

# **Template**

**KTH Thesis Report** 

Max Schaufelberger

#### **Author**

Max Schaufelberger <maxscha@kth.se> School of Engineering Sciences KTH Royal Institute of Technology

#### **Place for Project**

Stockholm, Sweden Ottignies-Louvain-la-Neuve, Belgium

#### **Examiner**

Prof. Olof Runborg Department of Numerical Analysis KTH Royal Institute of Technology Stockholm, Sweden

#### **Supervisor**

Prof. Elias Jarlebring Department of Numerical Analysis KTH Royal Institute of Technology Stockholm, Sweden

#### **Supervisor**

Arvind Kumar Division of Computational Science and Technology KTH Royal Institute of Technology Stockholm, Sweden

#### Supervisor

Frédéric Crevecoeur Institute of Information and Communication Technologies, Electronics and Applied Mathematics UCLouvain Catholic University of Louvain Louvain-la-Neuve, Belgium

### **Abstract**

This is a template for writing thesis reports for the ICT school at KTH. I do not own any of the images provided in the template and this can only be used to submit thesis work for KTH.

The report needs to be compiled using XeLaTeX as different fonts are needed for the project to look like the original report. You might have to change this manually in overleaf.

This template was created by Hannes Rabo <a href="mailto:kannes.rabo@gmail.com">kannes.rabo@gmail.com</a> or hrabo@kth.se> from the template provided by KTH. You can send me an email if you need help in making it work for you.

Write an abstract. Introduce the subject area for the project and describe the problems that are solved and described in the thesis. Present how the problems have been solved, methods used and present results for the project. Use probably one sentence for each chapter in the final report.

The presentation of the results should be the main part of the abstract. Use about ½ A4-page. English abstract

#### Keywords

Template, Thesis, Keywords ...

### **Abstract**

Svenskt abstract Svensk version av abstract – samma titel på svenska som på engelska.

Skriv samma abstract på svenska. Introducera ämnet för projektet och beskriv problemen som löses i materialet. Presentera

#### **Nyckelord**

Kandidat examensarbete, ...

# Acknowledgements

Write a short acknowledgements. Don't forget to give some credit to the examiner and supervisor.

# **Acronyms**

**DS** Dynamic System

**NN** Neural Network

**ANN** Artificial Neural Network

**SNN** Spiking neural network

**GPU** Graphics Processing Unit

**SOP** Synaptic Operation

**IF** Integrate and Fire

**LIF** Leaky-integrate-and-fire

**LSM** Liquid State Machine

**HH** Hodgkin–Huxley

**NLP** Natural Language Processing

**LQG** Linear Quadratic Gaussian

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### Introduction

Provide a general introduction to the area for the degree project. Use references!

Link things together with references. This is a reference to a section:

The human brain is a brilliant computing unit comprised of around 86 billion[5] neurons. Each of these neurons can have thousands of connections to other neurons. Between these connections, information travels trough the network as electrical impulses that interact with the neurons own electrical potential. With this network, the human brain is capable of performing vastly different and complex tasks. Machines and robots beat raw human computing power by several orders of magnitude, yet some tasks are next to impossible to solve by machines and classical algorithms alone. Moreover many machine implementations lack the speed, precision or flexibility of the human counterpart.

Researchers tried to remedy this by mimicking the brain's internal network structure to solve problems deemed unsuitable for classic algorithms.

Artificial Neural Networks (ANNs) have shown a great success in previously hard to solve problems.

Furthermore with the newer more biologically inspired networks we are able to solve a broader range of problems. One aspect of these are Graphics Processing Units (SNNs) which simulate the discrete spiking behaviour of natural neural networks. We set out to design such a network in order to control a linear system.

Maybe seperate this in intro and background

ome LSTM

orks or

A variety of different architectures for these ANNs have been proposed, with the most prevalent design being a feed-forward network. In these networks, information travels only in one direction and is not propagated by spikes but gradients usually set in [0,1] or [-1,1]. These ANNs have made impressive progress in the fields of image recognition, autonomic driving, medical diagnosis [24] or Natural Language Processing (NLP) (using Transformers [26]).

This abstract representation bears advantages e.g in modelling and implementation but also gives away some key features of the human brain. Due to the information travelling only towards the output, feed-forward networks cannot build a memory or easily process temporal data. Recurrent models exist which allow for memory and sequential data input but loose some of the advantages compared to the Feed-Forward due to its increased complexity.

A third generation[21] of network architectures has risen, which aims to be even more biologically plausible. Inspired from nature, they implement spiking behaviour and recurrence found in the human brain. This newer form of SNN is as powerful as the classic feed-forward but suited for temporal data.

While state of the art feed-forward networks are still outperforming SNNs, in some cases modern SNNs are on par or more performant with older feed-forward implementations. This comes with the added benefit of consuming much less power. Usually deep ANNs are run on Graphics Processing Units (GPUs), especially for training, in which the energy consumption can exceed 300W for modern chips¹. The brain however is estimated to only consume about 20W [8] for immense computing capacity. Accompanying the SNN with neuromorphic hardware can yield a similar boost in efficiency with processors energy consumption in the pJ per Synaptic Operation (SOP)[16] offering a huge potential.

#### This is a seperator

Present the background for the area. Give the context by explaining the parts that are needed to understand the degree project and thesis. (Still, keep in mind that this is an introductory part, which does not require too detailed description).

Use references<sup>2</sup>

Detailed description of the area should be moved to Chapter 2, where detailed

<sup>&</sup>lt;sup>1</sup>e.g. a NVidia RTX 3090

<sup>&</sup>lt;sup>2</sup>You can also add footnotes if you want to clarify the content on the same page.

information about background is given together with related work.

This background presents background to writing a report in latex.

Example citation [Jones2017] or for two authors: [Jones2017, Liu2017]

Look at sample table 1.0.1 for a table sample.

Table 1.0.1: Sample table. Make sure the column with adds up to 0.94 for a nice look.

SAMPLE	TABLE
One	Stuff 1
Two	Stuff 2
Three	Stuff 3

Boxes can be used to organize content

```
Development environment for prototype
```

#### Operating systems

computer: Linux - kernel 4.18.5-arch1-1-ARCH

android phone: 8.1.0

Build tools

exp (build tool): version 55.0.4

. . .

#### 1.1 Problem

Now list the goal: We want to do it for DS and check how good they are. Then method and then work. Take from below

Conventional Feed-Forward neural networks do are not designed to work with temporal data. They are static input output machines. This makes sense in the context of certain tasks but at the same time limits the power of these networks. There are workarounds to fit temporal data, for example by sampling the previous values back into the network or to quantize the whole input if the complete time horizon is available. For example with audio data the file is segmented into parts and fed into the network.

give some i

Find refs for that.

#### find refs for that.

more refs.

This is often done when ANNs are proposed for the control of LTI systems.

Secondly when it comes to simulation of biologic dynamic systems usually LQG control is used. LQG has been used widely for modelling biological movements and control.

#### this is another smaller separator

SNNs are inherently designed in time since neural impulses are integrated over time. This makes the use for temporal data natural.

The use of snn is online, can deal with much noise and offers an alternative way to reason for motor movement.

We hope that with SNN we have even better performance

From very biological to very abstract there have been many proposals

Cost performance trade off.

Spiking networks have gained similar or exceeding performance compared to the artificial one in some areas-> refs

Key advantage is in the temporal dimensional gain.

One field they are suited well is the control of dynamic systems

In this thesis we use a spiking neural network to control a linear dynamic system

The usual way to simulate biological dynamic systems is using LQG control -> ref

I believe because of the energy minimization

So we can compare them with usual NN and control in terms of performance... i guess

We start by giving an intro into spiking neural networks

Then spiking neural networks for dynamic systems

After control theory with SNN and maybe regular LQG control

Lately the learnign of SNNs for the control of dynamic system

#### Further work:

Maybe learning methods to control nonlinear dynamic systems

Maybe we can even do the adverserial attack to try to screw with the network.

Implement this on neuromorphic hardware

#### Problem:

4

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nonlinear s in gy. Maybe

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e/can pise but i ve yes.

\_\_\_\_

Problem is that it is unnatural for classic NN to use temporal data.

They usually quantize it and make a big input layer -> ref

There are recurrent networks but ... they need to have smth bad as well

The LQG control is also not great for some reason I need to find

There are many spkiking network archetypes like poisson and GLm and balanced

Also problem is that for some spiking networks learning rules could be hard to come by.

There are many prospects though as for example .....->refs

Also usually learning rules smth of an inverse and that the brain does not have or do I believe arvind said

#### Method:

We use a SNN to to control any arbitrary DS

Balanced networks show a some key motives seen in the brain like poisson distribution and smth else ->ref

The SNN is to be trained with a STDP rule

Then compared to optimal weights

Then investigated about robustness and other things as many before

One part of robustness is trying to get the most essential nodes of the snn to function well.

Then we have the potential to find a classic nn and train it with that ???

With that out of the way we can compare the performance of all the methods.

Then we could study the usability for biological interpretation.

Maybe even train time over performance or smth whatever

#### Work:

Explain the controller method aka what the math of the controller

In method explain the balanced and the derivation

In work summarize the implementation

Same for the conventional NN

Summarize the training method

Explain and derive the training method in method

#### **Results:**

To everthigh mentioned in method for performance and so on Answer the questions of the problem!!!!

NN have excelled at many fields
Fields where they are not fit
aka temporal data
They have ways to compromise on that
-> reference
Spiking nn inherently temporal
more natural choice
However they also have problems
like the following:::: reference!!

#### 1.2 Purpose

The purpose of the degree project/thesis is the purpose of the written material, i.e., the thesis. The thesis presents the work / discusses / illustrates and so on.

It is not "The project is about" even though this can be included in the purpose. If so, state the purpose of the project after purpose of the thesis).

Probably delete as a own paragraph but mention smth like that.

#### 1.3 Goal

The goal means the goal of the degree project. Present following: the goal(s), deliverables and results of the project.

exact fications. example collability The goal of this project is to create a SNN that can control any given linear Dynamic System (DS). Furthermore should the Neural Network (NN) be robust against failing neurons or connections to some degree. With this we can investigate to find the smallest SNN with acceptable performance. Its performance should be comparable or supersede conventional control systems, like Linear Quadratic Gaussian (LQG)

control, or NNs. We expect better results to conventional NNs because of the SNN's natural way to use temporal data. For the SNN itself we desire similarities to the brain, such as high precision or Poisson distributed spiking. To mimic the brain's learning, we want to use local training rules that are biologically plausible. The network should be converge to the optimal parameters. This requirement would allow us to give a justified measure on how close we are replicating the brain's control power compared to our artificial implementation in specific circumstances.

#### 1.4 Benefits, Ethics and Sustainability

Describe who will benefit from the degree project, the ethical issues (what ethical problems can arise) and the sustainability aspects of the project.

Use references!

#### 1.5 Methodology

Introduce, theoretically, the methodologies and methods that can be used in a project and, then, select and introduce the methodologies and methods that are used in the degree project. Must be described on the level that is enough to understand the contents of the thesis.

Use references!

Preferably, the philosophical assumptions, research methods, and research approaches are presented here. Write quantitative / qualitative, deductive / inductive / abductive. Start with theory about methods, choose the methods that are used in the thesis and apply.

Detailed description of these methodologies and methods should be presented in Chapter 3. In chapter 3, the focus could be research strategies, data collection, data analysis, and quality assurance.

We build a SNN for a control problem and check it for performance as mentioned above. In addition we design a conventional controller and compare the result. IF we have the time for it we put a conventional NN to it too. We see the performance compared to the others and look at the specs we mentioned above. The SNN is trained

What do we else want like the brain. Mayb low spike count? And what can we do? Also References!

This is ever more to asl than from a conventional NN, Say in method best there it has already been proven if I not mistake

sounds vag

by learning using STDP rule. We can compare the learned weights with the optimal weights when we have our own optimal controller/ we simulate our trajectory. For our approach we use a balanced spiking network.

#### 1.6 Stakeholders

Present the stakeholders for the degree project.

#### 1.7 Delimitations

Explain the delimitations. These are all the things that could affect the study if they were examined and included in the degree project. Use references!

#### 1.8 Outline

In text, describe what is presented in Chapters 2 and forward. Exclude the first chapter and references as well as appendix.

# <Theoretical Background>

In this chapter, a detailed description about background of the degree project is presented together with related work. Discuss what is found useful and what is less useful. Use valid arguments.

Explain what and how prior work / prior research will be applied on or used in the degree project /work (described in this thesis). Explain why and what is not used in the degree project and give valid reasons for rejecting the work/research.

Use references!

#### 2.1 Use headings to break the text

Do not use subtitles after each other without text in between the sections.

#### 2.2 Related Work

You should probably keep a heading about the related work here even though the entire chapter basically only contains related work.

Here just what has been done for each of the headlines

Previous efforts were already made to control dynamic systems with SNNs.

List here also efforts with other concepts apart from Balanced Networks

Neural networks in general spiking neural networks and their differences and what

they are better for. neuron models, iwazishi neuron and maybe one more mein neuron model und warum ich es ausgewaelt habe: einfach zu implementieren. Bereits fuer dynamische systeme verwendet, Nachteile dieses modells. Vlt vergleich mit einem anderen modell. Ganz kurzer ausflug in die regelung von dynamischen systemen.

What is a neural network? -> not here ref a paper. kurze erkl'rung in der einfuerung in der einfuhurng vlt auch hodgekin huxley erwaehen :)

#### 2.3 Dynamic systems

#### 2.4 autoencoder

#### 2.5 Neuron model

#### 2.5.1 Biological Neuron model

The most biologically accurate model of neuron spiking is the Hodgkin-Huxley (HH) model. The HH-model considers the neuron with its ion channels. The membrane acts as a capacitance and the travelling ions in each ion channel contribute a current to the overall membrane potential. These ion gates are voltage dependent and are defined positive in direction out of the cell.

A particular ion channel for ion X can be modelled as

$$I_X = g_X \cdot (V - V_X) \tag{2.1}$$

These currents are summed summed for the different ion channels in question, most commonly for Sodium, Potassium and a leak current. In reality there are a plethora of different channels and channel properties<sup>1</sup>. The  $V_X$  are the equilibrium potentials for each of the channels and can be computed using the Nernst equation [19].

$$C\frac{dV}{dt} = g_{Na} \cdot (V - V_{Na}) + g_K \cdot (V - V_K) + g_l \cdot (V - V_l)$$
 (2.2)

Do model the voltage dependency of the ion channels, the conductances are described with gating variables, usually called n, h and g for Na-Activation, Na-Inactivation and K-activation respectively. One gating variable is set between [0,1] and models the

ence to a ography.

<sup>&</sup>lt;sup>1</sup>See channelpedia.epfl.ch for an extensive list

permeability of said gate. Multiple gates are used to fit to each ion channel in order to match experimental data and the model behaviour.

Gates have first order dynamics of the form

$$\frac{dn}{dt} = \alpha_n (1 - n) - \beta_n n \tag{2.3}$$

for e.g the n gate. The other gates' dynamics are analogous. The functions  $\alpha$  and  $\beta$  are voltage but not time dependent. The discussion of initial values as well as functions for  $\alpha_p$ ,  $\beta_p$  p=(n,h,m) can be found in [12] or [19]. The gates for each ion channel's conductance are found to be

$$g_{Na} = \bar{g}_{Na}n^4$$
 
$$g_K = \bar{g}_K m^3 h$$
 (2.4)

and give form to the final model

$$\begin{split} C\frac{dV}{dt} &= I(t) - \bar{g}_{Na}n^4(V - V_{Na}) - \bar{g}_Km^3h(V - V_K) - g_L(V - V_L) \\ \frac{dn}{dt} &= (1-n)\alpha_n(V) - \beta_nn(V) \\ \frac{dm}{dt} &= (1-m)\alpha_m(V) - \beta_mm(V) \\ \frac{dh}{dt} &= (1-h)\alpha_h(V) - \beta_hh(V) \end{split} \tag{2.5}$$

We did not define a gate for the leak term as it is assumed constant.

#### 2.5.2 "IF and LIF"

In contrast of the HH model in eq. (2.5), the simplest models of neurons are the Integrate and Fire (IF) and Leaky-integrate-and-fire (LIF) models.

**IF Neurons** IF Neurons, as the name implies, integrate the incoming current over time.

$$\frac{dV(t)}{dt} = \frac{1}{C}I(t) \tag{2.6}$$

The membrane voltage is governed by the incoming current spikes of connected neurons and the membrane capacitance. The neuron potential does not change without a change of input current and thus presents as a perfect integrator of the input.

**LIF Neurons** In contrast to that the LIF neuron contains a leak term on the RHS which brings the voltage back to its resting potential over time. The model can be expressed as

$$\tau \frac{dV(t)}{dt} = -(V(t) - E_r) + RI(t), \tag{2.7} \label{eq:2.7}$$

where  $\tau=RC$  is the time constant the composed of the membrane resistance R and the membrane capacitance C and the resting potential  $E_r$ . In the absence of input I(t) the voltage settles on the membrane potential  $E_r$ .

The input I(t) encapsulates external inputs as well as a sum of Dirac functions indicating a spiking neuron

$$I(t) = \sum_{k} \delta(t - t^k) \tag{2.8}$$

and  $t_k$  being the time of the k-th spike. When the membrane voltage exceeds the threshold potential  $\bar{v}$ , a spike is sent out by the neuron and the voltage sets back to its reset voltage  $v_{res}$ .

is not truly ct. Forgot ats, but at ame time when there nore than 1

#### 2.5.3 Izhikevich Neuron

While the above models deliver a useful and cheap simplification, they lack in accuracy. The Izhikevich model [17] of the neuron tries be the of both worlds in terms of efficiency and accuracy. It is comprised of 2D ODEs with the membrane potential v as

$$\begin{split} \frac{dv}{dt} &= 0.04v^2 + 5v + 140 - u + I(t) \\ \frac{du}{dt} &= a(bv - u). \end{split} \tag{2.9}$$

With the chosen factors, the neuron experiences a spike when  $u \geq 30 \text{mV}$ , in which case the neuron resets to

$$u \leftarrow u + d$$

$$v \leftarrow c$$
(2.10)

The parameters describe a scale of recovery, b sensitivity, c the reset potential of v and d the reset of variable u. Depending on these parameters one can achieve different behaviours of the neuron e.g. regular spiking, fast spiking and low threshold spiking to name a few [17].

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could be
ded on.

#### 2.6 Neural Networks

#### 2.6.1 Biological Neural Network

#### 2.6.2 Artificial Neural Networks

#### 2.6.3 Spiking Neural Networks

A spiking Neural network is one step closer to a biologic representation of a brain. Instead of conveying information using a gradient in conventional NNs, information is propagated using discrete spikes of excitation, similar to biological neurons. Hereby one can distinguish between several ideas of implementation.

#### 2.6.4 Poisson Networks

Poisson networks are built around the idea that information is encoded in the firing rate of a neuron. The precise timing of a spike is essentially meaningless[7]. This makes a strong contrast to the approach chosen in this paper, where every spike is timed exactly to minimize a cost function. The encoding of a value, e.g. four, is set by endowing the input neurons with a Poisson point process with a suitable encoding rate  $r_i$ [9].

One typically uses probabilistic stimuli because observations in the spiking of the human brain do are different in a trial by trial basis.

Input spikes are travelling through the recurrent network with weighted connections. The decoding is done by counting the spikes of output neurons over a certain time window. The time window plays a crucial rule in the decoding. If it is set smaller, spatio temporal patterns can be captured which can convey information about the input. Equally the sensitivity to noise becomes greater. If the time window is set to large, the firing patterns are lost though the impact of random spikes is reduced.

Theoretically using a lot of spikes is unproblematic and with large spike counts neuromorphic hardware is still much more energy efficient than deep neural networks if one seeks to deploy it.

The connection weights are subject to change over the learning/training period[2]. This approach however has some conceptual problems. Firstly, this approach has the problem that responses are limited by the time window the spikes are counted[3]. This

Make clear distinction between forward nn and ann. B apparently are not the same!

The main difference i the motion time

Maaybe add that our approach d not rule rat out comple

Write that the error scales prett badly with squareroot and therefo we need a l of spikes to

get certain

means that the rate decoding is to slow to capture the fast travelling information and another needs to be another faster way to transmit information. However it has been shown that the firing rate does convey information about the stimuli's magnitude [1]. The second problem is that due to the Poisson process one needs more spikes to represent an average firing rate. An action potential consumes a lot of the cells energy[4], thus making it unfeasible to use a large number of spikes if one tries to model the brain. Evolution has found a better way to transmit information.

Although the above mentioned problems, rate encoded SNNs have seen interest by research. A big hurdle of deploying SNNs is the lack of performant learning algorithms. For this there efforts have been made to train recurrent or convolutional ANNs using backpropagation and afterwards convert the trained network to a SNN using rate encoding[11][10].

#### 2.6.5 Liquid state machines

write how the offline computing is pretty bad for brain things, but good for chess for example. The online computing is what the brain does and it is not yet as developed. add the TU graz paper to refs and some of it's references too, for example nr. 19

One alternative method has been the use of Liquid State Machine (LSM) or more general Reservoir computing.

The term Reservoir computing was introduced by Benjamin Schrauwen and describes a general group of recurrent network approach[27].

The "reservoir" is a non-linear map from input to outputs that combines the input in various, even random ways. These contain but are not limited to sums, differences, multiplications, division and exponentiation. In general the output  $\mathbf{x}(t)$  is higher dimensional that the input  $\mathbf{v}(t)$ , in order to allow for sufficient variety in the mapping. The output of the reservoir, which is usually treated as a black box, is fed in a linear decoder in order to retrieve the desired output signal.

The liquid can be made of any system that fulfils two properties.

- Non-linear nodes of computation
- Fading memory

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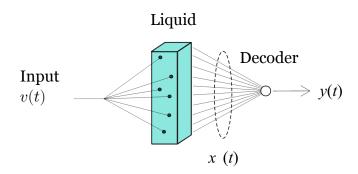


Figure 2.6.1: Abstract idea of Reservoir Computing. Adapted from [20]

To these points it is usually set for the system to be time invariant[20]. A reservoir can be a mathematical abstract formulation or physical object, e.g. a literal bucket of water [25].

After the choice of "liquid" in the reservoir is fixed, its dynamics are not altered. Only the linear decoder is trained to return the desired decoded output. This is a considerable time saver since the training of recurrent networks is expensive. On the contrary the linear decoder can be learned relatively cheaply.

A reservoir computer is called a LSM if one chooses a spiking neural network as the reservoir. The requirements mentioned above are fulfilled by the recurrent structure to retain information of the neurons and its non-linear spiking behaviour.

LSMs are capable of computing any dynamical system of any order of the form of

$$z^{(n)} = G(z, z^{(1)}, z^{(2)}, \dots, z^{(n-1)}) + u \tag{2.11} \label{eq:2.11}$$

given a sufficiently large liquid and a suitable feedback and decoder[23]. The systematic structure can be in fig. 2.6.2. The feedback K(x,u) is a function of the dynamical system input u(t) and the output x(t). The result of K(x,u) is fed back replaces the previous input v(t) into the Liquid. The decoder h(x) is not linear but can be simplified to be in a cost-performance trade-off when using a sufficiently large Liquid.

#### 2.6.6 Balanced Networks

The idea of tightly balanced spiking networks was first proposed by Boerlin et al.[6]. It uses predictive coding in combination with spikes to simulate arbitrary linear

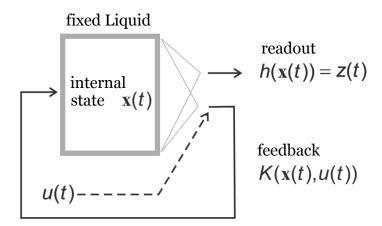


Figure 2.6.2: Adding suitable feedback allows LSMs to be universal approximator. Adapted from [22]

the ref to hapter systems. The technical derivation will be described in chapter. The approach defines a cost function measuring the networks' accuracy in addition with regularization terms that moderates the spiking behaviour. Using a greedy algorithm this cost function determines the voltage threshold and therefore the neurons' spiking behaviour.

For each neuron voltage can be understood as a projection of the global system error to a local error.

Therefore the spiking rule is set to fire if the Voltage of a neuron becomes to large in order to reset the neuron voltage and reduce part of the system error.

Balanced networks differ from the previous rate encoding in that excitation and inhibition is closely tracked. In rate encoded networks both inhibitory and excitatory spikes are received by a single neuron. An change of the variable is then governed by which type dominates. Here a rate coding is also used, however in combination with instantaneous decoding[18].

some more ral stuff

The derivation of its behaviour is adopted from [6],[14] and [15].

The derivation of the method used can be put to method or work/ here we can explain using only words and compare to the other methods and why we chose this one etc

The derivation of the balanced spiking network follows the derivation found in [6] and

[13]. The goal is to describe a dynamical system of the form

$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{c}(t) \tag{2.12}$$

with J state variables. The estimating is done by leaky integration of spiking trains  $\mathbf{o}(t)$  in

$$\dot{\hat{\mathbf{x}}} = -\lambda_d \hat{\mathbf{x}} + \mathbf{\Gamma} \mathbf{o}(t). \tag{2.13}$$

 $\Gamma$  is a given Matrix of size  $\mathbb{R}^{J\times N}$ , N being the number of neurons, with the different connection weights between the neurons. This matrix is given as initial and can be optimized by training later on.

In addition to the estimate  $\hat{\mathbf{x}}$  we define a spiking rate variable  $\mathbf{r}$  following the dynamics of

$$\dot{\mathbf{r}} = -\lambda_d \mathbf{r} + \lambda_d \mathbf{o}(t). \tag{2.14}$$

The rate variable is connected to the state vector in the

The spikes are calculated by minimizing a cost function. A spike is fired if it minimizes the cost function that tracks the error between the true and estimated value over time

$$E(t) = \int_0^t \|\mathbf{x}(u) - \hat{\mathbf{x}}(u)\|_2^2 du.$$
 (2.15)

The cost function integrates the error between the estimate and the real dynamic variable as well as regularization terms.

$$E(t) = \int_0^t \left( \|\mathbf{x}(u) - \hat{\mathbf{x}}(u)\|_2^2 + \nu \|\mathbf{r}(u)\|_1 + \mu \|\mathbf{r}(u)\|_2^2 \right) du \tag{2.16}$$

These two regularization terms are added to discourage undesired behaviours.

The first was termed "ping-pong" effect and is described in the supplementary material of [6]. Tp understand the issue, we imagine a minimal network consisting of 2 neurons with equal kernel but opposite sign.

The second regularization comes into play when there are kernels with different magnitude. Kernels with small kernel magnitude reach their threshold sooner and therefore fire more frequently. In the extreme case, only small number of neurons fire rapidly while the majority remains idle. By penalizing the rate in the 2-norm it forces

Write bette the ping po effect! May later the right to explain

e? Here,

all?

e appendix

the network to spread the firing among the whole network.

The dynamic variable x is tracked by firing spikes in when the defined "pseudo voltage" of a neuron surpasses its threshold. The voltage for each neuron is defined by

$$V_i(t) = \mathbf{\Gamma}^T(\mathbf{x}(t) - \hat{\mathbf{x}}(t)) - \mu \lambda_d r_i(t) \quad i = 1 \dots N. \tag{2.17}$$

For negligible quadratic cost  $\mu$  the voltage can be understood as measure of the error projected on  $\Gamma_i$ . The explicit derivation of the above equation is found in [6] and will be adapted. The voltage definition and the threshold definition

$$T_{i} = \frac{\nu \lambda_{d} + \mu \lambda_{d}^{2} + \left\| \mathbf{\Gamma}_{i} \right\|^{2}}{2}$$
 (2.18)

result from integrating the cost function eq. (2.16) over time step  $\epsilon$ . Then the condition described earlier fires a spike if the cost gets lowered. If there is no spike fired, the rate and estimated state variable in eq. (2.13) and eq. (2.14) respectively behave as

$$\dot{\hat{\mathbf{x}}} = -\lambda_d \hat{\mathbf{x}}$$
 (2.19)  $\dot{\mathbf{r}} = -\lambda_d \mathbf{r}$ 

and therefore decay exponentially with  $e^{-\lambda_d t}$ .

If a spike is fired, the inhomogeneous solution is found by variation of constants in eq. (2.14) to

$$\begin{split} r_i^h &= c_i(t)e^{-\lambda_d t}\\ c_i'(t)e^{-\lambda_d t} - c_i(t)\lambda_d e^{-\lambda_d t} &= -\lambda_d c_i(t)e^{-\lambda_d t} + \delta(t-t_i^k)\\ c_i'(t) &= \delta(t-t_i^k)e^{\lambda_d t}\\ c_i(t) &= e^{\lambda_d t_i^k} \boldsymbol{H}(t-t_i^k) \end{split} \tag{2.20}$$

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where H(t) denotes the Heaviside step function. It can been seen that at the time of firing the spike adds a decaying exponential to the rate variable. Similarly it adds a column of the previously defined connection matrix  $\Gamma$  to the state vector. Thus we can now compare the effects on cost function eq. (2.16) and compare its impact. The integral is approximated by a greedy optimization method such that for very small time steps  $\epsilon$  the exponential decays  $e^{-\lambda_d t - t_i^k} \approx 1$ . The greedy optimization is necessary since the unpredictable firing due to noise makes it impossible to predict future spikes. After

ember read where the noise this step the rewriting the terms and using the defintions of the voltage and threshold we arrive at the critera to spike when

$$V_i > T_i \quad i = 1 \dots N$$
 (2.21)

#### **Neuron Voltage**

As mentioned above, a neuron spikes if it meets the condition eq. (2.21). But so far we skipped over the dynamics how neuron voltage evolves over time. We start by defining the left pseudo-inverse of our output matrix  $\Gamma$ 

#### find a coherent name for the matrix

$$\mathbf{L} = \left(\mathbf{\Gamma}\mathbf{\Gamma}^T\right)^{-1}\mathbf{\Gamma} \tag{2.22}$$

such that  $\mathbf{L}\mathbf{\Gamma}^T = \mathbf{I}$ .

Next we take the derivative of eq. (2.17) and arrive at

$$\dot{\mathbf{V}}(t) = \mathbf{\Gamma}^T \left( \dot{\mathbf{x}}(t) - \dot{\hat{\mathbf{x}}}(t) \right) - \mu \lambda_d \dot{\mathbf{r}}(t). \tag{2.23}$$

We now use the pseudo-inverse to rewrite the voltage equation eq. (2.17) as

$$\begin{aligned} \mathbf{V}(t) &= \mathbf{\Gamma}^T(\mathbf{x}(t) - \hat{\mathbf{x}}(t)) - \mu \lambda_d \mathbf{r}(t) \\ \mathbf{L} \mathbf{V}(t) &= (\mathbf{x}(t) - \hat{\mathbf{x}}(t)) - \mu \lambda_d \mathbf{L} \mathbf{r}(t) \end{aligned} \tag{2.24}$$

We now replace the derivative terms in eq. (2.23) with their respective equations eq. (2.12) to eq. (2.14). Lastly we set

#### 2.6.7 Balanced networks as a controller

Here describe the derivation of the controller we set out to design

#### 2.6.8 Learning: SGD and STDP

Key to give any NN the ability to solve a task, it is integral to learn/train the network. The adaption of synapse weights is necessary to accomplish any functionality based on the underlying data[28]. There are various ways to train a network.

The most fundamental distinction can be made between supervised, unsupervised and reinforcement learning rules. One needs to remember that ANNs and SNNs require completely different learning algorithms because of their different transport of information.

For a review

#### **Supervised Learning methods**

Gradient based methods require differentiability and therefore continuity, thus are only applicable for ANNs.

Explain gradient methods. The derivative of the weights and biases is used for the derivative of the cost function. Efficient methods for building the derivative exists. With reference!

#### **Unsupervised Learning methods**

**STDP** 

#### Reinforcement learning

Here explain the conpects for each of the NNs Give references for the STDP variances

# <Engineering-related content,</p>Methodologies and Methods>

Describe the engineering-related contents (preferably with models) and the research methodology and methods that are used in the degree project.

Most likely it generally describes the method used in each step to make sure that you can answer the research question.

#### 3.1 Engineering-related and scientific content:

Applying engineering related and scientific skills; modelling, analysing, developing, and evaluating engineering-related and scientific content; correct choice of methods based on problem formulation; consciousness of aspects relating to society and ethics (if applicable).

As mentioned earlier, give a theoretical description of methodologies and methods and how these are applied in the degree project.

was ist meine research question?

zusammensetzung von den beiden systeme: dynamisches system und neuronales netz. mehr oder weniger die herleitung kopieren aus dem paper. Dann mit learning von den gewichten.

Here I describe what how it needs to be done. So this is the place for the derivation The concept and the process whatever that means Later there comes the how I implemented

it. Here is what we needs to be implemented.

Here very detailed explanation of the Balanced network for this problem

Very detailed way for the regular NN for this problem Basics of the controller design

used in this comparison aka LQG controller

Method of learning the weights for the SNN Method of comparison

### <The work>

Describe the degree project. What did you actually do? This is the practical description of how the method was applied.

### 4.1 Creating the SNN

How do we make the SNN MAtlab Balanced spiking network (say why to use that ) maybe pseudo code Ideally some theorem (convergence???) Simulation? nein kommt in den naechsten part

### 4.2 Creating the NN

#### 4.3 Creating the regular Controller

## <Result>

Describe the results of the degree project.

### <Conclusions>

Describe the conclusions (reflect on the whole introduction given in Chapter 1).

Discuss the positive effects and the drawbacks.

Describe the evaluation of the results of the degree project.

Describe valid future work.

The sections below are optional but could be added here.

#### 6.1 Discussion

- 6.1.1 Future Work
- 6.1.2 Final Words

# **Todo list**

Provide a general introduction to the area for the degree project.	Use
references!	
Link things together with references. This is a reference to a section:	1
Maybe seperate this in intro and background	1
cite some LSTM networks or others	2
This is a seperator	2
Now list the goal: We want to do it for DS and check how good they are.	Гhen
method and then work. Take from below	3
give some refs	3
Find refs for that	3
find refs for that	3
find more refs	4
Add that LQR made many improvements but is also trash because of	f the
matrix inversion, and nonlinear things in biology. Maybe also that it	is an
offline thing? Not sure whether thats true or if it is already online/ca	n do
noise but i believe yes	4
this is another smaller separator	4
give exact specifications. For example controllability	6
What do we else want like the brain.Maybe low spike count? And what	t can
we do? Also References!	• • • 7
This is even more to ask than from a conventional NN, Say in method bcs t	:here
it has already been proven if I am not mistaken	7
sounds vague	7
List here also efforts with other concepts apart from Balanced Networks	9
Add a reference to a monography.	10

This is not truly correct. Forgot weights, but at the same time only when there	
are more than 1 neuron	12
Maybe shitty explanation, which could be extended on	12
Make clear distinction between forward nns and ann. Bcs apparently they are	
not the same!	13
The main difference is the motion of time	13
Maaybe add that our approach does not rule rate out completely	13
Write that the error scales pretty badly with the squareroot and therefore we	
need a lot of spikes to get certain precision. I do not understand how and	
why. For regular timed spikes we the error scales linearly so we need many	
fewer spikes. But mention the CV value and explain it. Ref are the boerlin	
and nature paper. With that explain the pro and con like noise resistance	
bcs of many spikes and the inefficiency of the rate encoding	13
Maybe I can find a stat on how much more efficient neuromorphic hardware	
really is	13
sounds a bit bad	13
Maybe find a reference that the power consumption is really low even though	
the use rate based encoding	14
Say that the CV(explain what it is :sigma/mu and what it says) value is shit	
so you you need a ton of spikes. Then say that it has some use and some	
performance when you transmit from an ann and move it to a snn with	
neuromophic hardware. USe the papers from the nature paper forward to	
the right.	14
write how the offline computing is pretty bad for brain things, but good for	
chess for example. The online computing is what the brain does and it is not	
yet as developed. add the TU graz paper to refs and some of it's references	
too, for example nr. 19	14
Add the ref to the chapter	16
Add some more general stuff here!	16
The derivation of the method used can be put to method or work/ here we can	
explain using only words and compare to the other methods and why we	
chose this one etc	16
Write better the ping pong effect! Maybe later	17
find the right place to explain that!	18

#### CHAPTER 6. < CONCLUSIONS>

Where? Here, in the appendix of at all?	18
explain notation of spike time constant with i and k	18
Remember that i read somewhere that the noise is necessary. Maybe mention	
that here too. And find the reference	18
find a coherent name for the matrix	19
Put this reference in and say its is copied partly from them	19
Explain gradient methods. The derivative of the weights and biases is used	
for the derivative of the cost function. Efficient methods for building the	
derivative exists. With reference!	20

If you are using mendeley to manage references, you might have to export them manually in the end as the automatic ways removes the "date accessed" field

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# Appendix A

# **First Appendix**

This is only slightly related to the rest of the report

# **Appendix B**

# **Second Appendix**

this is the information