

A little more CFG parsing

Computational Linguistics (LING 455)

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Summary

CFGs

CFGs have rewrite rules of the shape $A \rightarrow \varphi$, where φ is a string of terminals and non-terminals.

- The restriction is on the LHS. This is what makes it context-free.

We can contemplate restrictions on the RHS as well:

- Rules like $A \rightarrow x$, $A \rightarrow xB$ only: finite-state/regular
- Rules like $A \rightarrow x$, $A \rightarrow BC$ only: Chomsky Normal Form

CNF is a convenience, not a restriction in expressive power.

The parsing task

A **grammar** is a way of finitely and succinctly specifying a (typically infinite) number of objects with a certain shape.

Parsing is the task of structuring a linear representation in a way sanctioned by some grammar.

Naive CFG parsing

```
parse g [x] = [ n | n :- y <- g, y==x ]  
parse g xs  = [ n | (ls,rs) <- breaks xs,  
                    nl <- parse g ls,  
                    nr <- parse g rs,  
                    n :> (l,r) <- g, l==nl, r==nr ]
```

For non-singleton strings:

- Break the input string into two (every possible way)
- Recurse, parsing the left half and the right half (given g)
- Try to combine the resulting yields `nl` and `nr` (given g)
- Return the resulting categories

Naive parsing is inefficient: each substring under a given length is parsed multiple (depending on the string length, maybe many) times.



Each substring is identified by a **span**, a pair of numbers (i, j) :

	"Mary"		"saw"		"the"		"elk"	
0		1		2		3		4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1	0,2	0,3	0,4
"Mary"		1,2	1,3	1,4
			2,3	2,4
				3,4

"saw"

"the"

"elk"

Each substring is identified by a **span**, a pair of numbers (i, j) :

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	0,1 DP	0,2	0,3	0,4
"Mary"		1,2	1,3	1,4
			2,3	2,4
				3,4

"saw"
"the"
"elk"

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	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
"saw"			2,3	2,4
"the"				3,4
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

	"Mary"		"saw"		"the"		"elk"	
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"Mary"		1,2 VT	1,3	1,4
"saw"			2,3	2,4
"the"				3,4
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
"saw"			2,3 D	2,4
"the"				3,4
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
"saw"			2,3 D	2,4
"the"				3,4
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

	"Mary"		"saw"		"the"		"elk"	
0		1		2		3		4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
			2,3 D	2,4
				3,4

"saw"
"the"
"elk"

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
"saw"			2,3 D	2,4
"the"				3,4 NP
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4
"saw"			2,3 D	2,4 DP
"the"				3,4 NP
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4
"Mary"		1,2 VT	1,3	1,4 VP
"saw"			2,3 D	2,4 DP
"the"				3,4 NP
"elk"				

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"	
0	1	2	3	4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4 S
"Mary"		1,2 VT	1,3	1,4 VP
			2,3 D	2,4 DP
"saw"				3,4 NP
			"the"	
				"elk"

Each substring is identified by a **span**, a pair of numbers (i, j) :

"Mary"	"saw"	"the"	"elk"
0	1	2	3
			4

Spans can be arranged in a table. Then parsing amounts to filling the table in. The key to efficiency: each span occurs exactly **once**!

	0,1 DP	0,2	0,3	0,4 S
"Mary"		1,2 VT	1,3	1,4 VP
			2,3 D	2,4 DP
				3,4 NP
		"saw"	"the"	"elk"

Enriched parsing

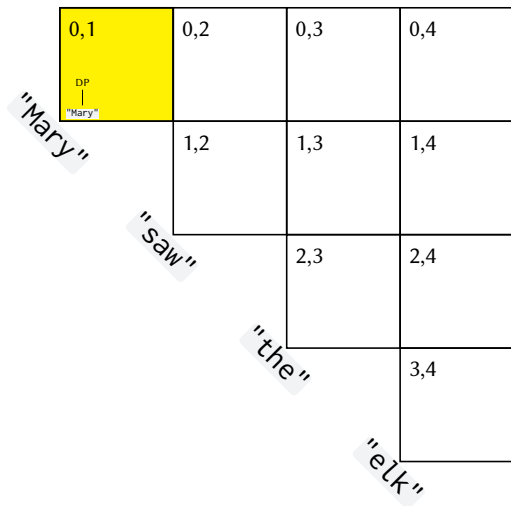
These parsing algorithms treat parse yields as (lists of) categories. We might be interested in other kinds of yields:

- Trees (e.g., LBT's) that encode the structure of the parsed object
- Weights that report (e.g.) how probable a derivation is
- Costs associated with a derivation

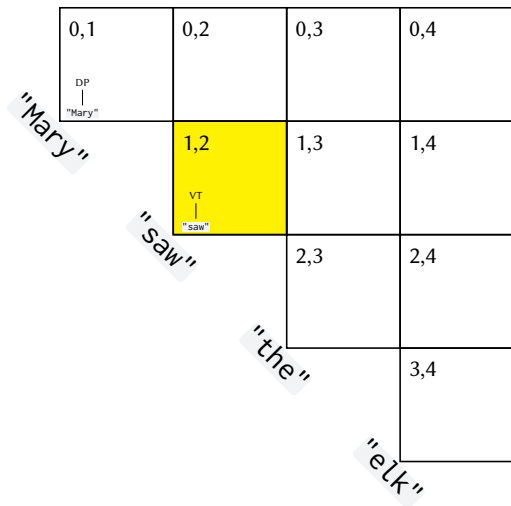
Parsing to trees

0,1	0,2	0,3	0,4
"Mary"	1,2	1,3	1,4
	"saw"	2,3	2,4
		"the"	3,4
			"elk"

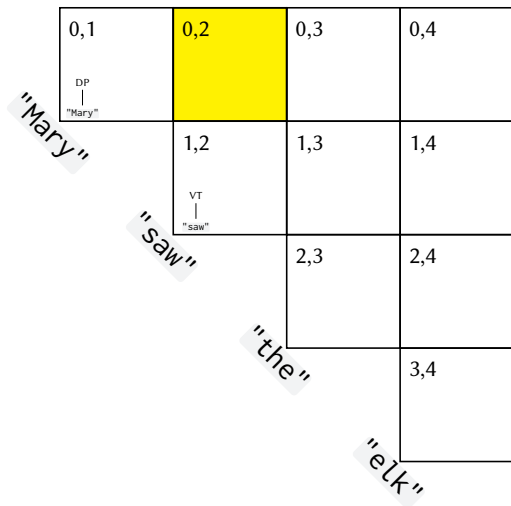
Parsing to trees



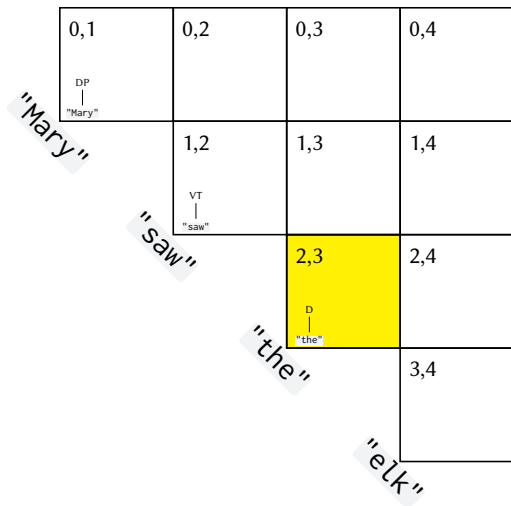
Parsing to trees



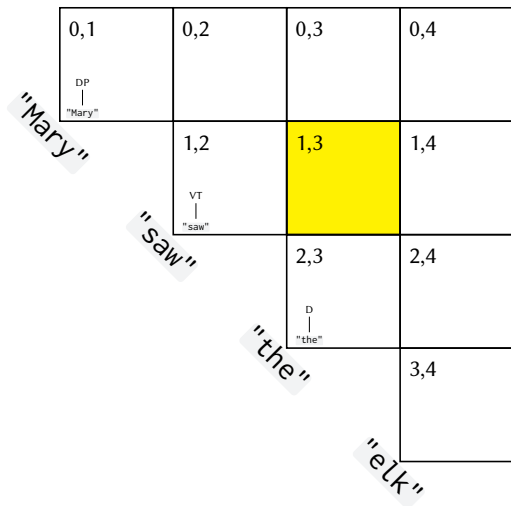
Parsing to trees



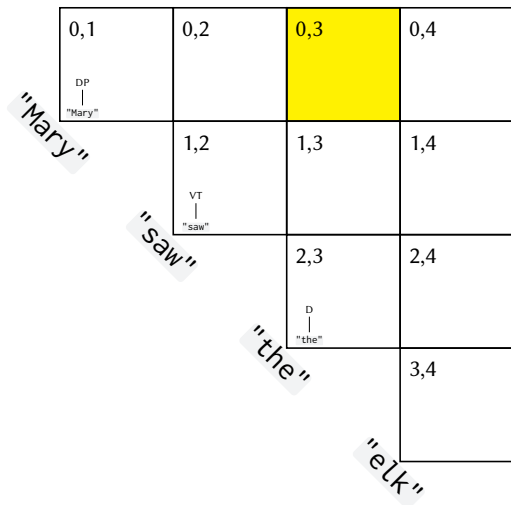
Parsing to trees



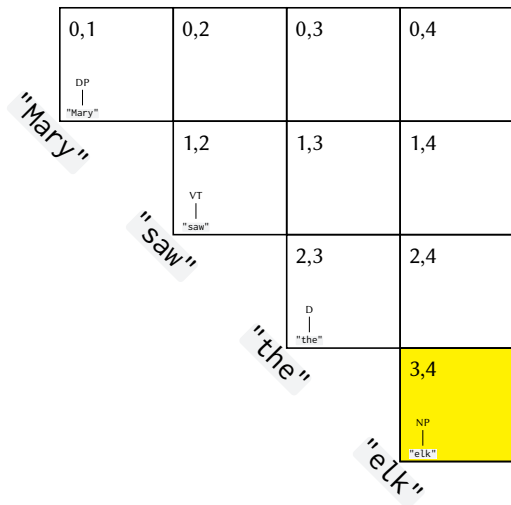
Parsing to trees



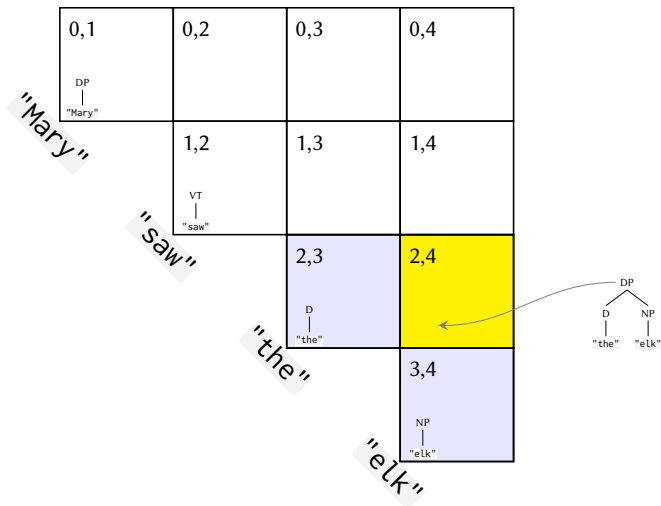
Parsing to trees



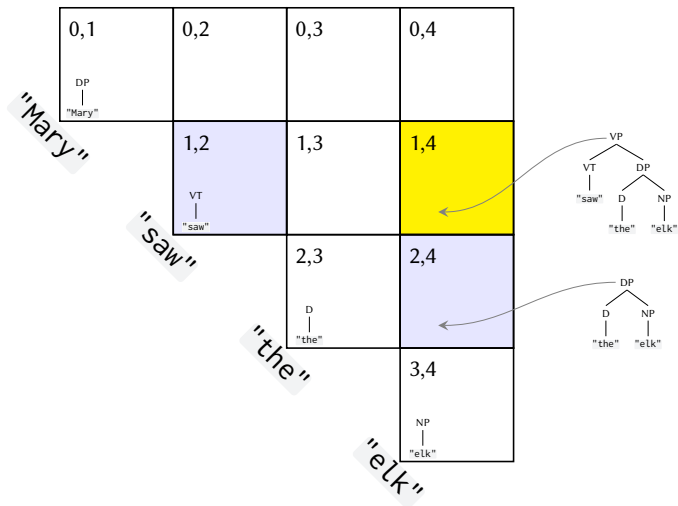
Parsing to trees



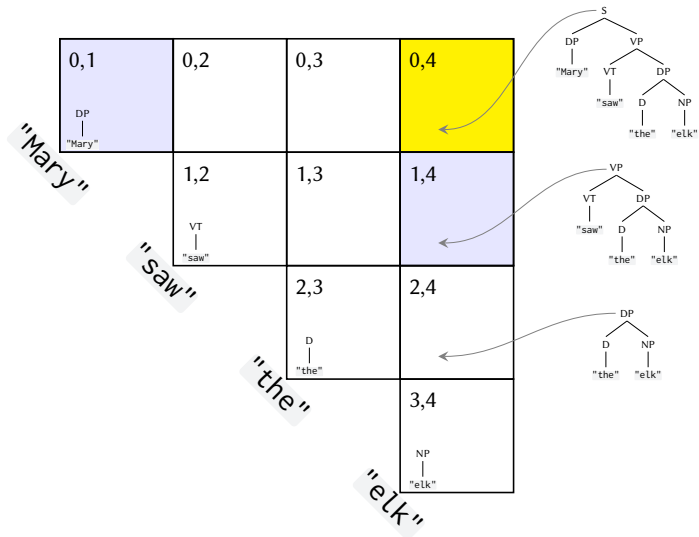
Parsing to trees



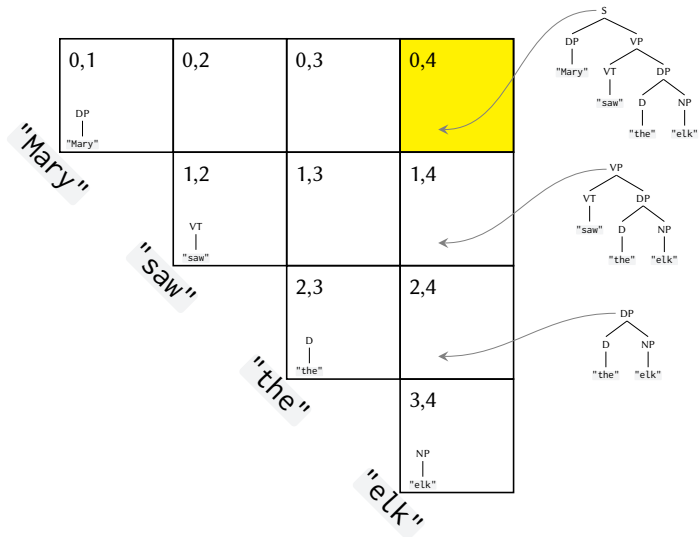
Parsing to trees



Parsing to trees



Parsing to trees



Enriched parsing

The strategy for parsing to LBT's is quite reminiscent of how we generalized FSA parsing to FST parsing:

```
step delta x (q,m) = [ (s, m<>n) | (r,y,n,s) <- delta,  
                                q==r, y==x ]
```

```
parseToLBT g [x] = [ Leaf n x | n :- y <- g, y==x ]  
parseToLBT g xs =  
  [ Branch n tl tr | (ls, rs) <- breaks xs,  
    tl <- parseToLBT g ls,  
    tr <- parseToLBT g rs,  
    n :> (l, r) <- g, label tl == l, label tr == r ]
```

The old result of a parse (previously, a state; now, a category) is **enriched** with some extra info (previously, a string; now, a tree).

Weighted or probabilistic CFGs

A straightforward extension of CFGs pairs rules with **weights**, **probabilities**, or **costs**.

```
type WCFG cat term weight = [(Rule cat term, weight)]
type PCFG cat term = WCFG cat term Double
```

Computing the weight of a whole analysis means **accumulating** the weights, via a monoid! (Exercise: change CYK.)

```
parseW g [x] = [ (n, w) | (n :- y, w) <- g, y==x ]
parseW g xs =
  [ (n, w<>wl<>wr) | (ls, rs) <- breaks xs,
                    (nl, wl) <- parseW g ls,
                    (nr, wr) <- parseW g rs,
                    (n :> (l,r), w) <- g, l==nl, r==nr ]
```


Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2	1,3	1,4
"saw"		2,3	2,4
	"the"		3,4
		"elk"	

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3	2,4
	"the"		3,4
		"elk"	

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3	2,4
		"the"	3,4
			"elk"

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3 D: 0.5	2,4
		"the"	3,4
		"elk"	

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3 D: 0.5	2,4
			3,4
			"the"
			"elk"

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3 D: 0.5	2,4
			3,4
			"the"
			"elk"

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3 D: 0.5	2,4
		"the"	3,4 NP: 0.5
		"elk"	

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4
"saw"		2,3 D: 0.5	2,4 DP: 0.25
		"the"	3,4 NP: 0.5
		"elk"	

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

0,1 DP: 0.5	0,2	0,3	0,4
"Mary"	1,2 VT: 1	1,3	1,4 VP: 0.25
"saw"		2,3 D: 0.5	2,4 DP: 0.25
"the"			3,4 NP: 0.5
"elk"			

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

"Mary"	0,1 DP: 0.5	0,2	0,3	0,4 S: 0.125
		1,2 VT: 1	1,3	1,4 VP: 0.25
			2,3 D: 0.5	2,4 DP: 0.25
				3,4 NP: 0.5
				"elk"

Parsing with weights (assume all $A \rightarrow BC$ rules weighted 1)

"Mary"	0,1 DP: 0.5	0,2	0,3	0,4 S: 0.125
		1,2 VT: 1	1,3	1,4 VP: 0.25
			2,3 D: 0.5	2,4 DP: 0.25
				3,4 NP: 0.5
"saw"				
"the"				
"elk"				

Transition-based parsing

Parsing as state transitions

Another way to conceptualize parsing is via transitions:

- Specify what a **starting stage** is
- Specify what a **goal stage** is
- Specify a **transition relation on stages**

Example: finite-state parsing

- A starting stage is a pair (A, xs) , where $A \in I$ and xs is the input
- A goal stage is a pair (A, ε) , where $A \in F$
- $(A, x_i x_{i+1} \dots x_n) \Rightarrow (B, x_{i+1} \dots x_n)$ iff $(A, x_i, B) \in \Delta$

Shift-reduce parsing

CFG parsing can work in a similar way. Given a set of rules G :

- A starting stage is (ε, xs) , where xs is the input
- A goal stage is (A, ε) , where A is a nonterminal
- Transitions either read a terminal or reduce 2 nonterminals:
 1. SHIFT: $(\Phi, x_i x_{i+1} \dots x_n) \Rightarrow (A\Phi, x_{i+1} \dots x_n)$, where $A \rightarrow x_i \in G$
 2. REDUCE: $(RL\Phi, xs) \Rightarrow (A\Phi, xs)$, where $A \rightarrow LR \in G$

An example

Type	Rule	Configuration
0		(ε , <i>Mary</i> saw the elk)

An example

Type		Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)
3	SHIFT	D \rightarrow the	(D VT DP, elk)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)
3	SHIFT	D \rightarrow the	(D VT DP, elk)
4	SHIFT	NP \rightarrow elk	(NP D VT DP, ϵ)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)
3	SHIFT	D \rightarrow the	(D VT DP, elk)
4	SHIFT	NP \rightarrow elk	(NP D VT DP, ϵ)
5	REDUCE	DP \rightarrow D NP	(DP VT DP, ϵ)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)
3	SHIFT	D \rightarrow the	(D VT DP, elk)
4	SHIFT	NP \rightarrow elk	(NP D VT DP, ϵ)
5	REDUCE	DP \rightarrow D NP	(DP VT DP, ϵ)
6	REDUCE	VP \rightarrow VT DP	(VP DP, ϵ)

An example

	Type	Rule	Configuration
0			(ϵ , Mary saw the elk)
1	SHIFT	DP \rightarrow Mary	(DP, saw the elk)
2	SHIFT	VT \rightarrow saw	(VT DP, the elk)
3	SHIFT	D \rightarrow the	(D VT DP, elk)
4	SHIFT	NP \rightarrow elk	(NP D VT DP, ϵ)
5	REDUCE	DP \rightarrow D NP	(DP VT DP, ϵ)
6	REDUCE	VP \rightarrow VT DP	(VP DP , ϵ)
7	REDUCE	S \rightarrow DP VP	(S , ϵ)

Another example

Type	Rule	Configuration
0		(ϵ , the elk saw Mary)

Another example

Type		Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	$D \rightarrow \text{the}$	(D, elk saw Mary)

Another example

Type		Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)

Another example

	Type	Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)
3	REDUCE	DP \rightarrow D NP	(DP, saw Mary)

Another example

	Type	Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)
3	REDUCE	DP \rightarrow D NP	(DP, saw Mary)
4	SHIFT	VT \rightarrow saw	(VT DP, Mary)

Another example

	Type	Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)
3	REDUCE	DP \rightarrow D NP	(DP, saw Mary)
4	SHIFT	VT \rightarrow saw	(VT DP, Mary)
5	SHIFT	DP \rightarrow Mary	(DP VT DP, ϵ)

Another example

	Type	Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)
3	REDUCE	DP \rightarrow D NP	(DP, saw Mary)
4	SHIFT	VT \rightarrow saw	(VT DP, Mary)
5	SHIFT	DP \rightarrow Mary	(DP VT DP, ϵ)
6	REDUCE	VP \rightarrow VT DP	(VP DP , ϵ)

Another example

	Type	Rule	Configuration
0			(ϵ , the elk saw Mary)
1	SHIFT	D \rightarrow the	(D, elk saw Mary)
2	SHIFT	NP \rightarrow elk	(NP D , saw Mary)
3	REDUCE	DP \rightarrow D NP	(DP, saw Mary)
4	SHIFT	VT \rightarrow saw	(VT DP, Mary)
5	SHIFT	DP \rightarrow Mary	(DP VT DP, ϵ)
6	REDUCE	VP \rightarrow VT DP	(VP DP , ϵ)
7	REDUCE	S \rightarrow DP VP	(S , ϵ)

Ambiguity in shift-reduce parsing

Type	Rule	Configuration
0		(ε , saw the elk with Mary)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	DP \rightarrow Mary	(DP P NP D VT, ϵ)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ε , saw the elk with Mary)
...
5	SHIFT	DP \rightarrow Mary	(DP P NP D VT, ε)
6	REDUCE	PP \rightarrow P DP	(PP NP D VT, ε)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	$DP \rightarrow \text{Mary}$	(DP P NP D VT, ϵ)
6	REDUCE	$PP \rightarrow P DP$	(PP NP D VT, ϵ)
7	REDUCE	$NP \rightarrow NP PP$	(NP D VT, ϵ)
...

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	$DP \rightarrow \text{Mary}$	(DP P NP D VT, ϵ)
6	REDUCE	$PP \rightarrow P DP$	(PP NP D VT, ϵ)
7	REDUCE	$NP \rightarrow NP PP$	(NP D VT, ϵ)
...

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ε , saw the elk with Mary)
...
5	SHIFT	DP \rightarrow Mary	(DP P NP D VT, ε)
6	REDUCE	PP \rightarrow P DP	(PP NP D VT, ε)
7	REDUCE	NP \rightarrow NP PP	(NP D VT, ε)
...

	Type	Rule	Configuration
0			(ε , saw the elk with Mary)
...

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	$DP \rightarrow \text{Mary}$	(DP P NP D VT, ϵ)
6	REDUCE	$PP \rightarrow P DP$	(PP NP D VT, ϵ)
7	REDUCE	$NP \rightarrow NP PP$	(NP D VT, ϵ)
...

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
3	SHIFT	$NP \rightarrow \text{elk}$	(NP D VT, with Mary)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	DP \rightarrow Mary	(DP P NP D VT, ϵ)
6	REDUCE	PP \rightarrow P DP	(PP NP D VT, ϵ)
7	REDUCE	NP \rightarrow NP PP	(NP D VT, ϵ)
...

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
3	SHIFT	NP \rightarrow elk	(NP D VT, with Mary)
4	REDUCE	DP \rightarrow D NP	(DP VT, with Mary)

Ambiguity in shift-reduce parsing

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
5	SHIFT	$DP \rightarrow \text{Mary}$	(DP P NP D VT, ϵ)
6	REDUCE	$PP \rightarrow P DP$	(PP NP D VT, ϵ)
7	REDUCE	$NP \rightarrow NP PP$	(NP D VT, ϵ)
...

	Type	Rule	Configuration
0			(ϵ , saw the elk with Mary)
...
3	SHIFT	$NP \rightarrow \text{elk}$	(NP D VT, with Mary)
4	REDUCE	$DP \rightarrow D NP$	(DP VT, with Mary)
5	REDUCE	$VP \rightarrow VT DP$	(VP, with Mary)
...

Stage's, shift, and reduce

```
type Stage cat term = ([cat], [term])
```

```
shift
```

```
  :: Eq term =>
```

```
    CFG cat term -> Stage cat term -> [Stage cat term]
```

```
shift g (cs, t:ts) = [(n:cs, ts) | n:-x <- g, x==t]
```

```
reduce
```

```
  :: Eq cat =>
```

```
    CFG cat term -> Stage cat term -> [Stage cat term]
```

```
reduce g (r:l:cs, ts) = [(n:cs, ts) | n:>(l',r') <- g,  
                                     l'==l, r'==r]
```

Nondeterminism in parsing

At any stage, the next course is not necessarily fully determined.

- This is how ambiguity can arise. After stage 3 in our derivation of *saw the elk with Mary*, do we SHIFT or REDUCE next?

This means that a single Stage in general begets a [Stage]. We need to try everything we can, to ensure we explore every path.

Trying everything

```
step
  :: (Eq cat, Eq term) =>
    CFG cat term -> Stage cat term -> [Stage cat term]
step g st@(r:l:cs, t:ts) = shift g st ++ reduce g st
step g st@(cs, t:ts)    = shift g st
step g st@(r:l:cs, ts)   = reduce g st
step g st                 = [st]
```

Keep taking steps till nothing changes

`helper` takes steps until we reach a **fixed point**:

```
parseSR :: (Eq cat, Eq term) =>
    CFG cat term -> [term] -> [Stage cat term]
parseSR g ws = helper g [([]), ws] where
    once stages = stages >=> step g      -- taking 1 step
    helper g stages
        | once stages == stages = stages -- fixed point
        | otherwise             = helper g (once stages)
```

```
*W12> s = words "Mary saw the elk with the binoculars"
*W12> parseSR eng s
[(S,[],), (S,[],)]
```

`parseSR` is really just a recognizer. Could you enrich it to parse to LBT's, or associate parse paths with weights, costs, etc?

Top-down parsing

Shift-reduce parsing works bottom-up: we find out what categories our terminals are, and start building structure.

- Bottom-up is also how CYK and naive parsing algos worked

Top-down parsers **predict** how a derivation will go:

- A starting stage is (A, xs) , where $A \in N$ and xs is the input
- A goal stage is $(\varepsilon, \varepsilon)$
- Transitions either expand a non-terminal or match a terminal:
 1. PREDICT: $(A\Phi, x_i \dots x_n) \Rightarrow (BC\Phi, x_i \dots x_n)$, where $A \rightarrow BC \in G$
 2. MATCH: $(A\Phi, x_i x_{i+1} \dots x_n) \Rightarrow (\Phi, x_{i+1} \dots x_n)$, where $A \rightarrow x_i \in G$

An example

Type	Rule	Configuration
0		(S , Mary saw the elk)

An example

Type		Rule	Configuration
0			(S , Mary saw the elk)
1	PREDICT	$S \rightarrow DP\ VP$	(DP VP, Mary saw the elk)

An example

Type		Rule	Configuration
0			(S , Mary saw the elk)
1	PREDICT	$S \rightarrow DP\ VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow Mary$	(VP , saw the elk)

An example

	Type	Rule	Configuration
0			(S , Mary saw the elk)
1	PREDICT	$S \rightarrow DP VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow \text{Mary}$	(VP , saw the elk)
3	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw the elk)

An example

	Type	Rule	Configuration
0			(S , Mary saw the elk)
1	PREDICT	$S \rightarrow DP VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow \text{Mary}$	(VP , saw the elk)
3	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw the elk)
4	MATCH	$VT \rightarrow \text{saw}$	(DP , the elk)

An example

	Type	Rule	Configuration
0			(S, Mary saw the elk)
1	PREDICT	$S \rightarrow DP VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow \text{Mary}$	(VP, saw the elk)
3	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw the elk)
4	MATCH	$VT \rightarrow \text{saw}$	(DP, the elk)
5	PREDICT	$DP \rightarrow D NP$	(D NP, the elk)

An example

	Type	Rule	Configuration
0			(S, Mary saw the elk)
1	PREDICT	$S \rightarrow DP VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow \text{Mary}$	(VP, saw the elk)
3	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw the elk)
4	MATCH	$VT \rightarrow \text{saw}$	(DP, the elk)
5	PREDICT	$DP \rightarrow D NP$	(D NP, the elk)
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)

An example

	Type	Rule	Configuration
0			(S, Mary saw the elk)
1	PREDICT	$S \rightarrow DP VP$	(DP VP, Mary saw the elk)
2	MATCH	$DP \rightarrow \text{Mary}$	(VP, saw the elk)
3	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw the elk)
4	MATCH	$VT \rightarrow \text{saw}$	(DP, the elk)
5	PREDICT	$DP \rightarrow D NP$	(D NP, the elk)
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)
7	MATCH	$NP \rightarrow \text{elk}$	(ϵ , ϵ)

There's something naturally incremental in top-down parsing. We build, or hypothesize, structure, immediately. In bottom-up parsing, REDUCE steps often depend on further-right SHIFT/REDUCE steps.

Another example

Type	Rule	Configuration
0		(S, the elk saw Mary)

Another example

Type		Rule	Configuration
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1	PREDICT	$S \rightarrow DP\ VP$	(DP VP, the elk saw Mary)

Another example

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Another example

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3	MATCH	$D \rightarrow \text{the}$	(NP VP, elk saw Mary)
4	MATCH	$NP \rightarrow \text{elk}$	(VP, saw Mary)
5	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw Mary)
6	MATCH	$VT \rightarrow \text{saw}$	(DP, Mary)

Another example

	Type	Rule	Configuration
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3	MATCH	$D \rightarrow \text{the}$	(NP VP, elk saw Mary)
4	MATCH	$NP \rightarrow \text{elk}$	(VP, saw Mary)
5	PREDICT	$VP \rightarrow VT DP$	(VT DP, saw Mary)
6	MATCH	$VT \rightarrow \text{saw}$	(DP, Mary)
7	MATCH	$DP \rightarrow \text{Mary}$	(ϵ , ϵ)

Non-termination

	Type	Rule	Configuration
...
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)

Non-termination

	Type	Rule	Configuration
...
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)
7	PREDICT	$NP \rightarrow NP PP$	(NP PP, elk)

Non-termination

	Type	Rule	Configuration
...
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)
7	PREDICT	$NP \rightarrow NP\ PP$	(NP PP, elk)
8	PREDICT	$NP \rightarrow NP\ PP$	(NP PP PP, elk)

Non-termination

	Type	Rule	Configuration
...
6	MATCH	$D \rightarrow \text{the}$	(NP, elk)
7	PREDICT	$NP \rightarrow NP\ PP$	(NP PP, elk)
8	PREDICT	$NP \rightarrow NP\ PP$	(NP PP PP, elk)
9	PREDICT	$NP \rightarrow NP\ PP$	(NP PP PP PP, elk)

If we keep PREDICT-ing, the parsing algorithm never terminates.
Which rules are problematic?

Non-termination

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If we keep PREDICT-ing, the parsing algorithm never terminates.
Which rules are problematic? **Left-recursive** rules, $A \rightarrow AB$.

Non-termination is **bad**. How might we deal with it here?

Non-termination

	Type	Rule	Configuration
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If we keep PREDICT-ing, the parsing algorithm never terminates.
Which rules are problematic? **Left-recursive** rules, $A \rightarrow AB$.

Non-termination is **bad**. How might we deal with it here?

- Look-ahead: curtail the expansions based on length of the input

Earley parsers

Another example of a parser that works top-down, but which does not suffer from non-termination in left-recursive grammars is an **Earley** parser.

We won't discuss Earley parsers in depth in this course, but the way that they avoid non-termination is easy enough to understand:

- Earley parsers have an **agenda** consisting of rules to try next
- A rule like $NP \rightarrow NP PP$ can be added to the agenda
- But adding this rule twice is no different from adding it once: it's already on the agenda!
- Once an agenda is stable (everything **new** that can be added has been), the parser gets to work trying its items

Transition-based parsing

In effect, transition-based parsing constructs something known as a **pushdown automaton** (PDA), in which a pushdown stack of nonterminals functions as an auxiliary memory source.

A pushdown stack is a special kind of memory in which we can only **pop** the top element off the stack, **push** a new element onto the stack, or do composite actions built out of those primitives.

CFG parsing is akin to finite-state parsing, with (pushdown) memory!