Given k people, what is the probability that some two of them have the same birthday? How big should k be for this probability to exceed  $\frac{1}{2}$ ?