

**Remark 2.4.** The set of all maps  $X \rightarrow Y$  is sometimes denoted by  $Y^X$ , so that Theorem ?? can be formulated as  $|Y^X| = |Y|^{|X|}$ . This is not the only reason for the notation  $Y^X$ . One can show that  $Z^{X \cup Y} = Z^X \times Z^Y$  for disjoint  $X$  and  $Y$ , and  $Z^{X \times Y} = (Z^X)^Y$ .

Also, the Cartesian power

$$X^n = \underbrace{X \times \cdots \times X}_n = \{(x_1, \dots, x_n) \mid x_i \in X \text{ for all } i\}$$

can be viewed as the set  $X^{\{1, \dots, n\}}$ : a sequence  $(x_1, \dots, x_n)$  corresponds to a map  $f: \{1, \dots, n\} \rightarrow X$ ,  $f(i) = x_i$ .