

Proof. One can argue by the product rule again. Or, one can establish a bijection between the set of binary sequences and the set of outcomes when tossing a coin: one encodes an outcome by putting 1 for “heads” and 0 for “tails”. It is easy to see that this is a bijection, thus by the previous theorem the number of binary sequences is 2^n . □