

$$\mathbf{x}_0 = \Pi \mathbf{x}_{00} + \mathbf{U}(\mathbf{U}^T \mathbf{A} \mathbf{U})^+ \mathbf{U}^T \mathbf{b}$$

$$\mathbf{r}_0 = \mathbf{b} - \mathbf{A} \mathbf{x}_0$$

$$\mathbf{Z}_0 = (\sum_{s=1}^N \mathbf{H}^{(s)}) \mathbf{r}_0$$

$$\mathbf{P}_0 = \Pi \mathbf{Z}_0$$

While not converged

$$\mathbf{Q}_i = \mathbf{A} \mathbf{P}_i$$

$$\Delta_i = \mathbf{Q}_i^T \mathbf{P}_i, \quad \gamma_i = \mathbf{P}_i^T \mathbf{r}_i, \quad \alpha_i = \Delta_i^+ \gamma_i$$

$$\mathbf{x}_{i+1} = \mathbf{x}_i + \mathbf{P}_i \alpha_i$$

$$\mathbf{r}_{i+1} = \mathbf{r}_i - \mathbf{Q}_i \alpha_i$$

$$\mathbf{Z}_{i+1} = (\sum_{s=1}^N \mathbf{H}^{(s)}) \mathbf{r}_{i+1}$$

For $s = 1, \dots, N$

$$t_i^s = \frac{\langle \mathbf{P}_i \alpha_i, \mathbf{A}^s \mathbf{P}_i \alpha_i \rangle}{\mathbf{r}_{i+1}^T \mathbf{H}^{(s)} \mathbf{r}_{i+1}}$$

$$t_i^s \leq \tau$$

true

false

$$\mathbf{Z}_{i+1} = [\mathbf{Z}_{i+1} | H^s \mathbf{r}_{i+1}]$$

\emptyset

For $j = 1, \dots, i$

$$\beta_{i,j} = \frac{\langle \mathbf{z}_{i+1}, \mathbf{A} \mathbf{p}_j \rangle}{\langle \mathbf{p}_j, \mathbf{A} \mathbf{p}_j \rangle}$$

$$\mathbf{P}_{i+1} = \Pi \mathbf{Z}_{i+1} - \mathbf{P}_i \beta_{i,j}$$