

UNIVERSITAT POLITÈCNICA DE CATALUNYA

MASTER THESIS

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# State Observers Design for PEMFC Systems

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*Dedicated to ...*



# *Acknowledgements*

Acknowledgements

# *Abstract*

Abstract

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# Abbreviations

<b>AFC</b>	<b>A</b> lkaline <b>F</b> uel <b>C</b> ell
<b>BD</b>	<b>B</b> ack <b>D</b> iffusion
<b>CL</b>	<b>C</b> atalyst <b>L</b> ayer
<b>DC</b>	<b>D</b> irect <b>C</b> urrent
<b>CHP</b>	<b>C</b> ombined <b>H</b> eat and <b>P</b> ower
<b>DMFC</b>	<b>D</b> irect <b>M</b> ethanol <b>F</b> uel <b>C</b> ell
<b>EOD</b>	<b>E</b> lectro- <b>O</b> smotic <b>D</b> rag
<b>GDL</b>	<b>G</b> as <b>D</b> iffusion <b>L</b> ayers
<b>HHV</b>	<b>H</b> igher <b>H</b> eating <b>V</b> alue
<b>LHV</b>	<b>L</b> ower <b>H</b> eating <b>V</b> alue
<b>LMI</b>	<b>L</b> inear <b>M</b> atrix <b>I</b> nequality
<b>MCFC</b>	<b>M</b> olten <b>C</b> arbonate <b>F</b> uel <b>C</b> ell
<b>MEA</b>	<b>M</b> embrane <b>E</b> lectrode <b>A</b> ssembly
<b>MIMO</b>	<b>M</b> ultiple- <b>I</b> nter and <b>M</b> ultiple- <b>O</b> utput
<b>PAFC</b>	<b>P</b> hosphoric <b>A</b> cid <b>F</b> uel <b>C</b> ell
<b>PDE</b>	<b>P</b> artial <b>D</b> ifferential <b>E</b> quation
<b>PEM</b>	<b>P</b> roton <b>E</b> xchange <b>M</b> embrane
<b>PEMFC</b>	<b>P</b> roton <b>E</b> xchange <b>M</b> embrane <b>F</b> uel <b>C</b> ell
<b>SISO</b>	<b>S</b> ingle- <b>I</b> nter and <b>S</b> ingle- <b>O</b> utput
<b>SMC</b>	<b>S</b> liding <b>M</b> ode <b>C</b> ontrol
<b>SOFC</b>	<b>S</b> olid <b>O</b> xide <b>F</b> uel <b>C</b> ell
<b>STA</b>	<b>S</b> uper- <b>T</b> wisting <b>A</b> lgorithm



# Nomenclature

## Roman letters

$A$	Electrode area	$\text{m}^2$
$C$	Volumetric capacitance	$\text{C V}^{-1} \text{ m}^{-3}$
$c$	Concentration	$\text{mol m}^{-3}$
$D$	Diffusion coefficient	$\text{m}^2 \text{ s}^{-1}$
$D_{i,k}^{eff}$	Diffusion coefficient	$\text{m}^2 \text{ s}^{-1}$
$D_W$	Self-diffusion coefficient of water in the membrane	$\text{m}^2 \text{ s}^{-1}$
$E$	Electrical potential	V
$f^V$	Surface enlargement factor	
$h$	Molar enthalpy	$\text{J mol}^{-1}$
$I$	Electrical current	A
$i$	Current density	$\text{A m}^{-2}$
$i_0$	Exchange current density	$\text{A m}^{-2}$
$L$	Length	m
$L_{x,y,z}$	Length through the $x$ , $y$ or $z$ coordinates	m
$M$	Molar mass	$\text{g mol}^{-1}$
$\dot{n}$	Molar flux density	$\text{mol m}^{-1} \text{ s}^{-1}$
$n$	Number of electrons per molecule of $\text{H}_2$	
$n_{Vol}$	Number of discretization volumes	
$P$	Electrical power	W
$p$	Pressure	Pa
$q$	Charge	Coulombs $\text{mol}^{-1}$
$r$	Reaction rate	$\text{mol m}^{-2} \text{ s}^{-1}$
$t$	Time	s
$t_W$	Transport number of water in the membrane	

$T$	Temperature	K
$U$	Voltage	V
$u$	Specific internal energy	J kg <sup>-1</sup>
$v$	Flow velocity	m s <sup>-1</sup>
$W_{el}$	Electrical work	J mol <sup>-1</sup>
$x$	Space coordinate	m
$X$	Ion exchange capacity	mol kg <sup>-1</sup>
$y$	Space coordinate	m
$z$	Space coordinate	m

### Greek letters

$\alpha$	Heat transfer coefficient	W m <sup>-2</sup> K <sup>-1</sup>
$\delta$	Thickness of layer in y-direction	m
$\kappa$	Electrical conductivity of the membrane	$\Omega^{-1}$ m <sup>-1</sup>
$\lambda$	Heat conductivity	W K <sup>-1</sup> m <sup>-2</sup>
$\Lambda$	Water content	$\frac{N(H_2O)}{N(\text{polymer})}$
$\mu$	Electrochemical potential	J mol <sup>-1</sup>
$\xi$	Mole fraction	
$\rho$	Density	kg m <sup>-3</sup>
$\Phi$	Electrical potential	V

### Subscripts

$i$	Component mass index on anode and cathode sides
$in$	Input flux
$j$	n-th discretization volume
$r$	Chemical reaction term
$ref$	Reference value





**Superscripts**

$A$	Anode
$amb$	Ambient conditions
$C$	Cathode
$dry$	Dry conditions
$k$	Anode side ( $k = A$ ) or cathode side ( $k = C$ )
$M$	Membrane
$S$	Solid



# Physical Constants

Faraday constant	$F$	$=$	$96485.3365 \text{ C mol}^{-1}$
Avogadro constant	$N_A$	$=$	$6.0221 \times 10^{23} \text{ molecules mol}^{-1}$
Charge of one $e^-$	$q_{el}$	$=$	$1.602 \times 10^{-19} \text{ C per } e^-$
Gas constant	$R$	$=$	$8.314472 \text{ J mol}^{-1} \text{ K}^{-1}$



# Chapter 1

## Chapter Title Here

### 1.1 Main Section 1

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## 1.2 Main Section 2

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# Bibliography