

Assignment 3: Bayes Net

**CSC384 Winter 2015 Assignment 3 Question 1**

a)  $\Pr(b|a)$

0.5

b)  $\Pr(c|a)$

0.5

c)  $\Pr(c|a,-e)$

0.5714285714285714

d)  $\Pr(c|a,-f)$

0.5

**CSC384 Winter 2015 Assignment 3 Question 2**

1.

$V1 = ss$  ,  $V2 = sm$  ,  $V3 = cc$

$P(cc|ss) = P(cc|ss,sm)$

$P(cc = \text{true} | ss = \text{okay}) = 0.80 = P(cc = \text{true} | ss = \text{okay}, sm = \text{okay}) = 0.80$

$P(cc = \text{false} | ss = \text{okay}) = 0.20 = P(cc = \text{false} | ss = \text{okay}, sm = \text{okay}) = 0.20$

$P(cc = \text{true} | ss = \text{okay}) = 0.80 = P(cc = \text{true} | ss = \text{okay}, sm = \text{faulty}) = 0.80$

$P(cc = \text{false} | ss = \text{okay}) = 0.20 = P(cc = \text{false} | ss = \text{okay}, sm = \text{faulty}) = 0.20$

$P(cc = \text{true} | ss = \text{faulty}) = 0.05 = P(cc = \text{true} | ss = \text{faulty}, sm = \text{okay}) = 0.05$

$P(cc = \text{false} | ss = \text{faulty}) = 0.95 = P(cc = \text{false} | ss = \text{faulty}, sm = \text{okay}) = 0.95$

$P(cc = \text{true} | ss = \text{faulty}) = 0.05 = P(cc = \text{true} | ss = \text{faulty}, sm = \text{faulty}) = 0.05$

$P(cc = \text{false} | ss = \text{faulty}) = 0.95 = P(cc = \text{false} | ss = \text{faulty}, sm = \text{faulty}) = 0.95$

These statements illustrate that probability of  $cc$  is conditionally independent on  $sm$  given  $ss$ .

2.

$V = sq, d = bad$

$V1 = pv, d1 = weak$

$V2 = sp, d2 = fouled$

$P(pv = weak) = 0.178$

$P(sp = fouled) = 0.200$

$P(pv = weak \mid sq = bad) = 0.533$

$P(sp = fouled \mid sq = bad) = 0.311$

$P(pv = weak \mid sq = bad, sp = fouled) = 0.000$

$P(sp = fouled \mid sq = bad, pv = weak) = 0.000$

These statements illustrate that  $sq = bad$  increases the probability of  $pv = weak$  and  $sp = fouled$ . However, once it is known that  $sp = fouled$ , which explains away the reason  $sq = bad$ , probability of  $pv = weak$  decreases and vice-versa.

3.

$V = ss, d = okay$

$V1 = sm, d1 = okay$

$V2 = mf, d2 = okay$

$V3 = bv, d3 = strong$

$P(ss = okay \mid sm = okay) < P(ss = okay \mid sm = okay, mf = okay) < P(ss = okay \mid sm = okay, mf = okay, bv = strong)$

$P(ss = okay \mid sm = okay) = 0.598$

$P(ss = okay \mid sm = okay, mf = okay) = 0.605$

$P(ss = okay \mid sm = okay, mf = okay, bv = strong) = 0.980$

These statements illustrate that probability of  $ss = okay$  increases monotonically as we add the evidence items of  $sm = okay$ ,  $mf = okay$ , and  $bv = strong$ .

4.

$V = st, d = \text{true}$

$V1 = sq, d1 = \text{bad}$

$V2 = fs, d2 = \text{faulty}$

$V3 = tm, d3 = \text{good}$

$V4 = asys, d4 = \text{faulty}$

$V5 = cc, d5 = \text{true}$

$P(st = \text{true} | sq = \text{bad}) > P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}) < P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good}) >$   
 $P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good}, asys = \text{faulty}) < P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good},$   
 $asys = \text{faulty}, cc = \text{true})$

[0.2803836125216086, 0.7196163874783914]

$P(st = \text{true} | sq = \text{bad}) = 0.462$

$P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}) = 0.032$

$P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good}) = 0.034$

$P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good}, asys = \text{faulty}) = 0.015$

$P(st = \text{true} | sq = \text{bad}, fs = \text{faulty}, tm = \text{good}, asys = \text{faulty}, cc = \text{true}) = 0.020$

These statements illustrate that probability of  $st = \text{true}$  both increases and decreases as we add the evidence items of  $sq = \text{bad}$ ,  $fs = \text{faulty}$ ,  $tm = \text{good}$ ,  $asys = \text{faulty}$ , and  $cc = \text{true}$ .