

**Remark 2.7.** One might argue that the number of binary sequences of length  $n$  is  $2^n$  because they represent all numbers from 0 to  $2^n - 1$  in the binary system. But this result itself requires a proof, which is not easier than our combinatorial argument.