Theorem 3.3. The number $\binom{n}{k}$ is equal to the number of binary words of length n containing exactly k digits 1.