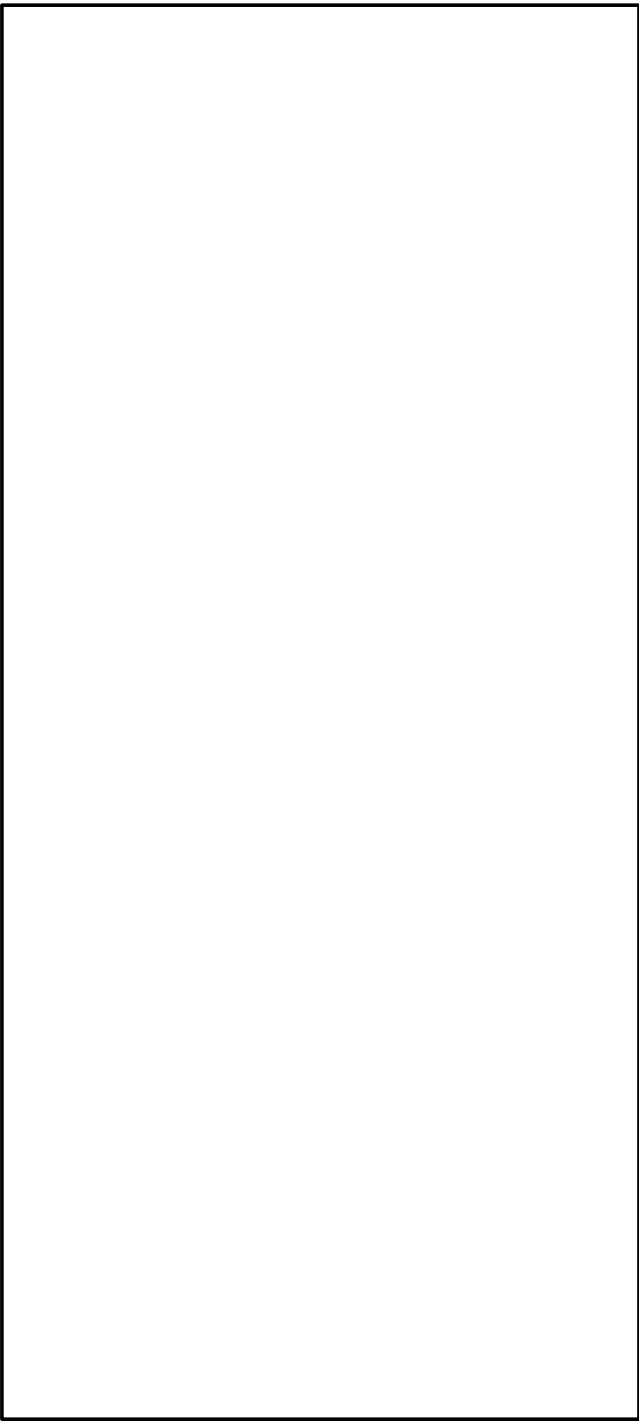


$$\frac{d^2 i}{dt^2} + \underbrace{\frac{R}{L}}_{\omega_0/Q} + \underbrace{\frac{1}{LC}}_{\omega_0^2} = 0$$

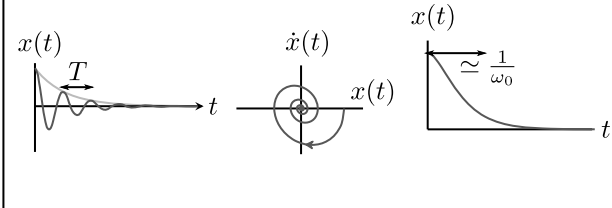


$$\ddot{x} + \frac{\omega_0}{Q}\dot{x} + \omega_0^2x = 0$$

$$x(t) = (A+Bt)e^{-\omega_0t}$$

$$x(t) = Ae^{r_1t} + Be^{r_2t}$$


$$r_{1,2} = \frac{\omega_0}{2Q} \left( \pm \sqrt{1-4Q^2} - 1 \right)$$






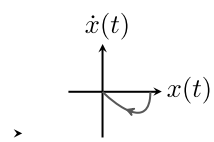
$$Q < \frac{1}{2}$$

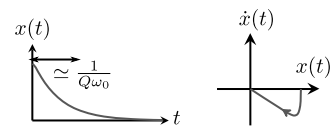
$$x(t) = Ae^{-t/\tau} \cos(\omega t + \varphi)$$

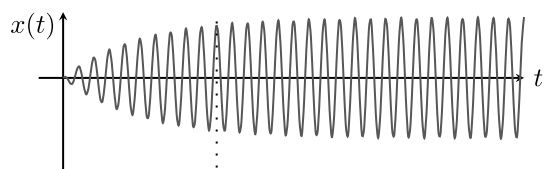
$\frac{2Q}{\omega_0}$ 


$\omega_0 \sqrt{1 - \frac{1}{4Q^2}}$ 






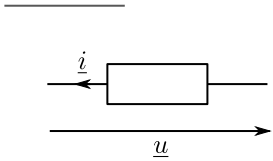




$$x(t) = X \cos(\omega t + \varphi)$$

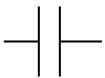
$$\longrightarrow \underline{x}(t) = X e^{j(\omega t + \varphi)}$$

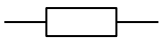
$$\begin{array}{ll} \dot{\underline{x}} = j\omega \underline{x} & x = Re(\underline{x}) \\ \ddot{\underline{x}} = -\omega^2 \underline{x} & X = |\underline{x}| \quad \omega t + \varphi = \arg(\underline{x}) \end{array}$$



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$$\underline{Z} = \frac{\underline{u}}{\underline{i}}$$





$C$

$$\underline{Z}_C = \frac{1}{jC\omega}$$

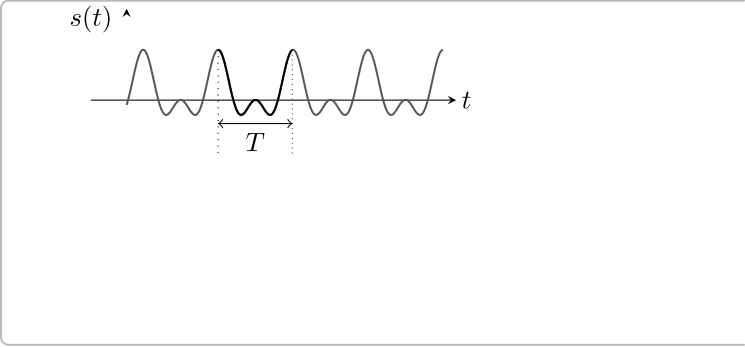
$$\underline{Z}_L = jL\omega$$

$$R$$

$$\underline{Z}_R = R$$









$T$  : période

$f = \frac{1}{T}$  : fréquence

$\omega = 2\pi f$  : pulsation

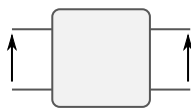
|

$$s(t) = c_0 + \sum_{i=1}^n c_n \cos(n\omega t + \varphi_n)$$



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$$\langle s(t) \rangle = \frac{1}{T} \int_0^T s(t) dt$$



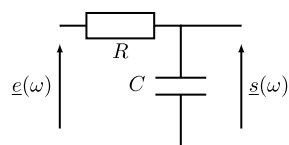
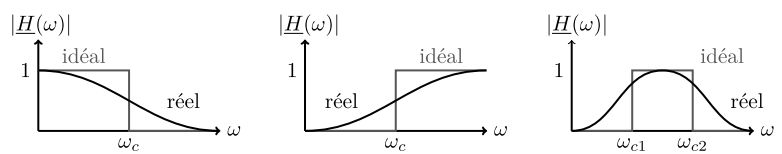
$$\langle s(t) \rangle = \sqrt{\frac{1}{T} \int_0^T s^2(t) dt}$$



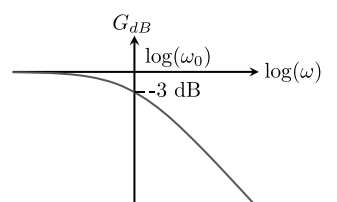
$$\underline{e}(\omega) \quad \underline{H}(\omega) \quad \underline{s}(\omega) \quad \underline{H}(\omega) = \frac{\underline{s}(\omega)}{\underline{e}(\omega)}$$

Gain :  $G = |\underline{H}(\omega)|$

Déphasage :  $\varphi = \arg(\underline{H}(\omega))$       Gain en décibels :  $G_{dB} = 20 \log(G)$



$$\underline{H}(\omega) = \frac{1}{1 + jRC\omega} = \frac{1}{1 + j\frac{\omega}{\omega_0}}.$$





$$\frac{d i}{d t} \quad i$$