

Assignment 3

2.

Insert function:

Time Complexity: $O(\log(n))$, Space Complexity: $O(1)$

This function has a space complexity of $O(1)$ since it only adds one new node to the tree. Building the tree with n nodes has a complexity of $O(n)$ though.

Preorder function:

Time Complexity: $O(n)$, Space Complexity: $O(n)$

The space complexity of this function is $O(n)$ since the function call takes $O(1)$ space, but it recursively visits each node in the tree, so it is actually $O(n * 1) = O(n)$.

FindMax function:

Time Complexity: $O(n)$, Space Complexity: $O(n)$

This function is in place, as there is a new Node called MaxNode is declared and set to the highest valued node while the function traverses the tree. The space complexity is $O(n)$ since each function call has the space of $O(1)$ but the function visits all n nodes. So $O(n * 1) = O(n)$.

MakeBST function:

Time Complexity: $O(n \log(n))$, Space Complexity: $O(n)$

When this function is called, it is not sorted in place, and `std::sort` actually has a space complexity of $O(\log(n))$. When added with $O(n)$ from the size of the vector needed to store the integers and strings of the nodes, the space complexity becomes $O(n + \log(n))$ which is $O(n)$.

3. Times for each function in seconds

Size	Build Tree	Preorder()	FindMax()	MakeBST()
100	0.000322978	0.002532	3.127e-6	0.002498
1000	0.010955028	0.00389	2.309e-5	0.119528
10000	0.475599963	0.036074	0.000105981	9.143192
100000	54.901834672	18.820266	0.002209046	N/A

My MakeBST function time for 100000 elements is N/A since I keep getting a seg fault. I'm pretty sure my call stack is over 1 mb with a size of 100000 and I was reading that on windows systems, programs terminate once this is violated.

Note: my test.cpp should print the times in nanoseconds or microseconds. I just converted them to seconds in the table to keep it uniform!