Proof. Apply the product rule. The coin is making n choices, each time from two possibilities. Thus the number of outcomes is $\underbrace{2 \cdots 2}_{n} = 2^n$. $\qquad\square$