Lemma 3.6. *For every $0 \leq k \leq n$ the following identity holds:*

$$\binom{n}{k} = \binom{n-1}{k-1} + \binom{n-1}{k}. \tag{1}$$