

Proof. A subset of $\{1, 2, \dots, n\}$ can be encoded with a binary word: the i -th digit of this word is 1 if and only if the number i belongs to the subset. The words with k digits 1 correspond to the k -element subsets, hence there are $\binom{n}{k}$ such words. \square