By keyword

centered

A polytope is centered if the origin is contained in the interior of \conv $V \setminus v$ for all v in V centergon(n), prodsumpolygon(d,n), sumcube(d), sumpolygon(d,n)

centrally-symmetric

cube(d)

diameter

Diameter is used in two different senses. In the <u>metric</u> sense, it means the length of the longest line segment between points in a set (see e.g.). In the combinatorial sense, it is used to mean the length of the longest path in the <u>skeleton</u> of a polytope, or of a graph in general. See also <u>ridge-diameter</u>.

<u>q4</u>

dwarfed

```
A polytope P is called dwarfed if (P) = (Q) \setminus (P) + (Q) \setminus (P) + (Q) \setminus (Q) \setminus (Q)
dwarfcube(d)
```

equidecomposable

A polytope is called equidecomposable if every <u>triangulation</u> has the same *f*-vector <u>prodsimplex(d)</u>

faces>>size

```
sum f_k >> d(f_0 + f_{d-1})
\frac{prodcyclic(d,n)}{prodsumcube(d)}, \frac{prodsumpolygon(d,n)}{prodsumpolygon(d,n)}
```

facet-degenerate

```
(some) facets contain more than d vertices, i.e. not <u>simplicial</u>.

\underline{\text{cube}(d)}, \underline{\text{cut}(n)}, \underline{\text{dwarfcube}(d)}, \underline{\text{metric}(n)}, \underline{\text{piercecube}(d)}, \underline{\text{prodsumcube}(d)}, \underline{\text{prodsumpolygon}(d,n)}
```

facets>>vertices

```
f_{d-1} >> f_0.

\operatorname{cyclic}(n,d), \operatorname{sumcube}(d), \operatorname{sumpolygon}(d,n)
```

incremental

Incremental algorithms for e.g. <u>facet-enumeration</u> proceed by adding the input points one by one, updating the list of facet-defining inequalities for the current intermediate polytope at each step. See also <u>double-description</u> and <u>Fourier-Motzkin elimination</u>

piercecube(d), prodcyclic(d,n), prodsumcube(d), prodsumpolygon(d,n)

neighbourly

```
each k < floor(d/2) vertices forms a face. 
 \underline{\operatorname{cyclic}(n,d)}
```

ridge-diameter

The <u>diameter</u> (in the graph theoretic sense) of the dual polytope.

metric(n)

simple

Exactly *d* facets intersect at each vertex.

```
\frac{centergon(n)}{sumpolygon(d,n)}, \frac{cube(d)}{sumpolygon(d,n)}, \frac{dwarfcube(d)}{sumpolygon(d,n)}, \frac{prodsimplex(d)}{sumpolygon(d,n)}, \frac{qd}{sumpolygon(d,n)}, \frac{qd}{sumpolygon(d,n)}
```

simplicial

Exactly *d* vertices on each facet.

```
centergon(n) , cyclic(n,d) , simplex(d)
```

triangle-free

P has no triangular 2-face.

cube(d)

triangulation

A <u>dissection</u> of a polytope into simplices such that any pair intersect in a (possibly empty) <u>face</u>.

```
cube(d) , prodcyclic(d,n) , prodsimplex(d) , prodsumcube(d) , prodsumpolygon(d,n)
```

truncationpolytope

```
dwarfcube(d) , simplex(d)
```

vertex-degenerate

(some) vertices are contained in more than d facets, i.e. not <u>simple</u>. See also <u>facet-degenerate</u>.

```
prodcyclic(d,n) , prodsumcube(d) , prodsumpolygon(d,n)
```

vertices>>facets

```
See facets>>vertices
```

cube(d)

zero-one

A polytope is called zero-one if every vertex coordinate has one exactly two values (e.g. 0 or 1).

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<u>cube(d)</u>, <u>hypersimplex(d,k)</u>, <u>prodsumcube(d)</u>, <u>sumcube(d)</u>
```

zonotope

A zonotope is the minkowski sum of a set of vectors.

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cube(d) , permutahedron(n)
```

By Name

hamming(n)

```
<u>hypersimplex(d,k)</u>
      zero-one
interval(a,b)
metric(n)
      facet-degenerate, ridge-diameter
permutahedron(n)
      simple, zonotope
piercecube(d)
      incremental, facet-degenerate
prodcyclic(d,n)
      incremental, vertex-degenerate, facet-degenerate, triangulation, faces>>size
prodsimplex(d)
      simple, facet-degenerate, triangulation, equidecomposable
prodsumcube(d)
      faces>>size, vertex-degenerate, facet-degenerate, triangulation, incremental, zero-one
prodsumpolygon(d,n)
      incremental, vertex-degenerate, facet-degenerate, triangulation, centered, faces>>size
<u>q4</u>
      simple, diameter
simplex(d)
      simple, simplicial, truncationpolytope
sumcube(d)
      centered, facets>>vertices, zero-one
sumpolygon(d,n)
      facets>>vertices, simple, centered
```