Table of Contents

1	1
Optional overhead	1
Run optimization)
Report	2
%%%%%%%%%%%%%% Main Entrance %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%	
%%%%%	
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%%%%%	
<pre>% Instruction: Please read through the code and fill in blanks % (marked by ***). Note that you need to do so for every involved % function i.e. m files</pre>	

Optional overhead

```
clear; % Clear the workspace
close all; % Close all windows
```

Optimization settings

Here we specify the objective function by giving the function handle to a variable, for example:

```
f = @(x)(x(1)^2+(x(2)-3)^2); % replace with your objective function
% In the same way, we also provide the gradient of the
% objective:
df = @(x)[x(1)*2;(x(2)-3)*2]; % replace accordingly
g = @(x)[-2*x(1)+x(2)^2;5*x(1)+(x(2)-1)^2-15];
dg=@(x)([-2,2*x(2);5,2*(x(2)-1)]);
% Note that explicit gradient and Hessian information is only
optional.
% However, providing these information to the search algorithm will
% computational cost from finite difference calculations for them.
% % Specify algorithm
%opt.alg = 'matlabqp'; % 'myqp' or 'matlabqp'
opt.alg = 'myqp';
% Turn on or off line search. You could turn on line search once other
% parts of the program are debugged.
opt.linesearch = true; % false or true
```

```
% Set the tolerance to be used as a termination criterion:
opt.eps = le-3;

% Set the initial guess:
x0 = [1;1];

% Feasibility check for the initial point.
if max(g(x0)>0)
    errordlg('Infeasible intial point! You need to start from a feasible one!');
    return
end
```

Run optimization

Run your implementation of SQP algorithm. See mysqp.m

```
solution = mysqp(f, df, g, dg, x0, opt);
inde=1:length(solution.x(1,:));
for i=1:length(solution.x(1,:))
ff(i)=f(solution.x(:,i));
end
sub1=g(solution.x(:,i));
x1=num2str(solution.x(1,i));
x2=num2str(solution.x(2,i));
figure
subplot(2,1,1)
plot(inde,ff);
xlabel('iteration')
ylabel('f(x)')
title(['@x=(',x1,',',x2,') g1= ',num2str(sub1(1)),'
g2=',num2str(sub1(2))])
subplot(2,1,2)
plot(solution.x(1,:), solution.x(2,:), '*-')
xlabel('x1')
ylabel('x2')
title(['global minimum @x=(',x1,'',',x2,'') f(x)='',num2str(ff(i))])
```

Report

```
function [s, mu] = solve activeset(x, W, c, A, b)
   % Given an active set, solve QP
   % Create the linear set of equations given in equation (7.79)
   M = [W, A'; A, zeros(size(A,1))];
   U = [-c; b];
   s = sol(1:numel(x));
                                % Extract s from the solution
   end
The following code performs line search on the merit function
% Armijo line search
function [a, w] = lineSearch(f, df, g, dg, x, s, mu_old, w_old)
   t = 0.1; % scale factor on current gradient: [0.01, 0.3]
   b = 0.8; % scale factor on backtracking: [0.1, 0.8]
   a = 1; % maximum step length
   D = s;
                      % direction for x
   % Calculate weights in the merit function using eaution (7.77)
   w = max(abs(mu_old), 0.5*(w_old+abs(mu_old)));
   % terminate if line search takes too long
   count = 0;
   while count<5
      % Calculate phi(alpha) using merit function in (7.76)
      phi_a = f(x + a*D) + w'*abs(min([0;0], -g(x+a*D)));
      % Caluclate psi(alpha) in the line search using phi(alpha)
      phi0 = f(x) + w'*abs(min([0;0], -q(x))); % phi(0)
      dphi0 = df(x)'D + w'*((dg(x)D)*(g(x))); % phi'(0)
      dphi0 = [df(x)]'*D + w'*[dg(x)]'*D;
      psi_a = phi0 + t*a*dphi0;
                                        % psi(alpha)
      % stop if condition satisfied
      if phi a<psi a
         break;
      else
         % backtracking
         a = a*b;
         count = count + 1;
      end
   end
end
```

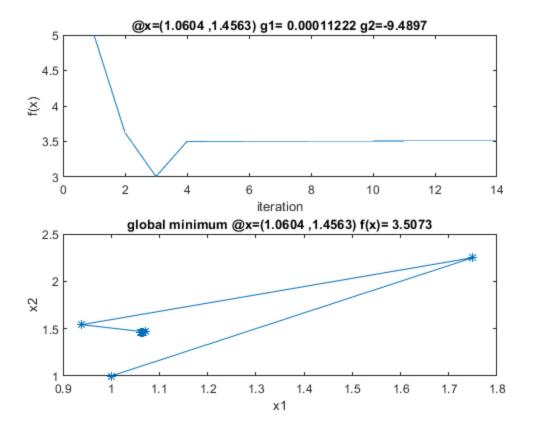
```
The following code solves the QP subproblem using active set strategy
function [s, mu0] = solveqp(x, W, df, g, dg)
   % Implement an Active-Set strategy to solve the QP problem given
by
   % min
           (1/2)*s'*W*s + c'*s
           A*s-b <= 0
   % s.t.
   % where As-b is the linearized active contraint set
   % Strategy should be as follows:
   % 1-) Start with empty working-set
   % 2-) Solve the problem using the working-set
   % 3-) Check the constraints and Lagrange multipliers
   % 4-) If all constraints are staisfied and Lagrange multipliers
are positive, terminate!
   % 5-) If some Lagrange multipliers are negative or zero, find the
most negative one
      and remove it from the active set
   % 6-) If some constraints are violated, add the most violated one
to the working set
   % 7-) Go to step 2
   % Compute c in the QP problem formulation
   c = [df(x)];
   % Compute A in the QP problem formulation
   A0 = dg(x);
   % Compute b in the QP problem formulation
   b0 = -q(x);
   % Initialize variables for active-set strategy
   stop = 0;
                    % Start with stop = 0
   % Start with empty working-set
                % A for empty working-set
   A = [];
   b = [];
                 % b for empty working-set
   % Indices of the constraints in the working-set
   while ~stop % Continue until stop = 1
      % Initialize all mu as zero and update the mu in the working
set
      mu0 = zeros(size(g(x)));
```

```
% Extact A corresponding to the working-set
       A = A0(active,:);
       % Extract b corresponding to the working-set
       b = b0(active);
       % Solve the QP problem given A and b
       [s, mu] = solve activeset(x, W, c, A, b);
       % Round mu to prevent numerical errors (Keep this)
       mu = round(mu*1e12)/1e12;
       % Update mu values for the working-set using the solved mu
values
       mu0(active) = mu;
       % Calculate the constraint values using the solved s values
       gcheck = A0*s-b0;
       % Round constraint values to prevent numerical errors (Keep
this)
       gcheck = round(gcheck*1e12)/1e12;
       % Variable to check if all mu values make sense.
       mucheck = 0;
                          % Initially set to 0
       % Indices of the constraints to be added to the working set
                              % Initialize as empty vector
       % Indices of the constraints to be added to the working set
       Iremove = [];
                              % Initialize as empty vector
       % Check mu values and set mucheck to 1 when they make sense
       if (numel(mu) == 0)
           % When there no mu values in the set
           mucheck = 1;
                               % OK
       elseif min(mu) > 0
           % When all mu values in the set positive
           mucheck = 1;
                                % OK
       else
           % When some of the mu are negative
           % Find the most negative mu and remove it from acitve set
           [~,Iremove] = min(mu); % Use Iremove to remove the
constraint
       end
       % Check if constraints are satisfied
       if max(qcheck) <= 0</pre>
           % If all constraints are satisfied
           if mucheck == 1
               % If all mu values are OK, terminate by setting stop =
1
               stop = 1;
           end
       else
```

```
% If some constraints are violated
            % Find the most violated one and add it to the working set
            [~, Iadd] = max(qcheck); % Use Iadd to add the constraint
        end
        % Remove the index Iremove from the working-set
        active = setdiff(active, active(Iremove));
        % Add the index Iadd to the working-set
        active = [active, Iadd];
        % Make sure there are no duplications in the working-set (Keep
this)
       active = unique(active);
   end
end
function solution = mysqp(f, df, g, dg, x0, opt)
    % Set initial conditions
   x = x0; % Set current solution to the initial guess
   % Initialize a structure to record search process
   solution = struct('x',[]);
    solution.x = [solution.x, x]; % save current solution to
 solution.x
    % Initialization of the Hessian matrix
   W = eye(numel(x));
                                   % Start with an identity Hessian
matrix
    % Initialization of the Lagrange multipliers
   mu_old = zeros(size(g(x))); % Start with zero Lagrange
multiplier estimates
   % Initialization of the weights in merit function
   w = zeros(size(q(x)));
                                  % Start with zero weights
   % Set the termination criterion
   gnorm = norm(df(x) + [dg(x)]'*mu_old); % norm of Largangian
gradient
   while gnorm>opt.eps % if not terminatedf
        % Implement QP problem and solve
        if strcmp(opt.alg, 'myqp')
            % Solve the QP subproblem to find s and mu (using your own
method)
            [s, mu\_new] = solveqp(x, W, df, g, dg);
        else
            % Solve the QP subproblem to find s and mu (using MATLAB's
solver)
           gpalg = optimset('Algorithm', 'active-
set','Display', 'off','TolX',1e-3);
            %qpalg = optimoptions('Display', 'iter');
```

```
[s, \sim, \sim, \sim, lambda] = quadprog(W, [df(x)]', dg(x), -g(x), [], [],
 [], [], x, qpalq);
           mu_new = lambda.ineqlin;
       end
       % opt.linesearch switches line search on or off.
       % You can first set the variable "a" to different constant
values and see how it
       % affects the convergence.
       if opt.linesearch
           [a, w] = lineSearch(f, df, g, dg, x, s, mu_old, w);
       else
           a = 0.1;
       end
       % Update the current solution using the step
                               % Step for x
       dx = a*s;
                               % Upda5te x using the step
       x = x + dx;
       % Update Hessian using BFGS. Use equations (7.36), (7.73) and
 (7.74)
       % Compute y_k
       y_k = [df(x) + mu_new'*dg(x) - df(x-dx) - mu_new'*dg(x-dx)]';
       y_k = [df(x) + [dg(x)]'*mu_new - df(x-dx) - [dg(x-
dx)]'*mu_new];
       % Compute theta
       if dx'*y k >= 0.2*dx'*W*dx
           theta = 1;
       else
           theta = (0.8*dx'*W*dx)/(dx'*W*dx-dx'*y_k);
       end
       % Compute dq k
       dg_k = theta*y_k + (1-theta)*W*dx;
       % Compute new Hessian
       W = W + (dg_k*dg_k')/(dg_k'*dx) - ((W*dx)*(W*dx)')/(dx'*W*dx);
       % Update termination criterion:
       gnorm = norm(df(x) + mu_new'*dg(x)); % norm of Largangian
gradient
       gnorm = norm(df(x) + [dg(x)]'*mu_new);
       mu old = mu new;
       % save current solution to solution.x
       solution.x = [solution.x, x];
       %disp(solution.x)
   end
end
This announcement is closed for comments
```

7



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