traindat, n.trees= 130,</pre>
                             distribution= "bernoulli", shrinkage= 0.02)
              preds <- suppressMessages(predict(gbmod, newdata= valdat, type="response"))</pre>
              preds[which(preds >= 0.5)] <- 1
              preds[which(preds < 0.5)] <- 0
              names(preds) <- rownames(valdat)</pre>
              preds <- as.factor(preds)</pre>
              ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
              mat <- as.matrix(ans[[1]])</pre>
              fscore <- round(ans[[2]], 4)
              acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
              type2 <- round((0.4 * acc + 0.6 * fscore), 4)
              FN <- as.numeric(mat[2,1])</pre>
              FP <- as.numeric(mat[1,2])</pre>
              return(c(fscore,acc,type2,FN,FP))
In [12]: # Get summary scores for gbclf_best, 1000 seeds.
          set.seed(1913)
          seed_vector <- sample(1:9999, 1000, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          dat_result <- get_cvInfo(seed_vector, traindat)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 35.47 secs
          Time difference of 35.47 secs
In [13]:
          dim(dat result)
          head(dat_result)
          5000 5
          A data.frame: 6 x 5
                  fscore
                          Acc Type2
                                      FΝ
                                            FP
                              <dbl> <dbl> <dbl>
                  <dbl> <dbl>
```

```
FΡ
                                      FΝ
                  fscore
                          Acc Type2
                               <dbl> <dbl>
                                          <dbl>
                  <dbl>
                        <dbl>
           4782--1 0.5652 0.6875 0.6141
                                       11
                                             9
           4782--2 0.6341 0.7656 0.6867
                                       11
                                             4
           4782--3 0.7925 0.8281 0.8067
                                        3
                                             8
           4782--4 0.5652 0.6875 0.6141
                                             9
                                       11
In [14]: | fscore mean <- round(mean(dat result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          # 0.613
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0745
          summary(dat result$fscore)
          'fscore mean: 0.613'
          'fscore StdDev: 0.0745'
             Min. 1st Qu. Median
                                       Mean 3rd Ou.
                                                         Max.
                                      0.613
            0.303 0.565
                             0.619
                                              0.667
                                                        0.851
In [15]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          # 0.7264
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0494
          summary(dat_result$Acc)
          'accuracy mean: 0.7264'
          'accuracy StdDev: 0.0494'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                         Max.
            0.562
                    0.688
                             0.734
                                      0.726
                                              0.766
                                                        0.891
In [16]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          # 0.6583
          paste0("Type2 StdDev: ", as.character(Type2_sd))
          # 0.0631
          summary(dat_result$Type2)
          'Type2 mean: 0.6583'
          'Type2 StdDev: 0.0631'
             Min. 1st Qu.
                                       Mean 3rd Qu.
                            Median
                                                         Max.
                                               0.700
            0.436
                     0.616
                             0.660
                                      0.658
                                                        0.867
In [17]: # Histogram of the Type2 scores for the svm02 model.
          options(repr.plot.width= 10, repr.plot.height= 6)
          hist(dat_result$Type2, breaks=10, xlab="Type2 score",
               main="Distribution of Type2 scores for gbclf_best")
```



```
In [18]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
          FN_sd <- round(sd(dat_result$FN), 4)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          # 9.81
          paste0("FN StdDev: ", as.character(FN_sd))
          # 2.31
          summary(dat_result$FN)
          'FN mean: 9.811'
          'FN StdDev: 2.3125'
             Min. 1st Qu.
                                       Mean 3rd Qu.
                            Median
                                                         Max.
             2.00
                      8.00
                             10.00
                                       9.81
                                              11.00
                                                        19.00
In [19]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
          FP_sd <- round(sd(dat_result$FP), 4)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          paste0("FP StdDev: ", as.character(FP_sd))
          summary(dat_result$FP)
          'FP mean: 7.6994'
          'FP StdDev: 2.5233'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                         Max.
              1.0
                       6.0
                                8.0
                                        7.7
                                                 9.0
                                                         18.0
```

# Find best set of weights for the new hybrid model

```
In [9]: # Function for obtaining average of confusion matrix
# f-score and percent correctly answered. This function
# is called from gridSearch06. It uses a gradient boosting
# model instead of an svm to generate prob01

get_cvScore_kmp1_v02 <- function(traindat, valdat, seed, wghts) {</pre>
```

```
# wghts is a named vector of weights to apply. The names, and
# order of the weights, correspond to the colnames of traindat
# below. (Here the names are: AST, CK, Daysrec, and prob01.)
# This is our current best gb model for the trainset data
set.seed(123)
gbmod <- gbm(Outcome ~ ., data= traindat, n.trees= 130,</pre>
               distribution= "bernoulli", shrinkage= 0.02)
preds01 <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
preds01[which(preds01 >= 0.5)] <- 1
preds01[which(preds01 < 0.5)] <- 0
traindat$prob01 <- preds01</pre>
###############################
# Transform and scale training set data for the
# k-means model.
traindat$AST <- log(traindat$AST)</pre>
traindat$CK <- log(traindat$CK)</pre>
traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
traindat scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
centers <- attr(traindat_scaled, "scaled:center")</pre>
scales <- attr(traindat_scaled, "scaled:scale")</pre>
###################################
# Apply weights to traindat. The sqrt should have
# been taken in the calling function.
cols <- names(wghts)</pre>
df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
traindat_wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
colnames(traindat_wghts) <- cols</pre>
#################################
# Prepare valdat.
# Compute the prob01 column.
preds01_b <- suppressMessages(predict(gbmod, newdata= valdat, type="response"))</pre>
preds01_b[which(preds01_b \ge 0.5)] <- 1
preds01_b[which(preds01_b < 0.5)] <- 0
valdat$prob01 <- preds01_b</pre>
# Transform and scale valdat.
valdat$AST <- log(valdat$AST)</pre>
valdat$CK <- log(valdat$CK)</pre>
valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
valdat scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
# Apply weights to valdat. (We want valdat to look exactly like
# traindat. The weights act as a transformation of the data.)
df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
colnames(valdat_wghts) <- cols</pre>
###############################
# Construct k-means model.
set.seed(seed)
kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
# See how the clusters are associated with Outcome.
dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                         row.names=rownames(traindat))
colnames(dfout) <- c("Outcome", "cluster")</pre>
c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
```

```
################################
              # Apply the k-means model to valdat wghts.
              # Each element of the following list is a row of valdat_wghts.
              valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                                        seq(nrow(valdat_wghts)))
              ctr_list <- vector("list", length= nrow(valdat))</pre>
              for(i in 1:nrow(valdat)) {
                   ctr_list[[i]] <- kmod$centers</pre>
              names(ctr_list) <- rownames(valdat)</pre>
              # Get the predictions for the validation set.
              cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                                            SIMPLIFY=TRUE, mc.cores=6)
              valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
              valdat wghts$pred Outcome <- NA
              if(c1_to_Outcome1) {
                   valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 1</pre>
                   valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
              } else {
                   valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 0</pre>
                   valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
              # Generate confusion matrix for the k-means clusters and
              # the corresponding f-score.
              preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
              names(preds) <- rownames(valdat)</pre>
              ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
              # The result returned is a Type2 score (which is a mixture
              # of accuracy and f-score).
              mat <- as.matrix(ans[[1]])</pre>
              percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
              result <- round((0.4 * percent_correct + 0.6 * ans[[2]]), 6)
              return(result)
In [11]: # There are 4 parameter lists to work with.
          lst <- vector("list", length= 4)</pre>
          names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow lst[[2]] \leftarrow lst[[3]] \leftarrow lst[[4]] \leftarrow seq(0.13, 0.37, by=0.02)
          start <- Sys.time()</pre>
          dfc01 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc01)
          # 1469
          1469 4
 In []: # Test on a sample of 10.
          set.seed(42)
          smp <- sample(rownames(dfc01), 10, replace=FALSE)</pre>
          tst_params <- dfc01[smp,]</pre>
          head(tst_params)
```

```
In [ ]: # Find the best weights of those in tst_params.
         set.seed(1233)
         seed vector <- sample(1:9999, 10, replace=FALSE)</pre>
         start <- Sys.time()</pre>
         dat_result <- gridSearch06(seed_vector, traindat, tst_params)</pre>
         stop <- Sys.time()</pre>
         round(stop - start, 2)
         # Time difference of 16 secs (for 10 rows)
 In [ ]: # Find the best parameters among those searched over.
         best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
         length(best_params)
         best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
 In [ ]: dfc01[best_params,]
         best_Type2
In [16]: # Find the best weights of those in dfc01 (1469 rows,
          # 11 seeds, 5 folds).
         set.seed(1233)
         seed vector <- sample(1:9999, 11, replace=FALSE)</pre>
         start <- Sys.time()</pre>
         paste("Start time: ", start, sep="")
         dat_result <- gridSearch06(seed_vector, traindat, dfc01)</pre>
         stop <- Sys.time()</pre>
         round(stop - start, 2)
         # Time difference of 53.12 mins
         'Start time: 2021-04-15 07:31:13'
         Time difference of 53.12 mins
In [17]: # Find the best parameters among those searched over.
         best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$row
         length(best params)
         best Type2 <- dat result[which(dat result$Type2 ==</pre>
                                            max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
In [18]: dfc01[best params,]
                   AST
                            CK
                                   Daysrec
                                                prob01
                          0.15
         # 5941 0.37
                                      0.31
                                                  0.17
         best_Type2
         # 0.67459
         A data.frame: 1 × 4
                      CK Daysrec prob01
```

```
<dbl>
                                     <dbl>
                <dbl> <dbl>
          0.67459
In [19]: # Refine the search.
          lst <- vector("list", length= 4)
names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow seq(0.34, 0.40, by= 0.01)
          lst[[2]] \leftarrow seq(0.12, 0.17, by= 0.01)
          lst[[3]] \leftarrow seq(0.28, 0.35, by= 0.01)
          lst[[4]] \leftarrow seq(0.12, 0.18, by=0.01)
          start <- Sys.time()</pre>
          dfc02 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc02)
          # 201
          201 4
In [20]: # Find the best weights of those in dfc01 (201 rows,
          # 11 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc02)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 7.23 mins
          'Start time: 2021-04-15 08:29:59'
          Time difference of 7.23 mins
In [21]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
In [22]: dfc02[best_params,]
                              CK
                                                    prob01
                    AST
                                      Daysrec
          # 1778 0.40
                             0.13
                                         0.30
                                                      0.17
          best_Type2
          # 0.67495
          A data.frame: 1 × 4
                  AST
                        CK Daysrec prob01
                <dbl> <dbl>
                              <dbl>
                                     <dbl>
```

```
CK Dayered prob01
          0.67495
In [23]: # Refine the search.
          lst <- vector("list", length= 4)</pre>
          names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow seq(0.39, 0.45, by= 0.01)
          lst[[2]] \leftarrow seq(0.10, 0.16, by= 0.01)
          lst[[3]] \leftarrow seq(0.28, 0.34, by= 0.01)
          lst[[4]] \leftarrow seq(0.15, 0.19, by=0.01)
          start <- Sys.time()</pre>
          dfc03 <- generate_combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc03)
          # 133
          133 4
In [24]: # Find the best weights of those in dfc01 (133 rows,
          # 11 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 11, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc03)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 5.32 mins
          'Start time: 2021-04-15 08:44:39'
          Time difference of 5.32 mins
In [25]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                              max(dat_result$Type2, na.rm=TRUE)),]$Type2
```

```
In [26]: dfc03[best_params,]
                    AST
                               CK
                                     Daysrec
                                                   prob01
          # 21
                   0.45
                            0.12
                                         0.28
                                                      0.15
          best_Type2
          # 0.67731
          A data.frame: 1 × 4
                AST
                      CK Daysrec prob01
               <dbl>
                                    <dbl>
                    <dbl>
                             <dbl>
           21
                0.45
                      0.12
                              0.28
                                     0.15
          0.67731
In [27]: # Refine the search.
          lst <- vector("list", length= 4)
names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow seq(0.43, 0.48, by= 0.01)
          lst[[2]] \leftarrow seq(0.09, 0.14, by= 0.01)
          lst[[3]] \leftarrow seq(0.25, 0.29, by= 0.01)
          lst[[4]] \leftarrow seq(0.12, 0.17, by=0.01)
          start <- Sys.time()</pre>
          dfc04 <- generate combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc04)
          # 115
          115 4
In [28]: # Find the best weights of those in dfc01 (115 rows,
          # 33 seeds, 5 folds). I have increased the seeds so
          # that we get a more stable result.
          set.seed(1233)
          seed_vector <- sample(1:9999, 33, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat result <- gridSearch06(seed vector, traindat, dfc04)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 14.22 mins
          'Start time: 2021-04-15 08:53:43'
          Time difference of 14.22 mins
In [29]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
```

```
In [30]: dfc04[best_params,]
                    AST
                               CK
                                      Daysrec
                                                    prob01
                            0.12
          # 21
                   0.48
                                         0.25
                                                      0.15
          best_Type2
          # 0.67726
          A data.frame: 1 × 4
                 AST
                       CK Daysrec prob01
                <dbl>
                     <dbl>
                              <dbl>
                                     <dbl>
                0.48
                       0.12
                               0.25
                                      0.15
          0.67726
In [31]: # Refine the search.
          lst <- vector("list", length= 4)
names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow seq(0.47, 0.54, by= 0.01)
          lst[[2]] \leftarrow seq(0.09, 0.14, by= 0.01)
          lst[[3]] \leftarrow seq(0.20, 0.26, by= 0.01)
          lst[[4]] \leftarrow seq(0.14, 0.16, by=0.01)
          start <- Sys.time()</pre>
          dfc05 <- generate combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc05)
          # 106 4
          106 4
In [32]: # Find the best weights of those in dfc01 (106 rows,
          # 33 seeds, 5 folds).
          set.seed(1233)
          seed_vector <- sample(1:9999, 33, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat_result <- gridSearch06(seed_vector, traindat, dfc05)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 13.2 mins
          'Start time: 2021-04-15 09:12:10'
          Time difference of 13.2 mins
In [33]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$row
          length(best params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
```

```
In [34]: dfc05[best_params,]
                    AST
                               CK
                                      Daysrec
                                                    prob01
                   0.54
          # 21
                            0.12
                                         0.20
                                                      0.14
          best_Type2
          # 0.67876
          A data.frame: 1 × 4
                AST
                       CK Daysrec prob01
               <dbl>
                                    <dbl>
                    <dbl>
                             <dbl>
           32
                0.54
                      0.12
                               0.2
                                     0.14
          0.67876
In [35]: # Refine the search.
          lst <- vector("list", length= 4)
names(lst) <- c("AST","CK","Daysrec","prob01")</pre>
          lst[[1]] \leftarrow seq(0.53, 0.60, by= 0.01)
          lst[[2]] \leftarrow seq(0.09, 0.14, by= 0.01)
          lst[[3]] \leftarrow seq(0.15, 0.20, by= 0.01)
          lst[[4]] \leftarrow seq(0.11, 0.15, by=0.01)
          start <- Sys.time()</pre>
          dfc06 <- generate combs(lst)</pre>
          stop <- Sys.time()</pre>
          # round(stop - start, 2)
          dim(dfc06)
          # 141 4
          141 4
In [36]: # Find the best weights of those in dfc01 (141 rows,
          # 33 seeds, 5 folds).
          # Using a new seed.
          set.seed(7731)
          seed_vector <- sample(1:9999, 33, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          dat result <- gridSearch06(seed vector, traindat, dfc06)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 17.7 mins
          'Start time: 2021-04-15 09:28:41'
          Time difference of 17.7 mins
In [37]: # Find the best parameters among those searched over.
          best_params <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat result$Type2, na.rm=TRUE)),]$row
          length(best_params)
          best_Type2 <- dat_result[which(dat_result$Type2 ==</pre>
                                               max(dat_result$Type2, na.rm=TRUE)),]$Type2
          1
```

```
In [38]: |dfc06[best_params,]
                  AST CK
                                   Daysrec
                                               prob01
         # 789
                0.57
                        0.11 0.19
                                                 0.13
         best_Type2
         # 0.68179
         A data.frame: 1 × 4
               AST
                      CK Daysrec prob01
              <dbl> <dbl>
                           <dbl>
                                  <dbl>
          789
               0.57
                     0.11
                            0.19
                                   0.13
         0.68179
```

## Summary info for the new hybrid model using gbclf\_best

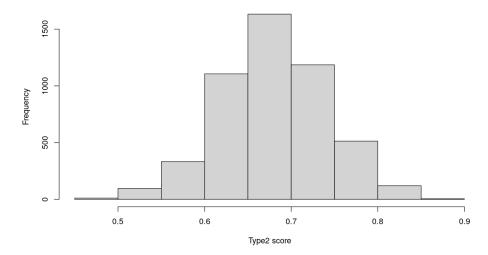
```
In [49]: # This function is called by get_cvInfo. It returns a vector
         # of scores: f-score, accuracy, Type2, false negatives, and
         # false positives, in the stated order. The scores are for
         # the hybrid k-means model with the prob01 column generated
         # by the gbclf best model.
         get_cvScores_kmp1_v02 <- function(traindat, valdat) {</pre>
              # This is our current best gb model for the trainset data
              set.seed(123)
              gbmod <- gbm(Outcome ~ ., data= traindat, n.trees= 130,</pre>
                             distribution= "bernoulli", shrinkage= 0.02)
              preds01 <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
              preds01[which(preds01 >= 0.5)] <- 1
              preds01[which(preds01 < 0.5)] <- 0
              traindat$prob01 <- preds01
              ######################################
              # Transform and scale training set data for the
              # k-means model.
              traindat$AST <- log(traindat$AST)</pre>
              traindat$CK <- log(traindat$CK)</pre>
              traindat$Daysrec <- sqrt(traindat$Daysrec)</pre>
              traindat_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
              centers <- attr(traindat scaled, "scaled:center")</pre>
              scales <- attr(traindat_scaled, "scaled:scale")</pre>
              ##############################
              # Apply weights to traindat.
              wghts <- c(0.57, 0.11, 0.19, 0.13)^{\circ}0.5
              names(wghts) <- cols <- c("AST","CK","Daysrec","prob01")</pre>
              df2 <- t(t(traindat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
              traindat_wghts <- as.data.frame(df2, row.names=rownames(traindat))</pre>
              colnames(traindat_wghts) <- cols</pre>
              ###############################
              # Prepare valdat.
              # Compute the prob01 column.
              preds01_b <- suppressMessages(predict(gbmod, newdata= valdat, type="response"))</pre>
              preds01_b[which(preds01_b >= 0.5)] <- 1
              preds01_b[which(preds01_b < 0.5)] <- 0
              valdat$prob01 <- preds01_b</pre>
```

```
# Transform and scale valdat.
valdat$AST <- log(valdat$AST)</pre>
valdat$CK <- log(valdat$CK)</pre>
valdat$Daysrec <- sqrt(valdat$Daysrec)</pre>
valdat scaled <- scale(valdat[, -1], center=centers, scale=scales)</pre>
valdat_scaled <- as.data.frame(valdat_scaled, row.names=rownames(valdat))</pre>
# Apply weights to valdat. (We want valdat to look exactly like
# traindat. The weights act as a transformation of the data.)
df2 <- t(t(valdat_scaled[, cols]) * as.numeric(wghts[cols]))</pre>
valdat_wghts <- as.data.frame(df2, row.names=rownames(valdat))</pre>
colnames(valdat_wghts) <- cols</pre>
##################################
# Construct k-means model.
kmod <- suppressWarnings(kmeans(traindat_wghts, 2, iter.max = 50, nstart=15))</pre>
# See how the clusters are associated with Outcome.
dfout <- as.data.frame(cbind(traindat$Outcome, kmod$cluster),</pre>
                         row.names=rownames(traindat))
colnames(dfout) <- c("Outcome", "cluster")</pre>
c1_to_Outcome1 <- c1_toLevel_1(dfout)</pre>
##################################
# Apply the k-means model to valdat_wghts.
# Each element of the following list is a row of valdat_wghts.
valdat_asList <- split(valdat_wghts[, colnames(kmod$centers)],</pre>
                         seq(nrow(valdat_wghts)))
ctr list <- vector("list", length= nrow(valdat))</pre>
for(i in 1:nrow(valdat)) {
    ctr_list[[i]] <- kmod$centers</pre>
names(ctr_list) <- rownames(valdat)</pre>
# Get the predictions for the validation set.
cluster_assgns <- mcmapply(getCluster, valdat_asList, ctr_list,</pre>
                             SIMPLIFY=TRUE, mc.cores=6)
valdat_wghts$cluster <- as.numeric(cluster_assgns)</pre>
valdat wghts$pred Outcome <- NA
if(c1 to Outcome1) {
    valdat wghts[which(valdat wghts$cluster==1),]$pred Outcome <- 1</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 0</pre>
} else {
    valdat_wghts[which(valdat_wghts$cluster==1),]$pred_Outcome <- 0</pre>
    valdat_wghts[which(valdat_wghts$cluster==2),]$pred_Outcome <- 1</pre>
# Generate confusion matrix for the k-means clusters and
# the corresponding f-score.
preds <- as.factor(valdat_wghts$pred_Outcome)</pre>
names(preds) <- rownames(valdat)</pre>
ans <- get_confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
mat <- as.matrix(ans[[1]])</pre>
fscore <- round(ans[[2]], 4)
acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
type2 <- round((0.4 * acc + 0.6 * fscore), 4)
FN <- as.numeric(mat[2,1])</pre>
FP <- as.numeric(mat[1,2])</pre>
return(c(fscore,acc,type2,FN,FP))
```

```
}
In [50]:
          # Get scores for hybrid model with prob01 generated
          # from gbclf_best.
          set.seed(1913)
          seed_vector <- sample(1:9999, 1000, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          dat_result <- get_cvInfo(seed_vector, traindat)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 3.25 mins
          Time difference of 3.25 mins
In [51]: dim(dat_result)
          head(dat result)
          5000 5
          A data.frame: 6 x 5
                                        FΝ
                                              FΡ
                  fscore
                          Acc Type2
                   <dbl>
                                           <dbl>
                         <dbl>
                                <dbl> <dbl>
           4782--1 0.5833 0.6875 0.6250
                                        10
                                              10
           4782--2 0.6977 0.7969 0.7374
                                         9
                                               4
           4782--3 0.7778 0.8125 0.7917
                                         3
                                               9
           4782--4 0.5652 0.6875 0.6141
                                        11
                                               9
           4782--5 0.5532 0.6719 0.6007
                                        10
                                              11
           9275--1 0.5556 0.6250 0.5834
                                              15
In [52]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          # 0.6424
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0689
          summary(dat_result$fscore)
          'fscore mean: 0.6424'
          'fscore StdDev: 0.0689'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
            0.381
                    0.596
                              0.640
                                        0.642
                                                0.694
                                                         0.857
In [53]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          paste0("accuracy StdDev: ", as.character(Acc sd))
          # 0.0506
          summary(dat_result$Acc)
          'accuracy mean: 0.7373'
          'accuracy StdDev: 0.0506'
```

```
Mean 3rd Qu.
            Min. 1st Qu.
                           Median
                                                       Max.
            0.562
                    0.703
                            0.734
                                     0.737
                                             0.766
                                                      0.891
In [54]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
         Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
         paste0("Type2 mean: ", as.character(Type2_mean))
         # 0.6644
         paste0("Type2 StdDev: ", as.character(Type2_sd))
         # 0.059
         summary(dat_result$Type2)
         'Type2 mean: 0.6804'
         'Type2 StdDev: 0.0605'
            Min. 1st Qu.
                           Median
                                      Mean 3rd Qu.
                                                       Max.
            0.466
                    0.639
                            0.682
                                     0.680
                                             0.722
                                                      0.871
In [55]: # Histogram of the Type2 scores for the svm02 model.
         options(repr.plot.width= 10, repr.plot.height= 6)
         hist(dat_result$Type2, breaks=10, xlab="Type2 score",
               main="Dist. of Type2 scores for hybrid model w/ gbclf_best probs.")
```

#### Dist. of Type2 scores for hybrid model w/ gbclf\_best probs.



```
In [56]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
          FN sd <- round(sd(dat result$FN), 4)
          paste0("FN mean: ", as.character(FN_mean))
          paste0("FN StdDev: ", as.character(FN_sd))
          # 2.11
          summary(dat_result$FN)
          'FN mean: 8.6318'
          'FN StdDev: 2.1093'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                        Max.
             2.00
                      7.00
                              9.00
                                       8.63
                                              10.00
                                                       16.00
In [57]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
```

```
FP_sd <- round(sd(dat_result$FP), 4)</pre>
         paste0("FP mean: ", as.character(FP_mean))
         paste0("FP StdDev: ", as.character(FP_sd))
         # 2.56
         summary(dat result$FP)
         'FP mean: 8.1806'
         'FP StdDev: 2.5607'
            Min. 1st Qu.
                           Median
                                      Mean 3rd Qu.
                                                       Max.
                                      8.18
                                              10.00
                                                      18.00
             1.00
                     6.00
                              8.00
In [20]: results <- read.csv("/home/greg/Documents/stat/github_repos/cows/model_results_Part1.csv",</pre>
                               header=TRUE, row.names=1)
         dim(results)
         6 10
 In [ ]: #&* Bookmark
In [21]: # The following table is an updated summary of all of
         # the 1000-seed results from above.
         results
```

A data.frame: 6 x 10

	fscore	fscore_sd	Type2	Type2_sd	accuracy	acc_sd	FN	FN_sd	FP	FP_sd
	<dbl></dbl>									
gbclf	0.6130	0.0745	0.6583	0.0631	0.7264	0.0494	9.81	2.31	7.70	2.52
svm02	0.6337	0.0653	0.6644	0.0590	0.7104	0.0526	10.82	2.82	7.72	2.16
k-means	0.6454	0.0565	0.6617	0.0542	0.6861	0.0533	5.51	1.96	14.58	2.91
km_p1	0.6320	0.0598	0.6559	0.0557	0.6918	0.0521	6.83	1.99	12.89	2.73
km_p1p2	0.6264	0.0603	0.6513	0.0556	0.6887	0.0521	7.06	2.13	12.86	2.96
km gbclf	0.6424	0.0689	0.6804	0.0605	0.7373	0.0506	8.63	2.11	8.18	2.56

### Final Comments for Part 1

Of the entries in the above table, the new hybrid model, km gbclf, has the best Type2 score (0.6804) and the best accuracy score (0.7373). It has the second-best f-score. Comparing Type2 scores, the Z-statistic for the difference in means between km\_gbclf and svm02 (which has the next best Type2 score) is 13.39. Comparing accuracy scores between these two models, the Z-statistic is 26.06. We can say with some confidence, then, that km\_gbclf is a better model for the downer cow dataset than svm02. On average, we see an increase in accuracy of 2.69 percentage points.

km\_gbclf has a much better Type2 score and much better accuracy score than the base k-means model.

km\_gbclf has a much better Type2 score than the gbclf model itself. Comparing accuracy scores between these two models, the Z-statistic is 10.90 (two-tailed p-value < 2e-16). On average, the accuracy score for km\_gbclf is about 1.1 percentage points better than gbclf\_best.

The prob02 column for km\_p1p2 is the outcome from gbclf\_best. But the accuracy score for km\_gbclf is almost 5 percentage points better than that for km\_p1p2, and km\_gbclf's f-score is 1.6 percentage points better. This adds to our evidence for thinking that the information from svm02 injected into the k-means model via prob01 conflicts with what is already there. Furthermore, since the average number of false negatives and average number of false positives for gbclf are not much different from the same averages for svm02, the stark difference of these numbers from those for the base

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k-means model might not be the source of the conflict.

When choosing svm02 for the prob01 column, I did so because it had a higher Type2 score than either the gradient boosting model or the best random forest model. But of these three models, gbclf has the highest accuracy score. Perhaps when adding a probability column to k-means, the choice needs to be made based on the accuracy score.

The work in this notebook shows that k-means can be used to boost the performance of models and even yield the best-performing model among those surveyed. But we have also seen that the choices made in the construction of the hybrid model matter a lot: we need to choose the "right" model for constructing the prob01 column in order to get a model better than the competing models. The work of Part 2 of this project also illustrates this fact, or truth. And in Parts 3 and 4 we see that there is no guarantee that using k-means in this way will provide us with the best performing model. But this is true about any modeling approach; there is no single algorithm or approach that will always provide us with the best predictive model.

\* \* \* \* \*

### **Addendum**

### Item 1: Get summary info for the g03 logistic model over 5000 folds

```
In [15]: # This function is called by get cvInfo. It returns a vector
         # of scores: f-score, accuracy, Type2, false negatives, and
         # false positives, in the stated order.
         # (First alter get_cvInfo to call this function.)
         get_cvScores_g03 <- function(traindat, valdat) {</pre>
              g03mod <- suppressWarnings(glm(Outcome ~ Daysrec + CK + I(log(AST)),</pre>
                             data= traindat, family= binomial, singular.ok=TRUE,
                             epsilon= 1e-7, maxit=50))
              preds <- suppressWarnings(predict(g03mod, newdata= valdat, type="response"))</pre>
              preds[which(preds >= 0.5)] <- 1
              preds[which(preds < 0.5)] <- 0
              names(preds) <- rownames(valdat)</pre>
              preds <- as.factor(preds)</pre>
              ans <- get confusion(preds, valdat[, "Outcome", drop=FALSE])</pre>
              mat <- as.matrix(ans[[1]])</pre>
              fscore <- round(ans[[2]], 4)
              acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
              type2 <- round((0.4 * acc + 0.6 * fscore), 4)
              FN <- as.numeric(mat[2,1])</pre>
              FP <- as.numeric(mat[1,2])</pre>
              return(c(fscore,acc,type2,FN,FP))
```

```
In [19]: # Get summary scores for the g03 logistic model, 1000 seeds.

set.seed(1913)
seed_vector <- sample(1:9999, 1000, replace=FALSE)

start <- Sys.time()
dat_result <- get_cvInfo(seed_vector, traindat)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 24.43 secs</pre>
```

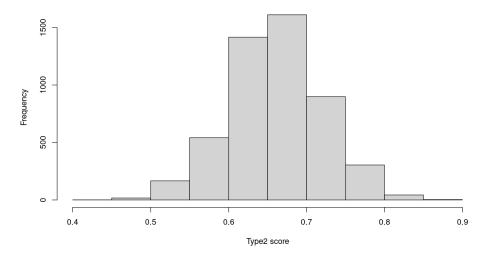
Time difference of 24.43 secs

```
In [20]: dim(dat_result)
          head(dat_result)
          5000 5
          A data.frame: 6 × 5
                                             FP
                                       FΝ
                  fscore
                          Acc Type2
                  <dbl> <dbl>
                               <dbl> <dbl>
                                          <dbl>
           4782--1 0.6250 0.7188 0.6625
                                              9
           4782--2 0.6667 0.7812 0.7125
                                        10
                                              4
           4782--3 0.7547 0.7969 0.7716
                                         4
                                              9
           4782--4 0.5417 0.6562 0.5875
                                             11
                                        11
           4782--5 0.5106 0.6406 0.5626
                                        11
                                             12
           9275--1 0.5714 0.6250 0.5928
                                             16
In [21]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0681
          summary(dat_result$fscore)
          'fscore mean: 0.623'
          'fscore StdDev: 0.0681'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                         Max.
                    0.578
                                       0.623 0.667
            0.333
                              0.625
                                                         0.875
In [22]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          # 0.7182
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0506
          summary(dat_result$Acc)
          'accuracy mean: 0.7182'
          'accuracy StdDev: 0.0506'
             Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                          Max.
            0.531
                    0.688
                              0.719
                                       0.718 0.750
                                                         0.906
In [23]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          paste0("Type2 StdDev: ", as.character(Type2 sd))
          # 0.0597
          summary(dat_result$Type2)
          'Type2 mean: 0.6611'
          'Type2 StdDev: 0.0597'
```

```
Mean 3rd Qu.
Min. 1st Qu. Median
                                         Max.
0.425
        0.622
                0.662
                        0.661
                                0.700
                                        0.887
```

```
In [24]: # Histogram of the Type2 scores for the svm02 model.
         options(repr.plot.width= 10, repr.plot.height= 6)
         hist(dat_result$Type2, breaks=10, xlab="Type2 score"
              main="Distribution of Type2 scores for the g03 logistic model")
```

#### Distribution of Type2 scores for the g03 logistic model



```
In [25]: FN_mean <- round(mean(dat_result$FN), 4)</pre>
          FN_sd <- round(sd(dat_result$FN), 4)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          paste0("FN StdDev: ", as.character(FN_sd))
          # 2.21
          summary(dat_result$FN)
          'FN mean: 8.8212'
```

'FN StdDev: 2.2106'

```
Min. 1st Qu.
              Median
                         Mean 3rd Qu.
                                         Max.
2.00
        7.00
                9.00
                         8.82
                                10.00
                                        17.00
```

```
In [26]: FP_mean <- round(mean(dat_result$FP), 4)</pre>
          FP_sd <- round(sd(dat_result$FP), 4)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          paste0("FP StdDev: ", as.character(FP_sd))
          # 2.77
          summary(dat_result$FP)
```

'FP mean: 9.211'

'FP StdDev: 2.7696'

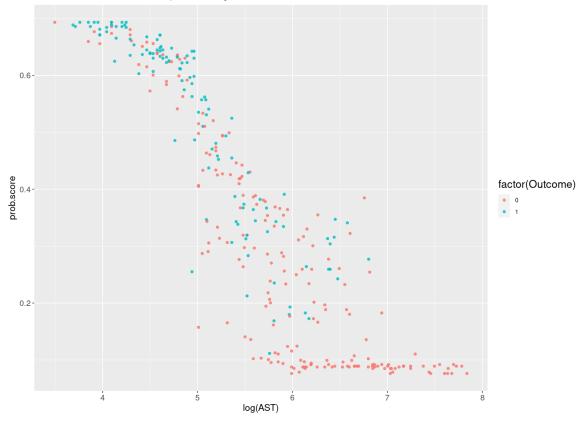
```
Min. 1st Qu.
             Median
                        Mean 3rd Qu.
                                        Max.
       7.00
1.00
                9.00
                        9.21
                              11.00
                                       20.00
```

# **Item 1 Comments**

The g03 logistic regression model is very competitive despite its construction not involving cross-validation. It has an average accuracy score of nearly 72% and an average Type2 score exceeding 66%.

# Item 2: More plots of separation of points by Outcome level

### Differences in AST and prob01, by Outcome level



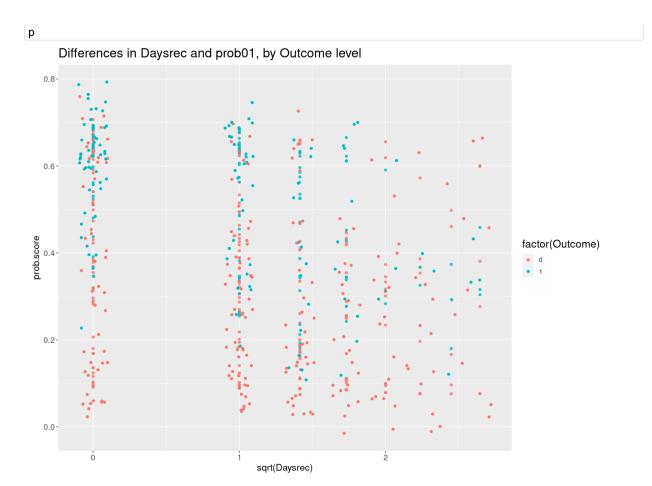
```
In [33]: # Plot Daysrec vs. prob01.

dat_plot <- newtrain[, c("Outcome", "Daysrec", "prob01"), drop=FALSE]
dat_plot$Daysrec <- sqrt(dat_plot$Daysrec)

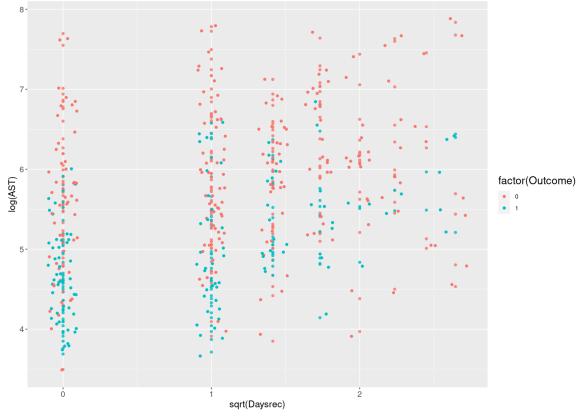
options(repr.plot.width= 12, repr.plot.height= 9)

p <- ggplot(dat_plot, aes(Daysrec, prob01, color= factor(Outcome))) +

geom_point(alpha= 0.8) + geom_jitter(width= 0.1, height= 0.1) +
    xlab("sqrt(Daysrec)") + ylab("prob.score") +
    ggtitle("Differences in Daysrec and prob01, by Outcome level") +
    theme(axis.text= element_text(size = 12)) +
    theme(axis.title= element_text(size= 14)) +
    theme(title= element_text(size= 16))</pre>
```



## Differences in Daysrec and AST, by Outcome level



```
In [ ]:
```