Modeling with k-means, Part 2

In this notebook I apply the methods of Part1 to the California housing dataset. See my CA_housing_analysis repository for an introduction to this dataset. In that analysis, the response variable was the median house value of 1990 Census districts in the state of California. Here I use the dataset for a classification model that distinguishes between the INLAND districts and the non-INLAND districts (i.e., those districts closer to the ocean). As with the downer cow dataset, I want to see whether we can construct a better classification model using k-means in combination with one or more supervised learning algorithms.

Prior work suggests that a k-means hybrid model will likely not be able to out-perform competing models which are already excellent classifiers. The greater the accuracy score of a competing model, the less room there is for improvement upon that score. One reason the hybrid model of Part 1 did well is due to the fact that k-means, as an unsupervised algorithm, was already very good at distinguishing between the surviving cows and the non-survivors. (In other words, k-means was already very competitive with the other models prior to using it in a hybrid model.) This meant that when we combined it with another model of the right sort, we were able to obtain a hybrid model which outperformed the competing models. This will not happen unless the models being combined contribute different, yet complementary, information. For example, the support vector classifier of Part 1 did not mix well with k-means, although the logistic regression model did. If I had tried to further boost the hybrid model by adding a second probability column generated from the gradient boosting model, we would have seen no further gain because the gradient boosting model does not have any further, or new, information to contribute.

One lesson from Part 1, then, is that a hybrid k-means model is more likely to outperform competing models when the competing models do not have great accuracy scores. The competing models in Part 1 had accuracy scores around 70%. It also helps quite a bit if the k-means algorithm itself, in an unsupervised setting, does a very good job of partitioning the data into the desired classes.

In prior work with the CA housing data (version 4 of this notebook), the best classifier was a random forest model with an accuracy score just under 90%. This model relied on 7 of the predictors, excluding latitude and longitude. (If we include latitude and longitude, it is far too easy to distinguish inland districts from those much closer to the ocean.) The k-means algorithm, unsupervised, does a very poor job distinguishing between the 2 classes. This meant that adding a prob01 column to the dataset that k-means worked with---the prob01 column containing probability scores from another classifier using supervised learning---was not enough to yield a hybrid model which was better than the all of the other models. The hybrid model was only second-best. If one adds a second probability column (generated from a model different from the one used for the prob01 column, of course), the hybrid model scores increase slightly, but not enough to beat the random forest model.

In version 4 of this notebook weights were of little help, likely because of the number of predictors being used in the model, but perhaps also because of the amount of data. I suspect that the more predictors, or dimensions, k-means has to work with (assuming all are meaningful predictors), the less benefit we will see from optimal weights. Furthermore, the more predictors we have and the more data, the harder it becomes to find optimal weights; the parameter space we have to search through becomes too large for a thorough search.

Thus in this notebook I will limit the number of predictors I work with so that competing classifiers have accuracy scores at or below 75%. This increases the likelihood of a hybrid model being able to out-perform the competing models. If I end up with only 3 predictors, I can again see if weights can improve the k-means model. The weights will be difficult to find, though, since the CA housing dataset is so much larger than the cow dataset.

* * * * *

Preliminaries

```
In [ ]: require(car)
    require(repr)
    require(ggplot2)
    require(stringr)
    require(parallel)
    require(faraway)
    require(randomForest)
```

```
require(gbm)
require(plyr)
require(e1071)

In [2]: options(digits= 5, show.signif.stars= FALSE)

Construct training and test sets
```

```
In [3]: traindat <- read.csv("/home/greg/Documents/stat/Geron_ML/datasets/housing/train_revised_27JU</pre>
                                 header=TRUE, row.names=1,
                                 colClasses= c("character", rep("numeric", 9), "character",
                                                 rep("numeric", 5), "character"))
          dim(traindat)
           16482 · 16
 In [4]: colnames(traindat)
           'longitude' · 'latitude' · 'housing_median_age' · 'total_rooms' · 'total_bedrooms' · 'population' · 'households' ·
           'median_income' · 'median_house_value' · 'ocean_proximity' · 'rooms_per_hh' · 'bdrms_per_room' · 'pop_per_hh' ·
           'HHdens_In' · 'long_transf' · 'income_cat'
 In [7]: table(as.factor(traindat$ocean_proximity))
                                                     OCEAN
              INLAND
                        NEAR BAY NEAR OCEAN
                                                     7338
                 5187
                             1820
                                         2137
 In [5]: testdat <- read.csv("/home/greg/Documents/stat/Geron_ML/datasets/housing/test_revised_27JUN2(</pre>
                                header=TRUE, row.names=1,
                                colClasses= c("character", rep("numeric", 9), "character",
                                                rep("numeric", 5), "character"))
          dim(testdat)
           4121 · 16
 In [8]: dat <- rbind(traindat, testdat)</pre>
          dat$Inland <- 0</pre>
          dat[which(dat$ocean_proximity== "INLAND"),]$Inland <- 1</pre>
          table(dat$Inland)
          14078 6525
In [10]: # Remove predictors that are collinear, that we do not need, or
          # that would be too helpful when identifying Inland districts.
          newcols <- colnames(dat)[which(!(colnames(dat) %in% c("HHdensity", "income_cat",</pre>
                                                                       "ocean_proximity", "longitude",
                                                                      "latitude", "long_transf",
                                                                      "median_income","population",
"total_bedrooms","total_rooms",
                                                                      "pop_per_hh","bdrms_per_room",
                                                                      "HHdens ln")))]
          newcols
```

'housing_median_age' 'households' 'median_house_value' 'rooms_per_hh' 'Inland'

```
In [11]: dat <- dat[, newcols]</pre>
         dim(dat)
         colnames(dat)
          20603 · 5
          'housing_median_age' · 'households' · 'median_house_value' · 'rooms_per_hh' · 'Inland'
In [12]: # Create training and test sets for use in testing
         # new k-means approach.
         set.seed(8763)
         smp <- sample(rownames(dat), 10603, replace=FALSE)</pre>
         traindat <- dat[smp,]</pre>
         testdat <- dat[which(!(rownames(dat) %in% smp)),]</pre>
         dim(testdat)
          10000 · 5
In [13]: rm(dat)
In [14]: # Move the response variable, Inland, to the first
         # column.
         newcols <- colnames(traindat)</pre>
         newcols <- newcols[which(!(newcols %in% c("Inland")))]</pre>
         newcols <- c("Inland", newcols)</pre>
         newcols
          'Inland' · 'housing median age' · 'households' · 'median house value' · 'rooms per hh'
In [15]: traindat <- traindat[, newcols]</pre>
         testdat <- testdat[, newcols]</pre>
In [16]: # Save out the files.
         write.csv(traindat, file="/home/greg/Documents/stat/github_repos/cows/CAhousing_train_10603.0
                    row.names= TRUE)
         write.csv(testdat, file="/home/greg/Documents/stat/github repos/cows/CAhousing test 10K.csv"
                    row.names= TRUE)
In [43]: traindat <- read.csv("/home/greg/Documents/stat/github repos/cows/CAhousing train 10603.csv"
                               header=TRUE, row.names=1, colClasses= c("character", rep("numeric",4)))
         dim(traindat)
          10603 · 5
In [44]: testdat <- read.csv("/home/greg/Documents/stat/github_repos/cows/CAhousing_test_10K.csv",</pre>
                               header=TRUE, row.names=1, colClasses= c("character", rep("numeric",4)))
         dim(testdat)
          10000 · 5
In [17]: # Get ratio of Inland to non-Inland in traindat.
          round(mean(traindat$Inland), 4)
         0.3105
In [18]: # Get ratio of Inland to non-Inland in testdat.
          round(mean(testdat$Inland), 4)
```

0.3233

Basic functions

```
In [19]: # Function for computing "proportion of deviance explained", an
          # R-sqrd statistic for link= logit. See p.41 of Julian Faraway's
          # "Extending the Linear Model with R" (2006: Chapman & Hall).
          # This statistic is due to N. Nagelkerke (1991; see Faraway's
          # bibliography).
          get_RsqrdDev <- function(modl) {</pre>
              n_obs <- length(modl$fitted.values)</pre>
              ans <- (1-exp((modl$deviance - modl$null.deviance)/n obs))/(1-exp(-modl$null.deviance/n
              return(round(ans, 4))
In [20]: # Function to compute f-score for a 2x2 confusion matrix.
          get_fscore <- function(mat) {</pre>
              mat[is.na(mat)] <- 0</pre>
              FN <- as.numeric(mat[2,1])</pre>
              TP <- as.numeric(mat[2,2])</pre>
              FP <- as.numeric(mat[1,2])</pre>
              recall <- TP/(TP + FN)
              precision <- TP/(TP + FP)</pre>
              f_score <- 2* (recall*precision)/(recall + precision)</pre>
              return(round(f score, 4))
In [21]: # Function to output a confusion matrix and the f-score
          # for that matrix (if it is 2x2).
          get_confusion <- function(preds, df_actual) {</pre>
              # df actual is a one-column dataframe;
              # preds is a named vector of predictions;
              # preds is of type factor; it is assumed there are
              # at least 2 factor levels
              levs <- levels(preds)</pre>
              n_levs <- length(levs)</pre>
              if(n_levs== 1) { levs <- c('0', '1') }</pre>
              n_levs <- max(n_levs, 2)</pre>
              actual <- as.vector(df_actual[, 1])</pre>
              names(actual) <- rownames(df_actual)</pre>
              datout \leftarrow rep(0, n_levs * (n_levs + 1))
              dim(datout) <- c(n_levs, n_levs + 1)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c(levs, "class.error")</pre>
              rownames(datout) <- levs
              result <- vector("list", length= 2)</pre>
              names(result) <- c("matrix", "f_score")</pre>
              # for each factor level, identify the rcd names
              # which should be classed as such
              for(rowlev in levs) {
                  actlev_names <- names(actual[actual == rowlev])</pre>
                   # columns are for the predicted values:
                  for(collev in levs) {
                       predlev_names <- names(preds[preds == collev])</pre>
                       if(length(predlev_names > 0)) {
                           datout[rowlev, collev] <- sum(predlev_names %in% actlev_names)</pre>
```

```
In [22]: # The following function is from Robert Kabacoff's "R in Action", pp.379-380.
         wssplot <- function(data, title="", nc=15, seed=1233) {</pre>
             # wss[1] is the total sum of squares when there is only
             # one cluster. In R's kmeans help this is called 'totss'.
             # Here is another way to compute totss:
             # ss <- function(x) sum(scale(x, scale = FALSE)^2)</pre>
             wss <- (nrow(data) - 1)*sum(apply(data, 2, var))</pre>
             for(i in 2:nc) {
                  set.seed(seed)
                  km model <- suppressWarnings(kmeans(data, centers=i, iter.max=50,
                                                        nstart=5))
                  wss[i] <- sum(km_model$withinss)</pre>
             plot(1:nc, wss, type='b', xlab="Number of clusters",
                  ylab="Within groups sum of squares",
                  main= title)
         }
```

```
In [23]: # Function for identifying which cluster each record
# belongs to.

getCluster <- function(x, centers) {

    # x is a row of a dataframe; its columns need
    # to be in the same order as centers (a matrix'
    # constructed from kmeans)

    cl_dist <- apply(centers, 1, function(y) sqrt(sum((x-y)^2)))
    return(which.min(cl_dist)[1])
}</pre>
```

```
param_vlens <- rep(NA, n_args)</pre>
              for(i in 1:n_args) {
                  param_vlens[i] <- length(arglist[[i]])</pre>
              n_rows <- prod(param_vlens)</pre>
              datout <- rep(NA, n_args*n_rows)</pre>
              dim(datout) <- c(n rows, n args)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- names(arglist)</pre>
              cprod <- 1
              for(j in 1:n_args) {
                  vect <- arglist[[j]]</pre>
                  val <- rep(vect, rep(cprod, length(vect)))</pre>
                  datout[, j] <- rep(val, n_rows/length(val))</pre>
                  cprod <- cprod*length(vect)</pre>
              # } ## end of 'if(FALSE)'
              # datout <- expand.grid(arglist, KEEP.OUT.ATTRS= FALSE)</pre>
              # colnames(datout) <- names(arglist)</pre>
              row_sums <- round(rowSums(datout), 4)</pre>
              names(row_sums) <- rownames(datout)</pre>
              tol <- tol
              row sums <- row sums[which((as.numeric(row sums) <= (1 + tol)) & (as.numeric(row sums) >=
              datout <- datout[names(row_sums),]</pre>
              return(datout)
In [25]: # Function to constrain range of data between 0 and 1.
          range01 <- function(x) {(x - min(x))/(max(x) - min(x))}
In [26]: # Function to constrain range of data between min_x and max_x.
          # This function is used to transform validation data.
          range02 <- function(x, min_x, max_x) \{(x - min_x)/(max_x - min_x)\}
In [165]: # Function returning mapping between clusters and
          # Inland levels. We choose the mapping that yields
          # the best f-score score.
          c1 toLevel 1 <- function(dat) {</pre>
              # Returns TRUE if cluster 1 maps to Inland = 1
              # dat is a dataframe with 2 columns, c("Inland", "cluster");
              # nrow(dat) = number of predictions from the model;
              # dat$Inland = traindat$Inland (from the calling function)
              # We find the correct mapping between cluster number and
              # Inland level by computing f-scores for the different
                                 We choose the mapping with the best
              # valid mappings.
              # f-score score.
              tbl <- as.matrix(table(dat$Inland, as.factor(dat$cluster)))</pre>
              # The colnames of tbl refer to the names of the clusters.
              # With only 2 levels for Inland, we need only 2 scores.
              scores <- rep(NA, 2)
              # First possibility: cluster 1 maps to the non-Inland districts
              tmpdat <- dat
              tmpdat[which(tmpdat$cluster== 1),]$Inland <- 0</pre>
```

tmpdat[which(tmpdat\$cluster== 2),]\$Inland <- 1</pre>

```
preds <- as.factor(tmpdat$Inland)</pre>
              names(preds) <- rownames(tmpdat)</pre>
              ans <- get_confusion(preds, dat[, "Inland", drop=FALSE])</pre>
              scores[1] <- ans[[2]]</pre>
              # Alternative mapping: cluster 1 maps to the Inland districts
              tmpdat <- dat
              tmpdat[which(tmpdat$cluster== 1),]$Inland <- 1</pre>
              tmpdat[which(tmpdat$cluster== 2),]$Inland <- 0</pre>
              preds <- as.factor(tmpdat$Inland)</pre>
              names(preds) <- rownames(tmpdat)</pre>
              ans <- get_confusion(preds, dat[, "Inland", drop=FALSE])</pre>
              scores[2] <- ans[[2]]
              return(scores[1] <= scores[2])</pre>
          }
In [ ]:
In [ ]:
In [12]: # This grid search searches for the best set of weights to use
          # in our k-means clustering model. The best weights are those
          # which generalize best to the validation set.
          gridSearch06 <- function(seed_vector, dat, df_params, folds=5) {</pre>
              datout <- rep(NA, 2*nrow(df params))</pre>
              dim(datout) <- c(nrow(df_params), 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("row", "Type2")</pre>
              datout$row <- rownames(df_params)</pre>
              # We want the sqrt of the weights.
              df_params <- df_params^0.5</pre>
              params_rows <- rownames(df_params)</pre>
              ###############################
              # Partition the data into folds.
              # divide dat by the number of folds
              segment size <- round(nrow(dat)/folds)</pre>
              diff <- nrow(dat) - folds * segment_size</pre>
              last_seg_size <- segment_size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              stopifnot(sum(segmentsv) == nrow(dat))
              # Create a dataframe, each row for a distinct seed.
              # Each column of the dataframe is for a distinct set
              # of weights. The entries in the cells are Type2
              # scores.
              seedv_len <- length(seed_vector)</pre>
              df_scores <- rep(NA, seedv_len*nrow(df_params))</pre>
              dim(df_scores) <- c(seedv_len, nrow(df_params))</pre>
              df_scores <- as.data.frame(df_scores)</pre>
              colnames(df scores) <- rownames(df params)</pre>
              rownames(df_scores) <- as.character(seed_vector)</pre>
              for(h in 1:seedv_len) {
                   cur_seed <- seed_vector[h]</pre>
                   set.seed(cur seed)
                   smp <- sample(rownames(dat), dim(dat)[1], replace= FALSE)</pre>
                   dat <- dat[smp,]</pre>
```

```
# Each element of row_list will be the rows we pick
        # out for one of the \overline{\mathsf{folds}}. E.g., the first element
        # of row_list will contain the rows we want for the
        # first fold, the second element of row_list will
        # contain the rows we want for the second fold, and
        # so forth.
        row list <- vector("list", length=folds)</pre>
        names(row_list) <- as.character(1:folds)</pre>
        startpt <- 1
        for(k in 1:folds) {
             endpt <- startpt + segmentsv[k] - 1</pre>
             stopifnot(endpt <= nrow(dat))</pre>
             row_list[[k]] <- rownames(dat)[startpt:endpt]</pre>
             startpt <- endpt + 1
        for(i in 1:nrow(df params)) {
             cur_row <- params_rows[i]</pre>
             wghts <- as.numeric(df_params[i,])</pre>
             names(wghts) <- colnames(df_params)</pre>
             train_list <- test_list <- vector("list", length= folds)</pre>
             for(j in 1:folds) {
                 testdat <- dat[row_list[[j]],]</pre>
                 traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                 stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == nrow(data)
                 test_list[[j]] <- testdat</pre>
                 train_list[[j]] <- traindat</pre>
             }
             # When there are only 5 folds, only 5 cores get used.
             ### NOTE: I change the following function call depending on
             ### the model I am scoring.
             scores <- mcmapply(get_cvScore_kmp1p2, train_list, test_list,</pre>
                                 MoreArgs= list(wghts=wghts),
                                 SIMPLIFY= TRUE, mc.cores=5)
             # For the current seed, store the average of the Type2
             # scores, the average taken over the folds.
             df_scores[as.character(cur_seed), cur_row] <- round(mean(scores), 5)</pre>
        } # end of for-loop, index i
    } ## end of for-loop, index h
    # Compute the average over the seeds of the Type2 scores
    # obtained for each set of parameters in df_params.
    datout$Type2 <- round(apply(df_scores, MARGIN=2, mean), 5)</pre>
    return(datout)
}
```

In []:

Section 1: Get non-k-means models for comparison

I consider four types of model: random forest, logistic, support vector, and gradient boosting. For each of these types, I do not need to find the best possible model because these models are used only for comparing scores to the hybrid k-means model we will construct, and the latter is constructed from two of the four non-k-means models. The better the prob01 and prob02 inputs to the hybrid k-means model, the better the scores will be for this model.

Find a "best" random forest model

Variable selection for the random forest model

```
In [45]: set.seed(123)
         rfclf <- randomForest(I(as.factor(Inland)) ~ ., data= traindat,</pre>
                                ntree= 900, mtry= 1, nodesize= 2,
                                importance=TRUE)
         print(rfclf)
         print(get_fscore(as.matrix(rfclf$confusion)))
         # [1] 0.7824
          randomForest(formula = I(as.factor(Inland)) \sim ., data = traindat, ntree = 900, mtry = 1000
         1, nodesize = 2, importance = TRUE)
                        Type of random forest: classification
                               Number of trees: 900
         No. of variables tried at each split: 1
                 00B estimate of error rate: 13.09%
         Confusion matrix:
                  1 class.error
              0
         0 6720 591
                        0.080837
         1 797 2495
                         0.242102
         [1] 0.7824
In [46]: print(round(rfclf$importance, 3))
                                       1 MeanDecreaseAccuracy MeanDecreaseGini
         housing_median_age 0.022 0.047
                                                        0.030
                                                                         576.37
                     0.013 0.006
                                                        0.011
                                                                         569.99
         households
         median_house_value 0.152 0.302
                                                        0.198
                                                                        2264.78
         rooms_per_hh
                            0.044 0.070
                                                        0.052
                                                                        814.16
In [47]: # Remove rooms_per_hh. I am aiming for a model with an
         # accuracy <= 0.75. It is currently at 87%.</pre>
         newcols <- colnames(traindat)[which(!(colnames(traindat) %in%</pre>
                                                c("rooms_per_hh")))]
         df <- traindat[, newcols]</pre>
```

```
In [48]: set.seed(123)
         rfclf <- randomForest(I(as.factor(Inland)) ~ ., data= df,</pre>
                               ntree= 900, mtry= 1, nodesize= 2,
                                importance=TRUE)
         print(rfclf)
         print(get_fscore(as.matrix(rfclf$confusion)))
         # [1] 0.7234
         Call:
          randomForest(formula = I(as.factor(Inland)) \sim ., data = df, ntree = 900,
                                                                                          mtry = 1, no
         desize = 2, importance = TRUE)
                        Type of random forest: classification
                               Number of trees: 900
         No. of variables tried at each split: 1
                 00B estimate of error rate: 16.62%
         Confusion matrix:
                 1 class.error
              0
         0 6537 774
                        0.10587
         1 988 2304
                         0.30012
         [1] 0.7234
In [49]: print(round(rfclf$importance, 3))
                                      1 MeanDecreaseAccuracy MeanDecreaseGini
         housing_median_age 0.034 0.064
                                                        0.043
                                                                        727.05
                                                        0.010
                                                                         811.27
         households 0.014 0.003
         median_house_value 0.125 0.280
                                                        0.173
                                                                        2414.49
In [ ]: #&* Bookmark
In [52]: # Identify the columns we will use for modeling. I am also
         # removing households since accuracy is still around 83%.
         cols <- c('Inland','housing median age','median house value')</pre>
In [53]: # Restrict variables in traindat and testdat for random forest
         # modeling.
         traindat <- traindat[, cols]</pre>
         testdat <- testdat[, cols]</pre>
```

Tune the random forest model

```
# result <- round((0.4 * percent_correct + 0.6 * ans[[2]]), 4)
              return(percent correct)
In [37]: # Function to obtain a cross-validation score, averaging the
          # accuracy scores of the folds. This function is called from
          # avg seedScores rf.
          get cvScore rf <- function(seed, dat, ntrees, mtry,</pre>
                                       nodesize, folds= 5) {
              # divide dat by the number of folds
              segment_size <- round(dim(dat)[1]/folds)</pre>
              diff <- nrow(dat) - folds * segment_size</pre>
              last_seg_size <- segment_size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              # print(segmentsv)
              stopifnot(sum(segmentsv) == nrow(dat))
              # shuffle dat
              set.seed(seed)
              smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
              dat <- dat[smp,]</pre>
              # split the data into the folds
              row_list <- vector("list", length= folds)</pre>
              names(row_list) <- as.character(1:folds)</pre>
              startpt <- 1
              for(i in 1:folds) {
                   endpt <- startpt + segmentsv[i] - 1</pre>
                   stopifnot(endpt <= dim(dat)[1])</pre>
                   row_list[[i]] <- rownames(dat)[startpt:endpt]</pre>
                  startpt <- endpt + 1</pre>
              }
              train_list <- test_list <- vector("list", length= folds)</pre>
              for(j in 1:folds) \overline{\{}
                  testdat <- dat[row list[[j]],]</pre>
                   traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                  stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == dim(dat)[1])
                  test_list[[j]] <- testdat</pre>
                  train_list[[j]] <- traindat</pre>
              }
              scores <- mcmapply(get_acc_rf, train_list, test_list,</pre>
                                   MoreArgs= list(ntrees= ntrees, mtry=mtry,
                                                   nodesize=nodesize),
                                   SIMPLIFY= TRUE, mc.cores=5)
              # The average is of accuracy scores.
              return(round(mean(scores), 5))
In [38]: # Since the seed value can have a big effect on the results,
```

```
In [39]: # This grid search is specific to finding the best random forest
          # classifier for traindat.
          gridSearch02 <- function(seed_vector, traindat, ntree_vector,</pre>
                                     mtry_vector, nodesizes, folds=5) {
              tree_len <- length(ntree_vector)</pre>
              mtry len <- length(mtry vector)</pre>
              node len <- length(nodesizes)</pre>
              # We need to capture the gridSearch parameters as well as
              # the cross-val scores.
              datout <- rep(NA, 2 * tree_len * mtry_len * node_len)</pre>
              dim(datout) <- c((tree_len * mtry_len * node_len), 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("params", "Acc")</pre>
              datout$params <- ""
              index <- 0
              for(i in 1:tree_len) {
                  n_trees <- ntree_vector[i]</pre>
                  for(j in 1:mtry_len) {
                      mtry <- mtry_vector[j]</pre>
                       for(k in 1:node len) {
                           index <- index + 1
                           nodesize <- nodesizes[k]</pre>
                           param_string <- paste(as.character(n_trees),</pre>
                                                   as.character(mtry),
                                                   as.character(nodesize), sep= "--")
                           datout$params[index] <- param_string</pre>
                           datout$Acc[index] <- avg_seedScores_rf(seed_vector, traindat, n_trees,</pre>
                                                                      folds=folds, mtry=mtry,
                                                                      nodesize=nodesize)
                       }
                  }
              }
              return(datout)
In [54]: # Run grid search to get better parameters for the
          # random forest model. Test with 10 seeds. For each
          # seed, an average is taken over 5 folds.
```

```
# Run grid search to get better parameters for the
# random forest model. Test with 10 seeds. For each
# seed, an average is taken over 5 folds.

set.seed(7543)
seed_smp <- sample(1:9999, 10, replace=FALSE)
tree_vector <- c(500, 900, 1200)
mtry_vector <- c(1)
node_vector <- c(1, 2, 3)

start <- Sys.time()
paste("Start time: ", start, sep="")
ans <- gridSearch02(seed_smp, traindat, tree_vector, mtry_vector, node_vector)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 6 mins

(best_params <- ans[which(ans$Acc == max(ans$Acc)),]$params)
# '1200--1--3'
(best_rf_Acc <- ans[which(ans$Acc == max(ans$Acc)),]$Acc)
# 0.8317

'Start time: 2021-07-27 13:40:24'</pre>
```

'Start time: 2021-07-27 13:40:24'

Time difference of 6.13 mins
'1200--1--3'

0.83172

```
In [55]: # I have a model with an accuracy score over 75%. Since
# I do not need a perfect model, I will choose the
# 500--1--3 model with an accuracy of 0.8311. This will
# allow for faster testing than if I used the 1200 tree
# model.
ans
```

 params
 Acc

 <chr>
 <dbl>

 500--1--1
 0.82982

 500--1--2
 0.83084

 500--1--3
 0.83109

 900--1--1
 0.83073

 900--1--2
 0.83073

 900--1--3
 0.83118

 1200--1--1
 0.82997

 1200--1--2
 0.83123

 1200--1--3
 0.83172

A data.frame: 9 x 2

Get scores for rfclf_best on traindat

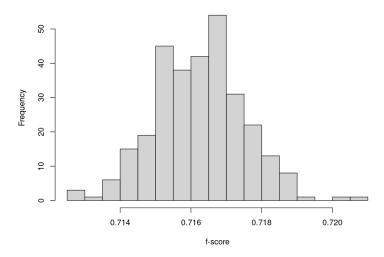
```
In [62]: # Get stable scores for the best random forest model. I will
          # refer to this model as rfclf best. Note that 300 seeds
          # are being used.
          set.seed(1433)
          seed_smp <- sample(1:9999, 300, replace=FALSE)</pre>
          datout <- rep(NA, 6 * length(seed_smp))</pre>
          dim(datout) <- c(length(seed smp), 6)</pre>
          datout <- as.data.frame(datout)</pre>
          colnames(datout) <- c("seed", "fscore", "Acc", "Type2", "FN", "FP")</pre>
          datout$seed <- seed_smp</pre>
          start <- Sys.time()</pre>
          paste0("Start time: ", start)
          for(i in 1:length(seed_smp)) {
              set.seed(seed smp[i])
              rfmod <- randomForest(I(as.factor(Inland)) ~ .,</pre>
                                            data= traindat, ntree=500,
                                            mtry= 1, nodesize= 3)
              # preds <- predict(rfmod, newdata= dat, type="response")</pre>
              # ans <- get confusion(preds, dat[, "Outcome", drop=FALSE])</pre>
              # mat <- as.matrix(ans[[1]])</pre>
              mat <- rfmod$confusion</pre>
              # percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
              # datout[i, c("Acc")] <- round(percent_correct, 4)</pre>
              datout[i, c("Acc")] <- acc <- round(1-median(rfmod$err.rate[,1]), 4)</pre>
              # datout[i, c("fscore")] <- round(ans[[2]], 4)</pre>
              datout[i, c("fscore")] <- fscore <- round(get fscore(mat), 4)</pre>
              datout[i, c("Type2")] \leftarrow round(0.4*acc + 0.6*fscore, 4)
              datout[i, c("FN")] <- as.numeric(mat[2,1])</pre>
              datout[i, c("FP")] <- as.numeric(mat[1,2])</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
```

```
# Time difference of 10 mins
```

'Start time: 2021-07-27 14:09:17'

Time difference of 10.08 mins

Distribution of f-scores for rfclf_best on traindat

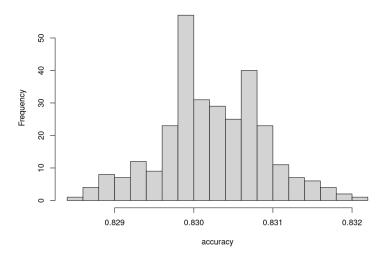


 $0.7163 \cdot 0.8303 \cdot 1025.15 \cdot 770.67$

```
In [65]: round(mean(datout$Type2), 4)
# 0.7619
```

0.7619

Distribution of accuracy scores for rfclf_best on traindat

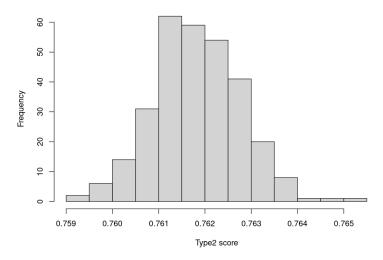


```
In [67]: # Identify seeds with an accuracy score between 0.8295
         # and 0.8310. When constructing rfclf_best, I will
         # use a seed which has an accuracy in the center of
         # the distribution of accuracy scores. (It may be that
         # rfclf_best will generalize better to the test data if
         # I choose a seed for it that is at the midpoint of the
         # accuracy distribution.)
         rf\_candidate\_seeds <- \ datout[which((datout\$Acc > 0.8295) \& (datout\$Acc < 0.8310)),]\$seed
         length(rf_candidate_seeds)
         # 226
         head(rf_candidate_seeds)
            9728
                  5605
                         5552
                                 3837
                                        2343
                                               1219
```

 $9728 \cdot 5605 \cdot 5552 \cdot 3837 \cdot 2343 \cdot 1219$

226

Distribution of Type2 scores for rfclf_best on traindat



```
In [70]: # Get representative model.
         set.seed(5552)
         (rfclf best <- randomForest(I(as.factor(Inland)) ~ .,</pre>
                                      data= traindat, ntree=500,
                                      mtry= 1, nodesize= 3, importance=TRUE))
          randomForest(formula = I(as.factor(Inland)) ~ ., data = traindat,
                                                                                   ntree = 500, mtry =
         1, nodesize = 3, importance = TRUE)
                        Type of random forest: classification
                               Number of trees: 500
         No. of variables tried at each split: 1
                 00B estimate of error rate: 16.87%
         Confusion matrix:
              0
                   1 class.error
         0 6544 767
                         0.10491
         1 1022 2270
                         0.31045
In [71]: print(round(rfclf best$importance, 3))
                                       1 MeanDecreaseAccuracy MeanDecreaseGini
```

Get comparative scores for rfclf_best on testdat

housing median age 0.028 0.075

median_house_value 0.136 0.314

```
In [74]: # Function for obtaining a set of scores on the testset data
# using rfclf_best as the classifier.

get_testdatScores_rf <- function(seedv, dat) {

    seedv_len <- length(seedv)
    datout <- rep(NA, 5 * seedv_len)
    dim(datout) <- c(seedv_len, 5)
    datout <- as.data.frame(datout)
    colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")
    rownames(datout) <- as.character(seedv)</pre>
```

0.043

0.191

672.46

2570.13

```
for(h in 1:seedv_len) {
                   # shuffle dat
                   cur seed <- seedv[h]</pre>
                   set.seed(cur_seed)
                   # It is expected that dat is testdat, which has 10K rcds
                   smp <- sample(rownames(dat), 4000, replace= FALSE)</pre>
                   df <- dat[smp,]</pre>
                   preds <- predict(rfclf_best, newdata= df, type="response")</pre>
                   ans <- get_confusion(preds, df[, "Inland", drop=FALSE])</pre>
                   mat <- as.matrix(ans[[1]])</pre>
                   fscore <- round(as.numeric(ans[[2]]), 4)</pre>
                   acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
                   type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
                   FN <- as.numeric(mat[2,1])</pre>
                   FP <- as.numeric(mat[1,2])</pre>
                   datout[as.character(cur_seed), 1:5] <- c(fscore,acc,type2,FN,FP)</pre>
              return(datout)
          }
In [75]: # Get rfclf_best's scores on the testset data. For each of
          # the 250 seeds, I sample 4K (no replacement) from the 10K
          # set of testdat records.
          set.seed(1821)
          seed_vector <- sample(1:9999, 250, replace=FALSE)</pre>
          start <- Sys.time()</pre>
          paste0("Start time: ", start)
          dat_result <- get_testdatScores_rf(seed_vector, testdat)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 44 secs
          'Start time: 2021-07-27 14:35:26'
          Time difference of 43.34 secs
In [76]: dim(dat result)
          head(dat_result)
           250 . 5
          A data.frame: 6 x 5
                                      FN
                                            FP
                fscore
                         Acc Type2
                 <dbl>
                            <dbl> <dbl> <dbl>
                      <dbl>
           5934 0.7144 0.8225 0.7576
                                     383
                                           327
           1953 0.7089 0.8198 0.7533
                                           309
                                     412
           7591 0.7083 0.8180 0.7522
                                     397
                                           331
           1038 0.7131 0.8238 0.7574
                                     376
                                           329
             49 0.7106 0.8168 0.7531
                                     428
                                           305
           3203 0.7212 0.8245 0.7625
                                     415
                                           287
In [77]: | fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          paste0("fscore StdDev: ", as.character(fscore sd))
          # 0.0075
```

```
summary(dat_result$fscore)
         'fscore mean: 0.7156'
          'fscore StdDev: 0.0075'
            Min. 1st Qu. Median
                                    Mean 3rd Qu.
                                                       Max.
            0.692 0.711 0.715
                                     0.716 0.721
                                                      0.738
In [78]: | Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
         Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
         paste0("accuracy mean: ", as.character(Acc_mean))
         paste0("accuracy StdDev: ", as.character(Acc_sd))
         # 0.0045
         summary(dat_result$Acc)
         'accuracy mean: 0.8228'
         'accuracy StdDev: 0.0045'
            Min. 1st Qu. Median
                                      Mean 3rd Qu.
                                                       Max.
            0.812 0.820
                           0.823
                                     0.823 0.826
                                                      0.835
In [79]: Type2 mean <- round(mean(dat result$Type2), 4)</pre>
         Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
         paste0("Type2 mean: ", as.character(Type2_mean))
         paste0("Type2 StdDev: ", as.character(Type2 sd))
         # 0.0061
         summary(dat_result$Type2)
          'Type2 mean: 0.7585'
          'Type2 StdDev: 0.0061'
            Min. 1st Qu. Median
                                     Mean 3rd Qu.
                                                       Max.
            0.740 0.755
                            0.758
                                     0.758 0.762
                                                      0.776
In [80]: FN_mean <- round(mean(dat_result$FN), 2)</pre>
         FN_sd <- round(sd(dat_result$FN), 2)</pre>
         paste0("FN mean: ", as.character(FN_mean))
         paste0("FN StdDev: ", as.character(FN_sd))
         # 14.48
         summary(dat_result$FN)
         'FN mean: 403.8'
         'FN StdDev: 14.48'
             Min. 1st Qu. Median
                                      Mean 3rd Qu.
                                                       Max.
              362
                      395
                               404
                                       404
                                               414
                                                        448
In [81]: FP mean <- round(mean(dat result$FP), 2)</pre>
         FP_sd <- round(sd(dat_result$FP), 2)</pre>
         paste0("FP mean: ", as.character(FP_mean))
         paste0("FP StdDev: ", as.character(FP_sd))
```

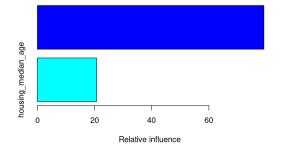
```
# 12.4
summary(dat_result$FP)
'FP mean: 304.86'
'FP StdDev: 12.4'
"

Min. 1st Qu. Median Mean 3rd Qu. Max.
269 296 305 305 313 336
```

Find best gradient boosting model

A data.frame: 2×2

	var	rel.inf
	<chr></chr>	<dbl></dbl>
median_house_value	median_house_value	79.262
housing_median_age	housing_median_age	20.738



```
In [73]: preds <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
          preds_transf <- preds</pre>
          names(preds_transf) <- rownames(traindat)</pre>
          preds_transf[which(preds_transf >= 0.5)] <- 1
preds_transf[which(preds_transf < 0.5)] <- 0</pre>
          preds_transf <- as.factor(preds_transf)</pre>
          ans <- get_confusion(preds_transf, traindat[, "Inland", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for gbmod: ", as.character(ans[[2]]), sep=""))
          # 0.7292
          # Accuracy is 0.8450
          # Type2 is 0.7755
                      1 class.error
          0 6748 563
                           0.0770
           1 1080 2212
                              0.3281
           [1] "f-score for gbmod: 0.7292"
```

Tune the gradient boosting model

```
In [85]: # Function to obtain a cross-validation score, averaging the
          # accuracy scores of the folds. This function is called from
         # avg seedScores gb.
         get_cvScore_gb <- function(seed, dat, ntrees, shrinkage,</pre>
                                       folds= 5) {
              # divide dat by the number of folds
              segment size <- round(dim(dat)[1]/folds)</pre>
              diff <- nrow(dat) - folds * segment_size</pre>
              last_seg_size <- segment_size + diff</pre>
              segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
              stopifnot(sum(segmentsv) == nrow(dat))
              # shuffle dat
              set.seed(seed)
              smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
              dat <- dat[smp,]</pre>
              # split the data into the folds
```

```
row_list <- vector("list", length= folds)</pre>
names(row list) <- as.character(1:folds)</pre>
startpt <- 1
for(i in 1:folds) {
    endpt <- startpt + segmentsv[i] - 1</pre>
    stopifnot(endpt <= dim(dat)[1])</pre>
    row list[[i]] <- rownames(dat)[startpt:endpt]</pre>
    startpt <- endpt + 1
}
train_list <- test_list <- vector("list", length= folds)</pre>
for(j in 1:folds) {
    testdat <- dat[row_list[[j]],]</pre>
    traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
    stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == dim(dat)[1])
    test_list[[j]] <- testdat</pre>
    train_list[[j]] <- traindat</pre>
}
scores <- mcmapply(get_acc_gb, train_list, test_list,</pre>
                     MoreArgs= list(ntrees= ntrees, shrinkage=shrinkage),
                     SIMPLIFY= TRUE, mc.cores=5)
# The average is of Type2 scores.
return(round(mean(scores), 5))
```

```
In [87]: # This grid search is specific to finding the best gradient boosting
          # classifier for traindat.
          gridSearch03 <- function(seed_vector, traindat, ntree_vector,</pre>
                                      shrinkagev, folds=5) {
              tree len <- length(ntree vector)</pre>
              shrink_len <- length(shrinkagev)</pre>
              # We need to capture the gridSearch parameters as well as
              # the cross-val scores.
              datout <- rep(NA, 2 * tree_len * shrink_len)</pre>
              dim(datout) <- c((tree_len * shrink_len ), 2)</pre>
              datout <- as.data.frame(datout)</pre>
              colnames(datout) <- c("params", "Acc")</pre>
              datout$params <- ""
              index <- 0
              for(i in 1:tree_len) {
                   n_trees <- ntree_vector[i]</pre>
                   for(j in 1:shrink_len) {
                       shrinkage <- shrinkagev[j]</pre>
                       index \leftarrow index + 1
                       param_string <- paste(as.character(n_trees),</pre>
                                                as.character(shrinkage), sep= "--")
                            datout$params[index] <- param_string</pre>
```

folds=folds, shrinkage=shrinkage)

datout\$Acc[index] <- avg_seedScores_gb(seed_vector, traindat, n_trees,</pre>

```
}
              }
              return(datout)
          }
In [88]: # Run grid search to get better parameters for the
          # gradient boosting model. Test with 21 seeds. For
          # each seed, an average is taken over 5 folds.
          set.seed(7543)
          seed_smp <- sample(1:9999, 21, replace=FALSE)</pre>
          tree vector \leftarrow c(500, 750, 900)
          shrinkage_v \leftarrow c(0.05, 0.08, 0.1, 0.15, 0.2)
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          ans <- gridSearch03(seed_smp, traindat, tree_vector, shrinkage_v)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 4 mins
          (best_params <- ans[which(ans$Acc == max(ans$Acc)),]$params)</pre>
          # '900--0.05'
          (best rf_Acc <- ans[which(ans$Acc == max(ans$Acc)),]$Acc)</pre>
          # 0.8412
          'Start time: 2021-07-27 14:43:23'
          Time difference of 3.94 mins
          '900--0.05'
          0.84119
In [89]: # Refine the search.
          set.seed(7541)
          seed smp <- sample(1:9999, 21, replace=FALSE)</pre>
          tree vector \leftarrow c(900, 1100, 1300)
          shrinkage_v \leftarrow c(0.01, 0.03, 0.05)
          start <- Sys.time()</pre>
          paste("Start time: ", start, sep="")
          ans <- gridSearch03(seed_smp, traindat, tree_vector, shrinkage_v)</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 3.5 mins
          (best_params <- ans[which(ans$Acc == max(ans$Acc)),]$params)</pre>
          # '1100--0.03'
          (best rf Acc <- ans[which(ans$Acc == max(ans$Acc)),]$Acc)</pre>
          # 0.8409
          'Start time: 2021-07-27 14:50:28'
          Time difference of 3.44 mins
          '1100--0.03'
          0.84094
In [90]: # We might as well choose 900--0.05 since
          # has a nearly equal score.
```

ans

Get scores for gbclf_best on traindat

```
In [94]: # Get stable scores for the best gradient boosting model.
          # I will refer to this model as gbclf_best. Note that
          # 300 seeds are being used.
          set.seed(1433)
          seed_smp <- sample(1:9999, 300, replace=FALSE)</pre>
          datout <- rep(NA, 6 * length(seed smp))</pre>
          dim(datout) <- c(length(seed smp), 6)</pre>
          datout <- as.data.frame(datout)</pre>
          colnames(datout) <- c("seed", "fscore", "Acc", "Type2", "FN", "FP")</pre>
          datout$seed <- seed_smp</pre>
          start <- Sys.time()</pre>
          for(i in 1:length(seed_smp)) {
              set.seed(seed_smp[i])
              gbmod <- gbm(Inland ~ ., data= traindat, n.trees=900,</pre>
                              distribution= "bernoulli", shrinkage=0.05)
              preds <- suppressMessages(predict(gbmod, newdata= traindat, type="response"))</pre>
              names(preds) <- rownames(traindat)</pre>
              preds[which(preds >= 0.5)] <- 1
              preds[which(preds < 0.5)] <- 0</pre>
              preds <- as.factor(preds)</pre>
              ans <- get_confusion(preds, traindat[, "Inland", drop=FALSE])</pre>
              mat <- as.matrix(ans[[1]])</pre>
              percent_correct <- sum(diag(mat))/floor(sum(mat))</pre>
              datout[i, c("Acc")] <- acc <- round(percent_correct, 4)</pre>
              datout[i, c("fscore")] <- fscore <- round(ans[[2]], 4)</pre>
              datout[i, c("Type2")] \leftarrow round(0.4*acc + 0.6*fscore, 4)
              datout[i, c("FN")] <- as.numeric(mat[2,1])</pre>
              datout[i, c("FP")] <- as.numeric(mat[1,2])</pre>
          stop <- Sys.time()</pre>
          round(stop - start, 2)
          # Time difference of 5 mins
```

Time difference of 5.01 mins

```
In [95]: options(repr.plot.width= 8, repr.plot.height= 6)
hist(datout$fscore, breaks=12, xlab="f-score",
```

main="Distribution of f-scores for gbclf_best on traindat")

Distribution of f-scores for gbclf_best on traindat

Frequency 10 20 30 40 50 60

0.728

f-score

0.731

0.732

In [97]: round(mean(datout\$Type2), 4)
0.7749

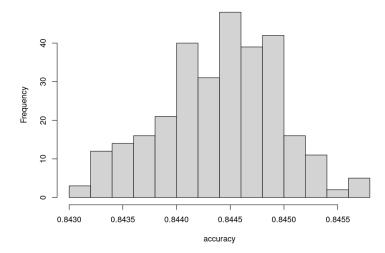
0.7749

0.725

0.726

0.727

Distribution of accuracy scores for gbclf_best on traindat

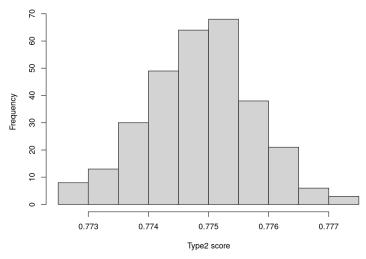


```
In [99]: # Identify seeds with an accuracy score between 0.8442
         # and 0.8447. When constructing gbclf_best, I will
         # use a seed which has an accuracy in the center of
         # the distribution of accuracy scores. (It may be that
         # gbclf_best will generalize better to the test data if
         # I choose a seed for it that is at the midpoint of the
         # accuracy distribution.)
         gb\_candidate\_seeds <- datout[which((datout\$Acc > 0.8442) \& (datout\$Acc < 0.8447)),]\$seed
         length(gb_candidate_seeds)
         head(gb_candidate_seeds)
           9728
                  3837
                         2551
                                 1465
                                        6565
                                               7097
```

9728 · 3837 · 2551 · 1465 · 6565 · 7097

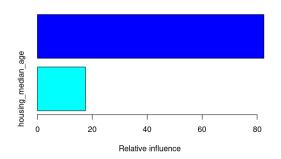
79

Distribution of Type2 scores for gbclf_best on traindat



A data.frame: 2 × 2

	var	rel.inf
	<chr></chr>	<dbl></dbl>
median_house_value	median_house_value	82.489
housing_median_age	housing_median_age	17.511



Get comparative scores for gbclf_best on testdat

```
seedv_len <- length(seedv)</pre>
               datout <- rep(NA, 5 * seedv_len)</pre>
               dim(datout) <- c(seedv_len, 5)</pre>
               datout <- as.data.frame(datout)</pre>
               colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")</pre>
                rownames(datout) <- as.character(seedv)</pre>
               for(h in 1:seedv_len) {
                    # shuffle dat
                    cur_seed <- seedv[h]</pre>
                    set.seed(cur_seed)
                    # It is expected that dat is testdat, which has 10K rcds
                    smp <- sample(rownames(dat), 4000, replace= FALSE)</pre>
                    df <- dat[smp,]</pre>
                    preds <- suppressMessages(predict(gbclf_best, newdata= df, type="response"))</pre>
                    names(preds) <- rownames(df)</pre>
                    preds[which(preds >= 0.5)] <- 1
                    preds[which(preds < 0.5)] <- 0
                    preds <- as.factor(preds)</pre>
                    ans <- get_confusion(preds, df[, "Inland", drop=FALSE])</pre>
                    mat <- as.matrix(ans[[1]])</pre>
                    fscore <- round(as.numeric(ans[[2]]), 4)</pre>
                    acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
                    type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
                    FN <- as.numeric(mat[2,1])</pre>
                    FP <- as.numeric(mat[1,2])</pre>
                    datout[as.character(cur seed), 1:5] <- c(fscore,acc,type2,FN,FP)</pre>
               return(datout)
In [104]: # Get gbclf_best's scores on the testset data. For each of
           # the 250 seeds, I sample 4K (no replacement) from the 10K
           # set of testdat records.
           set.seed(1821)
           seed_vector <- sample(1:9999, 250, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           dat_result <- get_testdatScores_gb(seed_vector, testdat)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 11.4 secs
           'Start time: 2021-07-27 15:13:26'
           Time difference of 11.43 secs
In [105]:
           dim(dat result)
           head(dat_result)
            250 . 5
           A data.frame: 6 x 5
                                             FΡ
                 fscore
                          Acc Type2
                                       FN
                  <dbl>
                        <dbl>
                               <dbl> <dbl>
                                          <dbl>
            5934 0.7220 0.8332 0.7665
                                      405
                                            262
```

1953 0.7087 0.8258 0.7555

7591 0.7230 0.8335 0.7672

1038 0.7200 0.8330 0.7652

49 0.7097 0.8212 0.7543

442

412

393

454

255

254

275

261

```
In [106]: | fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0077
          summary(dat_result$fscore)
          'fscore mean: 0.7183'
          'fscore StdDev: 0.0077'
             Min. 1st Qu. Median
                                     Mean 3rd Qu.
                                                        Max.
            0.694 0.713
                             0.719
                                      0.718
                                             0.723
                                                       0.744
In [107]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0044
          summary(dat_result$Acc)
          'accuracy mean: 0.8304'
          'accuracy StdDev: 0.0044'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
             0.820
                     0.828
                             0.831
                                      0.830
                                              0.833
                                                       0.842
In [108]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          paste0("Type2 StdDev: ", as.character(Type2_sd))
          # 0.0061
          summary(dat_result$Type2)
           'Type2 mean: 0.7632'
           'Type2 StdDev: 0.0061'
             Min. 1st Qu. Median
                                     Mean 3rd Qu.
                                                        Max.
            0.745 0.759 0.763 0.763 0.767
                                                       0.782
```

```
In [109]: FN_mean <- round(mean(dat_result$FN), 2)</pre>
          FN_sd <- round(sd(dat_result$FN), 2)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          paste0("FN StdDev: ", as.character(FN sd))
          summary(dat_result$FN)
          'FN mean: 430.03'
          'FN StdDev: 14.69'
             Min. 1st Qu. Median Mean 3rd Qu.
                                                       Max.
                      421
                             430
                                       430
                                               441
                                                        464
In [110]: FP_mean <- round(mean(dat_result$FP), 2)</pre>
          FP_sd <- round(sd(dat_result$FP), 2)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          # 248.52
          paste0("FP StdDev: ", as.character(FP_sd))
          # 11.69
          summary(dat_result$FP)
          'FP mean: 248.52'
          'FP StdDev: 11.69'
             Min. 1st Qu. Median Mean 3rd Qu.
                                                       Max.
              211
                      240 249
                                       249 256
                                                        275
  In [ ]: ### COMMENT:
          # gbclf_best has slightly better scores than rfclf_best.
```

Find best logistic regression model

In [114]: f01 <- glm(Inland ~ ., data=traindat, family=binomial())

```
summary(f01)
get_RsqrdDev(f01)
Call:
glm(formula = Inland ~ ., family = binomial(), data = traindat)
Deviance Residuals:
  Min
        1Q Median
                          30
                                  Max
-2.370 -0.691 -0.250
                      0.697
                                4.884
Coefficients:
                   Estimate Std. Error z value Pr(>|z|)
                                       38.6 <2e-16
(Intercept)
                   4.04e+00 1.05e-01
housing_median_age -5.53e-02
                              2.22e-03
                                        -24.9
                                                <2e-16
median_house_value -1.97e-05 4.60e-07
                                       -42.8
                                                <2e-16
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 13137 on 10602 degrees of freedom
Residual deviance: 8927 on 10600 degrees of freedom
AIC: 8933
Number of Fisher Scoring iterations: 6
```

0.4613

```
In [112]: # Add power transformation.
          f02 <- glm(Inland ~ housing_median_age +</pre>
                     I(log(median_house_value)),
                     data=df, family=binomial())
          summary(f02)
          get_RsqrdDev(f02)
          Call:
          glm(formula = Inland ~ housing_median_age + I(log(median_house_value)),
              family = binomial(), data = df)
          Deviance Residuals:
             Min
                     1Q Median
                                      30
                                             Max
                                   0.533
          -3.268 -0.619 -0.286
                                           3.661
          Coefficients:
                                     Estimate Std. Error z value Pr(>|z|)
          (Intercept)
                                     41.10321
                                                 0.86028
                                                            47.8
                                                                   <2e-16
          housing_median_age
                                     -0.06155
                                                 0.00235
                                                           -26.2
                                                                   <2e-16
          I(log(median_house_value)) -3.36644
                                                 0.07061
                                                          -47.7
                                                                   <2e-16
          (Dispersion parameter for binomial family taken to be 1)
              Null deviance: 13137 on 10602 degrees of freedom
          Residual deviance: 8376 on 10600 degrees of freedom
          AIC: 8382
          Number of Fisher Scoring iterations: 6
          0.5093
```

```
In [126]: # Tweak power transformation.
          f03 <- glm(Inland ~ I(housing_median_age^0.6) +</pre>
                     I(median_house_value^-0.08),
                     data=df, family=binomial())
          summary(f03)
          get_RsqrdDev(f03)
          glm(formula = Inland ~ I(housing_median_age^0.6) + I(median_house_value^-0.08),
              family = binomial(), data = df)
          Deviance Residuals:
                    1Q Median
                                      3Q
          -3.406 -0.612 -0.290
                                   0.517
                                           3.575
          Coefficients:
                                      Estimate Std. Error z value Pr(>|z|)
          (Intercept)
                                      -40.3261
                                                0.8587 -47.0
                                                                    <2e-16
                                       -0.3717
                                                   0.0138
                                                             -26.9
          I(housing_median_age^0.6)
                                                                     <2e-16
          I(median_house_value^-0.08) 109.5732
                                                   2.2850
                                                             48.0
                                                                    <2e-16
          (Dispersion parameter for binomial family taken to be 1)
              Null deviance: 13136.8 on 10602 degrees of freedom
          Residual deviance: 8334.4 on 10600 degrees of freedom
          AIC: 8340
          Number of Fisher Scoring iterations: 5
          0.5128
          f03 model diagnostics
In [127]: # Check for dispersion <> 1.
          # We want the following value to NOT be considerably larger
          # than 1. If it is, then we have to use family= quasibinomial
          # in our modeling. (See p.311 of Kabacoff's "R in Action".)
          phi <- deviance(f03)/df.residual(f03)</pre>
          print(round(phi, 3))
          [1] 0.786
 In [ ]: ### COMMENT:
          # The f03 model has dispersion < 1. This under-
          # dispersion does not affect the parameter estimates.
          # But it means that the standard error estimates for
```

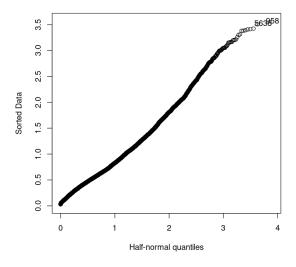
our model coefficients, as seen in the above summary,

are larger than what they should be.

```
In [128]: # Plot the residuals. Julian Faraway's half-normal plot can
# be used to check for outliers. See p.46 of Faraway's
# "Extending the Linear Model with R". The residuals plotted
# here are the deviance residuals.

options(repr.plot.width= 6, repr.plot.height= 6)

# Function halfnorm is from package faraway.
halfnorm(residuals(f03))
```



```
In [ ]: ### COMMENT:
     # The diagnostics look ok for our purposes.
```

Get comparative scores for f03 on testdat

```
In [129]: # Function for obtaining a set of scores on the testset data
            # using f03 as the classifier.
           get_testdatScores_f03 <- function(seedv, dat) {</pre>
                seedv_len <- length(seedv)</pre>
                datout <- rep(NA, 5 * seedv_len)</pre>
                dim(datout) <- c(seedv_len, 5)</pre>
                datout <- as.data.frame(datout)</pre>
                colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")
rownames(datout) <- as.character(seedv)</pre>
                for(h in 1:seedv_len) {
                     # shuffle dat
                     cur seed <- seedv[h]</pre>
                     set.seed(cur_seed)
                     # It is expected that dat is testdat, which has 10K rcds
                     smp <- sample(rownames(dat), 4000, replace= FALSE)</pre>
                     df <- dat[smp,]</pre>
                     preds <- predict(f03, newdata= df)</pre>
                     names(preds) <- rownames(df)</pre>
                     preds[which(preds >= 0.5)] <- 1
                     preds[which(preds < 0.5)] <- 0
                     preds <- as.factor(preds)</pre>
                     ans <- get_confusion(preds, df[, "Inland", drop=FALSE])</pre>
                     mat <- as.matrix(ans[[1]])</pre>
```

```
fscore <- round(as.numeric(ans[[2]]), 4)</pre>
                    acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
                    type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
                    FN <- as.numeric(mat[2,1])</pre>
                    FP <- as.numeric(mat[1,2])</pre>
                    datout[as.character(cur_seed), 1:5] <- c(fscore,acc,type2,FN,FP)</pre>
               return(datout)
In [130]: # Get f03's scores on the testset data. For each of
           # the 250 seeds, I sample 4K (no replacement) from the 10K
           # set of testdat records.
           set.seed(1821)
           seed_vector <- sample(1:9999, 250, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           # paste("Start time: ", start, sep="")
           dat_result <- get_testdatScores_f03(seed_vector, testdat)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 5 secs
           Time difference of 5.14 secs
In [131]: dim(dat_result)
           head(dat_result)
           250 · 5
           A data.frame: 6 × 5
                                      FΝ
                                            FP
                 fscore
                         Acc Type2
                 <dbl>
                              <dbl> <dbl> <dbl>
                        <dbl>
            5934 0.6742 0.8270 0.7353
                                      555
                                            137
            1953 0.6676 0.8208 0.7289
                                      570
                                            147
            7591 0.6828 0.8300 0.7417
                                      549
                                            131
            1038 0.6782 0.8285 0.7383
                                      529
                                            157
             49 0.6588 0.8130 0.7205
                                      606
                                            142
            3203 0.6676 0.8192 0.7282
                                      597
                                            126
In [132]: | fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
           fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
           paste0("fscore mean: ", as.character(fscore_mean))
           # 0.6704
           paste0("fscore StdDev: ", as.character(fscore sd))
           # 0.0090
           summary(dat_result$fscore)
           'fscore mean: 0.6704'
           'fscore StdDev: 0.009'
              Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                           Max.
             0.644
                    0.665
                              0.671
                                        0.670
                                               0.676
                                                          0.693
In [133]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
           Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
           paste0("accuracy mean: ", as.character(Acc_mean))
           # 0.8226
```

```
paste0("accuracy StdDev: ", as.character(Acc_sd))
          # 0.0046
          summary(dat_result$Acc)
           'accuracy mean: 0.8226'
           'accuracy StdDev: 0.0046'
              Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                         Max.
             0.810
                     0.819
                              0.823
                                       0.823
                                              0.826
                                                        0.836
In [134]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          # 0.7313
          paste0("Type2 StdDev: ", as.character(Type2_sd))
          # 0.0070
          summary(dat_result$Type2)
           'Type2 mean: 0.7313'
           'Type2 StdDev: 0.007'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                         Max.
             0.712
                    0.727
                              0.732
                                       0.731
                                              0.736
                                                        0.748
In [135]: FN_mean <- round(mean(dat_result$FN), 2)</pre>
          FN_sd <- round(sd(dat_result$FN), 2)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          # 574
          paste0("FN StdDev: ", as.character(FN_sd))
          # 17.1
          summary(dat_result$FN)
           'FN mean: 573.64'
           'FN StdDev: 17.08'
              Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                         Max.
               523
                       563
                                573
                                         574
                                                  585
                                                          617
In [136]: FP_mean <- round(mean(dat_result$FP), 2)</pre>
          FP_sd <- round(sd(dat_result$FP), 2)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          # 136
          paste0("FP StdDev: ", as.character(FP_sd))
          # 8.3
          summary(dat_result$FP)
           'FP mean: 136.04'
           'FP StdDev: 8.27'
              Min. 1st Qu. Median
                                        Mean 3rd Qu.
                                                         Max.
               114
                       131
                                136
                                         136
                                                  142
                                                          162
  In [ ]: | ### COMMENT:
          # f03 does a great job avoiding false positives.
```

```
# But it has a high number of false negatives.
# Overall, it is not as good a model as either
# rfclf_best or gbclf_best.
```

Find best SVM

```
In [138]: # We need to center and scale the data.
           svm_scaled <- scale(traindat[, -1])</pre>
           svm_centers <- attr(svm_scaled, "scaled:center")
svm_scales <- attr(svm_scaled, "scaled:scale")</pre>
           svm_scaled <- as.data.frame(cbind(as.numeric(traindat$Inland), svm_scaled),</pre>
                                            row.names=rownames(traindat))
           colnames(svm scaled) <- colnames(traindat)</pre>
In [140]: # Test out a support vector machine. Try kernel =
           # radial basis function.
           svm01 <- svm(I(as.factor(Inland)) ~ ., data=svm_scaled, kernel="radial",</pre>
                          gamma= 0.1, cost= 100, scale=FALSE)
           pred <- fitted(svm01)</pre>
           (ans <- table(pred, as.factor(svm_scaled$Inland)))</pre>
           get_fscore(as.matrix(ans))
               0 6777 1182
               1 534 2110
           0.7109
In [147]: # Function to compute an accuracy score for an svm cv-fold.
           get_acc_svm <- function(traindat, valdat, gamma, cost) {</pre>
                # traindat and valdat need to be scaled
                train_scaled <- scale(traindat[, -1])</pre>
                train_centers <- attr(train_scaled, "scaled:center")
train_scales <- attr(train_scaled, "scaled:scale")</pre>
                train_scaled <- as.data.frame(cbind(as.numeric(traindat$Inland), train_scaled),</pre>
                                                   row.names=rownames(traindat))
                colnames(train_scaled) <- colnames(traindat)</pre>
                svmmod <- svm(I(as.factor(Inland)) ~ ., data= train_scaled, gamma=gamma,</pre>
                                  cost=cost, scale=FALSE, kernel="radial")
                # Scale valdat.
                valdat scaled <- scale(valdat[, -1], center=train centers,</pre>
                                        scale=train_scales)
                valdat_scaled <- as.data.frame(valdat_scaled,</pre>
                                                    row.names=rownames(valdat),
                                                    col.names=colnames(valdat))
                preds <- predict(svmmod, newdata= valdat scaled)</pre>
                ans <- table(preds, as.factor(valdat$Inland))</pre>
                mat <- as.matrix(ans)</pre>
                mat[is.na(mat)] <- 0</pre>
                percent_correct <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
                # result <- round((0.4 * percent_correct + 0.6 * get_fscore(mat)), 4)</pre>
                return(percent correct)
           }
```

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In [145]: # This grid search searches for the best parameters for svm # modeling of the data. It takes a vector of seeds.

```
gridSearch svm <- function(seedv, dat, gammav, costv, folds=5) {</pre>
    gamma_len <- length(gammav)</pre>
    cost_len <- length(costv)</pre>
    # We need to capture the gridSearch parameters as well as
    # the cross-val scores.
    datout <- rep(NA, 2 * gamma_len * cost_len)</pre>
    dim(datout) <- c((gamma_len * cost_len), 2)</pre>
    datout <- as.data.frame(datout)</pre>
    colnames(datout) <- c("params", "Acc")</pre>
    datout$params <- ""
    # Divide dat by the number of folds to get a
    # size for each fold.
    segment_size <- round(nrow(dat)/folds)</pre>
    diff <- nrow(dat) - folds * segment_size</pre>
    last_seg_size <- segment_size + diff</pre>
    segmentsv <- c(rep(segment_size, (folds - 1)), last_seg_size)</pre>
    stopifnot(sum(segmentsv) == nrow(dat))
    index <- 0
    for(i in 1:gamma_len) {
         gamma <- gammav[i]</pre>
         for(j in 1:cost_len) {
             index \leftarrow index + 1
             cost <- costv[j]</pre>
             param_string <- paste(as.character(gamma),</pre>
                                     as.character(cost), sep= "--")
             datout$params[index] <- param_string</pre>
             # Each set of parameters gets tested over many folds.
             # The different folds are created using different seeds.
             # Create a vector to store the accuracy score for each seed.
             seedv len <- length(seedv)</pre>
             seed scores <- rep(NA, seedv len)
             for(h in 1:seedv_len) {
                 # shuffle dat
                 cur_seed <- seedv[h]</pre>
                 set.seed(cur seed)
                 smp <- sample(rownames(dat), nrow(dat), replace= FALSE)</pre>
                 dat <- dat[smp,]</pre>
                 # Each element of row_list will be the rows we pick
                 # out for one of the folds. E.g., the first element
                 # of row_list will contain the rows we want for the
                 # first fold, the second element of row list will
                 # contain the rows we want for the second fold, and
                 # so forth.
                 row_list <- vector("list", length=folds)</pre>
                 names(row_list) <- as.character(1:folds)</pre>
                 startpt <- 1
                 for(k in 1:folds) {
                      endpt <- startpt + segmentsv[k] - 1</pre>
                      stopifnot(endpt <= nrow(dat))</pre>
                      row_list[[k]] <- rownames(dat)[startpt:endpt]</pre>
                      startpt <- endpt + 1</pre>
                 }
                 train_list <- test_list <- vector("list", length= folds)</pre>
                 for(k in 1:folds) {
                      testdat <- dat[row_list[[k]],]</pre>
                      traindat <- dat[which(!(rownames(dat) %in% rownames(testdat))),]</pre>
                      stopifnot((length(rownames(traindat)) + length(rownames(testdat))) == nr
                      test_list[[k]] <- testdat</pre>
                      train_list[[k]] <- traindat</pre>
                 # When there are only 5 folds, only 5 cores get used.
```

```
In [149]: # Run grid search to get better parameters for the
           # svm classifier.
           set.seed(7543)
           seed_vector <- sample(1:9999, 5, replace=FALSE)</pre>
           gamma_v \leftarrow seq(0.02, 0.1, by=0.02)
           cost_v \leftarrow seq(50, 200, by=50)
           start <- Sys.time()</pre>
           paste("Start time: ", start, sep="")
           ans <- gridSearch svm(seed vector, traindat, gamma v, cost v)
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 5 mins (with 5 seeds)
           (best params <- ans[which(ans$Acc == max(ans$Acc)),]$params)</pre>
           # '0.02--50'
           (best_Acc <- ans[which(ans$Acc == max(ans$Acc)),]$Acc)</pre>
           # 0.8396
```

'Start time: 2021-07-27 15:52:54'

Time difference of 4.51 mins

'0.02--50'

0.83964

```
In [151]: # Refine the grid search.
          set.seed(7541)
          seed vector <- sample(1:9999, 21, replace=FALSE)</pre>
          gamma_v \leftarrow seq(0.01, 0.02, by=0.01)
          cost_v < - c(35, 50)
          start <- Sys.time()</pre>
          # paste("Start time: ", start, sep="")
          ans <- gridSearch svm(seed vector, traindat, gamma v, cost v)</pre>
          stop <- Sys.time()</pre>
           round(stop - start, 2)
          # Time difference of 3 mins (with 5 seeds)
           (best_params <- ans[which(ans$Acc == max(ans$Acc)),]$params)</pre>
          # '0.02--35'
           (best_Acc <- ans[which(ans$Acc == max(ans$Acc)),]$Acc)</pre>
           # 0.8399
           Time difference of 3.1 mins
           '0.02--35'
          0.83994
 In [ ]: #&* Bookmark
In [152]: # Construct an svm with the identified parameters.
          # We need to get probability estimates from the output.
          ## Note the use of svm_scaled (which is just svmtrain, scaled)
          svm02 <- svm(I(as.factor(Inland)) ~ ., data=svm_scaled, kernel="radial",</pre>
                          gamma=0.02, cost=35, scale=FALSE, probability=TRUE)
          pred <- fitted(svm02)</pre>
           (ans <- table(pred, as.factor(svm_scaled$Inland)))</pre>
          print(paste("f-score for 'best' svm classifier, trainset: "
                       as.character(get_fscore(as.matrix(ans))), sep=""))
          # 0.7236
          # Accuracy is 0.8400
          # Type2 is 0.7702
           pred
              0 6687 1072
              1 624 2220
           [1] "f-score for 'best' svm classifier, trainset: 0.7236"
```

Get comparative scores for svm02 on testdat

```
In [153]: # Function for obtaining a set of scores on the testset data
# using svm02 as the classifier.

get_testdatScores_svm02 <- function(seedv, dat) {

    seedv_len <- length(seedv)
    datout <- rep(NA, 5 * seedv_len)
    dim(datout) <- c(seedv_len, 5)
    datout <- as.data.frame(datout)
    colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")
    rownames(datout) <- as.character(seedv)</pre>
```

```
for(h in 1:seedv_len) {
         # shuffle dat
         cur_seed <- seedv[h]</pre>
         set.seed(cur_seed)
         # It is expected that dat is testdat, which has 10K rcds
         smp <- sample(rownames(dat), 4000, replace= FALSE)</pre>
         df <- dat[smp,]</pre>
         df_scaled <- scale(df[, -1], center=svm_centers,</pre>
                           scale=svm_scales)
         df_scaled <- as.data.frame(cbind(as.numeric(df$Inland),df_scaled),</pre>
                                       row.names=rownames(df))
         colnames(df_scaled) <- colnames(df)</pre>
         preds <- predict(svm02, newdata=df_scaled, scale=FALSE, probability=TRUE)</pre>
         preds_transf <- as.numeric(attr(preds, "probabilities")[, 2])</pre>
         names(preds transf) <- rownames(df)</pre>
         preds_transf[which(preds_transf >= 0.5)] <- 1</pre>
         preds_transf[which(preds_transf < 0.5)] <- 0</pre>
         preds_transf <- as.factor(preds_transf)</pre>
         ans <- get_confusion(preds_transf, df[, "Inland", drop=FALSE])</pre>
         mat <- as.matrix(ans[[1]])</pre>
         mat[is.na(mat)] <- 0</pre>
         fscore <- round(as.numeric(ans[[2]]), 4)</pre>
         acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
         type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
         FN <- as.numeric(mat[2,1])</pre>
         FP <- as.numeric(mat[1,2])</pre>
         datout[as.character(cur_seed), 1:5] <- c(fscore,acc,type2,FN,FP)</pre>
    return(datout)
}
```

```
In [154]: # Get svm02's scores on the testset data. For each of
# the 250 seeds, I sample 4K (no replacement) from the 10K
# set of testdat records.

set.seed(1821)
seed_vector <- sample(1:9999, 250, replace=FALSE)

start <- Sys.time()
# paste("Start time: ", start, sep="")
dat_result <- get_testdatScores_svm02(seed_vector, testdat)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 58 secs</pre>
```

Time difference of 57.92 secs

```
In [155]: dim(dat_result)
head(dat_result)
```

250 · 5

A data.frame: 6×5

	fscore	Acc	Type2	FN	FP
	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>	<dbl></dbl>
5934	0.7167	0.8310	0.7624	416	260
1953	0.7165	0.8295	0.7617	428	254
7591	0.7214	0.8338	0.7664	420	245
1038	0.7170	0.8315	0.7628	398	276
49	0.7091	0.8208	0.7538	454	263

```
In [156]: fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
          fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
          paste0("fscore mean: ", as.character(fscore_mean))
          paste0("fscore StdDev: ", as.character(fscore_sd))
          # 0.0078
          summary(dat_result$fscore)
           'fscore mean: 0.7175'
           'fscore StdDev: 0.0078'
              Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
             0.694
                    0.713
                             0.717
                                       0.718
                                             0.723
                                                        0.741
In [157]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          # 0.8306
          paste0("accuracy StdDev: ", as.character(Acc sd))
          # 0.0044
          summary(dat_result$Acc)
           'accuracy mean: 0.8306'
           'accuracy StdDev: 0.0044'
             Min. 1st Qu.
                            Median
                                       Mean 3rd Qu.
                                                        Max.
             0.819
                    0.828
                              0.831
                                       0.831
                                              0.834
                                                        0.842
In [158]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          # 0.7628
          paste0("Type2 StdDev: ", as.character(Type2_sd))
           # 0.0062
          summary(dat_result$Type2)
           'Type2 mean: 0.7628'
           'Type2 StdDev: 0.0062'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
             0.745
                   0.759
                             0.763
                                      0.763
                                             0.767
                                                        0.780
In [159]: FN_mean <- round(mean(dat_result$FN), 2)</pre>
          FN_sd <- round(sd(dat_result$FN), 2)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          paste0("FN StdDev: ", as.character(FN sd))
          summary(dat_result$FN)
          'FN mean: 434.43'
           'FN StdDev: 14.59'
```

```
Min. 1st Qu. Median
                                      Mean 3rd Qu.
                                                      Max.
              389
                     425
                              435
                                       434 444
                                                       474
In [160]: FP_mean <- round(mean(dat_result$FP), 2)</pre>
          FP_sd <- round(sd(dat_result$FP), 2)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          paste0("FP StdDev: ", as.character(FP_sd))
          # 11.1
          summary(dat_result$FP)
          'FP mean: 243.31'
          'FP StdDev: 11.14'
             Min. 1st Qu. Median Mean 3rd Qu.
                                                      Max.
              214
                      236
                            244
                                      243
                                                       276
 In [ ]: ### COMMENT:
          # svm02's performance is equal to that of gbclf_best.
 In [ ]:
```

Section 2: Model data with k-means

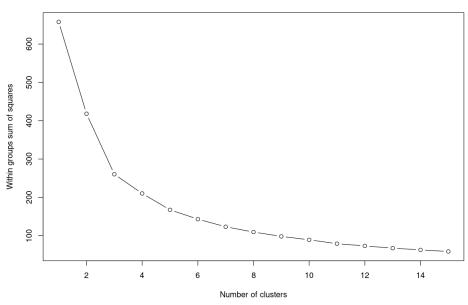
```
In [162]: # We need to first scale the data.
          kmtrain_scaled <- scale(traindat[, -1], center=TRUE, scale=TRUE)</pre>
          kmtrain_centers <- attr(kmtrain_scaled, "scaled:center")</pre>
          kmtrain_scales <- attr(kmtrain_scaled, "scaled:scale")</pre>
          # Map the values into the range [0, 1]. (I am not
          # sure whether this makes things better or worse.)
          kmtrain_scaled <- apply(kmtrain_scaled, MARGIN=2, range01)</pre>
          summary(kmtrain_scaled)
          kmtrain_scaled <- as.data.frame(cbind(as.numeric(traindat$Inland), kmtrain_scaled),</pre>
                                       row.names=rownames(traindat))
          colnames(kmtrain_scaled) <- colnames(traindat)</pre>
           housing_median_age median_house_value
           Min. :0.000
                          Min. :0.000
           1st Qu.:0.233
                              1st Qu.:0.138
           Median :0.384
                              Median :0.216
           Mean :0.385
                              Mean :0.258
           3rd Qu.:0.493
                              3rd Qu.:0.328
                 :1.000
           Max.
                              Max. :1.000
```

Construct initial k-means model

```
In [163]: # Run k-means algorithm with number of clusters set to 2.
           # Make sure to remove the Inland column.
           set.seed(1233)
           start <- Sys.time()</pre>
           km_mod <- kmeans(kmtrain_scaled[, -1], 2, iter.max = 50, nstart = 15)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 0.04 secs
           print(km mod$size)
           Time difference of 0.05 secs
           [1] 5139 5464
In [164]: datout <- as.data.frame(cbind(kmtrain_scaled$Inland, km_mod$cluster))</pre>
           colnames(datout) <- c("Inland", "cluster")</pre>
           rownames(datout) <- rownames(kmtrain_scaled)</pre>
           head(datout)
           A data.frame: 6 × 2
                 Inland cluster
                  <dbl>
                         <dbl>
           15111
                            2
                     n
           20002
                     1
                            2
           13570
                     1
                            1
           20333
                     0
                            2
            10614
                     0
                            2
           18538
                     0
                            2
In [166]: # max_vals identifies the Inland level we would expect
           # each cluster to map to.
           (mat <- as.matrix(table(datout$Inland, as.factor(datout$cluster))))</pre>
           max_vals <- apply(mat, MARGIN=2, which.max); print(max_vals)</pre>
             0 4227 3084
             1 912 2380
           1 2
           1 1
In [167]: # Use function c1 toLevel 1 to get the correct
           # mapping between clusters and Inland levels.
           c1_to_Inland1 <- c1_toLevel_1(datout)</pre>
           paste("Map cluster 1 to Inland level 1? : ", c1_to_Inland1, sep="")
           'Map cluster 1 to Inland level 1?: FALSE'
In [171]: tmpdat <- datout</pre>
           tmpdat[which(tmpdat$cluster== 1),]$Inland <- 0</pre>
           tmpdat[which(tmpdat$cluster== 2),]$Inland <- 1</pre>
           dim(tmpdat)
           10603 · 2
```

```
In [172]: sum(rownames(tmpdat) == rownames(kmtrain_scaled)) == nrow(kmtrain_scaled)
          table(as.factor(tmpdat$Inland))
          TRUE
             0
          5139 5464
In [173]: # Get initial set of scores for the k-means base model.
          preds <- as.factor(tmpdat$Inland)</pre>
          names(preds) <- rownames(tmpdat)</pre>
          ans <- get_confusion(preds, kmtrain_scaled[, "Inland", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for k-means base model on training set: ", as.character(ans[[2]]), sep=
          # f-score: 0.5436
          # Accuracy: 0.6231
          # Type2: 0.5754
               0 1 class.error
          0 4227 3084
                          0.4218
          1 912 2380
                           0.2770
          [1] "f-score for k-means base model on training set: 0.5436"
 In [ ]: ### COMMENT:
          # The k-means algorithm has difficulty with this dataset.
          # We see from the following wss plot that k-means would
          # do somewhat better if we asked it to find 3 clusters, not
          # 2.
```

wss plot for the CA data; no prob01 column



```
In []: ### COMMENT:

# The wss plot suggests that a more natural solution
# might be 3 clusters rather than 2.

# So, unlike the downer cow data, there is not a natural
# ordering into 2 subgroups. Recall that with the cow data
# the specific purpose of collecting variables such as
# AST and CK was to see if they could help in distinguishing
# the surviving cows from the non-survivors. By contrast,
# the CA housing variables I am working with were not
# collected with the purpose of distinguishing Inland
# districts from districts closer to the ocean. So it is
# reasonable that a 2-cluster solution is not obvious.
```

Construct hybrid k-means model with prob01 from f03

If a hybrid model exists which outperforms the other models we have surveyed (namely svm02 and gbclf_best, since they have the best sets of scores), it very likely will require at least 2 probability columns. The first will be needed simply to nudge k-means to a 2-cluster solution. The second might then be able to further boost the hybrid model's scores.

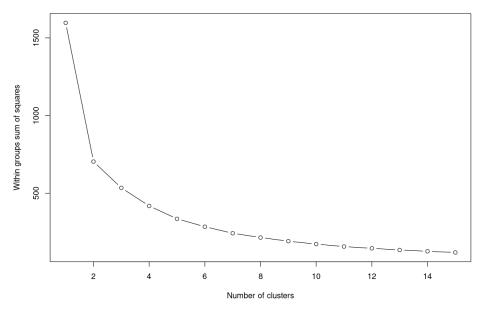
For the first probability column I will use the weakest model, f03, not because it is the weakest but rather because it so clearly differs from the other models, having far fewer false positives. Then for prob02 I can choose between gbclf_best and svm02.

```
In [177]: # Add a prob01 column to kmtrain.

preds <- predict(f03, newdata=traindat, type="response")

kmtrain_scaled$prob01 <- preds
summary(kmtrain_scaled$prob01)</pre>
```

wss plot for the CA data with prob01 column



```
In [ ]: ### COMMENT:

# This is exactly the kind of curve we want to see if
# we want to partition the data into 2 clusters.
```

Get scores on trainset for k-means with prob01, no weights

In [179]: # Run k-means algorithm with number of clusters set to 2.

```
set.seed(1233)
start <- Sys.time()
kmp1 <- kmeans(kmtrain_scaled[, -1], 2, iter.max = 50, nstart = 15)
stop <- Sys.time()
round(stop - start, 2)
# Time difference of 0.03 secs
print(kmp1$size)

Time difference of 0.04 secs
[1] 6955 3648

In [180]: datout <- as.data.frame(cbind(kmtrain_scaled$Inland, kmp1$cluster))
colnames(datout) <- c("Inland", "cluster")
rownames(datout) <- rownames(kmtrain_scaled)
c1_to_Inland1 <- c1_toLevel_1(datout)
paste("Map cluster 1 to Inland level 1? : ", c1_to_Inland1, sep="")</pre>
```

'Map cluster 1 to Inland level 1?: FALSE'

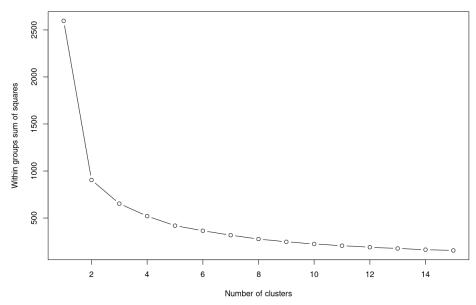
```
In [181]: tmpdat <- datout</pre>
          tmpdat[which(tmpdat$cluster== 1),]$Inland <- 0</pre>
          tmpdat[which(tmpdat$cluster== 2),]$Inland <- 1</pre>
          dim(tmpdat)
           10603 · 2
In [182]:
          sum(rownames(tmpdat) == rownames(kmtrain_scaled)) == nrow(kmtrain_scaled)
          table(as.factor(tmpdat$Inland))
          TRUE
           6955 3648
In [183]: # Get initial set of scores for the k-means hybrid model
          # with prob01 built from g03.
          preds <- as.factor(tmpdat$Inland)</pre>
          names(preds) <- rownames(tmpdat)</pre>
          ans <- get_confusion(preds, kmtrain_scaled[, "Inland", drop=FALSE])</pre>
          print(ans$matrix)
          print(paste("f-score for k-means hybrid model on training set: ", as.character(ans[[2]]), se
          # f-score: 0.7352
          # Accuracy: 0.8267
          # Type2: 0.7718
                     1 class.error
          0 6214 1097
                            0.1500
          1 741 2551
                            0.2251
           [1] "f-score for k-means base model on training set: 0.7352"
```

Add a prob02 column using gbclf_best

```
In [185]: # Add a prob02 column to kmtrain.
preds <- suppressMessages(predict(gbclf_best, newdata=traindat, type="response"))
kmtrain_scaled$prob02 <- preds
summary(kmtrain_scaled$prob02)

Min. 1st Qu. Median Mean 3rd Qu. Max.
0.00873 0.06008 0.16665 0.31080 0.53070 0.99635</pre>
```

wss plot for the CA data with prob01 & prob02 columns



Get scores on trainset for k-means with prob01 & prob02, no weights

```
In [193]: # Run k-means algorithm with number of clusters set to 2.
           set.seed(1233)
           start <- Sys.time()</pre>
           kmplp2 <- kmeans(kmtrain_scaled[, -1], 2, iter.max = 50, nstart = 15)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 0.03 secs
           print(kmp1p2$size)
           Time difference of 0.04 secs
           [1] 7228 3375
In [194]: datout <- as.data.frame(cbind(kmtrain scaled$Inland, kmp1p2$cluster))</pre>
           colnames(datout) <- c("Inland", "cluster")</pre>
           rownames(datout) <- rownames(kmtrain_scaled)</pre>
           c1_to_Inland1 <- c1_toLevel_1(datout)</pre>
           paste("Map cluster 1 to Inland level 1? : ", c1_to_Inland1, sep="")
           'Map cluster 1 to Inland level 1?: FALSE'
In [189]:
          tmpdat <- datout
           tmpdat[which(tmpdat$cluster== 1),]$Inland <- 0</pre>
           tmpdat[which(tmpdat$cluster== 2),]$Inland <- 1</pre>
           dim(tmpdat)
           10603 · 2
```

```
In [190]: sum(rownames(tmpdat) == rownames(kmtrain_scaled)) == nrow(kmtrain_scaled)
          table(as.factor(tmpdat$Inland))
          TRUE
             Θ
          7228 3375
In [191]: # Get initial set of scores for the k-means hybrid model
          # which has the prob01 and prob02 columns.
          preds <- as.factor(tmpdat$Inland)</pre>
          names(preds) <- rownames(tmpdat)</pre>
          ans <- get_confusion(preds, kmtrain_scaled[, "Inland", drop=FALSE])</pre>
          print(paste("f-score for k-means hybrid model on training set: ", as.character(ans[[2]]), set
          # f-score: 0.7419
          # Accuracy: 0.8377
          # Type2: 0.7802
                    1 class.error
               0
          0 6409 902
                         0.1234
          1 819 2473
                           0.2488
          [1] "f-score for k-means hybrid model on training set: 0.7419"
 In [ ]:
```

Get comparative scores for the hybrid model, no weights

```
In [200]: # Scale the testset data.
          kmtest_scaled <- scale(testdat[, -1], center=kmtrain_centers, scale=kmtrain_scales)</pre>
          kmtest scaled <- as.data.frame(cbind(as.numeric(testdat$Inland), kmtest scaled),</pre>
                                           row.names=rownames(testdat))
          colnames(kmtest_scaled) <- colnames(testdat)</pre>
In [198]: # We can get predictions for prob01 and prob02 prior
          # to getting scores for 250 4K-sized samples from testdat.
          kmtest prob01 <- predict(f03, newdata=testdat, type="response")</pre>
          kmtest_prob02 <- suppressMessages(predict(gbclf_best, newdata=testdat, type="response"))</pre>
          names(kmtest_prob02) <- names(kmtest_prob01)</pre>
          summary(kmtest_prob01)
          summary(kmtest_prob02)
             Min. 1st Qu. Median
                                      Mean 3rd Qu.
          0.00045 0.05923 0.19335 0.31786 0.55535 0.99979
             Min. 1st Qu. Median
                                      Mean 3rd Qu.
          0.00966 0.06061 0.17155 0.31955 0.56083 0.99560
In [201]: # Function for obtaining a set of scores on the testset data
          # using the k-means hybrid model as the classifier.
          get_testdatScores_kmp1p2 <- function(seedv, dat) {</pre>
              n smp <- 4000
```

```
seedv len <- length(seedv)</pre>
    datout <- rep(NA, 5 * seedv_len)</pre>
    dim(datout) <- c(seedv_len, 5)</pre>
    datout <- as.data.frame(datout)</pre>
    colnames(datout) <- c("fscore", "Acc", "Type2", "FN", "FP")</pre>
    rownames(datout) <- as.character(seedv)</pre>
    # Using model kmp1p2 from above.
    ctr_list <- vector("list", length= n_smp)</pre>
    for(i in 1:n_smp) {
         ctr_list[[i]] <- kmp1p2$centers</pre>
    for(h in 1:seedv_len) {
         cur_seed <- seedv[h]</pre>
         set.seed(cur seed)
         # dat should be kmtest_scaled, which has 10K rcds
         smp <- sample(rownames(dat), n_smp, replace= FALSE)</pre>
         df <- dat[smp,]</pre>
         # Apply min-max scaling to df.
         df_scaled <- apply(df[, -1], MARGIN=2, range01)</pre>
         df_scaled <- as.data.frame(df_scaled, row.names=rownames(df))</pre>
         df_scaled$prob01 <- as.numeric(kmtest_prob01[smp])</pre>
         df_scaled$prob02 <- as.numeric(kmtest_prob02[smp])</pre>
         colnames(df_scaled) <- colnames(kmp1p2$centers)</pre>
         # Each element of the following list is a row of df_scaled.
         df_asList <- split(df_scaled, seq(n_smp))</pre>
         names(ctr_list) <- rownames(df)</pre>
         # Get the predictions for df.
         cluster assgns <- mcmapply(getCluster, df asList, ctr list,</pre>
                             SIMPLIFY=TRUE, mc.cores=6)
         df$cluster <- as.numeric(cluster_assgns)</pre>
         ### NOTE: c1_to_Inland1 is a global variable based on
         ### model kmp1p2.
         df$pred Inland <- NA
         if(c1_to_Inland1) {
             df[which(df$cluster==1),]$pred_Inland <- 1</pre>
             df[which(df$cluster==2),]$pred_Inland <- 0</pre>
             df[which(df$cluster==1),]$pred Inland <- 0</pre>
             df[which(df$cluster==2),]$pred Inland <- 1</pre>
         }
         # Generate confusion matrix.
         preds <- as.factor(df$pred_Inland)</pre>
         names(preds) <- rownames(df)</pre>
         ans <- get_confusion(preds, df[, "Inland", drop=FALSE])</pre>
         mat <- as.matrix(ans[[1]])</pre>
         fscore <- round(as.numeric(ans[[2]]), 4)</pre>
         acc <- round(sum(diag(mat))/floor(sum(mat)), 4)</pre>
         type2 <- round((0.4 * acc + 0.6 * ans[[2]]), 4)
         FN <- as.numeric(mat[2,1])</pre>
         FP <- as.numeric(mat[1,2])</pre>
         datout[as.character(cur seed), 1:5] <- c(fscore,acc,type2,FN,FP)</pre>
    return(datout)
}
```

In [204]: # Get kmp1p2's scores on the testset data. For each of

```
# the 250 seeds, I sample 4K (no replacement) from the 10K
           # set of testdat records.
           set.seed(1821)
           seed_vector <- sample(1:9999, 250, replace=FALSE)</pre>
           start <- Sys.time()</pre>
           paste0("Start time: ", start)
           dat_result <- get_testdatScores_kmp1p2(seed_vector, kmtest_scaled)</pre>
           stop <- Sys.time()</pre>
           round(stop - start, 2)
           # Time difference of 7.24 mins; for comparison, we obtained
           # scores above for gbclf_best in less than 12 seconds.
           'Start time: 2021-07-27 18:47:53'
           Time difference of 7.24 mins
In [205]: dim(dat_result)
           head(dat_result)
            250 · 5
           A data.frame: 6 x 5
                                            FP
                 fscore
                         Acc Type2
                                      FN
                 <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
            5934 0.7279 0.8222 0.7656
                                      320
                                            391
            1953 0.7297 0.8235 0.7672
                                      337
                                            369
            7591 0.7280 0.8212 0.7653
                                      324
                                            391
            1038 0.7249 0.8228 0.7641
                                      318
                                            391
             49 0.7239 0.8158 0.7607
                                      362
                                            375
            3203 0.7397 0.8282 0.7751
                                      347
                                            340
In [206]: | fscore_mean <- round(mean(dat_result$fscore), 4)</pre>
           fscore_sd <- round(sd(dat_result$fscore), 4)</pre>
           paste0("fscore mean: ", as.character(fscore_mean))
           # 0.7310
           paste0("fscore StdDev: ", as.character(fscore_sd))
           # 0.0074
           summary(dat_result$fscore)
           'fscore mean: 0.731'
           'fscore StdDev: 0.0074'
              Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                           Max.
                      0.726
             0.707
                              0.731 0.731
                                                0.736
                                                          0.756
```

```
In [207]: Acc_mean <- round(mean(dat_result$Acc), 4)</pre>
          Acc_sd <- round(sd(dat_result$Acc), 4)</pre>
          paste0("accuracy mean: ", as.character(Acc_mean))
          paste0("accuracy StdDev: ", as.character(Acc sd))
          summary(dat_result$Acc)
          'accuracy mean: 0.8238'
          'accuracy StdDev: 0.0044'
             Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
             0.814 0.821
                            0.824
                                    0.824
                                             0.827
                                                       0.836
In [208]: Type2_mean <- round(mean(dat_result$Type2), 4)</pre>
          Type2_sd <- round(sd(dat_result$Type2), 4)</pre>
          paste0("Type2 mean: ", as.character(Type2_mean))
          # 0.7681
          paste0("Type2 StdDev: ", as.character(Type2_sd))
          # 0.006
          summary(dat_result$Type2)
           'Type2 mean: 0.7681'
          'Type2 StdDev: 0.006'
             Min. 1st Qu. Median
                                     Mean 3rd Qu.
                                                        Max.
             0.750 0.764 0.768
                                      0.768 0.772
                                                       0.788
In [209]: FN_mean <- round(mean(dat_result$FN), 2)</pre>
          FN_sd <- round(sd(dat_result$FN), 2)</pre>
          paste0("FN mean: ", as.character(FN_mean))
          # 338
          paste0("FN StdDev: ", as.character(FN_sd))
          # 13.1
          summary(dat_result$FN)
          'FN mean: 337.55'
          'FN StdDev: 13.09'
              Min. 1st Qu. Median
                                       Mean 3rd Qu.
                                                        Max.
               299
                       328
                                338
                                        338 347
                                                         370
In [210]: FP_mean <- round(mean(dat_result$FP), 2)</pre>
          FP sd <- round(sd(dat result$FP), 2)</pre>
          paste0("FP mean: ", as.character(FP_mean))
          paste0("FP StdDev: ", as.character(FP_sd))
          # 14.3
          summary(dat_result$FP)
          'FP mean: 367.3'
          'FP StdDev: 14.31'
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max.
```

Comments on kmp1p2, no weights

A table summarizing the comparative scores obtained thus far is shown immediately below. The hybrid k-means model, kmp1p2, with prob01 constructed from f03 and prob02 constructed from gbclf_best, is a better model than any of rfclf_best, gbclf_best, svm02, or f03 IF we compare the models based on either f-score or the Type2 score.

The p-value for the hypothesis 0.7681 > 0.7632 (the next-best Type2 score) is < 2e-16. The p-value for the hypothesis 0.7310 > 0.7183 (the next-best f-score) is < 2e-16. But for the accuracy score, the p-value for the hypothesis that 0.8306 (the best accuracy score; model svm02) > 0.8238 is also < 2e-16. Recall that the Type2 score is 40% accuracy and 60% f-score; if we reversed these weights, the hybrid k-means model would no longer have the best Type2 score.

We should be able to obtain better scores for the kmp1p2 hybrid k-means model by finding weights for it. This is done in Section 3 below.

Table Summarizing Results Thus Far

```
In [3]: results <- read.csv("/home/greg/Documents/stat/github_repos/cows/model_results_Part2_Section</pre>
                                   header=TRUE, row.names=1)
          dim(results)
           5 · 10
In [4]: results
          A data.frame: 5 x 10
                                                                        FN FN_sd
                                                                                     FP FP_sd
                   fscore fscore_sd accuracy acc_sd Type2 Type2_sd
                                               <dbl> <dbl>
                    <dbl>
                              <dbl>
                                       <dbl>
                                                                <dbl> <int>
                                                                             <dbl>
                                                                                   <int>
                                                                                          <dbl>
              rfclf 0.7156
                             0.0075
                                      0.8228
                                              0.0045 0.7585
                                                               0.0061
                                                                        404
                                                                              14.5
                                                                                     305
                                                                                            12.4
                             0.0077
                                      0.8304
                                              0.0044 0.7632
                                                                        430
             gbclf 0.7183
                                                               0.0061
                                                                              147
                                                                                     249
                                                                                           117
               f03 0.6704
                             0.0090
                                      0.8226
                                              0.0046 0.7313
                                                               0.0070
                                                                        574
                                                                              17.1
                                                                                     136
                                                                                            8.3
            svm02 0.7175
                             0.0078
                                      0.8306
                                             0.0044 0.7628
                                                               0.0062
                                                                        434
                                                                              14.6
                                                                                     243
                                                                                           11.1
           kmp1p2 0.7310
                             0.0074
                                      0.8238 0.0044 0.7681
                                                               0.0060
                                                                        338
                                                                              13.1
                                                                                     367
                                                                                           14.3
In [ ]:
```

Section 3: Find optimal weights for kmp1p2

In []:	
In []:	

Part 2 Final Comments

As in Part 1, we see in this notebook that we can obtain a better classification model from existing classification models by using one or more of the latter to inform a hybrid k-means model. In this example, the accuracy scores of the non-k-means models are in the low 80's. The greater these accuracy scores, the less likely it is that we can improve upon them using a hybrid k-means model.

I have not experimented with other hybrid models using the current dataset and the two variables of housing_median_age and median_house_value. It may be that a different combination of two of (rfclf_best, gbclf_best, f03, svm02) will yield an even better hybrid k-means model.

In []: