

Section 2: Graph Search

Section 8

MxN 공간이라면, 상태공간 크기는? $4MN(V_{max}+1)$

엔하인 거리 (agent → exit) admissible 한가? NO

Admissible heuristic은 경의 해 보아라.

Relaxation (no walls, can turn and change speed) d 맨하탄/Vmax

Section 5

1. Transition Function과 Reward Function은?

$T(s, Stop, Done) = 1$

$T(0, Draw, s') = 1/3$ for $s' \in \{2, 3, 4\}$

$T(2, Draw, s') = 1/3$ for $s' \in \{4, 5, Done\}$ $R(s, Stop, Done) = s, s \leq 5$

$T(3, Draw, s') = 1/3$ for $s' = 5$ $R(s, s, s') = 0$ otherwise

$T(4, Draw, Done) = 1$

$T(5, s') \leftarrow \max_{s'} \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V_k(s')]$

States	0	2	3	4	5
V_0	0	0	0	0	0
V_1	0	2	3	4	5
V_2	3	3	3	4	5
V_3	10/3	3	3	4	5
V_4	10/3	3	3	4	5

States	0	2	3	4	5
π_0	Draw	Draw	Stop	Stop	Stop
$\pi_{i+1}(s) = \arg \max_{s'} \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V^{\pi_i}(s')]$					

Section 9

factor 세팅

Factor의 세팅이 가장 작게 생성되는 방법

Section 9

Likelihood weighting

$P(W_2 = R \mid I_1 = T, I_2 = F) = \frac{\hat{P}(W_2 = R, I_1 = T, I_2 = F)}{\hat{P}(I_1 = T, I_2 = F)}$

$\hat{P}(W_2 = R, I_1 = T, I_2 = F) = \frac{0.72+0.16+0.72}{0.72+0.16+0.72+0.09+0.09+0.02} = 0.889$

Weight = 0.48 Weight = 0.48 Weight = 0.32 Weight = 0.48 Weight = 0.64

$P(C = 1 \mid B = 1, E = 1) = \frac{1}{24} = 0.733333333333$

데이터 선택으로 분리 가능하다.

The data are linearly separable.

Section 11

Sec11.3.3 세로 구간의 weight를 separate 불가능하다

Points 3, 4에서 작용하지 않기 때문

$-1 \cdot 1 + 1 \cdot 2 + -1 \cdot 4 = -3 < 0$

$-1 \cdot 1 + 1 \cdot 3 + -1 \cdot 4 = -2 < 0$

$w = w + y^* \cdot f$

step	Weights	Score	Correct?
1	-1, 0, 0	$-1 \cdot 1 + 0 \cdot 1 + 0 \cdot 1 = -1$	yes
2	-1, 0, 0	$-1 \cdot 1 + 0 \cdot 3 + 0 \cdot 2 = -1$	no
3	0, 3, 2	$0 \cdot 1 + 3 \cdot 2 + 2 \cdot 4 = 14$	yes
4	0, 3, 2	$0 \cdot 1 + 3 \cdot 3 + 2 \cdot 4 = 17$	yes
5	0, 3, 2	$0 \cdot 1 + 3 \cdot 2 + 2 \cdot 3 = 12$	no

Final weights: [-1, 1, -1]

EU(accept) = P(hired|U(accept, hired)) + P(not hired|U(accept, not hired)) = 6500

EU(decline) = P(hired|U(decline, hired)) + P(not hired|U(decline, not hired)) = 2500

Action	Google outcome	U
accept Acme offer	hired	2000
accept Acme offer	not hired	8000
reject Acme offer	hired	10000
reject Acme offer	not hired	0

Answer: 6500.0

Answer: 2500.0

Google outcome	Info	P(Google outcome Info)
good news	hired	0.7
bad news	hired	0.3
good news	not hired	0.1
bad news	not hired	0.9

Info	Action	EU(Action Info)	
hired	good news	accept Acme offer	Answer: 3800.0
not hired	good news	reject Acme offer	Answer: 7000.0
hired	bad news	accept Acme offer	Answer: 7400.0
not hired	bad news	reject Acme offer	Answer: 1000.0

sample = $R(s, a, s') + \gamma \max_{a'} Q(s, a')$

$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + \alpha [sample]$

$V_{t+1}(s) \leftarrow \sum_{a'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_t^*(s)]$

Sample of V(s): $sample = R(s, \pi(s), s') + \gamma V^*(s')$

Update to V(s): $V^*(s) \leftarrow (1 - \alpha)V^*(s) + \alpha sample$

Same update: $V^*(s) \leftarrow V^*(s) + \alpha (sample - V^*(s))$

$V^*(s) \leftarrow (1 - \alpha)V^*(s) + \alpha [R(s, \pi(s), s') + \gamma V^*(s')]$

$Q_{t+1}(s, a) \leftarrow T(s, a, s') [R(s, a, s') + \gamma \max_{a'} Q_t(s, a')]$

$MEU(e) = \max_s \sum_{s'} P(s|e) U(s, a)$

$VPI(e|e') = (\sum_s P(e'|e) MEU(e, e')) - MEU(e)$

X is conditionally independent of Y given Z

if and only if: $X \perp\!\!\!\perp Y \mid Z$

$\forall x, y, z : P(x, y|z) = P(x|z)P(y|z)$

or, equivalently, if and only if

$\forall x, y, z : P(x|z, y) = P(x|z)$

$P_{LAP,k}(x) = \frac{c(x) + k}{N + k|X|}$

N : 관찰 데이터 개수

x 변수 종류의 개수

$c(x)$: 변수 x의 관찰 데이터 개수

$P_{LAP,k}(x|y) = \frac{c(x, y) + k}{c(y) + k|X|}$

1. Calculate the expected gain from buying car, given no test.

$EU(buy) = P(Q = +q) \cdot U(+q, buy) + P(Q = -q) \cdot U(-q, buy)$

$= 7 \cdot 500 + 0.3 \cdot (-200) = 290$

2. Tests can be described by the probability that the car will pass or fail the test given that the car is in good or bad shape. We have the following information:

$P(T = pass|Q = +q) = 0.9$

$P(T = pass|Q = -q) = 0.2$

Calculate the probability that the car will pass (or fail) its test, and then the probability that it is in good (or bad) shape given each possible test outcome.

$P(T = pass) = \sum_q P(T = pass, Q = q)$

$= \frac{P(T = pass|Q = +q)P(Q = +q) + P(T = pass|Q = -q)P(Q = -q)}{1}$

$= \frac{0.9 \cdot 0.7}{0.69} = \frac{21}{23} \approx 0.91$

$P(Q = +q|T = fail) = \frac{P(T = fail|Q = +q)P(Q = +q)}{P(T = fail)}$

$= \frac{0.1 \cdot 0.7}{0.31} = \frac{7}{31} \approx 0.22$

3. Calculate the optimal decisions given either a pass or a fail, and their expected utilities.

$EU(buy|T = pass) = P(Q = +q|T = pass)U(+q, buy) + P(Q = -q|T = pass)U(-q, buy)$

$\approx 0.91 \cdot 500 + 0.09 \cdot (-200) \approx 437$

$EU(buy|T = fail) = P(Q = +q|T = fail)U(+q, buy) + P(Q = -q|T = fail)U(-q, buy)$

$\approx 0.22 \cdot 500 + 0.78 \cdot (-200) = -46$

$EU(-buy|T = pass) = 0$

$EU(-buy|T = fail) = 0$

Therefore: $MEU(T = pass) = 437$ (with buy) and $MEU(T = fail) = 0$ (using -buy)

4. Calculate the value of (perfect) information of the test. Should the buyer pay for a test?

$VPI(T) = (\sum_t P(T = t) MEU(T = t)) - MEU(\phi)$

$= 0.69 \cdot 437 + 0.31 \cdot 0 = 290 \approx 11.53$

You shouldn't pay for it, since the cost is \$50.

Variables:

- R: Raining
- T: Traffic
- D: Roof drips
- S: I'm sad

Questions:

$T \perp\!\!\!\perp D$

$T \perp\!\!\!\perp D \mid R$ Yes

$T \perp\!\!\!\perp D \mid R, S$

$R \perp\!\!\!\perp B$ Yes

$R \perp\!\!\!\perp B \mid T$

$R \perp\!\!\!\perp B \mid T'$

$L \perp\!\!\!\perp T' \mid R$ Yes

$L \perp\!\!\!\perp B$ Yes

$L \perp\!\!\!\perp B \mid T$

$L \perp\!\!\!\perp B \mid T'$

$L \perp\!\!\!\perp B \mid T, R$ Yes

$R \perp\!\!\!\perp B$

$R \perp\!\!\!\perp B \mid T$

$R \perp\!\!\!\perp B \mid T'$

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π_0	Draw	Draw	Stop	Stop	Stop
$\pi_{i+1}(s) = \arg \max_{s'} \sum_{s'} T(s, a, s') [R(s, a, s') + \gamma V^{\pi_i}(s')]$					

Conditional Probabilities

$P(a|b) = \frac{P(a, b)}{P(b)}$

The Product Rule

$P(y)P(x|y) = P(x, y) \iff P(y) = \frac{P(x, y)}{P(x)}$

The Chain Rule

$P(x_1, x_2, x_3) = P(x_1)P(x_2|x_1)P(x_3|x_1, x_2)$

$P(X_1, X_2, \dots, X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots$

Causal Chains

$P(x, y, z) = P(x)P(y|x)P(z|y)$

Common Cause

$P(x, y, z) = P(y)P(x|y)P(z|y)$

Bayes' Rule

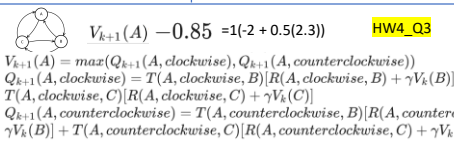
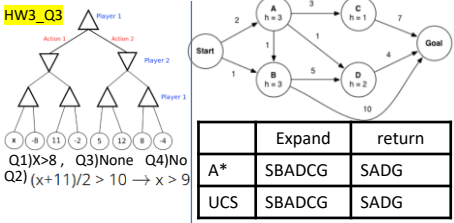
$P(x|y) = \frac{P(y|x)}{P(y)} P(x)$

independent

$P(x, y) = P(x)P(y) \iff X \perp\!\!\!\perp Y$

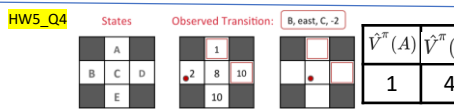
conditionally independent

$P(x, y|z) = P(x|z)P(y|z) \iff X \perp\!\!\!\perp Y \mid Z$



Part 2: Here is the formula to calculate $Q^*(A, \text{clockwise})$.
 $Q^*(A, \text{clockwise}) = T(A, \text{clockwise}, B)[R(A, \text{clockwise}, B) + \gamma V^*(B)] + T(A, \text{clockwise}, C)[R(A, \text{clockwise}, C) + \gamma V^*(C)]$
 Part 3: Here is the formula to calculate $Q^*(A, \text{counterclockwise})$.
 $Q^*(A, \text{counterclockwise}) = T(A, \text{counterclockwise}, B)[R(A, \text{counterclockwise}, B) + \gamma V^*(B)] + T(A, \text{counterclockwise}, C)[R(A, \text{counterclockwise}, C) + \gamma V^*(C)]$

$Q^*(A, \text{clockwise}) - 0.75$ $Q^*(A, \text{counterclockwise}) - 0.8$
 optimal action from state A: Clockwise

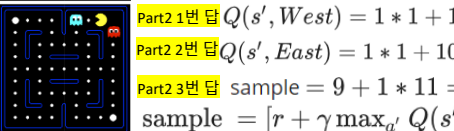
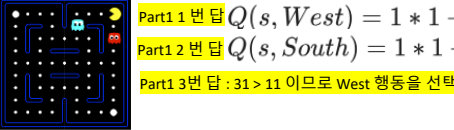


$V^\pi(s) \leftarrow (1 - \alpha)V^\pi(s) + \alpha [R(s, \pi(s), s') + \gamma V^\pi(s')]$

HW5_Q5 Model-Free RL: Cycle $\alpha \gamma 0.5$.

	A	B	C
Clockwise	0.048	1.0	1.165
Counterclockwise	3.254	2.66	7.516

$Q(s, a) = (1 - \alpha) * Q(s, a) + \alpha * (R(s, a, s') + \gamma * \max_{a'} Q(s', a'))$



Difference 구하기 difference = $[r + \gamma \max_{a'} Q(s', a')] - Q(s, a) =$
 difference = $20 - 31 = -11$

새로운 w1 $w_1 \leftarrow w_1 + \alpha (\text{difference}) f_1(s, a) =$
 $w_1 = 1 + .5 * (-11) * 1 = -4.5$
새로운 w2 $w_2 \leftarrow w_2 + \alpha (\text{difference}) f_2(s, a) =$
 $w_2 = 10 + .5 * (-11) * 3 = -6.5$

Discount Factor, $\gamma = 0.5$

s	a	s'	T(s,a,s')	R(s,a,s')
A	Clockwise	B	1.0	-2.0
A	Counterclockwise	B	0.4	-1.0
A	Counterclockwise	C	0.6	-2.0
B	Clockwise	C	1.0	2.0
B	Counterclockwise	A	0.6	0.0
B	Counterclockwise	C	0.4	0.0
C	Clockwise	A	0.6	1.0
C	Clockwise	B	0.4	0.0
C	Counterclockwise	A	0.4	1.0
C	Counterclockwise	B	0.6	0.0

HW4_Q8 Discount Factor, $\gamma = 0.5$

s	a	s'	T(s,a,s')	R(s,a,s')
A	Clockwise	B	1.0	-1.0
A	Counterclockwise	B	0.2	-1.0
A	Counterclockwise	C	0.8	2.0
B	Clockwise	A	0.4	0.0
B	Clockwise	C	0.6	-2.0
B	Counterclockwise	A	1.0	-2.0
C	Clockwise	A	0.8	2.0
C	Clockwise	B	0.2	1.0
C	Counterclockwise	B	1.0	-2.0

$Q_k^*(A, \text{counterclockwise}) = T(A, \text{counterclockwise}, B)[R(A, \text{counterclockwise}, B) + \gamma V_k^*(B)] + T(A, \text{counterclockwise}, C)[R(A, \text{counterclockwise}, C) + \gamma V_k^*(C)]$
 updated action for state C: Clockwise

HW5_Q2

s	a	s'	T(s,a,s')	R(s,a,s')
A	Clockwise	B	0.600	0
A	Clockwise	C	0.400	10
A	Counterclockwise	B	0.200	0.000
A	Counterclockwise	C	0.800	-1.000
B	Clockwise	A	0.400	-6.000
B	Clockwise	C	0.600	0.000
B	Counterclockwise	A	0.800	-4.000
B	Counterclockwise	C	0.200	0.000
C	Clockwise	A	0.600	0.000
C	Clockwise	B	0.400	-6.000
C	Counterclockwise	B	1.000	-9.000

$V_{k+1}^*(C) - 2.65$
 $V_{k+1}^*(A) = T(A, \text{clockwise}, B)[R(A, \text{clockwise}, B) + \gamma V_k^*(B)] + T(A, \text{clockwise}, C)[R(A, \text{clockwise}, C) + \gamma V_k^*(C)]$
 $Q_\infty^*(C, \text{clockwise}) 1.6$
 $Q_\infty^*(A, \text{clockwise}) = T(A, \text{clockwise}, B)[R(A, \text{clockwise}, B) + \gamma V_\infty^*(B)] + T(A, \text{clockwise}, C)[R(A, \text{clockwise}, C) + \gamma V_\infty^*(C)]$
 $Q_\infty^*(C, \text{counterclockwise}) - 3.0$
 $Q_\infty^*(A, \text{counterclockwise}) = T(A, \text{counterclockwise}, B)[R(A, \text{counterclockwise}, B) + \gamma V_\infty^*(B)] + T(A, \text{counterclockwise}, C)[R(A, \text{counterclockwise}, C) + \gamma V_\infty^*(C)]$

$Q_k(s, a)$

	A	B	C
Clockwise	2.8	-2.32	-1.68
Counterclockwise	-2.0	-1.84	-10.2

$T(R + r * V()) + T(R + r * V())$
 $3.112 = 0.6(0 + 0.5 * (-1.84)) + 0.4(10 + 0.5 * (-1.68))$

Q2 Part2 번 답

Q k+1(s,a)	A	B	C
Clockwise	3.112	-2.344	-1.928
Counterclo	-1.656	-2.248	-9.920

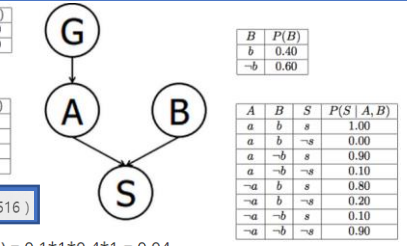
Q2 Part3 번 답

A	B	C
Clockwise	Counterclo	Clockwise

HW6_Q5

G	P(G)
g	0.10
~g	0.90

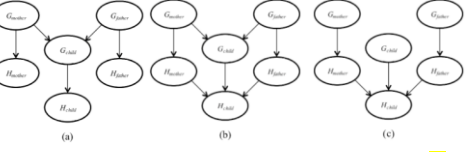
G	A	P(A G)
g	a	1.00
g	~a	0.00
~g	a	0.10
~g	~a	0.90



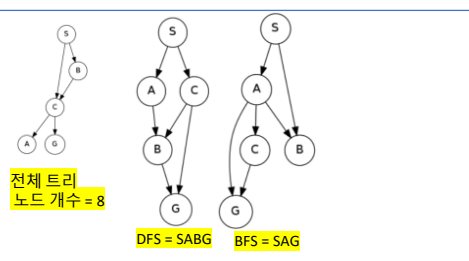
Q1 $P(g, a, b, s) = P(g) * P(a|g) * P(b|s) * P(s|b, a) = 0.1 * 1 * 0.4 * 1 = 0.04$
Q2 $P(a) = P(a|g) * P(g) + P(a|~g) * P(~g) = 1.0 * 0.1 + 0.1 * 0.9 = 0.19$
Q3 $P(a|b) = P(a) = 0.19$.
Q4 $P(a|s, b) = P(a, b, s) / (P(a, b, s) + P(~a, b, s)) = (P(a) * P(b) * P(s|a, b)) / ((P(a) * P(b) * P(s|a, b)) + (P(~a) * P(b) * P(s|~a, b))) = (0.19 * 0.4 * 1) / (0.19 * 0.4 * 1 + 0.81 * 0.4 * 0.8) = 0.076 / (0.076 + 0.2592) = 0.2267$
Q5 $P(g|a) = P(g) * P(a|g) / (P(g) * P(a|g) + P(~g) * P(a|~g)) = 0.1 * 1 / (0.1 * 1 + 0.9 * 0.1) = 0.1 / (0.1 + 0.09) = 0.5263$.
Q6 $P(g|b) = P(g) = 0.1$

a) Depth-first search.
 States Expanded: Start, A, C, D, B, Goal
 Path Returned: Start-A-C-D-Goal

b) Breadth-first search.
 States Expanded: Start, A, B, D, C, Goal
 Path Returned: Start-D-Goal



$P(G_{father}, G_{mother}, G_{child}) = P(G_{father})P(G_{mother})P(G_{child})$ (c)
 세 가지 네트워크 중에 독립성 가설과 일치한 것 = (a) (b)
 가장 좋은 가설은 (a)



Q2 Part2 번 답

Q k+1(s,a)	A	B	C
Clockwise	3.112	-2.344	-1.928
Counterclo	-1.656	-2.248	-9.920

Q2 Part3 번 답

A	B	C
Clockwise	Counterclo	Clockwise

HW6_Q5

G	P(G)
g	0.10
~g	0.90

G	A	P(A G)
g	a	1.00
g	~a	0.00
~g	a	0.10
~g	~a	0.90

