Introduction

The following project documentation was written as work assignment for the module "Multivariate Analysis" of the Master in Statistics for Data Science at the Universidad Carlos III de Madrid. It contains the Multivariate Analysis of a Kaggel dataset on Sleep Health and Lifestyle (https://www.kaggle.com/datasets/uom190346a/sleep-health-and-lifestyle-dataset). The work is split into two parts, where in a first part a exploratory data analysis is performed, some data preprocessing steps are taken and a Prinicipal Component Analysis (PCA) is performed. In the second part, distance based metrics will then be applied to identify clusters emerging from the PCA.

The dataset at hand is composed out of the collumns shown in the table below. It has been modified compared to the kaggle source data by turning the "Sleep Disorder" Variable into a binary variable (yes/no) and by seperating the blood pressure variables into the two variables blood pressure systolic and blood pressure diastolic. The resulting data set is composed out of the variables shown in the following table.

Variable	Description
Person ID	An identifier for each individual.
Gender	The gender of the person (Male/Female).
Age	The age of the person in years.
Occupation	The occupation or profession of the person.
Sleep Duration (hours)	The number of hours the person sleeps per day.
Quality of Sleep (scale: 1-10)	A subjective rating of the quality of sleep, ranging from 1 to 10.
Physical Activity Level (minutes/day)	The number of minutes the person engages in physical activity daily.
Stress Level (scale: 1-10)	A subjective rating of the stress level experienced by the person, ranging from 1 to 10.
BMI Category	The BMI category of the person (e.g., Underweight, Normal, Overweight).
Blood Pressure (systolic)	The blood pressure measurement of the person (systolic pressure)
Blood Pressure (diastolic)	The blood pressure measurement of the person (diastolic pressure)
Heart Rate (bpm)	The resting heart rate of the person in beats per minute.
Daily Steps	The number of steps the person takes per day.

Variable	Description
Sleep Disorder	The presence or absence of a sleep disorder in the person (Binary)

Based on unique value counts and the variable description, the numeric and categorical variables are identified as:

Type	Variables
Numeric Variables	age, sleep_duration, physical_activity_level, heart_rate, daily_steps, blood_pressure_systolic, blood_pressure_diastolic
Categorical Variables	gender, occupation, quality_of_sleep, stress_level, bmi_category, sleep_disorder

Reviewing the unique values of the identified categorical values, a duplicate in bmi_category in the values "Normal" and "Normal Weight" can be identified. This is solved by replacing all instances of "Normal Weight" with "Normal"

Doing so concludes the required initial preprocessing steps and allows to begin with the first part of this project work.

Part 1 - Exploratory Analysis and Dimension Reduction via PCA

The first part of this work contains the initial exploratory analysis of the dataset as well as a Principal Component Analysis (PCA) of the dataset.

Exploratory Data Analysis

The Exploratory Data Analysis contains a general overview of the datasets structure and correlations.

The categorical Variables can be further sperated into the following categories with:

Two Binary variable:

- gender
- sleep disorder

Three ordinal variables:

- quality of sleep
- stress level
- bmi_category

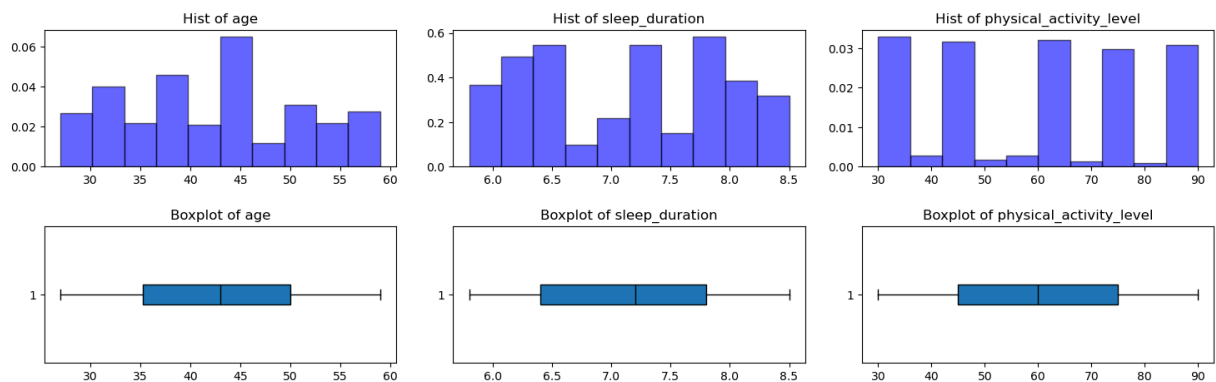And one nominal variables:

- occupation

Plotting barplots for the categorical variables, beginning with the binary variables of gender and sleep disorder, shows an even distribution between male and female and a fairly even distribution between observations with and without sleep disorders. In the meantime, stress level shows a decrease in observations towards higher stress levels, and equally, quality of sleep and body mass index (BMI) show a continuous decrease in observations for quality of sleep from 8 to 4 and for BMI categories from normal to obese. Lastly, the variable occupation shows a somewhat uneven distribution of observations between the different occupations, with the two occupations that individually contribute the most to the overall dataset being Nurses and Doctors. The bias of potential overrepresentation of the medical field with irregular working hours in shifts cannot be further analyzed in this work but has to be taken into account in later conclusions.
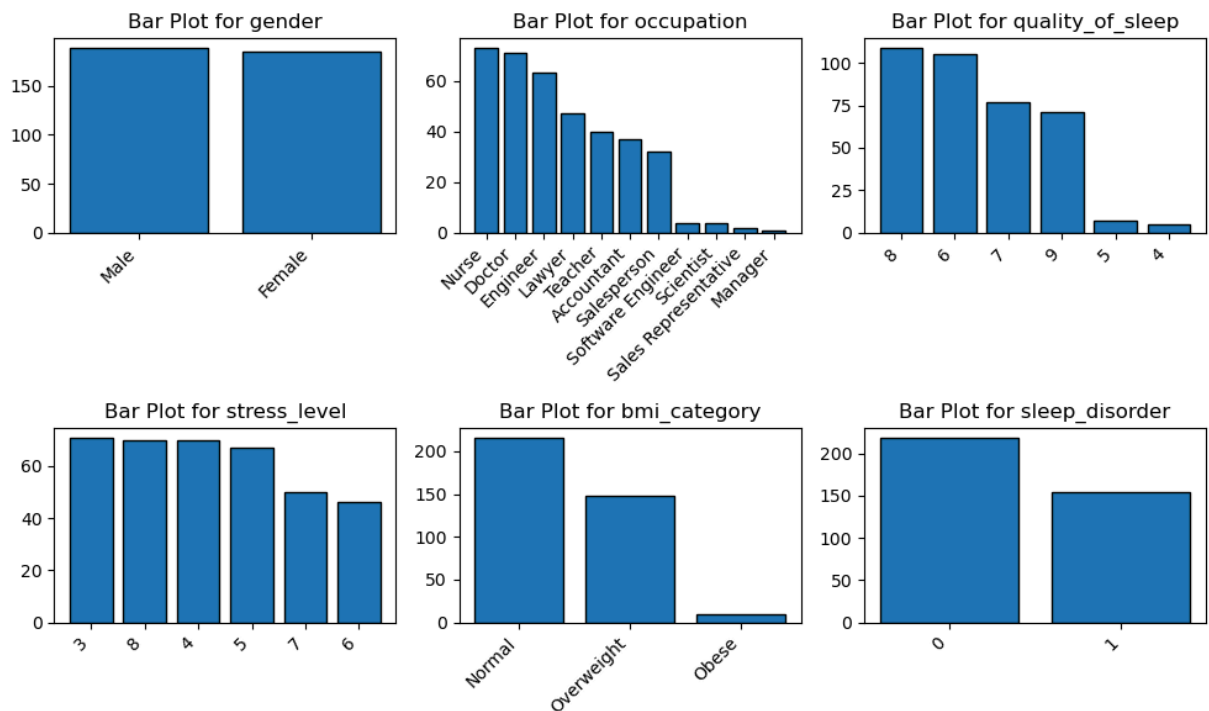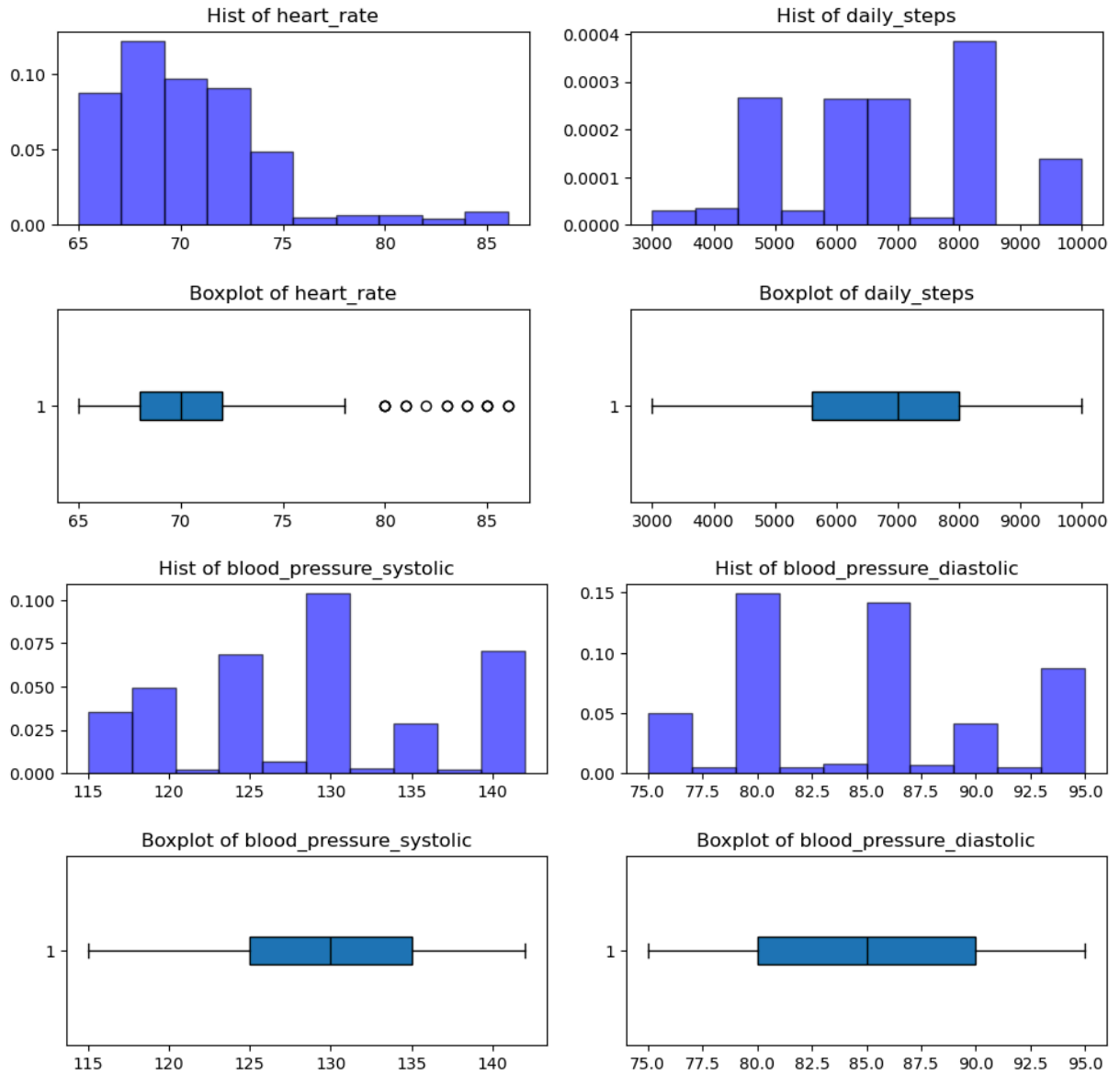

Of the seven numerical variables, all are continuous. Plotting histograms and boxplots side by side, two categories emerge:

- Measured variables
- Estimated/rounded variables (variables that were probably estimated as part of a questionnaire by participants)

For the measured variables, age, heart rate, and sleep duration, a more or less continuous distribution can be identified. Age, while showing variance, still is somewhat uniformly distributed between the limits of around 30 to 60. Sleep duration appears to show three groups: one group having very little sleep (up to 6.5 hours) and one group sleeping for longer times (more than 8 hours), with a dip in sleeping time observed between these two groups. As the last variable of this group, the heart rate is shown to have the majority of its observations between 65 and 75, with visual hints of a normal distribution. However, it shows significant outliers for higher heart rates in both the histogram and boxplot, which will need to be addressed in the preprocessing step. The estimated/rounded variables (physical activity level, daily steps, blood pressure systolic/diastolic) show a specific characteristic with oscillations between highs and lows, attributed to the way people estimate numeric values in increments, like evaluating physical activity level (mins/day) mostly in increments of 15 minutes (half an hour, 45 minutes, one hour, etc.). The lows in between then show observations with more specific answers like 42 minutes, leading to the somewhat irregular appearance of the histograms. Taking this into account, the physical activity level shows a fairly uniform distribution of observations, while daily steps tend more toward a right-skewed uniform distribution, indicating an overall potentially above-average fit sample of people. The high percentage of medical workers with great walking distances as part of their profession might further contribute to this. Meanwhile, the blood pressure systolic/diastolic appears to be more or less evenly distributed.

Hist of heart_rate

Hist of daily_steps

Boxplot of heart_rate

Boxplot of daily_steps

Hist of blood_pressure_systolic

Hist of blood_pressure_diastolic

Boxplot of blood_pressure_systolic

Boxplot of blood_pressure_diastolic

As a first attempt to evaluate the correlations found in this dataset, the following set of Metrics is applied and plotted.

$$q_1 = \left(1 - \frac{\min \lambda_j}{\max \lambda_j}\right)^{p+2}, \qquad q_4 = \left(\frac{\max \lambda_j}{p}\right)^{3/2},$$

$$q_2 = 1 - \frac{p}{\sum_{j=1}^{p}\left(1/\lambda_j\right)}, \qquad q_5 = \left(1 - \frac{\min \lambda_j}{p}\right)^{5},$$

$$q_3 = 1 - \sqrt{|R|}, \qquad q_6 = \sum_{j=1}^{p} \frac{1 - 1/r_{ij}}{p}.$$
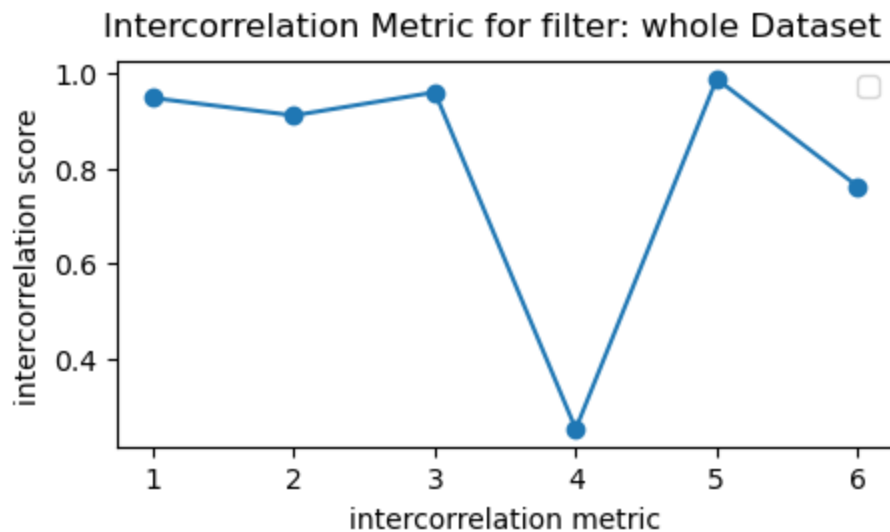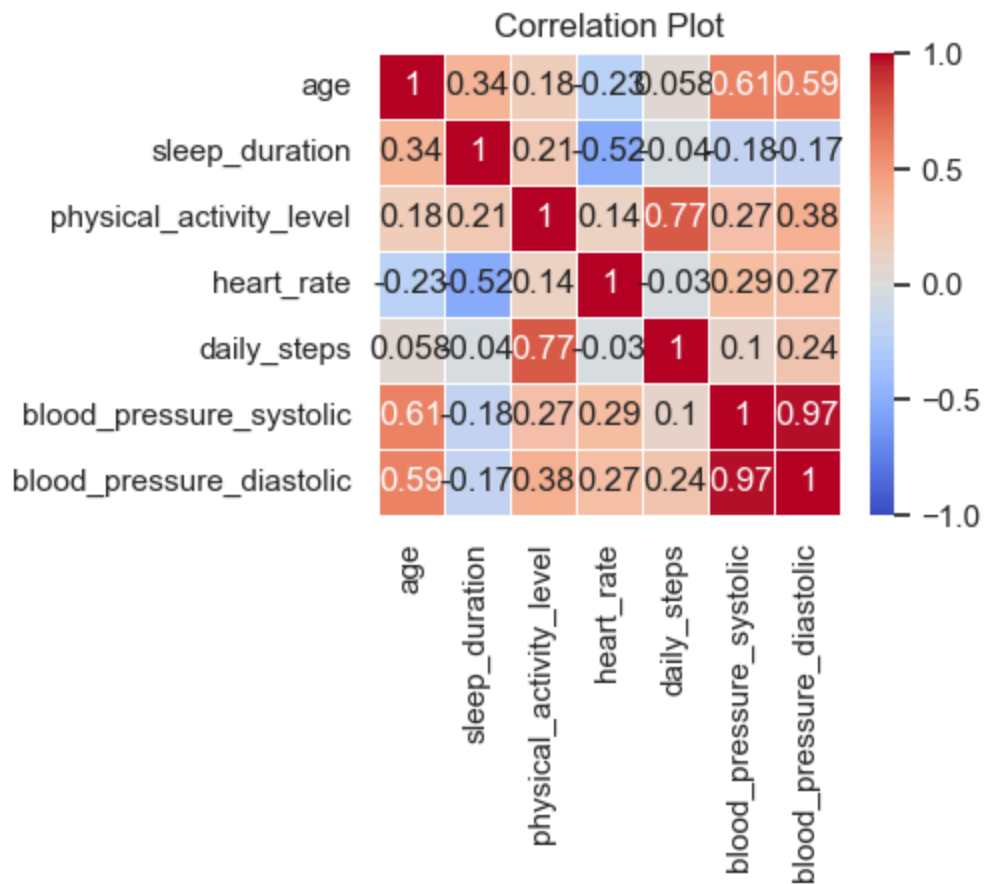
Applying the same method to a dataset filtered on the binary variable sleep disorder shows an overall higher than before correlation in the subset with sleep disorder while the subset for people without sleep disorder shows lower correlation metrics than the joined dataset.
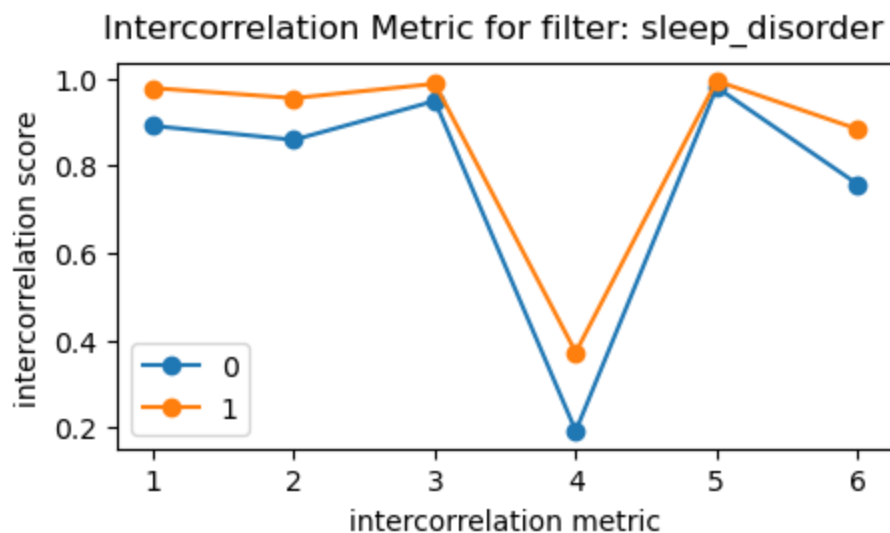

Expanding the correlation analysis with a pair plot shows a variety of potential correlations between variables, the most notable being the linear correlation between blood pressure systolic and diastolic, as well as between daily steps and heart rate/blood pressure. Further correlation can be seen between physical activity level and sleep duration, while the plot of age vs. sleep duration appears to show certain clusters that may be further analyzed in the second part of this work.
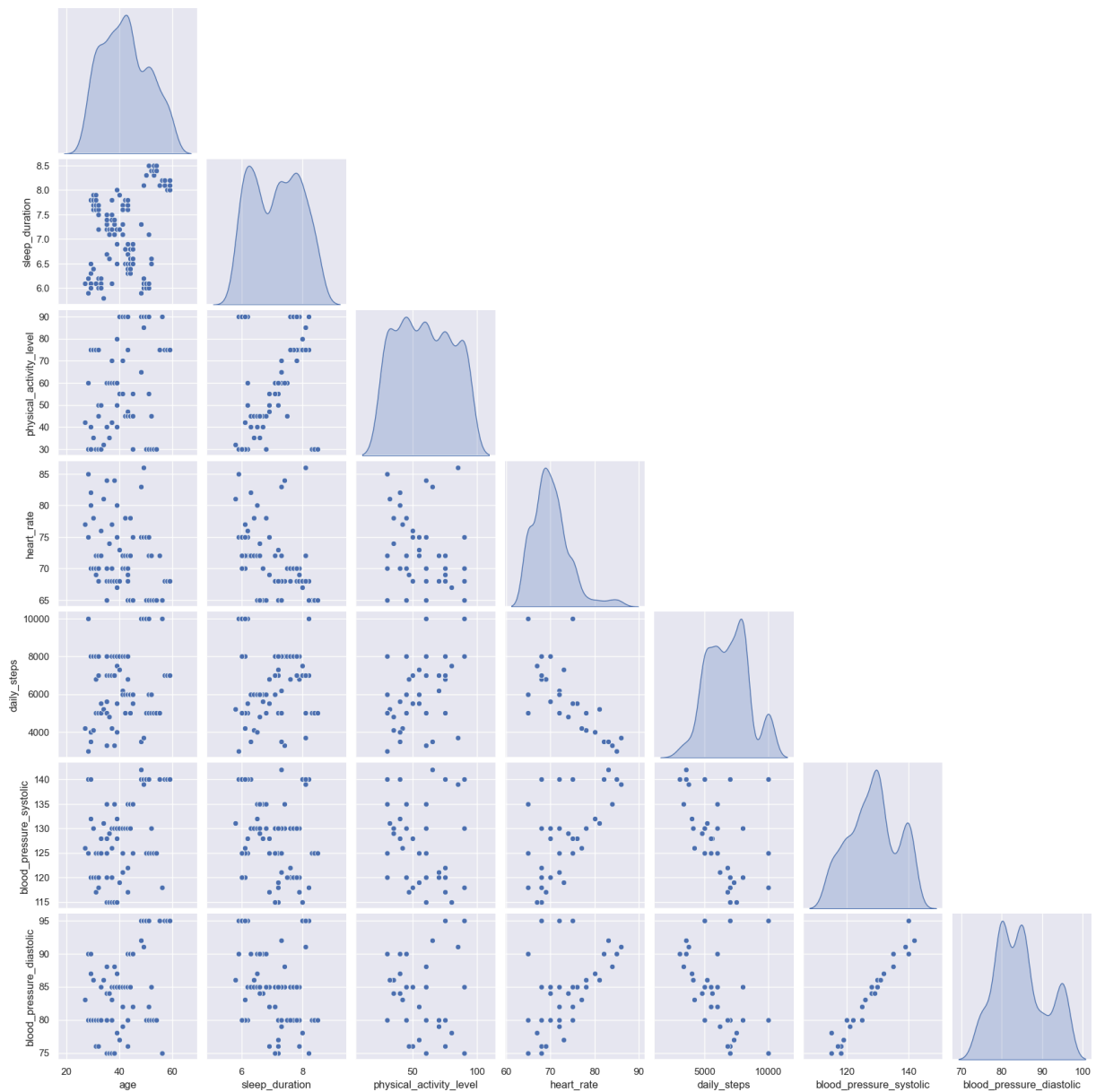
Plotting the correlation corresponding matrix reflects some of the observations made in the pairplot, with the verious near 100% correlation between blood pressure systolic and diastolic very aparent. Two previously less apparent correlations are the ones between age and blood pressure as well as the correlation between physical activity and daily steps.

Correlation Plot

	age	sleep_duration	physical_activity_level	heart_rate	daily_steps	blood_pressure_systolic	blood_pressure_diastolic
age	1	0.34	0.18	-0.23	0.058	0.61	0.59
sleep_duration	0.34	1	0.21	-0.52	0.04	-0.18	-0.17
physical_activity_level	0.18	0.21	1	0.14	0.77	0.27	0.38
heart_rate	-0.23	-0.52	0.14	1	-0.03	0.29	0.27
daily_steps	0.058	0.04	0.77	-0.03	1	0.1	0.24
blood_pressure_systolic	0.61	-0.18	0.27	0.29	0.1	1	0.97
blood_pressure_diastolic	0.59	-0.17	0.38	0.27	0.24	0.97	1

Plotting the covariance matrix however shows an issue with the current format of the data, where daily steps outweighs all other variances due to its scale (3000 - 10000). This issue will be adressed in the next section of part one of this work.
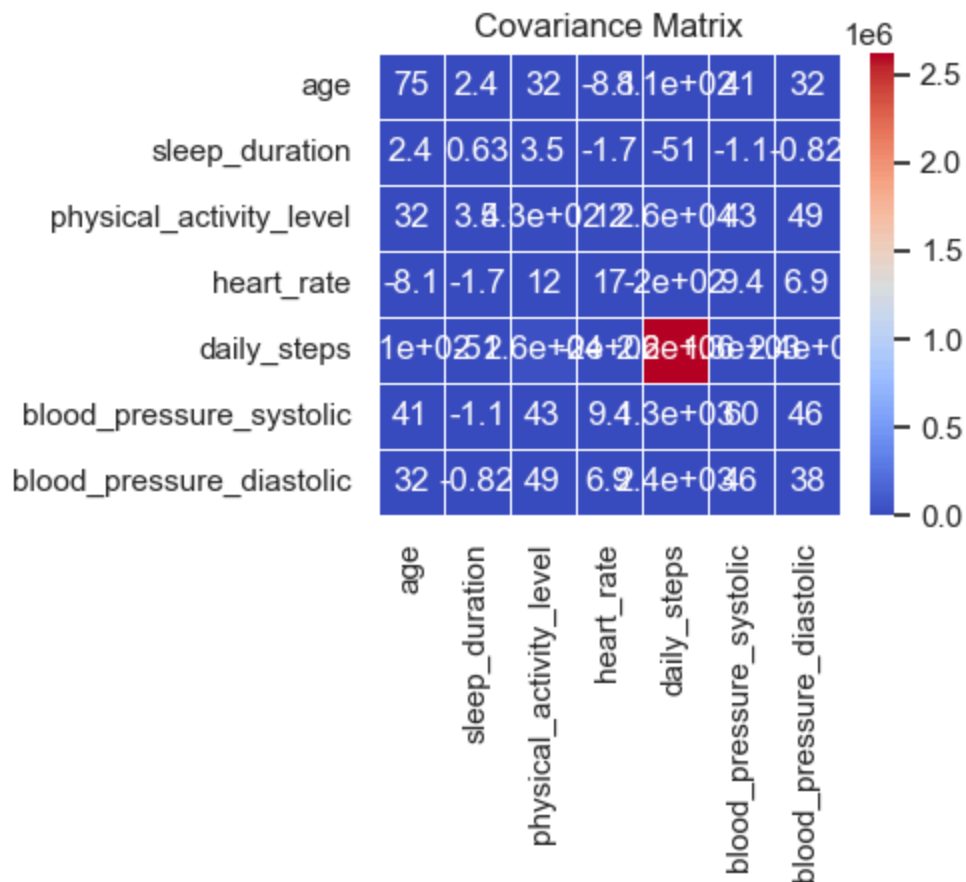
Having a general overview of structure and correlation in the data, the next step is to scaling and outlier issues in the next subsection.

Preprocessing

The following two issues in the current data set:

- Outliers in variable "heart rate"
- Scaling issue to (among others) variable "daily steps"

This section corrects outliers, validates skewness and standardizes the numeric variables.

Outliers and Skewness

The aim of this part of the preprocessing, is to obtain symmetric variables without outliers in order to apply in a correct form the PCA.

It is observed that only one variable has outliers and positive skewness problems (heart rate). Therefore, the first step is to cut the outliers (4% of the dataframe), and then, check if the skewness problem is also corrected.

```
Skewness of age : 0.2561893511793312
Skewness of sleep_duration : 0.037403602518975176
Skewness of physical_activity_level : 0.07418782500797434
Skewness of heart_rate : 1.2199056700731632
Skewness of daily_steps : 0.17756151681455
Skewness of blood_pressure_systolic : -0.03552565092220491
Skewness of blood_pressure_diastolic : 0.37705009626387237
```

```
The threshold for age upper outliers is  72.125
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
The threshold for sleep_duration upper outliers is  9.899999999999999
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
The threshold for physical_activity_level upper outliers is  120.0
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
The threshold for heart_rate upper outliers is  78.0
 then there are 15 outliers in this variable, representing the 4.01 % of the dataset
The threshold for daily_steps upper outliers is  11600.0
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
The threshold for blood_pressure_systolic upper outliers is  150.0
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
The threshold for blood_pressure_diastolic upper outliers is  105.0
 then there are 0 outliers in this variable, representing the 0.0 % of the dataset
```

We can see that the skewness was also corrected by cutting the oultiers observations. For that reason, there is not needed another type of transformation.

```
Skewness of heart_rate : 0.207482395234077
```
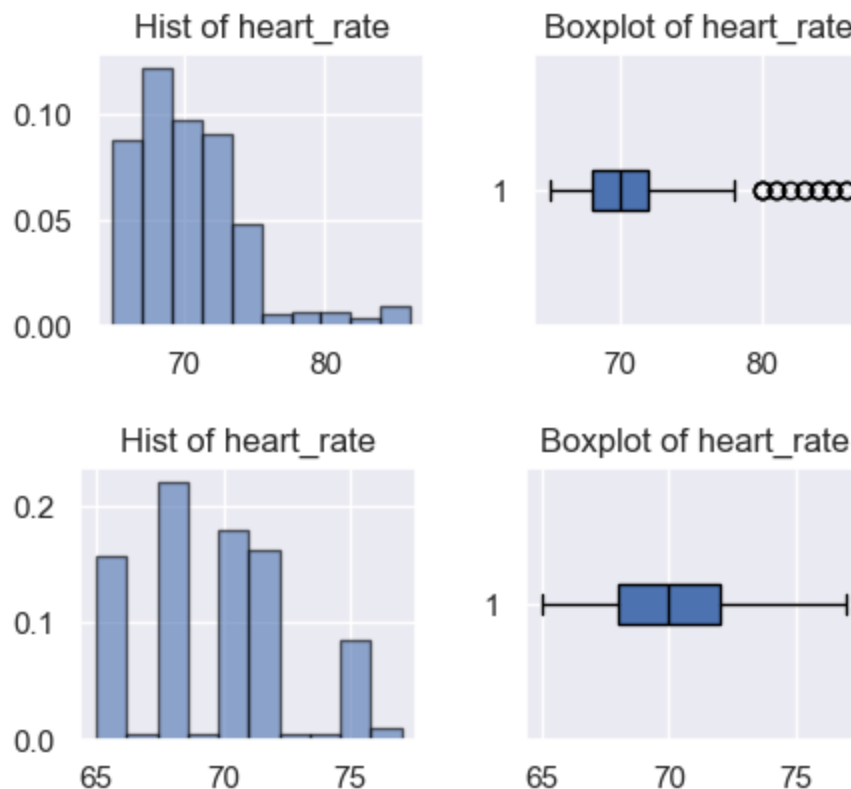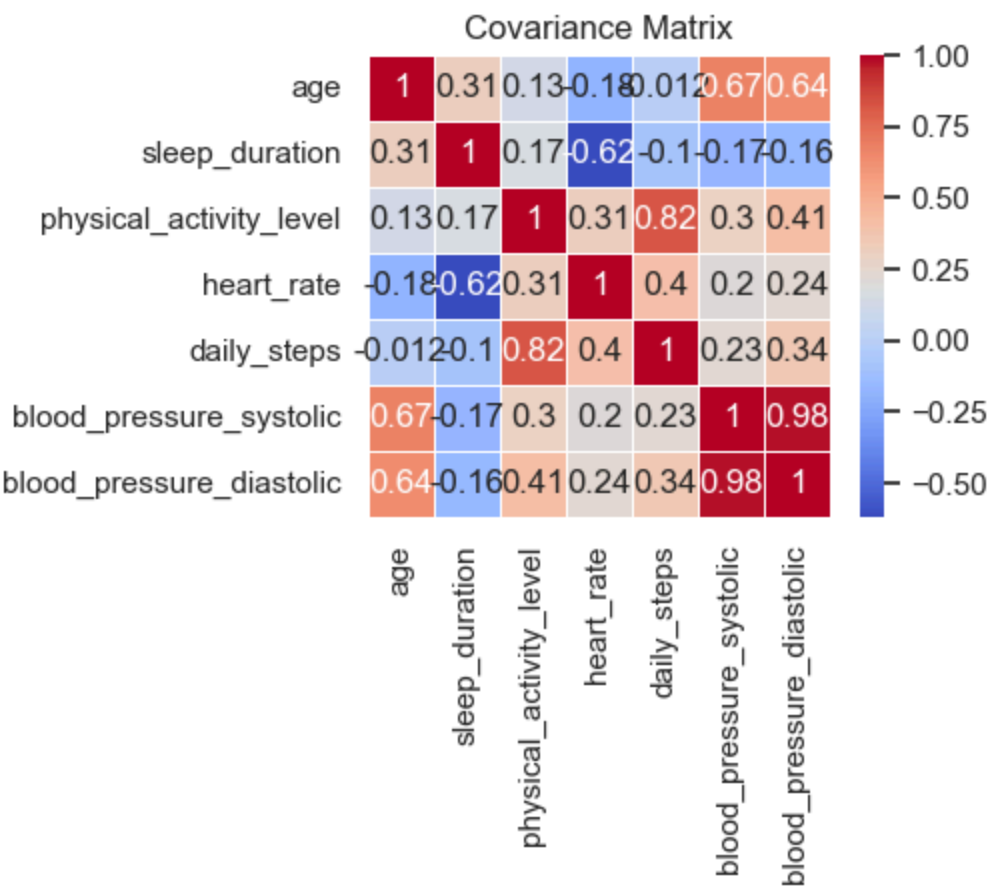

Standardize numeric variables

Having seen in the exploratory data analysis that there exists a strong imbalance in scale between numerical variables in the dataset, the dataset is standardized in this step to mean 0 and scaled on its standarddeviation.

Comparing the boxplots pre-standardized and post-standardized shows the major impact the rescaling has, where daily steps previously dominated and now an even distribution for all numeric variables can be seen.
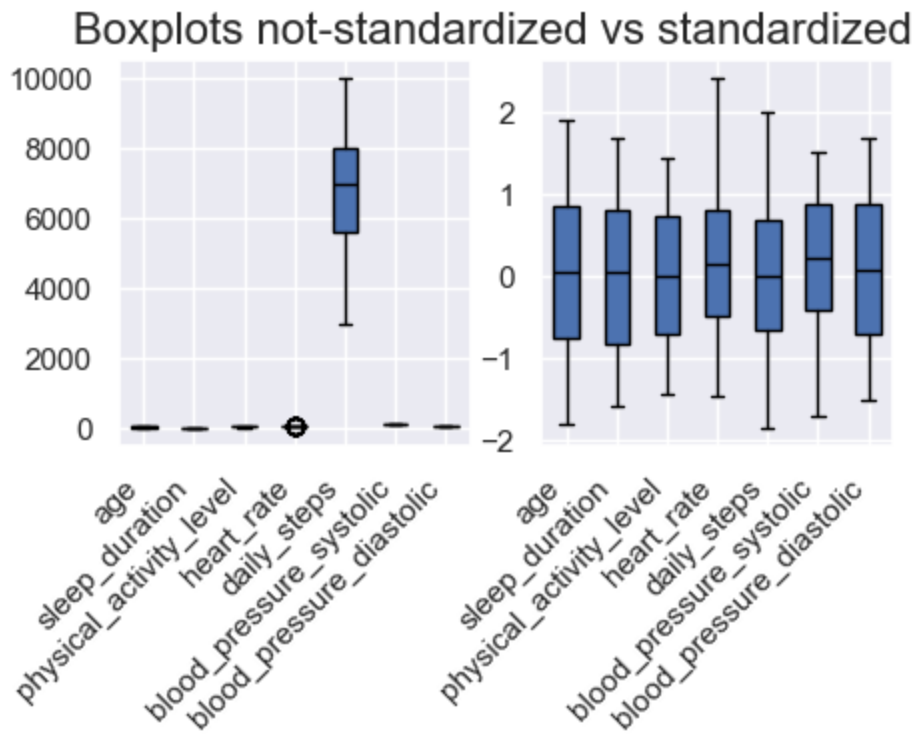
As a result from scaling, now the covariance matrix can be constructed, showing similar results compared to the previously analyzed correlation matrix.

Covariance Matrix

|	age	sleep_duration	physical_activity_level	heart_rate	daily_steps	blood_pressure_systolic	blood_pressure_diastolic
age	1	0.31	0.13	-0.18	-0.012	0.67	0.64
sleep_duration	0.31	1	0.17	-0.62	-0.1	-0.17	-0.16
physical_activity_level	0.13	0.17	1	0.31	0.82	0.3	0.41
heart_rate	-0.18	-0.62	0.31	1	0.4	0.2	0.24
daily_steps	-0.012	-0.1	0.82	0.4	1	0.23	0.34
blood_pressure_systolic	0.67	-0.17	0.3	0.2	0.23	1	0.98
blood_pressure_diastolic	0.64	-0.16	0.41	0.24	0.34	0.98	1

PCA

Having analyzed the data and its characteristic and highly correlated variables identified, as well as having eliminated outliers as well as having standardized the numeric variables, principal component analysis can now be applied in an attempt to reduce dimensionality.

Number of Principal Components

By analysing the Explained Variance (eigenvalues) trend, and the Joliffe´s and Kaiser´s criterion, for this project there are selected 3 Principal components that explain the 90% of the variability.

```
trace:  7.000000000000005
```
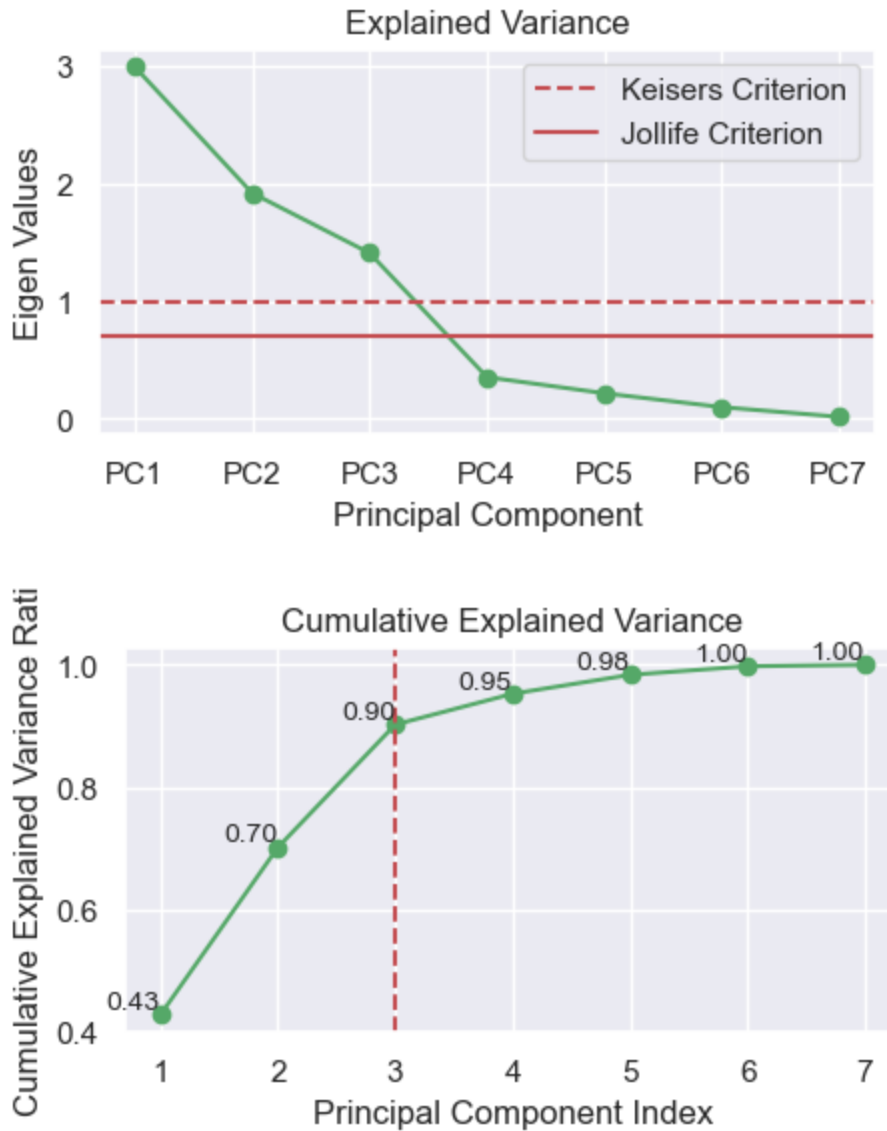
| Value	PC1	PC2	PC3	PC4	PC5	PC6	PC7
Eigen Values	2.98968	1.91745	1.40832	0.35319	0.21651	0.09865	0.01619
% Variability	42.7097	27.3922	20.1188	5.04559	3.09299	1.40933	0.23132
Cum. Variance	42.7097	70.1019	90.2207	95.2663	98.3593	99.7686	100.000

Contribution of Variables to Principal Components and Interpretation

Plotting the Composition of the Principal Components as a Barplot shows a general overlap in the contribution of all variables to the new found principle components, making a very clear seperation into characteristics that are described by the prinicipal components a more dificult task. Since all outliers and scale differences have been treated in the preprocessing steps, the dataset simply seems not to have directly obvious meaningfull interpretation of its

principal components. While interpreability in more general terms is one of the challenges associated to PCA, an attempt is made to give some intuition to the three principal component dimensions selected to represent this data set. The first principal component PC1 can be interpreted as overall characteristics of a person, with all variables except for sleep_duration somewhat evenly related. PC2 could be interpreted as the dimension of age, with age, leep duration and heart rate mainly contributing. Simelarly, PC3 could be interpreted as the physical condition dimension, with physical activity level, daily steps and sleep duration primarily contributing.
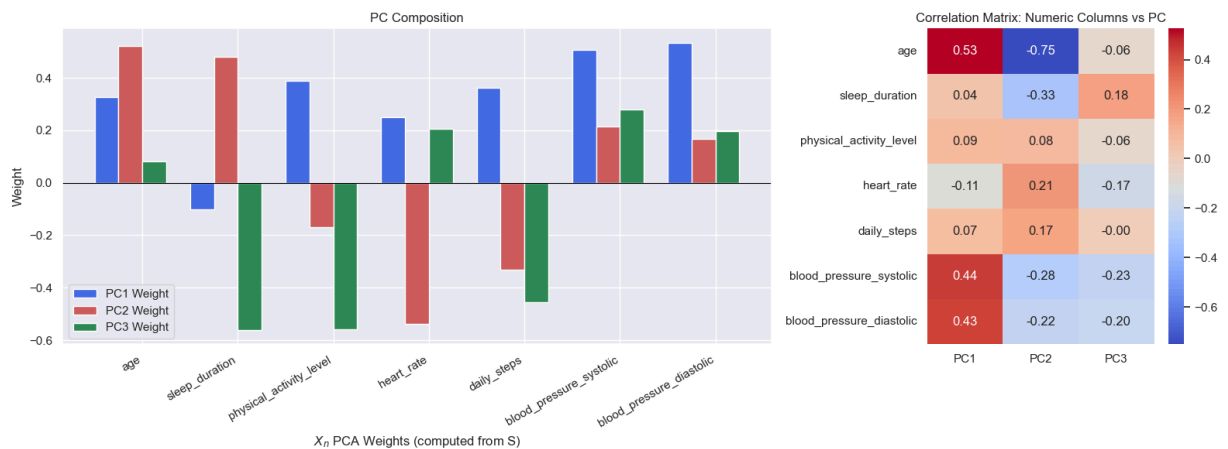
Plotting the data transformed into the three first principal components shows a similarly entangled image image as already shown in the barplots, with no obious interpretation.
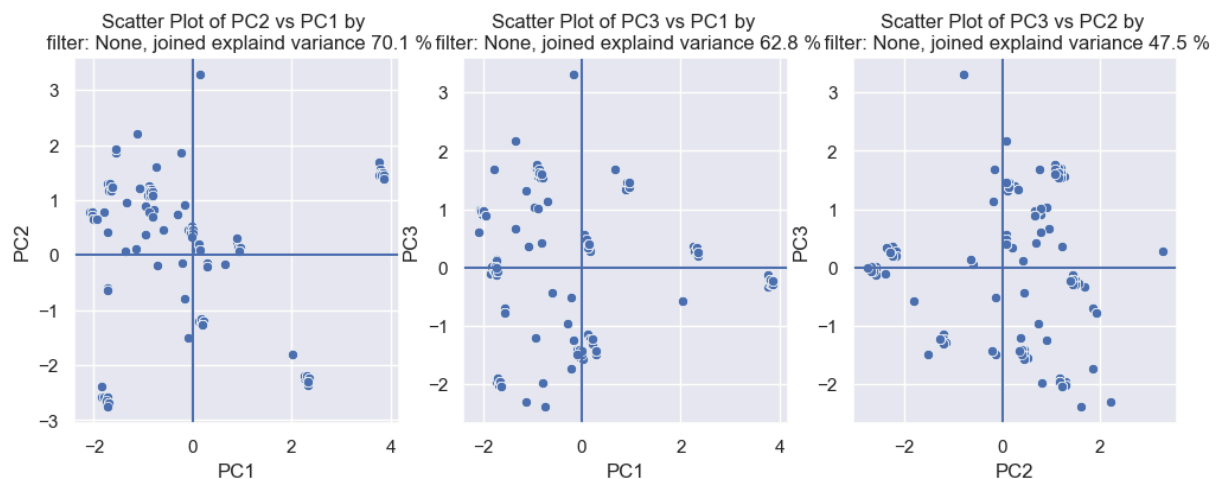

By plotting the 3 principal planes obtained labeled with the categorical variables, interesting relations were found. This relations could help us to give names to each PC.

- **PC1 (Wellness):** Can be interpreted as a person wellness because it makes a good separation between having or not a sleep disorder and also of having or not overweight.

- **PC2 (Stress Level):** Higher values of the PC2 indicates higher stress levels (The stress level is well organized in this component). Also, positive values of this component are

related with a greater age and having high pressure, while lower values are related with a more active life.

- **PC3 (Physical Activity):** In this component a relation is less clear with any of the categorical variables, so the interpretation from the continous variables contribution is mantained as the PC name.
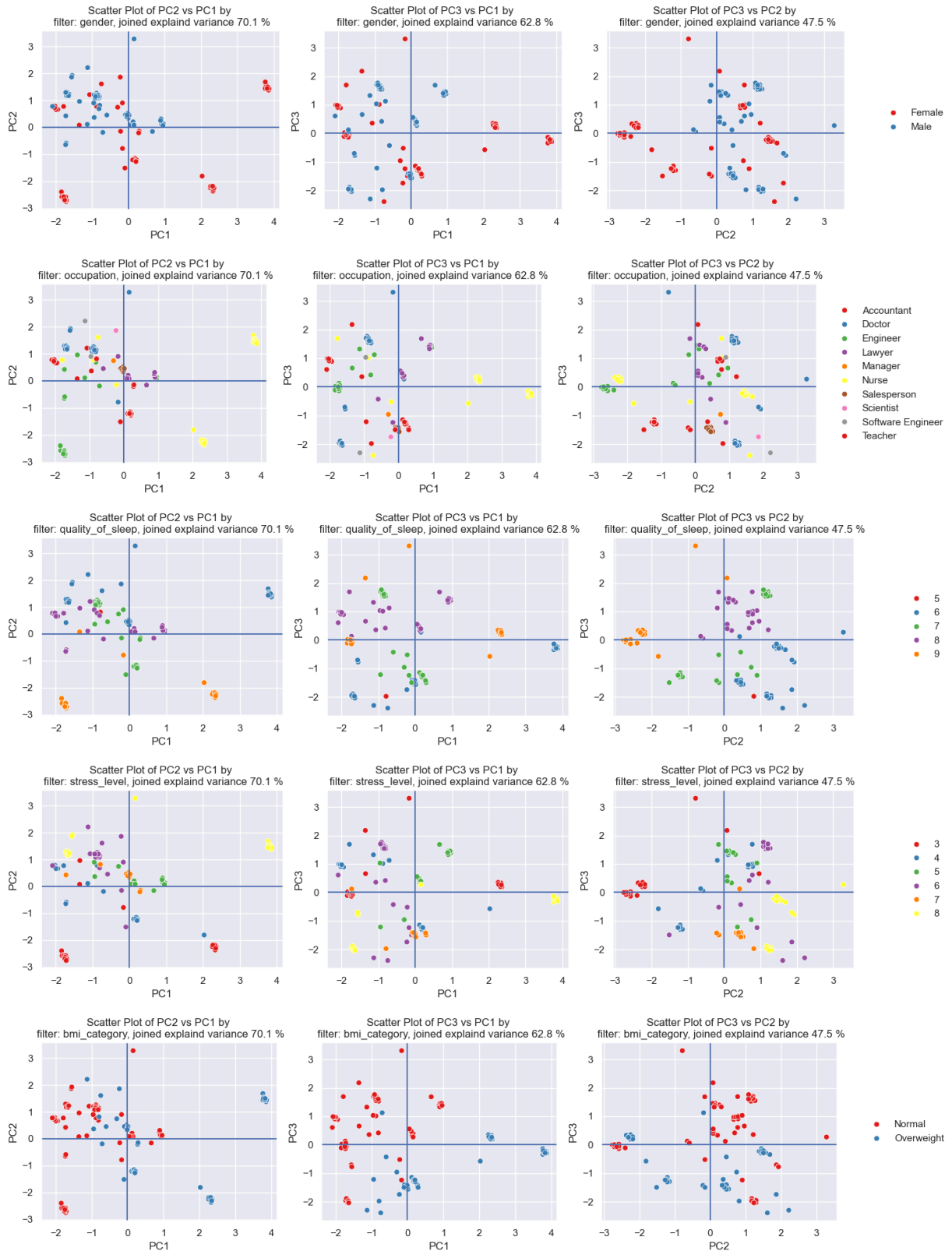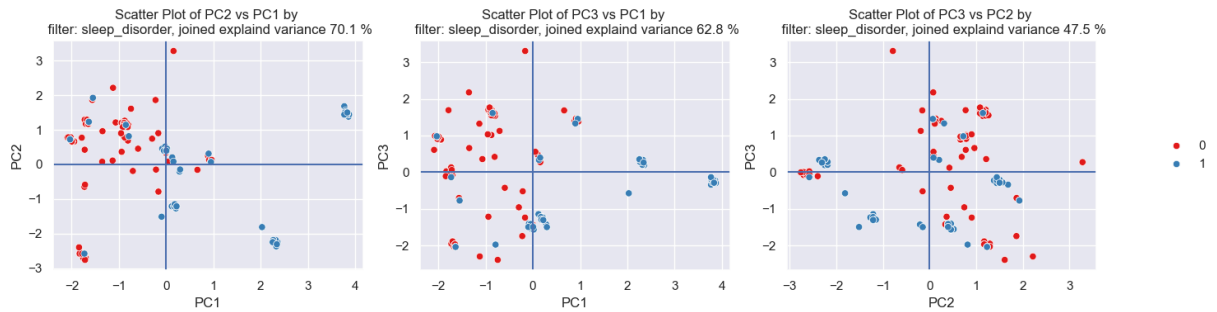
A first glance at possible meaning behind the principal components is only found when plotting the transformed data in three dimensions with a colorcoding for the categorical features. Doing so, first patterns emerge. Some observable pattern include:

- male data points being closer to the origin and female values data points
- clusters of occupations visible, sometimes in combination with stress level like two clusters for nurses, one with low and one with high stress level
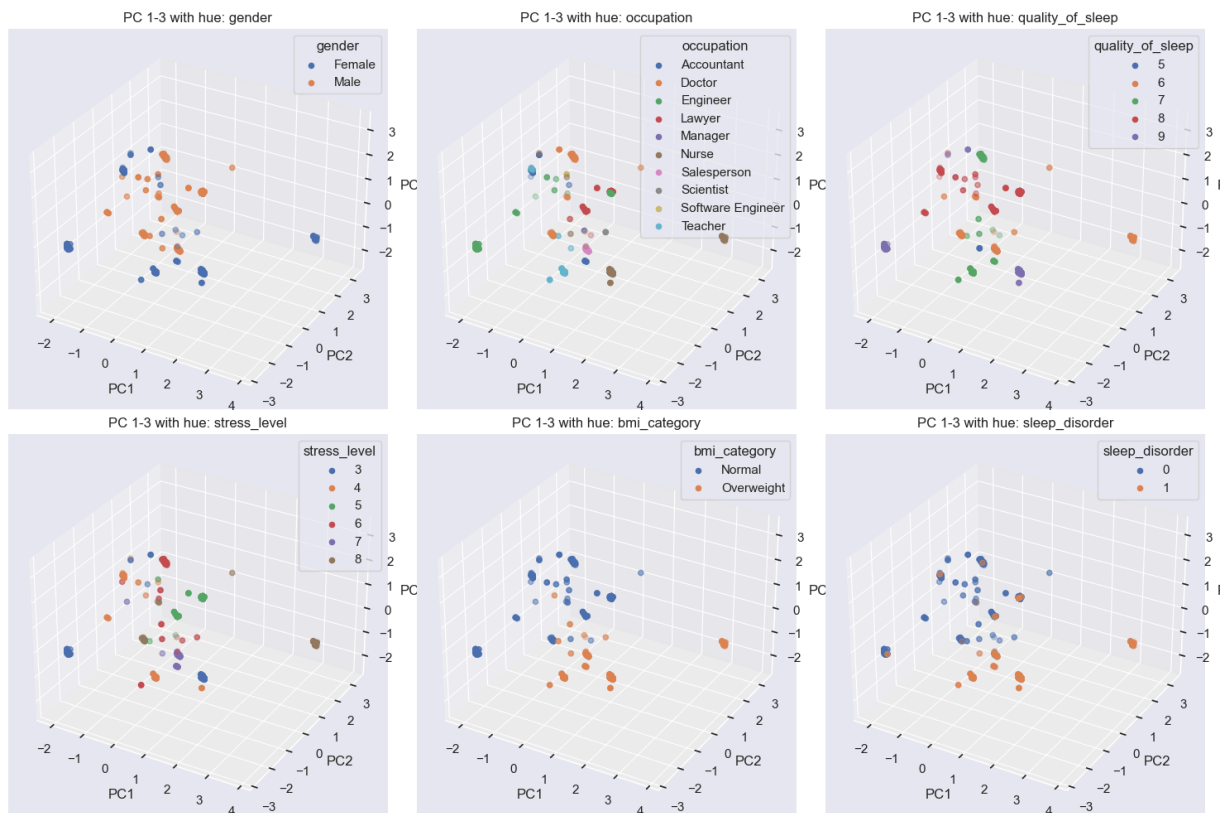

These emerging patterns between the principal components, the numerical and categorical variables and more specifically sleep disorder show an apparent clustering potential that can be further investigated in the second part of this project via distance based metrics.

Stability of the Principal components

To perform the stability analysis using the leave-one-out method, we obtained 354 different outputs, which makes it challenging to interpret the results visually. Even though you can see

that the values are very consistence across both graph.

The values in the table are quite consistent across the different PCAs, indicating that they all exhibit similar average Euclidean distances and very low standard deviations. This suggests that the principal components are stable, remaining unaffected by changes in the data. Consequently, this implies that the PCA captures the underlying structure of the data reliably, providing confidence in the robustness of the results. In general, this suggests that the PCA model is likely to generalize well to new data.
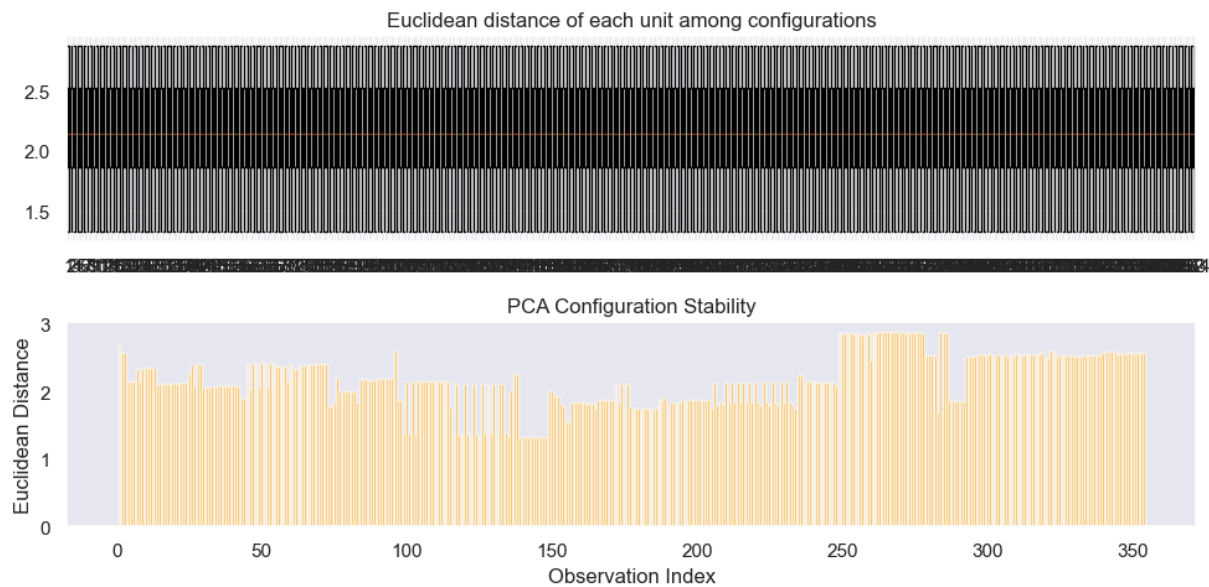
Out[38]:

	Mean	Standard Deviation	Median	Mean Absolute Deviation (MAD)
PCA 1	2.169042	0.396796	2.139104	0.306660
PCA 2	2.170711	0.396445	2.140058	0.305647
PCA 3	2.169899	0.396737	2.139598	0.306719
PCA 4	2.169952	0.396728	2.139642	0.306678
PCA 5	2.170067	0.396691	2.139747	0.306680
PCA 6	2.170119	0.396667	2.139757	0.306644

Conclusion Part 1

In the first Part of this project work, an exploratory data analysis has been performed in support of a principal component analysis. The principal component analysis has been shown to deliver three principal components that explain the datas variance well and are stable when genaralizing to new data, while attributing intuitive characteristics to the new dimensions has shown to be challanging. Only when visualizing the categorical variables together with the data in the new dimensions, patterns and cluster emerge. To further

understand the in this analysis discovered patterns will be the task of the second part of this work.